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The wisdom of the inner crowd in three large natural experiments

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The quality of decisions depends on the accuracy of estimates of relevant quantities. According to the wisdom of crowds principle, accurate estimates can be obtained by combining the judgements of different individuals[1,2]. This principle has been successfully applied to improve, for example, economic forecasts[3–5], medical judgements[6–9] and meteorological predictions[10–13]. Unfortunately, there are many situations in which it is infeasible to collect judgements of others. Recent research proposes that a similar principle applies to repeated judgements from the same person[14]. This paper tests this promising approach on a large scale in a real-world context. Using proprietary data comprising 1.2 million observations from three incentivized guessing competitions, we find that within-person aggregation indeed improves accuracy and that the method works better when there is a time delay between subsequent judgements. However, the benefit pales against that of between-person aggregation: the average of a large number of judgements from the same person is barely better than the average of two judgements from different people.

Many human decisions, whether in the business, political, medical or personal domain, require the decision-maker to estimate unknown quantities. One way to improve accuracy is to combine the estimates of a group of individuals. Aggregated estimates generally outperform most and sometimes all of the underlying estimates, and are often close to the true value. This phenomenon has become known as 'the wisdom of crowds'[1,2]. It arises from the statistical principle that aggregation of imperfect estimates diminishes the role of errors[15–18]. Generally, one has to combine only a few estimates to get most of the effect[19].

The phenomenon was first described in *Nature* by the renowned British scientist Sir Francis Galton[20]. Galton witnessed a weight judging competition at the 1906 West of England Fat Stock and Poultry Exhibition, where visitors could win a prize by paying six pence and estimating the weight of an exhibited ox after it had been "slaughtered and dressed". Galton collected all 800 tickets with estimates and found that the aggregate judgement of the group closely approximated the true value: the mean judgement was 1,197 lb, and the true value was 1,198 lb[21,22]. Similar results have since been observed in a wide range of experiments[23–29].

Recent research proposes that the same principle applies to repeated judgements from the same person[14]. Laboratory experiments confirm that estimation accuracy can indeed be improved by aggregating estimates from a single individual[16,30–35]. The benefit of within-person aggregation reflects what has been dubbed 'the wisdom of the inner crowd', and can potentially boost the quality of individual decision making[36].

This paper analyses within-person aggregation outside the psychological laboratory. We use three large proprietary data sets from three incentivized natural ('naturally occurring') experiments that resemble the one observed by Galton over a century ago. We show that within-person aggregation indeed improves accuracy, but not as much as between-person aggregation: the average of a large number of judgements from the same person is barely better than the average of two judgements from different people, even if the advantages of time delay between estimations are being exploited.

Our data are from three promotional events organized by the Dutch state-owned casino chain Holland Casino. During the last 7 weeks of 2013, 2014 and 2015, anybody who visited one of the casinos received a voucher with a login code. Via a terminal inside the casino and via the Internet, this code granted access to a competition in which participants were asked to estimate the number of objects in a transparent plastic container located just inside the entrance. This container, shaped to represent a champagne glass, was filled with small objects that represented pearls in 2013, pearls and diamonds in 2014 and casino chips in 2015 (Supplementary Fig. 1). Both the container and the exact number of objects were the same at every location. There were 12,564 objects in the container in 2013, 23,363 in 2014, and 22,186 in 2015. A prize of €100,000 was shared equally by those whose estimate was closest to the actual value. In 2013, the prize money was awarded to 16 people, and in 2014 and 2015, the entire amount was won by one person. All winners had submitted exactly the right number.

Our pseudonymized data sets contain all entries for the three years: a total of 369,260 estimates from 163,719 different players in 2013, 388,352 estimates from 154,790 players in 2014, and 407,622 estimates from 162,275 players in 2015. Many players submitted multiple estimates (Supplementary Fig. 2). Across the combined data sets, 60% of the participants were male and the average age was 39 yr. The Supplementary Information provides further details about the data.

The distributions of the estimates have a log-normal, right-skewed shape (Supplementary Figs. 7 and 8). Such a shape is in line with the tendency to estimate large numerical values in a logarithmically compressed manner[29,32,37]. This tendency seems to be the result of an innate intuition for numbers, with numbers logarithmically encoded in the brain[38–43].

Immediately after Galton published his classic article, the aggregation measure to be used became a topic of debate[21,44]. The arithmetic mean is now the most commonly adopted aggregation measure[45–49]; however, with log-normal distributions, the preferred metric of central tendency is the geometric mean[29,32,33]. For our data, the geometric mean indeed performs much better than the arithmetic mean. The arithmetic mean overestimates the true value by ≥346% (Table 1), and is more accurate than only 10–14% of the underlying individual estimates across the three years. The

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geometric mean overestimates the true value by 86% in 2015, and is 19% and 32% below the true value in 2013 and 2014, respectively. In 2013 and 2014, the geometric mean is better than respectively 90% and 84% of the underlying individual estimates, and in 2015, it outperforms approximately 50%. Restricting the data to participants' first estimate gives a similar picture (Supplementary Table 1).

Given the log-normal distributions of the estimates, our analyses follow the convention of using a logarithmic transformation[29,32,33]. After a logarithmic transformation, the arithmetic mean corresponds to the logarithm of the geometric mean of the original values. To make the distributions comparable across the three competitions, we divide the estimates by the true value before taking the logarithm. This two-step transformation yields approximately normal distributions (Supplementary Fig. 9), where zero represents the true value and deviations from zero measure the positive or negative estimation error. Our accuracy measure is the mean squared error (MSE). The Supplementary Information presents similar results for the mean absolute error and for the untransformed data.

For every event, approximately 60,000 participants submitted more than one estimate. In 2013, the average of their first two estimates was more accurate than either estimate alone ($MSE_1 = 3.12$, $MSE_2 = 2.73$, $MSE_{1\&2} = 2.47$, with $t(60{,}869) > 21.90$ and two-sided $P < 0.0001$ in the two comparisons). This was also true in 2014 ($MSE_1 = 3.07$, $MSE_2 = 2.77$, $MSE_{1\&2} = 2.50$, $t(59{,}156) > 23.20$, $P < 0.0001$), and in 2015 ($MSE_1 = 3.45$, $MSE_2 = 3.30$, $MSE_{1\&2} = 2.96$, $t(61{,}893) > 31.73$, $P < 0.0001$). However, the effect sizes are relatively small: Cohen's d varies between 0.08 and 0.11 for the three comparisons between the average and the first estimate, and between 0.05 and 0.06 for the three comparisons between the average and the second estimate.

Table 1 | Arithmetic and geometric mean across all estimates

Year	*N*	True value	Arithmetic mean		Geometric mean	
2013	369,260	12,564	74,936	(+496%)	10,168	(−19%)
2014	388,352	23,363	104,209	(+346%)	15,986	(−32%)
2015	407,622	22,186	224,278	(+911%)	41,278	(+86%)

Aggregation measures are calculated across all estimates. *N* is the number of estimates. Percentage deviations relative to the true values are in parentheses.

If judgements can be improved by aggregating two estimates, aggregating a greater number of estimates is likely to lead to further improvements. The MSE of aggregations across the first t consecutive estimates for players who provided at least $K = 5$ or $K = 10$ estimates in a given year is plotted in Fig. 1 (in black; see Supplementary Fig. 10 for alternative values of K). In all cases, the MSE declines with t, at a decreasing marginal rate.

Figure 1 also plots the MSE of the average of T different players' first estimates (in dark grey), showing that aggregating across individuals works substantially better than aggregating judgements from the same individual. The 'outer crowd' MSE declines with the number of estimates, but at a much faster rate than the MSE of the inner crowd.

To more formally compare the wisdom of the inner and the outer crowd, we define $T_t^\star$ as the number of estimates one needs to average across individuals to achieve the same squared error as the squared error that results from averaging t estimates from a single individual (see Methods)[33].

Depending on the sample that we use, $T_5^\star$ varies between 1.44 and 1.66, and $T_{10}^\star$ varies between 1.63 and 1.96. This implies that averaging five or ten estimates from the same individual is, in expectation, inferior to averaging two estimates from randomly selected individuals.

Aggregating even more estimates yields hardly any additional benefits. The MSE of the inner crowd can be approximated by the hyperbolic function $MSE = (a / t) + b$, where a represents the average individual variance and b represents the average individual squared error (see Methods)[33]. Integrating an infinite number of estimates from a single individual therefore yields $MSE = b$ in expectation.

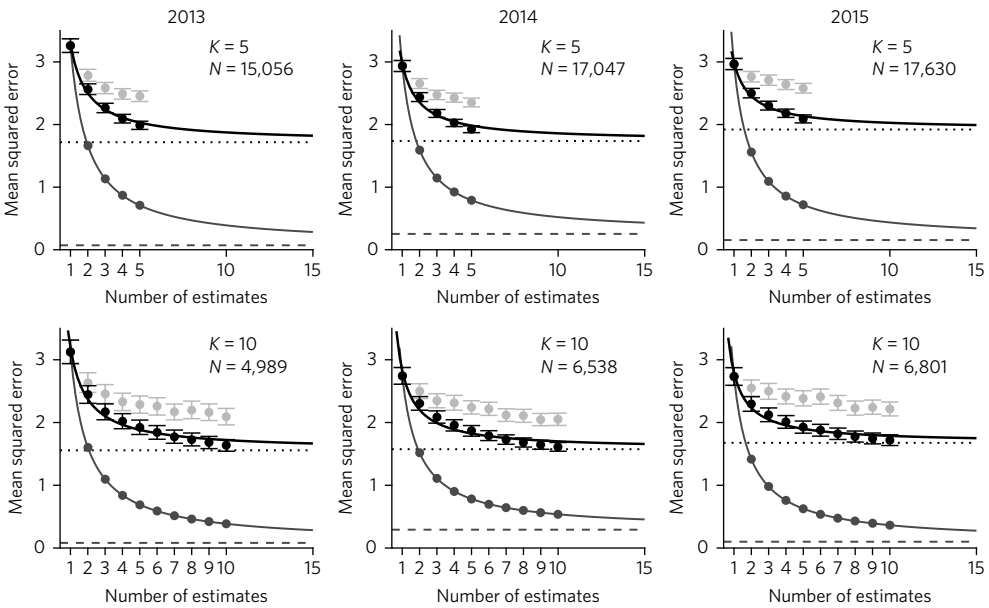

Fig. 1 | MSE of the inner crowd and the outer crowd as a function of the number of included estimates. The MSE of the inner crowd is shown in black and the outer crowd in dark grey. The graphs also show the MSE of individual consecutive estimates (light grey). The upper graphs use the estimates of players who submitted at least $K = 5$ estimates in a given year, and the bottom graphs use the estimates of players who submitted at least $K = 10$ estimates in a given year. The curve for the inner crowd represents the best-fitting hyperbolic function $MSE = (a / t) + b$ (using nonlinear least squares); the dotted line represents b. Values for the outer crowd are mathematically determined using the diversity prediction theorem (see Methods); the dashed line represents the limit as the number of included estimates goes to infinity. Error bars represent 95% confidence intervals. *N* is the number of players.

The number of estimates needed to obtain this MSE by aggregating across individuals, $T^{\star}_{\infty}$, varies between 1.59 and 2.06 across the samples. Hence, the expected potential benefit from within-person aggregation barely exceeds the expected benefit from aggregating the judgements of two randomly selected individuals.

Figure 1 also shows the MSE of the jth individual estimate (in light grey). Throughout the competitions, no information was revealed about the contents of the container, but players could potentially improve their estimates over time by using the power of aggregation. Communication was not restricted, and players therefore had the opportunity to aggregate not only their own estimates but also those of their peers. Earlier research indicates that people underestimate the merits of averaging judgements across individuals[50,51], and that they do not average their own estimates as often as they ideally should[32,34,52]. The patterns of the MSE of individual consecutive estimates in our guessing competitions are in line with these findings: estimates improve over time, but the improvements do not match the improvements that could have been obtained by averaging. Of course, the decreasing MSE can also be the consequence of other forms of learning, such as better approaches and better comprehension.

In the previous analyses, the benefit of aggregating estimates from the same person may partly derive from such learning effects. For practical purposes, the exact sources and their contributions to the gain from within-person aggregation are unimportant, but here we are also interested in the strength of within-person aggregation in the absence of learning. Therefore, we have analogously investigated the pattern of the MSE when the first K estimates from the same person are aggregated in a random order (Supplementary Fig. 11). To ensure an equal base of comparison, we similarly used all first K estimates to determine the MSEs of between-person aggregation—not just the very first ones as we previously did. Depending on the sample, with random ordering, $T^{\star}_{5}$ varies between 1.34 and 1.41, $T^{\star}_{10}$ between 1.43 and 1.49, and $T^{\star}_{\infty}$ between 1.46 and 1.57. Hence, the 'pure' within-person aggregation benefit is considerably lower than the benefit of aggregating two judgements from different individuals.

When learning effects are absent, the benefit of within-person aggregation relative to between-person aggregation is entirely driven by the degree to which the variation in estimates is due to variation within individuals (random noise) versus variation in individual-level systematic error (idiosyncratic bias). Aggregating multiple estimates from a single individual eliminates the influence of random noise only, whereas aggregating across different individuals eliminates the influence of both random noise and idiosyncratic bias. If we express the error of the jth estimate of person i, $x_{i,j}$, as an additive function of the overall bias in the population μ, idiosyncratic bias u_i and random noise $v_{i,j}$ (that is, $x_{i,j}=\mu+u_i+v_{i,j}$), and assume that $u_i \sim N(0,\tau^2)$ and $v_{i,j} \sim N(0,\sigma^2)$, then $T^{\star}_{\infty}=1+\sigma^2/\tau^2$ (see Methods). Hence, the previous estimates of 1.46–1.57 for $T^{\star}_{\infty}$ imply that the variance of idiosyncratic bias (across individuals; τ^2) is about twice as large as the variance of random noise (within individuals; σ^2). Direct estimations of those variances for each of the various subsamples confirm this ratio and the values of $T^{\star}_{\infty}$ (Supplementary Table 2).

When we estimate the two variances across all entries of all participants for each of the three competitions, the implied values of $T^{\star}_{\infty}$ range between 1.36 and 1.45 (Supplementary Table 3). Again, aggregating estimates from a single individual clearly fails to approach the benefit of aggregating estimates from only two randomly selected individuals.

Previous studies show that the accuracy gain from within-person aggregation is higher if people are asked to base their second estimate on different knowledge or assumptions than their first[31,34,36]. Such new perspectives happen naturally when people forget, and it has indeed been observed that accuracy gains are larger for individuals with lower working memory spans[53] and increase with the delay between estimates[14]. However, the beneficial effect of delay was not found in a pre-registered replication study [54].

We exploit the variation in the timing between players' first and second estimates to investigate the effect of delay on the benefit of aggregation. Because this variation happened naturally and was therefore not exogenously imposed, the results need to be interpreted with some caution. To quantify the benefit of aggregation, we define a participant's accuracy gain as the resulting percentage decrease of the squared error (squared error of the average of the estimates relative to the average squared error of the individual estimates). Figure 2a shows that the accuracy gain increases almost monotonically with the delay. For two estimates provided at a single point in time—a participant could enter up to five estimates simultaneously—the average accuracy gain from aggregation is 16–18%. For estimates submitted more than 5 weeks apart, the average accuracy gain is approximately 30%.

Figure 2b indicates that the increase in accuracy gain is a consequence of the decrease in correlation between the estimates. The Pearson correlation coefficient decreases from more than 0.8 when people entered the estimates simultaneously to approximately 0.5 when multiple weeks passed between the attempts.

Two estimates are said to bracket the true value if they fall on opposite sides of it. Bracketing is an important driver of aggregation benefits, and the degree of bracketing is sometimes used as an indicator for the wisdom of crowds[29,31,50]. Figure 2c shows that the bracketing rate increases if estimates are made further apart in time: bracketing rates are about 15% for estimates made at a single time-point,

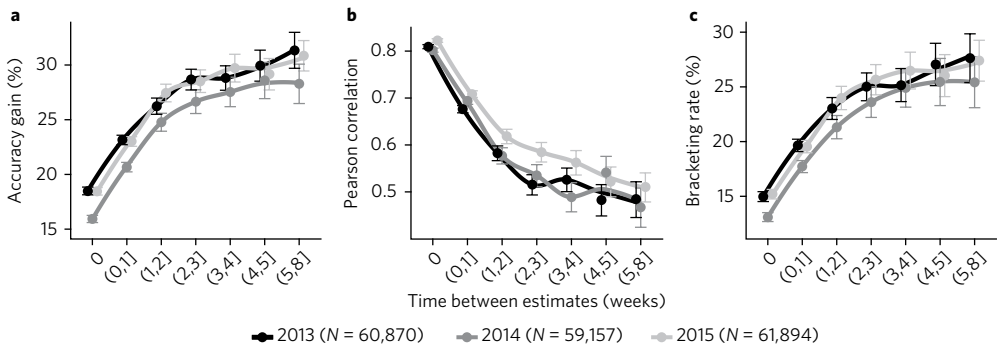

Fig. 2 | Delay benefits. a–c, Accuracy gain (**a**), Pearson correlation coefficient (**b**) and bracketing rate (**c**) for participants' first two estimates as a function of the time between the estimates. Error bars represent 95% confidence intervals. Smoothed (LOESS) curves are added to illustrate the time trends. *N* is the number of players.

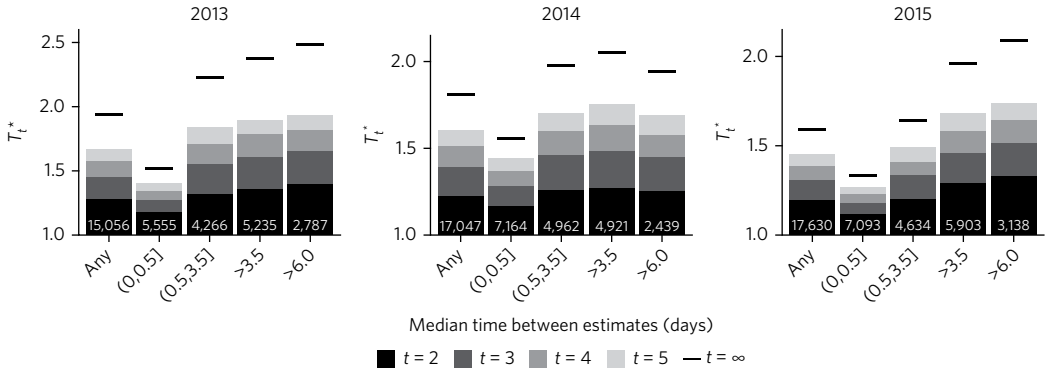

Fig. 3 | Values of T_t^* for different delays. The graphs use the first five estimates of players who submitted at least five estimates in a given year. Results are shown for the full samples and for subsamples that differ in terms of the median time between the estimates. The numbers at the bottom of the bars represent the numbers of included players.

and increase to >25% when multiple weeks passed. Overall, our data thus yield evidence of substantial delay benefits. These benefits are similar across the three independent data sets, suggesting that the advantageous effect of delay is more robust than previously thought[14,54].

Figure 3 depicts estimates for $T_t^\star$ as a function of the median time between the first five estimates for players who provided five or more estimates in a given year. Across the three competitions, $T_5^\star$ varies between only 1.29 and 1.44 if the median delay is no longer than half a day, and increases to values between 1.74 and 1.93 if the median delay is more than 6 days. Averaging an infinite number of estimates with a median delay of more than 6 days allows an individual to outperform the aggregated estimate of two randomly selected individuals, but not by much: $T_\infty^\star$ then varies between 1.94 and 2.48. Even though delay can be used to increase the relative merit of aggregating estimates from a single individual, between-person aggregation remains substantially more powerful.

Note that in situations where decision time is limited, there is a trade-off between making additional estimates and taking more time between estimates. For example, aggregating five estimates with a median delay of only half a day or less is roughly equivalent to or better than aggregating two estimates that are made more than six days apart. Under time pressure, making multiple estimates in short succession can therefore be the better option.

As before, the above T_t^* values also reflect the improvements from learning that we observed earlier. When we control for learning by aggregating estimates in a random order, we still observe delay benefits, and as expected, the T_t^* values are lower (Supplementary Fig. 12). For the category with the longest median delay, T_∞^* decreases to values between 1.65 and 1.75. However, these values need not reflect the full potential of within-person aggregation, because a median delay of more than six days does not guarantee that the correlation between estimates has reached its minimum. Indeed, Fig. 2b indicates that the correlation decreases with longer delays, and only stabilizes when the delay spans multiple weeks (at values of about 0.5).

To capture the maximum delay effect, we decompose the estimation error as before, but we now allow the covariance between estimates from the same person to have a delay-dependent part that declines exponentially with the duration of the delay (see Methods). Estimations of the error components on the full data sets indeed confirm that a threshold of six days is not sufficient for convergence in the covariance to occur; the delay-dependent part of the covariance halves about every eight days, meaning that it takes multiple weeks until most of it has dissipated (Supplementary Table 4). More importantly, the estimation results again show the limited efficacy of within-person aggregation; even if we fully exploit the advantageous effect of delay by allowing the delay-dependent part of the covariance to completely evaporate—which can be seen as allowing a person to take infinitely long delays between consecutive estimates—$T_\infty^\star$ remains relatively low at values between 1.75 and 1.99 (Supplementary Table 4).

In conclusion, the present study finds that the effectiveness of within-person aggregation is considerably lower than that of between-person aggregation: the average of a large number of judgements from the same person is barely better than the average of two judgements from different people. The efficacy difference is a consequence of the existence of individual-level systematic errors (idiosyncratic bias). The effect of these errors can be eliminated by combining estimates from multiple people, not by combining multiple estimates from a single person.

In the context of our guessing competitions, all individuals were exposed to the same (visual) information about the container and the objects in it, and the sources of variation in idiosyncratic bias were limited to differences in individuals' comprehension of the task, visual perception, and geometric skills. In many other real-world contexts, additional sources of idiosyncratic bias exist, which can be expected to lower the comparative benefit of within-person aggregation even more.

Within-person aggregation is potentially useful in situations where only one individual can make sufficiently informed estimates. This may be the case, for example, in strictly personal matters and under extreme degrees of specialization. Because of the relatively limited accuracy gains from within-person aggregation, between-person aggregation should be preferred whenever practicable.

Methods

The diversity prediction theorem and T_t^*. Estimates made by different individuals are considered to be realizations of a random variable X. The diversity prediction theorem says that the crowd's error, or population bias, equals the average error minus the diversity in estimates. More formally, it states that the collective squared error (CSE) relative to the true value θ, $\mathrm{CSE}(X) = (\mathrm{E}(X) - \theta)^2$, equals the MSE of the individual estimates, $\mathrm{MSE}(X) = \mathrm{E}((X-\theta)^2)$, minus the variance of the estimates, $\mathrm{VAR}(X) = \mathrm{E}(X^2) - \mathrm{E}(X)^2$ (refs [2,55]):

$$\mathrm{CSE}(X) = \mathrm{MSE}(X) - \mathrm{VAR}(X)$$

The theorem can be used to mathematically determine the MSE of the average of T estimates from different individuals $\bar{X}_T$ (ref. [33]):

$$\mathrm{MSE}(\bar{X}_T) = \frac{\mathrm{VAR}(X)}{T} + \mathrm{CSE}(X)$$

It can also be used to compare between-person and within-person aggregation. We define $T_t^\star$ as the number of estimates one needs to average across individuals to achieve the same squared error as the squared error of IC_t,

which represents the arithmetic mean of t estimates from one individual (the inner crowd). From the above framework, it follows that[33]:

$$T_t^\star = \frac{\mathrm{VAR}(X)}{\mathrm{MSE}(\mathrm{IC}_t) - \mathrm{CSE}(X)}$$

Estimation error decomposition and $T_\infty^\star$. In the absence of learning, the error of the jth estimate of individual i, $x_{i,j}$, can be decomposed into population bias μ, idiosyncratic bias u_i, and random noise $v_{i,j}$:

$$x_{i,j} = \mu + u_i + v_{i,j}$$

We assume that $u_i \sim N(0, \tau^2)$ and $v_{i,j} \sim N(0, \sigma^2)$. The MSE of the average of T estimates from different individuals $\bar{X}_T$, is then given by:

$$\mathrm{MSE}(\bar{X}_T) = \mu^2 + \frac{\tau^2 + \sigma^2}{T}$$

and the MSE of the arithmetic mean of t estimates from one individual, IC_t, is then given by:

$$\mathrm{MSE}(\mathrm{IC}_t) = \mu^2 + \tau^2 + \frac{\sigma^2}{t}$$

$T_\infty^\star$ is the number of estimates needed to average across individuals to achieve the same squared error as the squared error of the average of an infinite number of estimates from one individual. Equating $\mathrm{MSE}(\bar{X}_T)$ and $\mathrm{MSE}(\mathrm{IC}_t)$, and solving for T if $t \to \infty$, gives:

$$T_\infty^\star = 1 + \frac{\sigma^2}{\tau^2}$$

Estimation error decomposition with delay-dependent covariance. We modify the error decomposition to allow for delay-dependent individual-level noise. Estimation errors can be decomposed into population bias μ, individual-level bias u_i that remains irrespective of the delay, and delay-dependent individual-level noise $v_{i,j}$:

$$x_{i,j} = \mu + u_i + v_{i,j}$$

We assume that $u_i \sim N(0, \tau^2)$ and $(v_{i,1}, \ldots, v_{i,j}) \sim N(0, \Sigma)$, where Σ is a variance–covariance matrix with constant variance σ^2 and delay-dependent covariances:

$$\Sigma_{j,j} = \sigma^2$$

$$\Sigma_{j,j'} = f(\Delta(j,j'))$$

We assume that $f(\Delta(j,j'))$ decays exponentially with the delay $\Delta(j,j')$ between estimates $x_{i,j}$ and $x_{i,j'}$ from the same individual:

$$f(\Delta(j,j')) = \sigma^2(1-\delta)e^{-\lambda\Delta(j,j')}$$

where λ determines the speed of decay, and $(1-\delta)$ allows for a discontinuous jump such that estimates provided simultaneously are not required to be perfectly correlated. The half-life of the decay-dependent covariance, $t_{1/2}$, is:

$$t_{1/2} = \frac{\ln(2)}{\lambda}$$

The (overall) covariance between two estimates $x_{i,j}$ and $x_{i,j'}$ from the same individual is then given by:

$$\tau^2 + \sigma^2(1-\delta)e^{-\lambda\Delta(j,j')}$$

which converges to τ^2 if $\Delta(j,j') \to \infty$. $T_\infty^\star$ then converges to $1 + \sigma^2/\tau^2$, which is the highest possible value of $T_\infty^\star$ that can be obtained by exploiting the benefits of delay.

Life Sciences Reporting Summary. Further information on experimental design is available in the Life Sciences Reporting Summary.

Code availability. The code used to generate the results in this study is available in the Supplementary Information.

Data availability. The data used in this study are from Holland Casino. In accordance with the Dutch Personal Data Protection Act, the data were provided in pseudonymized form, under non-disclosure agreements, and for scientific purposes only. Because of the non-disclosure agreements, the data are not publicly available. For reproducibility, the authors will archive the data on a secure VU Amsterdam server for at least five years after publication (contact: D.v.D.).

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Author contributions

D.v.D. and M.J.v.d.A. designed the research, performed the research, contributed new analytic tools, analysed the data, and wrote the paper.

Competing interests

The authors declare no competing interests.

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Experimental design

1. Sample size

Describe how sample size was determined.

The paper uses archival data from three large natural experiments organized by a casino company. Sample size was equal to the frequency of participation by casino visitors.

2. Data exclusions

Describe any data exclusions.

Our raw data consists of 1,165,279 entries made in the three guessing competitions. Of these observations, we remove 27 duplicate entries and 18 entries made prior to the official starting dates of the competitions (the latter entries were clearly contrived and most likely test inputs by employees of the Casino to confirm that the system worked as planned). These data cleaning steps are described on page 2 of the Supplement. Apart from these few deletions, all data is used in the analyses.

3. Replication

Describe whether the experimental findings were reliably reproduced.

We study data from the three guessing competitions, organized by the same casino company in different years, separately to see whether findings are reliably reproduced across the different competitions. Our results show that the findings were indeed reliably reproduced.

4. Randomization

Describe how samples/organisms/participants were allocated into experimental groups.

Participants are not allocated into experimental groups. We use archival data.

5. Blinding

Describe whether the investigators were blinded to group allocation during data collection and/or analysis.

Participants are not allocated into experimental groups. We use archival data.

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For all figures and tables that use statistical methods, confirm that the following items are present in relevant figure legends (or in the Methods section if additional space is needed).

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7. Software

Describe the software used to analyze the data in this study.	The statistical program R was used to analyze the data.

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8. Materials availability

Indicate whether there are restrictions on availability of unique materials or if these materials are only available for distribution by a for-profit company.	The data used in this study were provided by Holland Casino. In accordance with the Dutch Personal Data Protection Act, the data were provided in pseudonymized form, under non-disclosure agreements, and for scientific purposes only. For reproducibility, the authors will archive the data on a secure VU Amsterdam server for at least five years after publication. Because of the non-disclosure agreements, the data are not publicly available.

9. Antibodies

Describe the antibodies used and how they were validated for use in the system under study (i.e. assay and species).	No antibodies were used.

10. Eukaryotic cell lines

a. State the source of each eukaryotic cell line used.	No eukaryotic cell lines were used.
b. Describe the method of cell line authentication used.	No eukaryotic cell lines were used.
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Policy information about studies involving animals; when reporting animal research, follow the ARRIVE guidelines

11. Description of research animals

Provide details on animals and/or animal-derived materials used in the study.	No animals were used.

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12. Description of human research participants

Describe the covariate-relevant population characteristics of the human research participants.	Our study does not involve human research participants, in the sense that there was no intervention or interaction with individuals and we do not have specific information that can be used to identify individuals. We use archival data on guessing competitions organized by a casino company. Across the three years of data combined, 60% of the participants were male and the average age was 39 years.