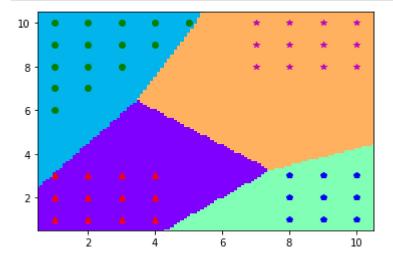
```
In [1]:
         import numpy as np
         import matplotlib.pyplot as plt
In [2]:
         data0 = np.loadtxt("data0.txt")
         X0 = data0[:,:2]
         y0 = data0[:,-1]
         print(X0.shape, y0.shape)
        (48, 2) (48,)
In [3]:
         def converged(w, b, X, y):
           predictions = np.argmax((X @ w) + b.reshape((1, -1)), axis=1)
           return np.allclose(predictions, y)
         def perceptron(X, y):
           num_classes = len(np.unique(y))
           n = X.shape[0]
           w = np.zeros((X.shape[1], num_classes))
           b = np.zeros(num_classes)
           perm = np.random.choice(range(n), n, replace=False)
           X_{perm} = X[perm]
           y_perm = y[perm]
           num iterations = 0
           max iterations = 999
           while not converged(w, b, X, y) and num iterations < max iterations:</pre>
             for i in range(n):
               Xi = X_perm[i]
               yi = int(y_perm[i])
               y_pred = int(np.argmax(Xi.reshape((1, -1)) @ w + b))
               if yi != y_pred:
                 w[:,yi] += Xi
                 b[yi] += 1
                 w[:,y pred] -= Xi
                 b[y\_pred] -= 1
             num iterations += 1
           return w, b
         def plot0(X, y, w, b):
           min_x1, max_x1 = np.min(X[:,0]) - 0.5, np.max(X[:,0]) + 0.5
           min_x2, max_x2 = np.min(X[:,1]) - 0.5, np.max(X[:,1]) + 0.5
           delta = 0.1
           plt.xlim(min_x1, max_x1)
           plt.ylim(min x2, max x2)
           xx, yy = np.meshgrid(np.arange(min_x1, max_x1 + delta, delta), np.arange(min_x2, max_
           pairs = np.c [xx.flatten(), yy.flatten()]
           zz = np.zeros(len(pairs))
           for i, pair in enumerate(pairs):
             pair2 = pair.reshape((1, -1))
             zz[i] = np.argmax((pair2 @ w ).flatten() + b)
           zz = zz.reshape(xx.shape)
           styles = ["^r", "og", "pb", "*m"]
           for i in range(4):
```

```
Xi, yi = X[y==i], y[y==i]
plt.plot(Xi[:,0], Xi[:,1], styles[i])
plt.pcolormesh(xx, yy, zz, cmap="rainbow", vmin=0, vmax=4)
plt.show()
```



Q7

```
In [5]:
    data1 = np.loadtxt("data1.txt")
    data2 = np.loadtxt("data2.txt")

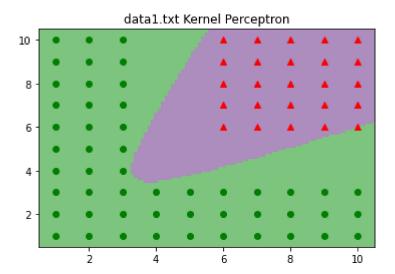
X1, y1 = data1[:,:-1], data1[:,-1]
    X2, y2 = data2[:,:-1], data2[:,-1]
    print(X1.shape, X2.shape, y1.shape, y2.shape)
```

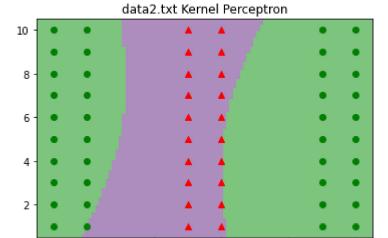
(76, 2) (60, 2) (76,) (60,)

```
In [6]:
         def kernel_classify(b, X, x, y, alpha):
           terms = alpha.flatten() * y.flatten()
           dots = np.square(1 + X @ x.reshape((-1, 1))).flatten()
           w dot phi = np.dot(terms, dots)
           decision = w dot phi + b
           return np.sign(decision)
         def kernel_converge(b, X, y, alpha):
           dot_matrix = np.square(1 + X @ X.T)
           column_terms = (alpha * y).reshape((-1, 1))
           logit_matrix = dot_matrix * column_terms
           predictions = np.sum(logit matrix, axis=0) + b
           return np.allclose(np.sign(predictions), y)
         def kernel_perceptron(X, y):
           n, d = X.shape
           alpha = np.zeros(n)
```

```
b = 0
           for i in range(8000):
             perm = np.random.choice(n, n, replace=False)
             for j in perm:
               xj = X[j]
               yj = y[j]
               if kernel_classify(b, X, xj, y, alpha) != yj:
                 alpha[j] += 1
                 b += yj
             if kernel_converge(b, X, y, alpha):
               return alpha, b, X, y
           raise Exception("Did not converge")
         def gen_classify(alpha, b, X, y):
           def clas(x):
             phis = ((1 + X @ x.reshape((-1, 1))) ** 2).flatten()
             decision = np.sum(alpha * y * phis) + b
             return np.sign(decision)
           return clas
         def plot1(X, y, classify, title=""):
           min x1, max_x1 = np.min(X[:,0]) - 0.5, np.max(X[:,0]) + 0.5
           min_x^2, max_x^2 = np.min(X[:,1]) - 0.5, np.max(X[:,1]) + 0.5
           delta = 0.1
           plt.xlim(min x1, max x1)
           plt.ylim(min x2, max x2)
           xx, yy = np.meshgrid(np.arange(min x1, max x1 + delta, delta), np.arange(min x2, max
           pairs = np.c [xx.flatten(), yy.flatten()]
           zz = np.zeros(len(pairs))
           for i, pair in enumerate(pairs):
             pair2 = pair.reshape((1, -1))
             zz[i] = classify(pair)
           zz = zz.reshape(xx.shape)
           styles = ["^r", "og"]
           for idx, label in enumerate([-1, 1]):
             Xi, yi = X[y==label], y[y==label]
             plt.plot(Xi[:,0], Xi[:,1], styles[idx])
           plt.pcolormesh(xx, yy, zz, cmap=plt.cm.PRGn, vmin=-2, vmax=2)
           if title:
             plt.title(title)
           plt.show()
In [7]:
         np.random.seed(123)
         alpha_1, b_1, X_1, y_1 = kernel_perceptron(X1, y1)
         clas 1 = gen classify(alpha 1, b 1, X 1, y 1)
         plot1(X_1, y_1, clas_1, title = "data1.txt Kernel Perceptron")
         np.random.seed(999)
         alpha_2, b_2, X_2, y_2 = kernel_perceptron(X2, y2)
         clas 2 = gen classify(alpha 2, b 2, X 2, y 2)
```

plot1(X 2, y 2, clas 2, title = "data2.txt Kernel Perceptron")

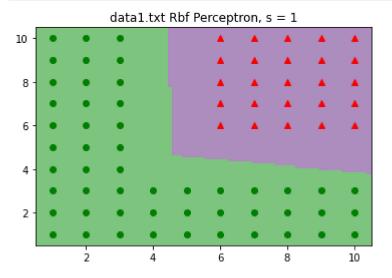


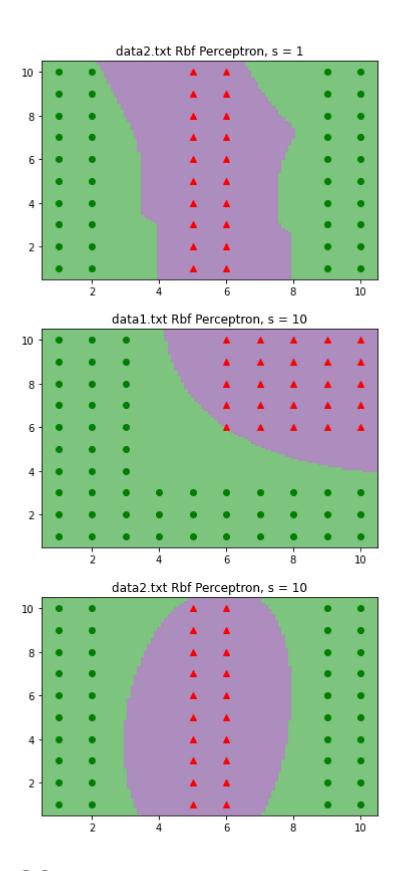


```
In [8]:
         def rbf_classify(b, X, x, y, alpha, s):
           terms = alpha.flatten() * y.flatten()
           distances = np.exp(-np.sum(np.square(X - x.reshape((1, -1))), axis = 1) / (s ** 2))
           decision = np.sum(distances * terms) + b
           return np.sign(decision)
         def rbf_converge(b, X, y, alpha, s):
           n, d = X.shape
           terms = alpha.flatten() * y.flatten()
           for i in range(n):
             xi = X[i]
             yi = y[i]
             distances = np.exp(-np.sum(np.square(X - xi.reshape((1, -1))), axis = 1) / (s ** 2)
             decision = np.sum(distances * terms) + b
             if not np.sign(decision) == yi:
               return False
           return True
         def rbf_perceptron(X, y, s):
           n, d = X.shape
           alpha = np.zeros(n)
           b = 0
           for i in range(8000):
             perm = np.random.choice(n, n, replace=False)
```

```
for j in perm:
      xj = X[j]
      yj = y[j]
      if rbf_classify(b, X, xj, y, alpha, s) != yj:
        alpha[j] += 1
        b += yj
    if rbf_converge(b, X, y, alpha, s):
      return alpha, b, X, y
  raise Exception("Did not converge")
def rbf_gen_classify(alpha, b, X, y, s):
  def clas(x):
    terms = alpha.flatten() * y.flatten()
    distances = np.exp(-np.sum(np.square(X - x.reshape((1, -1))), axis = 1) / (s ** 2))
    decision = np.sum(distances * terms) + b
    return np.sign(decision)
  return clas
```

```
In [9]:
         s = 1
         np.random.seed(123)
         alpha_1, b_1, X_1, y_1 = rbf_perceptron(X1, y1, s)
         clas_1 = rbf_gen_classify(alpha_1, b_1, X_1, y_1, s)
         plot1(X_1, y_1, clas_1, title = f"data1.txt Rbf Perceptron, s = {s}")
         np.random.seed(999)
         alpha 2, b 2, X 2, y 2 = rbf perceptron(X2, y2, s)
         clas 2 = rbf gen classify(alpha 2, b 2, X 2, y 2, s)
         plot1(X 2, y 2, clas 2, title = f"data2.txt Rbf Perceptron, s = {s}")
         s = 10
         np.random.seed(123)
         alpha_1, b_1, X_1, y_1 = rbf_perceptron(X1, y1, s)
         clas_1 = rbf_gen_classify(alpha_1, b_1, X_1, y_1, s)
         plot1(X_1, y_1, clas_1, title = f"data1.txt Rbf Perceptron, s = {s}")
         np.random.seed(999)
         alpha_2, b_2, X_2, y_2 = rbf_perceptron(X2, y2, s)
         clas 2 = rbf gen classify(alpha 2, b 2, X 2, y 2, s)
         plot1(X 2, y 2, clas 2, title = f"data2.txt Rbf Perceptron, s = {s}")
```





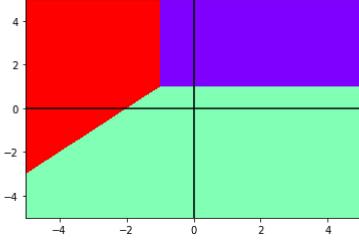
Q8

```
import sklearn.datasets as ds
data = ds.fetch_openml("mnist_784")
```

```
he pandas parser may return different data types. See the Notes Section in fetch openm
         l's API doc for details.
           warn(
In [11]:
          X = data['data'].to numpy()
          y = np.array([int(q) for q in data['target']])
          print(X.shape, y.shape)
          X \text{ tr}, X \text{ te} = X[:60000,:], X[60000:,:]
          y_{tr}, y_{te} = y[:60000], y[60000:]
          print(X tr.shape, X te.shape, y tr.shape, y te.shape)
         (70000, 784) (70000,)
         (60000, 784) (10000, 784) (60000,) (10000,)
In [12]:
          from sklearn.svm import LinearSVC
          def experiment(svm: LinearSVC, X_tr, X_te, y_tr, y_te):
            reg = svm.fit(X_tr, y_tr)
            pred tr = reg.predict(X tr)
            pred te = reg.predict(X te)
            err tr = np.mean(np.not equal(y tr.flatten(), pred tr))
            err te = np.mean(np.not equal(y te.flatten(), pred te))
            return err tr, err te, reg
          for C in [0.01, 0.1, 1.0, 10, 100]:
            svm = LinearSVC(loss="hinge", C=C, max iter=100)
            err tr, err te, reg = experiment(svm, X_tr, X_te, y_tr, y_te)
            print(f"C={C}")
            print(f"\t{err_tr=}, {err_te=}")
         c:\Users\James\anaconda3\envs\mlenv\lib\site-packages\sklearn\svm\ base.py:1244: Converg
         enceWarning: Liblinear failed to converge, increase the number of iterations.
           warnings.warn(
         C = 0.01
                 err tr=0.1543833333333334, err te=0.1579
         c:\Users\James\anaconda3\envs\mlenv\lib\site-packages\sklearn\svm\ base.py:1244: Converg
         enceWarning: Liblinear failed to converge, increase the number of iterations.
           warnings.warn(
         C = 0.1
                 c:\Users\James\anaconda3\envs\mlenv\lib\site-packages\sklearn\svm\ base.py:1244: Converg
         enceWarning: Liblinear failed to converge, increase the number of iterations.
           warnings.warn(
         C = 1.0
                 err tr=0.1203833333333333, err te=0.1219
         c:\Users\James\anaconda3\envs\mlenv\lib\site-packages\sklearn\svm\_base.py:1244: Converg
         enceWarning: Liblinear failed to converge, increase the number of iterations.
           warnings.warn(
         C=10
```

c:\Users\James\anaconda3\envs\mlenv\lib\site-packages\sklearn\datasets_openml.py:932: F
utureWarning: The default value of `parser` will change from `'liac-arff'` to `'auto'` i
n 1.4. You can set `parser='auto'` to silence this warning. Therefore, an `ImportError`
will be raised from 1.4 if the dataset is dense and pandas is not installed. Note that t

```
err_tr=0.15, err_te=0.1626
         c:\Users\James\anaconda3\envs\mlenv\lib\site-packages\sklearn\svm\_base.py:1244: Converg
         enceWarning: Liblinear failed to converge, increase the number of iterations.
           warnings.warn(
In [14]:
          from sklearn.svm import SVC
          svm = SVC(kernel="poly", degree = 2, C=1.0, max_iter=500)
          err tr, err te, reg = experiment(svm, X tr, X te, y tr, y te)
          print(f"C={1}")
          print(f"\t{err_tr=}, {err_te=}")
          print(f"\tnum_sup_vec = {len(reg.support_)=}")
         c:\Users\James\anaconda3\envs\mlenv\lib\site-packages\sklearn\svm\ base.py:299: Converge
         nceWarning: Solver terminated early (max_iter=500). Consider pre-processing your data w
         ith StandardScaler or MinMaxScaler.
           warnings.warn(
         C=1
                 num_sup_vec = len(reg.support_)=9158
In [15]:
          import matplotlib.pyplot as plt
In [22]:
          xx, yy = np.meshgrid(np.arange(-5, 5, 0.01), np.arange(-5, 5, 0.01))
          c1 = xx + yy
          c2 = xx + 1
          c3 = yy - 1
          z = np.argmax(np.stack((c1, c2, c3)), axis=0)
          print(xx.shape, yy.shape)
          print(z.shape)
          plt.pcolormesh(xx, yy, z, cmap="rainbow", vmin=0, vmax=2)
          plt.axhline(0, color='black')
          plt.axvline(0, color='black')
         (1000, 1000) (1000, 1000)
         (1000, 1000)
Out[22]: <matplotlib.lines.Line2D at 0x22e52dd4580>
          4
```



C=100