

## Assignment 7

### 1 Problem 1

[20 points] 7.4 In Section 7.4.4, we describe a situation in which we prevent deadlock by ensuring that all locks are acquired in a certain order. However, we also point out that deadlock is possible in this situation if two threads simultaneously invoke the transaction() function. Fix the transaction() function to prevent deadlocks.

```
void transaction(Account from, Account to, double amount) {
    mutex lock1, lock2;
    lock1 = get_lock(from);
    lock2 = get_lock(to);
    acquire(lock1);
    acquire(lock2);
    withdraw(from, amount);
    deposit(to, amount);
    release(lock2);
    release(lock1);
}
```

#### 1.1 Answer

Add a new lock to this function. This third lock must be acquired before the two locks associated with the accounts are acquired.

The transaction() function now appears as follows:

```
void transaction(Account from, Account to, double amount)
{
    Semaphore lock1, lock2, lock3;
    wait(lock3); //acquire lock3
    lock1 = getLock(from); //request to get lock for lock1
    lock2 = getLock(to); //request to get lock for lock2
    wait(lock1); //acquire the lock1 to perform the transaction
    wait(lock2); //acquire the lock2 to perform the transaction
    withdraw(from, amount);
    deposit(to, amount);
    signal(lock3); //first release the lock3
    signal(lock2);
    signal(lock1);
}
```

## 2 Problem 2

[20 points] 7.7 Consider a system consisting of four resources of the same type that are shared by three processes, each of which needs at most two resources. Show that the system is deadlock free.

### 2.1 Answer

This system is deadlock-free.

To show it by contradiction:

Suppose the system is deadlocked. This implies that each process is holding one resource and is waiting for one more. Since there are three processes and four resources, one process must be able to obtain two resources. This process requires no more resources and, therefore it will release its resources when it is finished. Then the available resources are always larger or equal to the each needs. Hence, the system is deadlock-free.

By Banker's algorithm:

$$\begin{aligned} \text{Max}_i &= 2 \\ \sum_i^n \text{Need}_i &= \sum_i^n \text{Max}_i - \sum_i^n \text{Allocation}_i \\ &= 2 * 3 - 4 \\ &= 2 < N = 3 \end{aligned}$$

This imply that at least one process can release  $\text{Max} = 2$  resources. Hence, the system is deadlock-free.