

## Example Code

Suppose we are interested in finding the vertical intercept "a" of a dataset consisting of three variables:  $y$  is a function of two independent variables  $x_1$  and  $x_2$  with the dependency:

$$y(x_1, x_2) = a + b \cdot x_1 + c \cdot x_2^2$$

At each measurement of  $y(x_1, x_2)$  there is random noise present. The parameters  $(a, b, c)$  are estimated with a multivariate fit to the data which is averaged over  $N$  measurements of  $y(x_1, x_2)$ . The quality of the fitted parameter  $a$  is evaluated as a function of  $N$  to test how many measurements are required to obtain a good estimate.

For example, this could represent the following investigation. We believe from an analytical model that the intensity of light received at a pixel located at  $(x_1, x_2)$  is given by

$$y(x_1, x_2) = a + b \cdot x_1 + c \cdot x_2^2$$

when observing a feature on the surface of a star. There is also a random level of noise present at each pixel associated with stochastic effects arising from the photosphere of the star. In order to estimate the value  $a$  of the light intensity present at  $(0, 0)$  on the CCD we take several photographs. An estimate of  $(a, b, c)$  is made for each photograph based on a fit to the function  $y(x_1, x_2)$  and then an overall estimate for  $a$  is found by averaging the value calculated from each photograph.