

**Swinburne University of Technology**  
*Faculty of Science, Engineering and Technology*

**ASSIGNMENT COVER SHEET**

---

**Subject Code:** COS30008  
**Subject Title:** Data Structures and Patterns  
**Assignment number and title:** 4, Binary Search Trees & In-Order Traversal  
**Due date:** May 26, 2022, 14:30  
**Lecturer:** Dr. Markus Lumpe

---

**Your name:** \_\_\_\_\_ **Your student id:** \_\_\_\_\_

|                   |              |              |               |               |               |               |               |              |              |              |              |
|-------------------|--------------|--------------|---------------|---------------|---------------|---------------|---------------|--------------|--------------|--------------|--------------|
| Check<br>Tutorial | Mon<br>10:30 | Mon<br>14:30 | Tues<br>08:30 | Tues<br>10:30 | Tues<br>12:30 | Tues<br>14:30 | Tues<br>16:30 | Wed<br>08:30 | Wed<br>10:30 | Wed<br>12:30 | Wed<br>14:30 |
|                   |              |              |               |               |               |               |               |              |              |              |              |

---

Marker's comments:

| Problem | Marks   | Obtained |
|---------|---------|----------|
| 1       | 94      |          |
| 2       | 42      |          |
| 3       | 8+86=94 |          |
| Total   | 230     |          |

---

**Extension certification:**

This assignment has been given an extension and is now due on \_\_\_\_\_

Signature of Convener: \_\_\_\_\_

```
1
2 // COS30008, Problem Set 4, Problem 1, 2022
3
4 #pragma once
5
6 #include <stdexcept>
7 #include <algorithm>
8
9 template<typename T>
10 struct BinaryTreeNode
11 {
12     using BNode = BinaryTreeNode<T>; //BNode represents the btree
13     using BTreeNode = BNode*; //BTreeNode represents the pointer
14
15     T key; //data
16     BTreeNode left;
17     BTreeNode right;
18
19     static BNode NIL;
20
21     const T& findMax() const
22     {
23         if ( empty() )
24         {
25             throw std::domain_error( "Empty tree encountered." );
26         }
27
28         return right->empty() ? key : right->findMax(); // if right is empty then return the node, otherwise keep going
29     }
30
31     const T& findMin() const
32     {
33         if ( empty() )
34         {
35             throw std::domain_error( "Empty tree encountered." );
36         }
37
38         return left->empty() ? key : left->findMin(); // if left is empty then return the node, otherwise keep going
39     }
40
41     bool remove( const T& aKey, BTreeNode aParent )
42     {
43         BTreeNode x = this; // BNode<S>* x
44         BTreeNode y = aParent;
45
46         while ( !x->empty() ) //while current node is not empty
47         {
```

```
48         if ( aKey == x->key ) //if the given key matches the node we break
49         {
50             break;
51         }
52
53         y = x;                                     // new parent (current
           node becomes the parent)
54
55         x = aKey < x->key ? x->left : x->right;      //ternary for if
           the given key is less than current then its set to left,
           otherwise set to right
56     }
57
58     if ( x->empty() )
59     {
60         return false;                             // delete failed
61     }
62
63     if ( !x->left->empty() )
64     {
65         const T& lKey = x->left->findMax();         // find max to left
66         x->key = lKey;
67         x->left->remove( lKey, x );
68     }
69     else
70     {
71         if ( !x->right->empty() )
72         {
73             const T& lKey = x->right->findMin();    // find min to right
74             x->key = lKey;
75             x->right->remove( lKey, x );
76         }
77         else
78         {
79             if ( y != &NIL )                       // y can be NIL
80             {
81                 if ( y->left == x )
82                 {
83                     y->left = &NIL;
84                 }
85                 else
86                 {
87                     y->right = &NIL;
88                 }
89             }
90
91             delete x;                               // free deleted node
92         }
93     }
```

```
94
95     return true;
96 }
97
98 // PS4 starts here
99
100
101 ~BinaryTreeNode()
102 {
103     if (!empty())
104     {
105         if (left != &NIL)
106         {
107             delete left;
108         }
109         if (right != &NIL)
110         {
111             delete right;
112         }
113     }
114 }
115
116 const bool empty()
117 {
118     return this == &NIL;
119 }
120
121 const bool leaf()
122 {
123     return left == &NIL && right == &NIL;
124 }
125
126
127 const size_t height()
128 {
129     if (empty())
130     {
131         throw std::domain_error("Empty tree encountered.");
132     }
133
134     if (leaf())
135     {
136         return 0;
137     }
138
139     size_t left_side = 0;
140     try {
141         left_side = this->left->height(); //get the max height of the left
142             subtree recursively(could also do it iteratively)
```

```
142     }
143     catch(domain_error e) {
144         left_side = 0;
145     }
146
147     size_t right_side = 0;
148     try {
149         right_side = this->right->height(); //get the max height of the right subtree
150     }
151     catch (domain_error e) {
152         right_side = 0;
153     }
154
155     if (left_side > right_side) //compare which side is higher + 1 and return max height
156     {
157         return left_side + 1;
158     }
159     else
160     {
161         return right_side + 1;
162     }
163 }
164
165 const size_t max(size_t left, size_t right)
166 {
167     if (left > right) {
168         return left;
169     }
170     return right;
171 }
172
173
174 bool insert(const T& aKey)
175 {
176     BTreeNode x = this; // BTreeNode x == BNode<S>* x
177     BTreeNode y = &NIL;
178
179     while (!x->empty()) //if root node is NOT empty
180     {
181         y = x; //copy it into y
182
183         if (aKey == x->key) // if there is a duplicate key then theres an error
184         {
185             return false;
186         }
187     }
```

```
188         x = aKey < x->key ? x->left : x->right; //otherwise if the key is  $\rightarrow$ 
           less than current insert to left otherwise to the right
189     }
190
191     BTreeNode z = new BinaryTreeNode(aKey);
192
193     if (y->empty())
194     {
195         return false; // if y is empty x was empty, insertion will fail  $\rightarrow$ 
           (NIL)
196     }
197     else
198     {
199         if (aKey < y->key) //if given key is less than current key,  $\rightarrow$ 
           insert left
200         {
201             y->left = z;
202         }
203         else
204         {
205             y->right = z; //otherwise insert right
206         }
207     }
208     return true;
209 }
210
211 BinaryTreeNode() :
212     key(T()),
213     left(&NIL),
214     right(&NIL)
215 {}
216
217 BinaryTreeNode(const T& aKey):
218     key(aKey),
219     left(&NIL),
220     right(&NIL)
221 {}
222
223 BinaryTreeNode(T&& aKey)
224 :
225     key(std::move(aKey)),
226     left(&NIL),
227     right(&NIL)
228 {}
229 };
230
231 template<typename T>
232 BinaryTreeNode<T> BinaryTreeNode<T>::NIL;
233
```

234

235

```
1
2 // COS30008, Problem Set 4, Problem 2, 2022
3
4 #pragma once
5
6 #include "BinaryTreeNode.h"
7
8 #include <stdexcept>
9
10 // Problem 3 requirement
11 template<typename T>
12 class BinarySearchTreeIterator;
13
14 template<typename T>
15 class BinarySearchTree
16 {
17 private:
18     using BNode = BinaryTreeNode<T>;
19     using BTreeNode = BNode*;
20
21     BTreeNode fRoot;
22
23 public:
24     BinarySearchTree()
25     {
26         fRoot = &BNode::NIL;
27     }
28
29     ~BinarySearchTree() {
30         if (!empty())
31         {
32             if (fRoot->left != &BNode::NIL)
33             {
34                 delete fRoot->left;
35             }
36             if (fRoot->right != &BNode::NIL)
37             {
38                 delete fRoot->right;
39             }
40         }
41     }
42
43     bool empty() const
44     {
45         return fRoot->empty();
46     }
47 }
```



```
50
51     size_t height() const
52     {
53         if (fRoot == NULL)
54         {
55             return 0;
56         }
57         return fRoot->height();
58     }
59
60     bool insert(const T& aKey)
61     {
62         if (empty()) {
63             fRoot = new BNode(aKey);
64             return true;
65         }
66         return fRoot->insert(aKey);
67     }
68
69     bool remove(const T& aKey) {
70
71         //return fRoot->remove(aKey, &BTreeNode::NIL);
72         //return fRoot->remove(aKey, fRoot->NIL);
73         return false;
74     }
75
76
77     // Problem 3 methods
78
79     using Iterator = BinarySearchTreeIterator<T>;
80
81     // Allow iterator to access private member variables
82     friend class BinarySearchTreeIterator<T>;
83
84     Iterator begin() const
85     {
86         return BinarySearchTree<T>(*this);
87     }
88     Iterator end() const
89     {
90         return begin().end();
91     }
92 };
93
```

```
1
2 // COS30008, Problem Set 4, Problem 3, 2022
3
4 #pragma once
5
6 #include "BinarySearchTree.h"
7
8 #include <stack>
9
10 template<typename T>
11 class BinarySearchTreeIterator
12 {
13 private:
14
15     using BSTree = BinarySearchTree<T>;
16     using BNode = BinaryTreeNode<T>;
17     using BTreeNode = BNode*;
18     using BTNStack = std::stack<BTreeNode>;
19
20     const BSTree& fBSTree;    // binary search tree
21     BTNStack fStack;         // DFS traversal stack
22
23     void pushLeft(BTreeNode aNode) {
24         while (!aNode->empty())
25         {
26             if (!fBSTree.fRoot->empty())
27             {
28                 fStack.push(aNode); // pushes aNode to the root
29                 fBSTree.fRoot = fBSTree.fRoot->left; // makes root = left node
30             }
31         }
32     }
33
34 public:
35
36     using Iterator = BinarySearchTreeIterator<T>;
37
38     BinarySearchTreeIterator(const BSTree& aBSTree)
39     :
40         fBSTree(&BNode::NIL),
41         fStack(&BNode::NIL)
42     {
43     }
44
45     const T& operator*() const //get key
46     {
47         if (fStack.empty() == false)
```

```
50     {
51         return fStack.top();
52     }
53 }
54
55 Iterator& operator++()
56 {
57     if ( fStack.empty() == false)
58     {
59         fStack.pop();
60         //fBSTree = fBSTree.fRoot->right;
61         return *this;
62     }
63 }
64
65 Iterator operator++(int)
66 {
67     BinarySearchTreeIterator temp = *this;
68     ++(*this);
69     return temp;
70 }
71
72 bool operator==( const Iterator& aOtherIter ) const
73 {
74     return fStack.size() == aOtherIter.fStack.size();
75 }
76
77 bool operator!=(const Iterator& aOtherIter) const
78 {
79     return !(*this == aOtherIter);
80 }
81
82 Iterator begin() const {
83     return BinarySearchTreeIterator<T>(*this);
84 }
85 Iterator end() const
86 {
87     return begin().end();
88 }
89 };
90
```