

# Introduction to machine learning

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# Course information

- Instructor - Victor Vladimirovich Kitov
  - MSU, NES
  - practical experience
  - academic experience
  - ensemble learning
- Tasks of the course
- Structure: lectures, seminars
- Practice:
  - theoretical tasks
  - programming using python
    - ipython notebook, numpy, scipy, pandas, scikit-learn.

## Recommended materials

- Лекции К.В.Воронцова (видео-лекции и материалы на [machinelearning.ru](http://machinelearning.ru))
- **Statistical Pattern Recognition.** 3rd Edition, Andrew R. Webb, Keith D. Copsey, John Wiley & Sons Ltd., 2011.
- **The Elements of Statistical Learning: Data Mining, Inference, and Prediction.** Trevor Hastie, Robert Tibshirani, Jerome Friedman, 2nd Edition, Springer, 2009. <http://statweb.stanford.edu/~tibs/ElemStatLearn/>.
- **Machine Learning: A Probabilistic Perspective.** Kevin P. Murphy. Massachusetts Institute of Technology. 2012.
- **Pattern Recognition and Machine Learning.** Christopher M. Bishop. Springer. 2006.
- **Any additional public sources** - wikipedia, articles, tutorials, video-lectures.

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- 1 Tasks solved by machine learning
- 2 Main concepts of machine learning.
- 3 Practical applications of machine learning

## Formal definitions of machine learning

- Machine learning is a field of study that gives computers the ability to learn without being explicitly programmed.
- A computer program is said to learn from **experience E** with respect to some **class of tasks T** and **performance measure P**, if its performance P at tasks in T improves with experience E.
- Examples: spam filtering, speech recognition, image recognition (face detection, eyes detection, pose detection, person identification).

## Major niches of ML

- dealing with huge datasets with many attributes (text categorization)
- hard to formulate explicit rules (image recognition)
- further adaptation to usage conditions is required (voice detection)
- fast adaptation to changing conditions (stock prices prediction)

## Connections with other fields

- Computer science
- Pattern recognition
  - recognize patterns and regularities in the data
- Artificial intelligence
  - create devices capable of intelligent behavior
- Time-series analysis
- Theory of probability, statistics
  - rely on probabilistic model
- Optimization methods
- Theory of algorithms

# General problem statement

- Set of objects  $O$
- Each object is described by a vector of known characteristics  $\mathbf{x} \in \mathcal{X}$  and predicted characteristics  $y \in \mathcal{Y}$ .

$$o \in O \longrightarrow (\mathbf{x}, y)$$

- Usually  $\mathcal{X} = \mathbb{R}^D$ ,  $\mathcal{Y}$  - a scalar, but they may be any structural descriptors of objects in general.



## General problem statement

- Task: find a mapping  $f$ , which could accurately approximate  $\mathcal{X} \rightarrow \mathcal{Y}$ .
  - using a finite «training» set of objects with known  $(x, y)$ .
  - to apply on a set of objects of interest
- Questions solved in ML:
  - how to select object descriptors - features
  - in what sense a mapping  $f$  should approximate true relationship
  - how to construct  $f$

# Examples

- Spam filtering
- Document classification
- Web-page ranking
- Sentimental analysis
- Intrusion/fraud detection
- Churn prediction
- Target detection / classification
- Handwriting recognition
- Part-of-speech tagging
- Credit scoring
- Particle classification

## Variants of problem statement

- For each new object  $x$  need to associate  $y$ .
- What is known:
  - $(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)$  - supervised learning:
  - $x_1, x_2, \dots, x_N$  - unsupervised learning
    - dimensionality reduction
    - clustering
  - $(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N), x_{N+1}, x_{N+2}, \dots, x_{N+M}$  - semi-supervised learning.
- If predicted objects  $x'_1, x'_2, \dots, x'_K$  for which  $y$  is forecasted, are known in advance, then this is «transductive» learning.

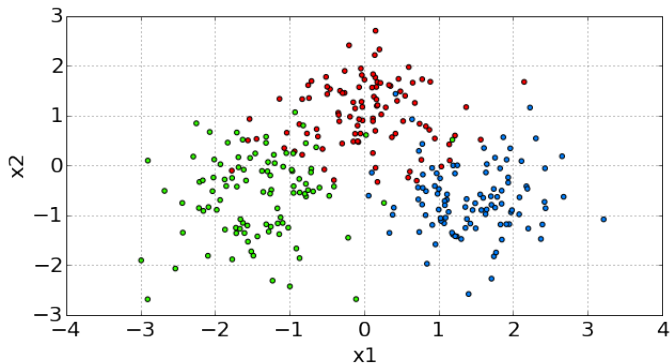
# Types of target variable

- Types of target variable:
  - $\mathcal{Y} = \mathbb{R}$  - regression (in supervised learning)
  - $\mathcal{Y} = \mathbb{R}^M$  - vector regression (in supervised learning) or feature extraction (in unsupervised learning)
  - $\mathcal{Y} = \{\omega_1, \omega_2, \dots, \omega_C\}$  - classification (in supervised learning) or clustering (in unsupervised learning).
    - $C=2$ : binary classification, encoding -  $\mathcal{Y} = \{+1, -1\}$  or  $\mathcal{Y} = \{0, 1\}$ .
    - $C>2$ : multiclass classification
  - $\mathcal{Y}$ -set of all sets of  $\{\omega_1, \omega_2, \dots, \omega_C\}$  - labeling
    - $\mathcal{Y} = \{y \in \mathbb{R}^C : y_i \in \{0, 1\}\}$ ,  $y_i = 1 \Leftrightarrow$  object is associated with  $\omega_i$ .

# Types of features

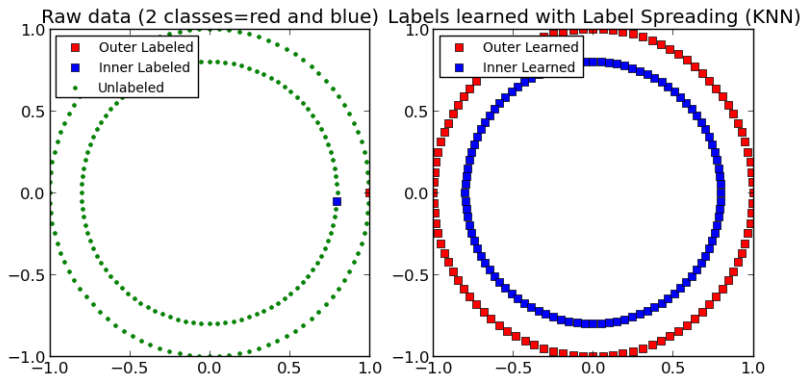
- Full object description  $\mathbf{x} \in \mathcal{X}$  consists of individual features  $x_i \in \mathcal{X}_i$
- Types of feature:
  - $\mathcal{X}_i = \{0, 1\}$  - binary feature
  - $|\mathcal{X}_i| < \infty$  - discrete (nominal) feature
  - $|\mathcal{X}_i| < \infty$  and  $\mathcal{X}_i$  is ordered - ordinal feature
  - $\mathcal{X}_i = \mathbb{R}$  - real feature

## Example of classification



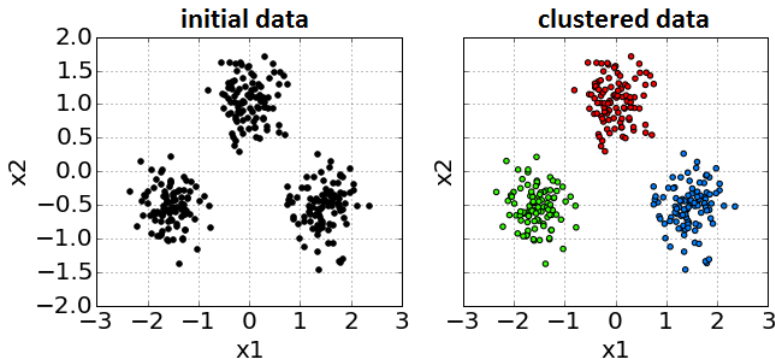
Supervised learning:  $x = (x_1, x_2)$ ,  $y$  is shown with color

# Example of semi-supervised learning



Semi-supervised learning.

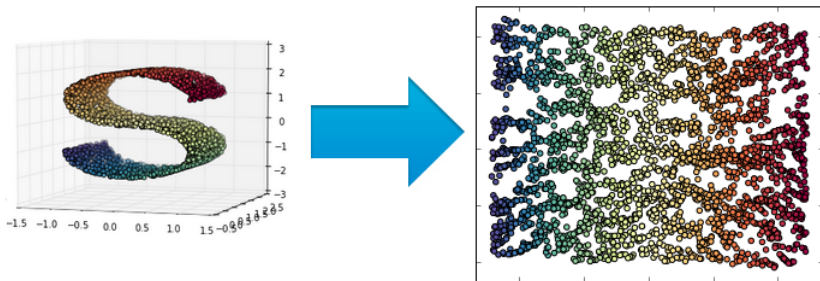
# Example of clustering



Unsupervised learning: clustering



# Example of dimensionality reduction



Unsupervised learning: dimensionality reduction

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# Training set

- **Training set:**  $X \in \mathbb{R}^{N \times D}$  - **design matrix**,  $Y \in \mathbb{R}^N$  - predicted outputs (target values)
- Using  $X, Y$  the task is to estimate unknown parameters  $\hat{\theta}$  of mapping  $\hat{y} = f_{\theta}(x)$  so that it will approximate true relationship  $y = y(x)$
- It is assumed that  $z_n = (x_n, y_n)$  for  $n = 1, 2, \dots, N$  - are independent and identically distributed random variables (i.i.d).
- Two steps of ML:
  - **training**
  - **application**

# Loss function

- **Loss function**  $\mathcal{L}(\hat{y}, y)$

- Examples:

- classification:

- misclassification rate

$$\mathcal{L}(\hat{y}, y) = \mathbb{I}[\hat{y} \neq y]$$

- regression:

- MAE (mean absolute error):

$$\mathcal{L}(\hat{y}, y) = |\hat{y} - y|$$

- MSE (mean squared error):

$$\mathcal{L}(\hat{y}, y) = (\hat{y} - y)^2$$

- absolute relative error:  $\frac{|\hat{y}-y|}{|y|}$ , squared relative error:  $\left(\frac{\hat{y}-y}{y}\right)^2$

## Function class

- **Function class** - parametrized set of functions  
 $F = \{f_\theta, \theta \in \Theta\}$ , from which the true relationship  $\mathcal{X} \rightarrow \mathcal{Y}$  is approximated.

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  - regression:

$$f(x) = \theta_0 + \theta_1 x^1 + \theta_2 x^2 + \dots + \theta_D x^D$$

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$$f(x) = \theta_0 + \theta_1 x^1 + \theta_2 x^2 + \dots + \theta_D x^D$$

- binary classification  $y \in \{+1, -1\}$ :

$$f(x) = \text{sign}\{\theta_0 + \theta_1 x^1 + \theta_2 x^2 + \dots + \theta_D x^D\},$$

# Empirical risk

- **Machine learning algorithm** associates  $f_{\hat{\theta}}(\cdot)$  to  $(X, Y)$ 
  - in the function class  $F = \{f_{\theta}, \theta \in \Theta\}$
  - for given loss function  $\mathcal{L}(\hat{y}, y)$
- **Empirical risk:**

$$L(\theta|X, Y) = \frac{1}{N} \sum_{n=1}^N \mathcal{L}(f_{\theta}(x_n), y_n)$$

- **Method of empirical risk minimization:**

$$\hat{\theta} = \arg \min_{\theta} L(\theta|X, Y)$$



## Estimation of empirical risk

- Generally it holds that:

$$L(\hat{\theta}|X, Y) < L(\hat{\theta}|X', Y')$$

where  $X, Y$  is the training sample and  $X', Y'$  is the new data.

- $L(\hat{\theta}|X', Y')$  can be estimated using :
  - separate **validation set**
  - **cross-validation**
  - **leave-one-out** method

## Levels of fitting

### Underfitted model

Model that oversimplifies true relationship  $\mathcal{X} \rightarrow \mathcal{Y}$ .

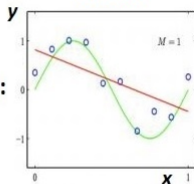
### Overfitted model

Model that is too tuned on particular peculiarities (noise) of the training set instead of the true relationship  $\mathcal{X} \rightarrow \mathcal{Y}$ .

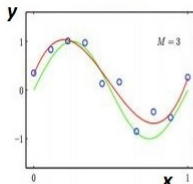
# Examples of overfitted/underfitted models

- true relationship
- estimated relationship with polynimes of order  $M$
- objects of the training sample

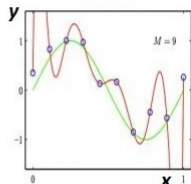
underfitted  
model



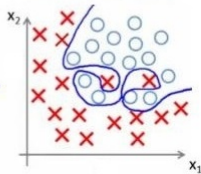
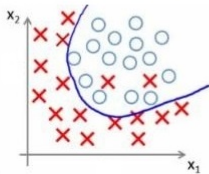
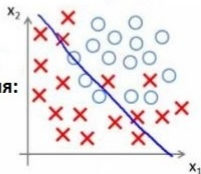
relevant  
model



overfitted  
model



классификация:



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## Examples of ML applications

### Classification:

- spam filtering
- search engine: do query and document match each other?
- is series of network transactions regular or a hacking attempt?
- will the client with given characteristics switch his mobile operator?
- will given client of a bank return his debt?
- does the signal correspond to the target or noise in radar detection?

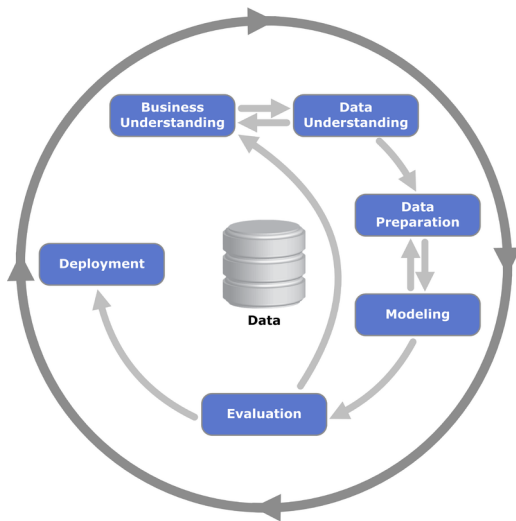
### Labelling:

- assignment of topics to text documents

### Regression:

- determine the flat price by its characteristics
- predict demand for certain product

# CrispDM methodology



## CrispDM general comments

- Log each step
  - quantitative: procedures and results in report.
  - qualitative: explain why certain option was taken and alternative options ignored.

## CrispDM - Business understanding

- Understand business goals and constraints
- State business objective in business terms
- State relevant data mining objective in technical terms
- State success criteria
- Produce plan of project



# CrispDM - Data understanding

- Collect data
- Understand data
  - qualitative meaning (what and how was measured)
  - quantitative distribution (data type, range, variance, skewness)
- Explore data
  - basic dependencies
  - interesting subsets
  - statistical analysis
- Quality check
  - outliers
  - missing data
  - errors in measurements

# CrispDM - Data preparation

usually takes most of the time

- Select data (select datasets, records, attributes)
- Clean data
  - missing values
  - outliers
  - erroneous values
  - inconsistent groups of attributes
- Construct data
  - derive attributes (normalization, aggregation, composition)
  - use background knowledge
  - fill missing values
- Integrate data together into connected structures (e.g. joined tables)
- Format data (uppercase/lowercase, encoding, etc.)

# CrispDM - Modeling

- Select relevant models
  - depending on data mining objective
  - depending on data properties (possibly need to return to data preparation)
- Divide dataset into training/validation/test sets
- Build models
  - choose initial values for model parameters
  - choose parameter estimation techniques
  - estimate parameters
  - post-process results using domain knowledge

## CrispDM - Evaluation

- evaluate model output quality using technical data mining criteria
  - compare to baseline
  - reliability of results (statistical significance, dependence on specific data assumptions)
  - check for systematic errors and interpret them (may be caused by missed factors/constraints)
- evaluate resulting models (interpretability, efficiency, scalability)
- analyze final business effect

## CrispDM - Deployment

- plan deployment
- plan monitoring and maintainence
- produce final report
- review project experience
  - from project team
  - from customers

## Notation used in the course

- If this corresponds the context and there are no redefinitions, then:
  - $x$  - vector of known input characteristics of an object
  - $y$  - predicted target characteristics of an object specified by  $x$
  - $x_i$  -  $i$ -th object of a set,  $y_i$  - corresponding target characteristic
  - $x^k$  -  $k$ -th feature of object specified by  $x$
  - $x_i^k$  -  $k$ -th feature of object specified by  $x_i$
  - $D$  - dimensionality of the feature space:  $x \in \mathbb{R}^D$
  - $N$  - the number of objects in the training set
  - $X$  - design matrix,  $X \in \mathbb{R}^{N \times D}$
  - $Y \in \mathbb{R}^N$  - target characteristics of a training set
  - $\mathcal{L}(\hat{y}, y)$  - loss function, where  $y$  is the true value and  $\hat{y}$  is the predicted value.
  - $\{\omega_1, \omega_2, \dots, \omega_C\}$  - possible classes,  $C$  - total number of classes.
  - $\hat{z}$  defines an estimate of  $z$ , based on the training set: for example,  $\hat{\theta}$  is the estimate of  $\theta$ ,  $\hat{y}$  is the estimate of  $y$ , etc.