

COMSM1302

Overview of Computer Architecture

Lecture 1 – Introduction & representation of data

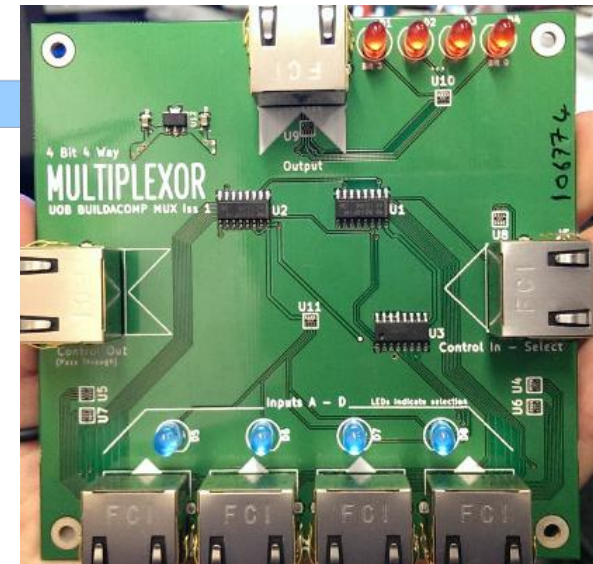
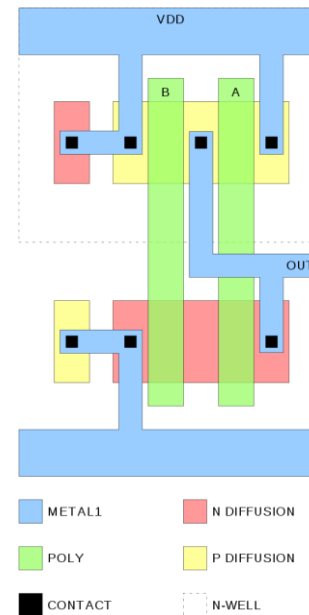


What to expect

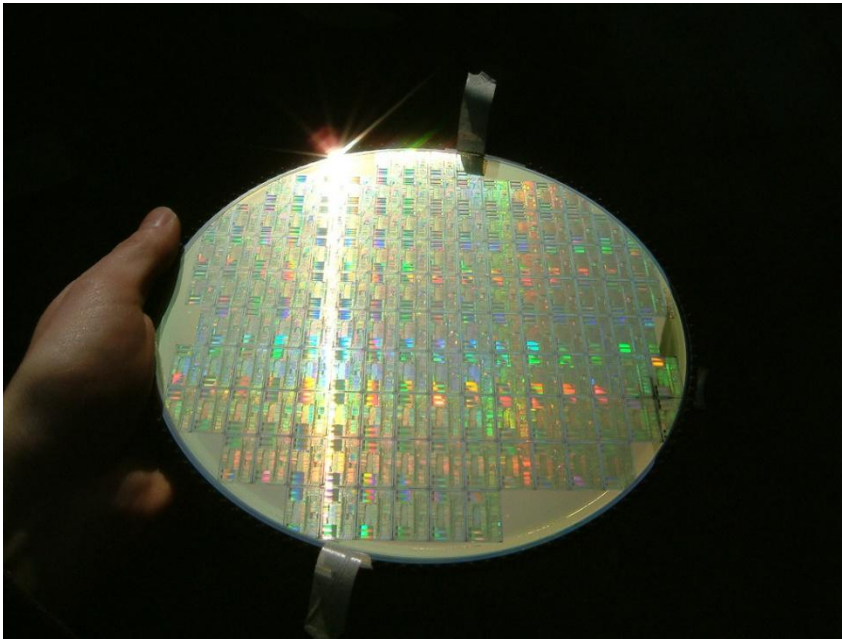
INTRODUCTION

🔥 Where are you?

- This is a unit on **computer architecture**.
- But *what is that?*
- Modern computer systems are extremely complex.
- Computer architecture is about how we design and construct them.
 - And make sure they're **useful!**



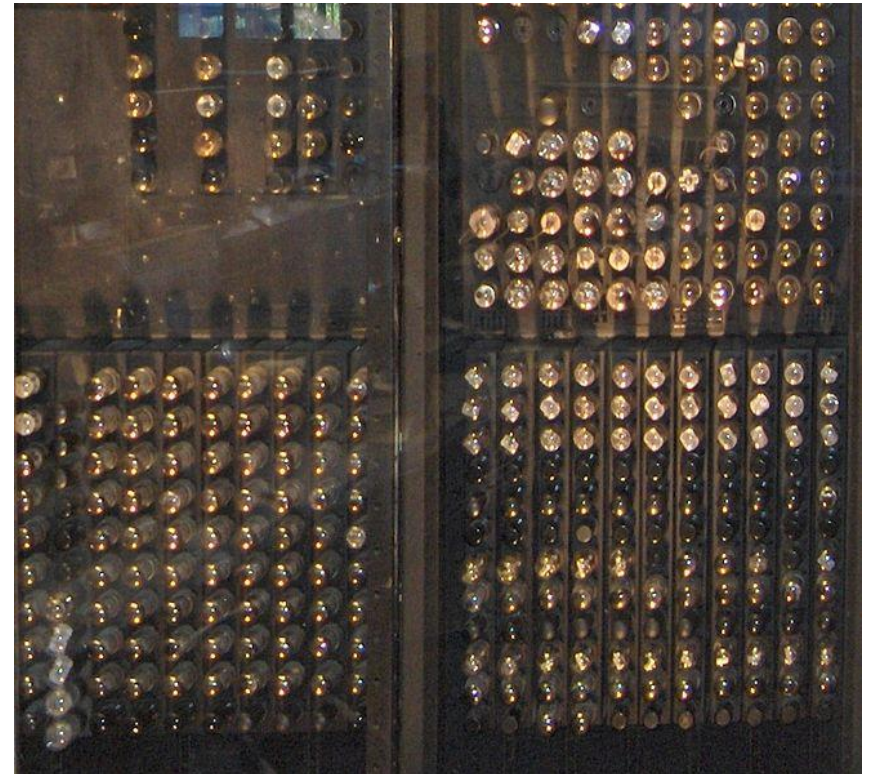
Unit structure



- Teaching
 - Two lectures per week, 1 hour each.
 - Lab sessions, every week, 2 hours each.
 - Worksheets (self assessed).
- **Assessment**
 - **Lab-based** assignments.
 - End of unit **viva** (short interview).

🔥 Getting help

- Questions in lectures
- Supervision and demonstration in labs
- [Unit web page](#)
- [Forum](#)
 - Register for e-mail alerts
 - Help each other
- Don't be shy 😊



In this unit

Foundations

- Data representation, logic.

Building blocks

- Transistors, transistor based logic, simple devices, storage.

Modules

- Hex modules, memory, simple controller and processor.

Programming

- Assembly, assembler, language, compilation phases, boot-strapping.

Bigger systems

- ARM & Thumb, I/O, protecting shared systems, memory hierarchy, multi-processors, networks.

Wrap-up

- More examples, historical computers, contemporary systems.



What's in a number? What's in a bit?

DATA REPRESENTATION

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What is a number?



- Counting

1

2

3

—

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- Without which a large portion of mathematics is meaningless.

Representation - Bases



- Sometimes we think about counting in terms of “Units, tens, hundreds, ...”

100s	10s	1s	Result
0	0	0	0
0	0	1	1
0	0	3	3
0	1	3	13
1	0	0	100
1	2	8	128

Representation - Bases

- An expression for this:

$$Y = \sum_{i=0}^{N-1} x_i \cdot 10^i$$

- Example:

$$x = \{ 1, 0, 4 \}$$

$$Y = 1 \times 10^2 + 0 \times 10^1 + 4 \times 10^0$$

$$Y = 104$$

- **Base-10** numerical representation.

Representation - Bases

- Base-10 is the most obvious, because we use it widely.
 - We (typically) have ten digits on our hands.
- But the base **does not have to be 10**.

$$Y = \sum_{i=0}^{N-1} x_i \cdot B^i$$

- Constraint:

$$x_i < B$$

Representation – Base-2



Base-10

10s	1s	Result
0	0	0
0	1	1
0	2	2
0	3	3
0	4	4
0	5	5
0	6	6
0	7	7
0	8	8
0	9	9
1	0	10

Base-2

8s	4s	2s	1s	Result
0	0	0	0	0
0	0	0	1	1
0	0	1	0	10
0	0	1	1	11
0	1	0	0	100
0	1	0	1	101
0	1	1	0	110
0	1	1	1	111
1	0	0	0	1000
1	0	0	1	1001
1	0	1	0	1010

🔥 Representation – Bases 8 and 16

🔥 Base-8

8s	1s	
0	0	
0	1	
0	2	
0	3	
0	4	4
0	5	5
0	6	6
0	7	7
1	0	10
1	1	11
1	2	12

Remember...

1, 2, 3
a, b, c

They're just symbols!

Base-16

16s	1s	Result
0	0	0
0	1	1
0	2	2
0	3	3
0	4	4
0	5	5
0	6	6
0	7	7
0	8	8
0	9	9
0	a	a

Final notes on bases

- Base-16 needs 16 symbols per digit:
 - 0,1,2,3,4,5,6,7,8,9,a,b,c,d,e,f
- And it doesn't stop there... Base-64
 - A,B,C,D,E,F,G,H,I,J,K,L,M,N,O,P,Q,R,S,T,U,V,W,X,Y,Z,
a,b,c,d,e,f,g,h,i,j,k,l,m,n,o,p,q,r,s,t,u,v,w,x,y,z,
0,1,2,3,4,5,6,7,8,9,+,/
- Sometimes we give hints with prefixes:
 - 0b1011 (Base-2, binary)
 - 0o1011 (Base-8, octal)
 - 0x1011 (Base-16, hexadecimal)
 - Because it's **not always obvious** what base something is!

🔥 In comp-arch, base-2 is king



- Computers tend to represent data internally in base-2 (binary).
 - We will see why next lecture!
- Binary isn't very easy to read as a human.
- Base-16 (hexadecimal) is easier, more compact.

0x	8				b			
0b	1	0	0	0	1	0	1	1

🔥 What's in a number?

- We now know about how to represent numbers.
- But what do those numbers represent?

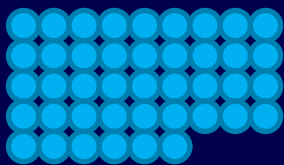
42, 0x2a, 0b101010, “Forty two”

A quantity

An intensity
of colour

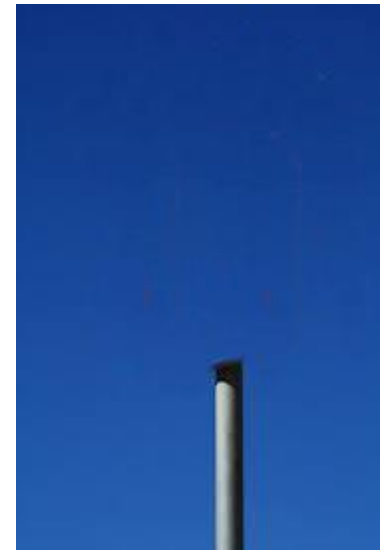
A character

An angle



Binary number representations

- Size
 - Bits
- Limited range
 - Unsigned
 - Signed
 - Fixed point
- Dynamic range
 - Floating point



Bits



- Information theory
 - A **bit** is a unit of information gained from, or uncertainty (entropy) prior to, observing an outcome.
 - Flipping a coin – one bit of information
 - Rolling a 6-sided die – $\log_2(6) \approx 2.58$ bits
 - Claude Shannon, 1948, A Mathematical Theory of Communication - <http://www3.alcatel-lucent.com/bstj/vol27-1948/articles/bstj27-3-379.pdf>

Bits



- In binary, each digit contains **one bit** of information.
 - Analogous to an on/off switch
- In computer architecture, most of what we do is governed by **how many bits** we use to represent something.
 - 8-bit, 16-bit, 32-bit, ...

🔥 Unsigned numbers



- Follows the expression we defined
- $B = 2$
- $N = ?$

$$Y = \sum_{i=0}^{N-1} x_i \cdot B^i$$

🔥 Binary

0b10000000

🔥 Hex

0x10

🔥 C

```
uint32_t foo = 128;  
uint32_t bar = 0x10;
```

```
if (foo == bar) {  
    return 1;  
} else {  
    return 0;  
}
```

🔥 Unsigned numbers in 8 bits

- If we have limited storage space, we have limited range.
- For N bits:

$$0 \leq Y \leq 2^N - 1$$

🔥 Binary

0b11111111 + 0b00000001

=

0b00000000

🔥 Hex

0xff + 0x01

=

0x0

🔥 C

```
uint8_t a = 0xff;  
uint8_t b = a + 1;
```

```
printf("%u\n", b);
```

🔥 Signed numbers



- We typically represent numbers with an implicit “+” and an explicit “-” when we write them.
- Computer architecture requires some space to store that information.
- Simplest example: sign-magnitude

Neg	64	32	16	8	4	2	1	Base 10
0	0	0	0	1	0	1	0	10
1	0	0	0	1	0	1	0	-10

What's wrong with sign-magnitude?

- In 8 bits, what range of numbers can we represent?

Example on the board

2s complement

- Let's change what the **most significant bit** (MSB), represents.

$$Y = -x_{N-1} \cdot 2^{N-1} + \sum_{i=0}^{N-2} x_i \cdot 2^i$$

-128	64	32	16	8	4	2	1	Base 10
0	0	0	0	1	0	1	0	10
1	0	0	0	1	0	1	0	-118

2s complement range

- In 8 bits, what range of numbers can we represent?

Example on the board

🔥 What's wrong with integers?

- Whole numbers
- Limited range
- 32-bit int (int32_t) range is -2^{31} to $2^{31}-1$

$$3 \div 2 = ?$$

Fixed point

- In decimal, we have the **decimal-point** (1.5)
- Let's introduce a point...
- Let $p = 1$

$$Y = \sum_{i=0-p}^{N-1-p} x_i \cdot 2^i$$

64	32	16	8	4	2	1	0.5	Base 10
0	0	0	0	1	0	1	1	5.5
1	0	0	0	1	0	0	0	68

Fixed point



- Choose the location of the point carefully.
- What **precision** do you need?
- What **range** do you need?

8	4	2	1	0.5	0.25	0.125	0.0625	Base 10
0	0	0	0	1	0	1	1	0.6875
1	0	0	0	1	0	0	0	8.5

Floating point



- Flexible representation by having a point that can be moved.

$$Y = (-1)^S \cdot M \cdot 2^E$$

Sign	Exponent			Mantissa				Base 10
S	-4	2	1	8	4	2	1	
0	0	0	1	1	0	0	1	18
1	1	0	1	1	0	0	1	-1.125

See the difference



```
printf("%d\n", 3/2);           //Integer  
printf("%f\n", 3.0/2.0);      //Float
```

🔥 What's wrong with floating point?



- Its precision can be a problem
 - Divide a **very large** number by a **very small** number... get an inaccurate answer.
- How do we choose the number of bits in E and M?
- **IEEE 754** tells us!
 - Defines different types of floating point representation.
 - How special values like infinity and not-a-number (NaN) should be represented.

Summary



- Different bases
 - Ease of understanding
 - Ease of implementation
- What a number represents
 - Anything!
- Representing numbers
 - Signed / unsigned
 - Integer / fixed- or floating-point
 - Space, bits, range and precision

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