

Writeup for second project of
CMSC 420: “Data Structures”
Section 0101, Fall 2019

Theme: AVL-G trees

Handout date: Wednesday, **09-11-2019**

On-time deadline: **09-25-2019**

Late deadline (30% penalty): **09-27-2019**

1 Overview

Jason is tired of *the man* telling him that AVL trees should rotate whenever we detect an imbalance of **2 (two)** or **-2 (minus two)** in any given subtree! As we have seen in class, AVL trees are **excellent for search** given their height of $\lfloor \log_2 n \rfloor$ or $\lfloor \log_2 n \rfloor + 1$. Unfortunately, to achieve this efficient search, they have to use **rotations** during **insertions** and **deletions**, and those **take time**!

In this project, you will implement **AVL-G** trees, a simple modification of AVL Trees that allows for tuning the balance of an AVL Tree based on a constructor parameter. Simply put, an AVL- G tree, where $G = 1, 2, 3, \dots$, allows for any given subtree to have a balance of **at most G**. This means that our classic AVL trees can be referred to as “AVL-1” trees. Refer to section [2](#) for examples.

2 AVL-G trees

Remind yourselves of our basic definitions:

- **Height** of a binary tree: The **height** of a binary tree is defined as follows:
 - A **null** (empty) binary tree has a height of -1.

- A non-empty binary tree has a height equal to the maximum of the height of its subtrees + 1 (plus one). A corollary of this is that a “stub” binary tree (one that consists of a single “leaf” node without any children) has a height of 0 (zero).
- **Balance** of a node: The balance of a node is defined by convention as the height of its **left** subtree minus the height of its **right** subtree.

Figure 1 shows an imbalance detected after an insertion into an AVL-1 tree (“classic” AVL tree). The imbalance is detected at the node that contains the key 40 and is equal to -2. If instead we had an AVL-2 tree, this insertion would **not** have triggered a rotation, since -2 is an **admissible** balance metric for AVL-2 trees!

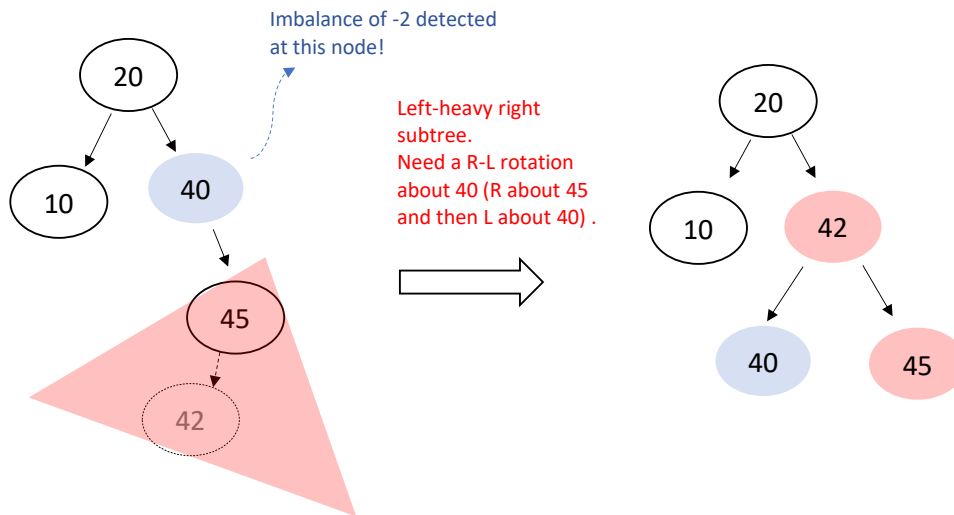


Figure 1: A rotation triggered by an insertion in an AVL-1 (“classic” AVL) tree.

An example of an imbalance and corresponding rotation in an AVL-2 tree is shown in Figure 2. Of course, this insertion would **not** have triggered a rotation in an AVL-3 tree!

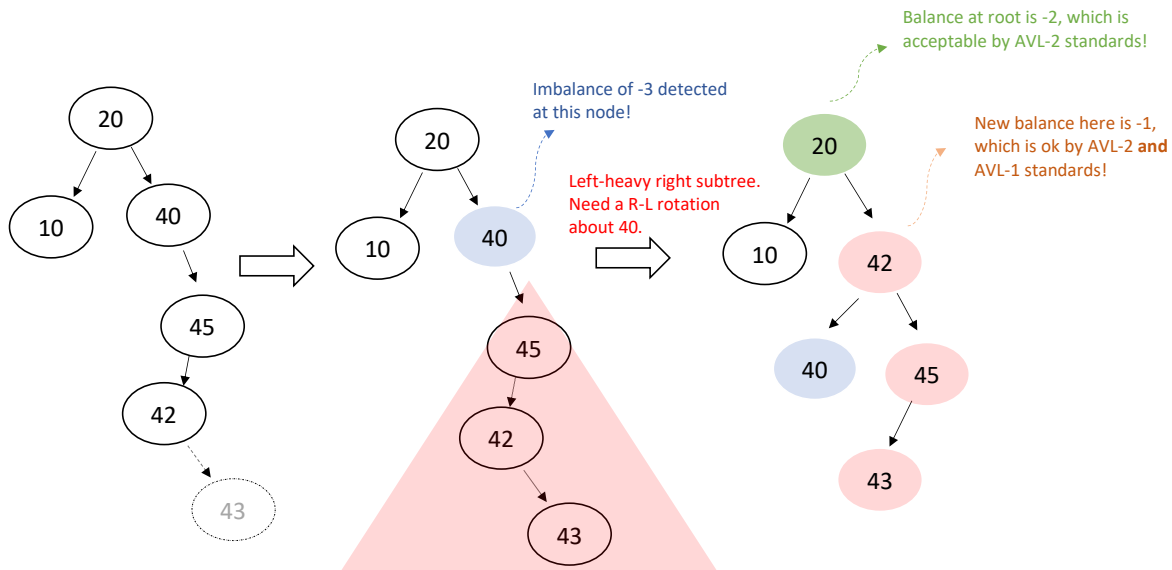


Figure 2: A rotation triggered by an insertion in an AVL-2 tree.

Note that we detect the imbalance at **the node that contains 40**. In order to rectify this imbalance, we need to perform a **R-L rotation** about that node!

An example of an imbalance detected in an AVL-3 tree is shown in Figure 3. Note that this example is based on a **deletion**, just to provide you with a variety of examples. Remember that in deletions, when a certain node detects an imbalance, it is the *opposite* subtree that will have to be mutated so that the entire tree is re-balanced!

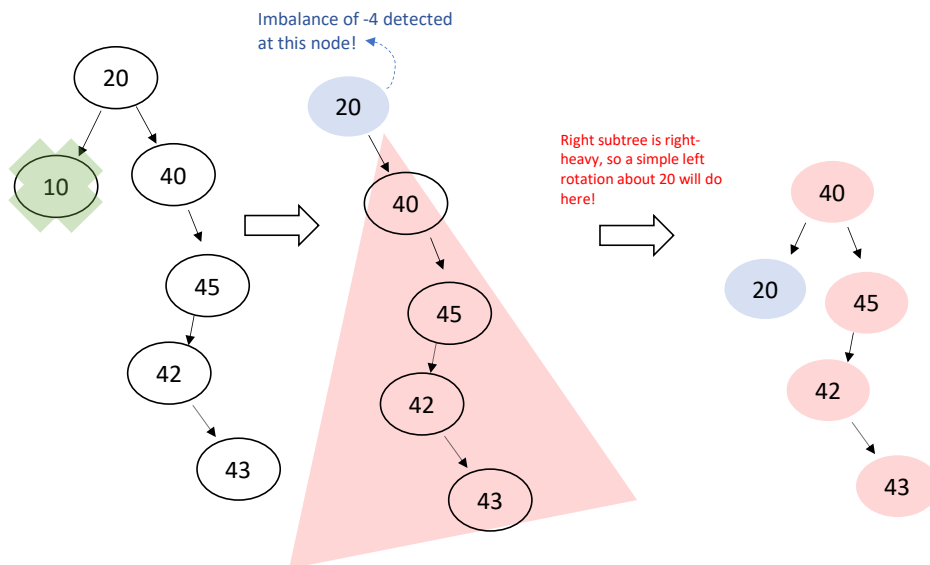


Figure 3: A rotation triggered by a deletion in an AVL-3 tree.

3 Starter Code and Git hints

Everything you need is available in our [Github repository](#). The code for this project is specifically under the sub-package `projects.avlg`. You will only need to implement the class `AVLGTree`. You should read the docs *very carefully*, and make sure you **do not** erase anything from the sub-package `projects.avlg.exceptions`. Those exceptions are used by the `AVLGTree` class and our tests.

You should first run a `git add -A` and a `git commit` to add your code from project 1 and homework 1 to the staging area and then to git's commit history. Doing a `git pull` should then simply add source code and documentation for project 2. There is a chance that you would need to resolve some **merge conflicts**. To resolve them, simply open the files that the command line is telling you have overlapping changes on and choose the parts of the files you want to keep. Since your first project's implementation has already been submitted on the submit server, there is **no way** that any code you have written for your projects can be lost, so you don't have to worry about that at all.

Note that the submit server does **not care at all** about your implementation of the first project; it only cares about the class `projects.avlg.AVLGTree`. As with the first project, if you would like to add classes, enums, interfaces, custom exceptions, extra packages, etc., you are **absolutely free** to do so, yet you should **not** move the class `AVLGTree` from its location in the code tree.

4 Advice / Hints

- The first thing you should do after you pull the code and read this writeup is to read the Javadocs for `AVLGTree` to understand its public interface. By “interface” here we do not refer to a Java interface, but to the way the class “interfaces” with its environment; its API. Once you are certain you understand what the different methods receive as an argument, what they return to the caller and **what kinds of Exceptions they throw**, start writing unit tests **before** you implement your code.
- The core of this project is **understanding rotations**. When should we do a single left or a single right rotation? When is a combination of two rotations appropriate? How can I detect those separate cases in my code? How do I update **heights** during the rotations in the case of an **insertion** and how in the case of a **deletion**?
- The methods `isBST` and `isAVLGBalanced` that you have to implement are **awesome** for testing. Use them to your advantage! Just make sure that

they are implemented correctly by unit-testing **them** as well!

- Read the comments in the file `StudentTests.java`, which contains some starter tests which you can use for your implementation.

