

Title

Name

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Abstract: A few sentences summarizing the topics of each problem. The document should be in APS PRB format.

I. PROBLEM 1

Here we look to find a root for the equation $f(x) = e^{x^2} \ln(x^2) - x$, utilizing an implimentation of the secant method. We look at how the delta (δ) affects how close the program gets to the true root value.

The secant method is similar to Newton's method, only it doesn't require knowing the derivative of the function: It takes two starting points instead of one and draws a secant line from them which should (hopefully) intersect with the x-axis. The value is taken from that intersection and plugged back into the equation. The first guess point is replaced with the second, and the second is replaced with the point that was just obtained. This process is repeated until a guess is within a distance of δ to the previous guess.

The simulation was run with δ ranging from 10^{-100} to 10^{-10} , anything larger yielded a single value. The results plotted the root value obtained over δ :

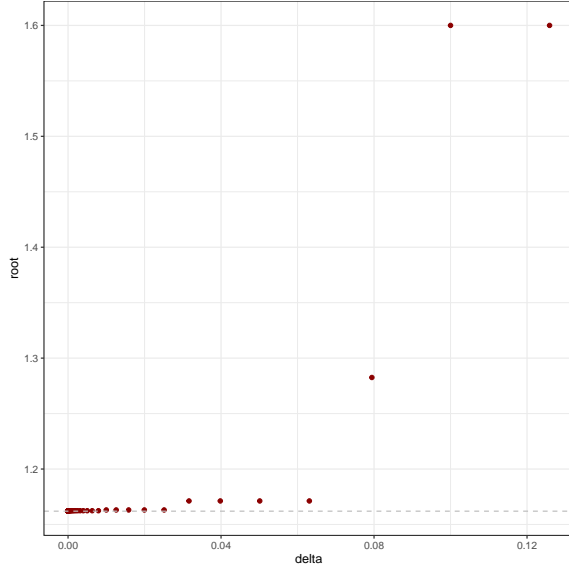


FIG. 1. Secant Method

Here it's clear that smaller values of delta yield results that are closer to the true root, represented with a gray dotted line. We can also see that there are clear "steps" as we get closer and closer to the root, starting at 1.6, representing each step the secant method takes to get to the root.

II. PROBLEM 2

Here we look to use an implimentation of Newton's method to solve a system of equations:

$$f_1(x_1, x_2) = e^{x_1^2} \ln(x_2) - x_1 \quad (1)$$

$$f_2(x_1, x_2) = e^{x_2^2} \ln(x_1) - x_2^2 \quad (2)$$

We look at how the delta (δ) affects how close the program gets to the true root value.

Newton's method has a few differences when using it on multidimensional systems of equations.

$$x_{n+1} = x_n + \frac{f(x_n)}{f'(x_n)} \quad (3)$$

$$\mathbf{f}(\mathbf{x} + \Delta \mathbf{x}) = \mathbf{f}(\mathbf{x}) + \mathbf{J}(\mathbf{x}) \Delta \mathbf{x} \quad (4)$$

$$-\mathbf{f}(\mathbf{x}) \approx \mathbf{J}(\mathbf{x}) \Delta \mathbf{x} \quad (5)$$

LU decomposition is used to solve equation 5 for $\Delta \mathbf{x}$.

The simulation was run with δ ranging from 10^{-100} to 1. The results plotted the root value's y component over it's x component with the color gradient representing δ :

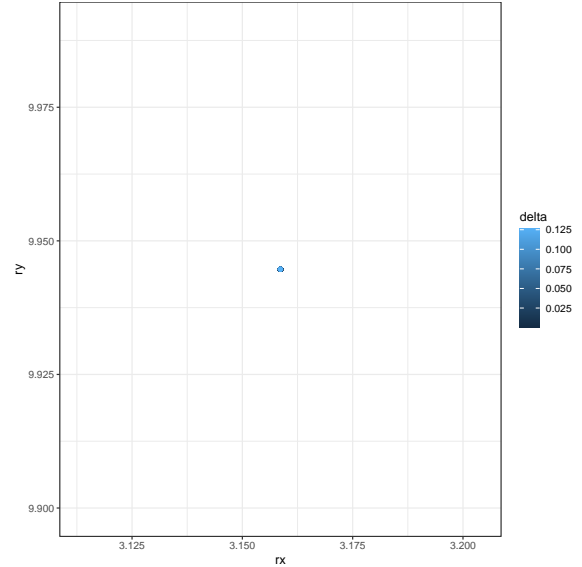


FIG. 2. Plot of something really interesting

Something clearly went wrong in the code here as the root values stay at one point. Ideally we would be able

to see the path the algorithm takes to obtain the root with a gradient color as it approaches.

Make sure you include references to documents [1] you may have used.

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- [1] T. Pang, *Introduction to Computational Physics*, Cambridge University Press (2006).