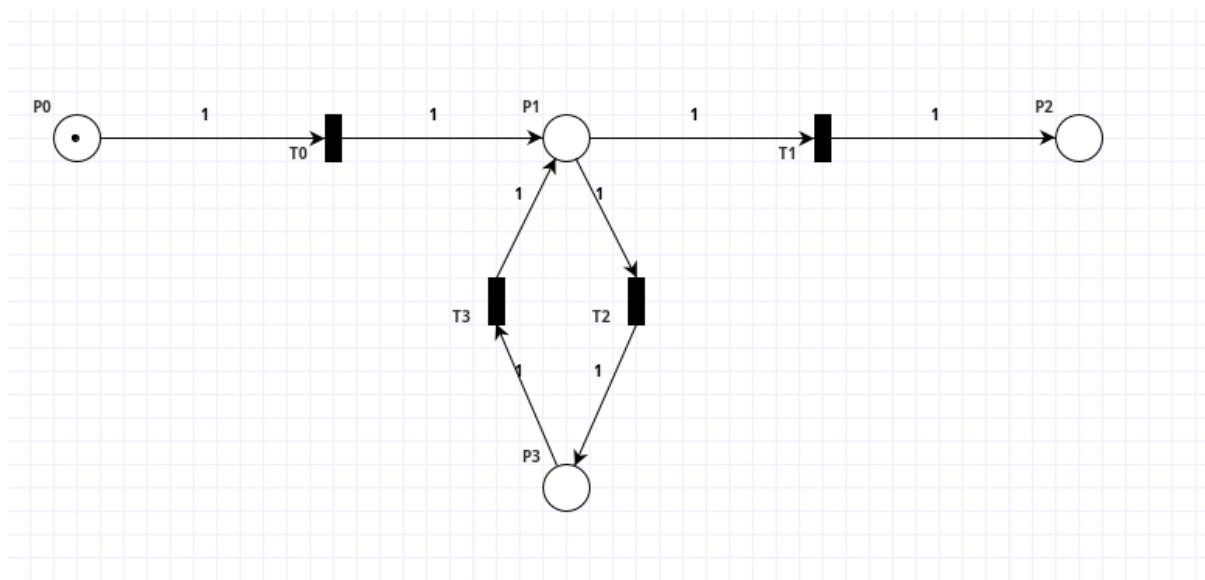


Sieci Petriego

Jan Gawroński

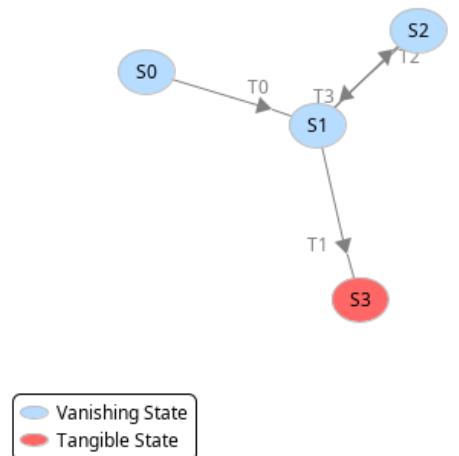
20.01.2026

1 Zadanie 1



Petri net simulation results

Place	Average number of tokens	95% confidence interval (+/-)
P0	0	0
P1	0.4	0.07972
P2	0.2	0.15944
P3	0.2	0.23916



Petri net invariant analysis results

T-Invariants

T0	T1	T2	T3
0	0	1	1

The net is not covered by positive T-Invariants, therefore we do not know if it is bounded and live.

P-Invariants

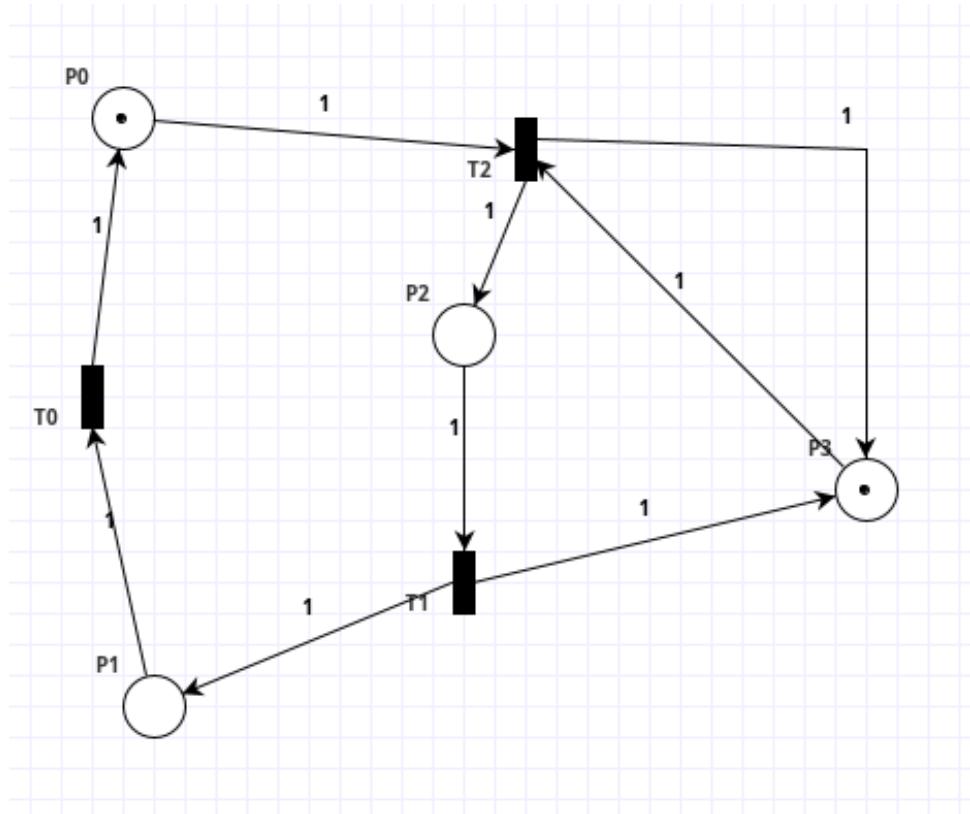
P0	P1	P2	P3
1	1	1	1

The net is covered by positive P-Invariants, therefore it is bounded.

P-Invariant equations

$$M(P_0) + M(P_1) + M(P_2) + M(P_3) = 1$$

2 Zadanie 2



Petri net invariant analysis results

T-Invariants

T0	T1	T2
----	----	----

The net is not covered by positive T-Invariants, therefore we do not know if it is bounded and live.

P-Invariants

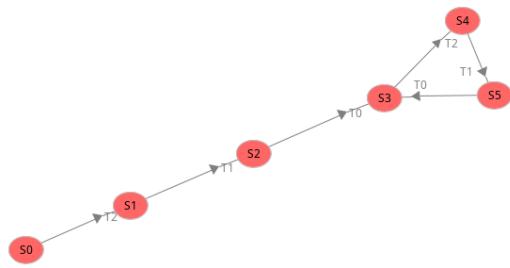
P0	P1	P2	P3
1	1	1	0

The net is not covered by positive P-Invariants, therefore we do not know if it is bounded.

P-Invariant equations

$$M(P0) + M(P1) + M(P2) = 1$$

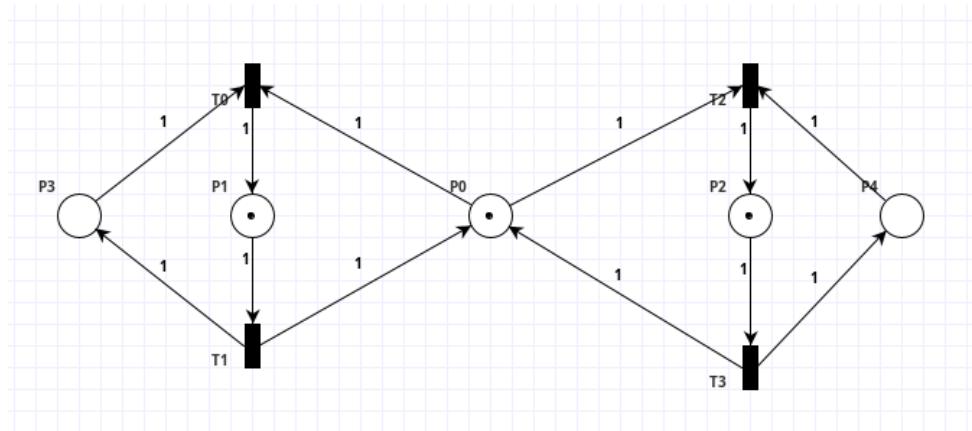
Sieć nie jest pokryta niezmiennikami, więc nie jest odwracalna.



Sieć jest żywa. Sieć cały czas przechodzi przez cykl T_0, T_1, T_2 , używając po kolejni każdego z przejść.

Sieć nie jest ograniczona, ponieważ w miejscu P_3 może się nagromadzić dowolna liczba znaczników.

3 Zadanie 3



Petri net invariant analysis results

T-Invariants

T0	T1	T2	T3
1	1	0	0
0	0	1	1

The net is covered by positive T-Invariants, therefore it might be bounded and live.

P-Invariants

P0	P1	P2	P3	P4
1	1	1	0	0
0	1	0	1	0
0	0	1	0	1

The net is covered by positive P-Invariants, therefore it is bounded.

P-Invariant equations

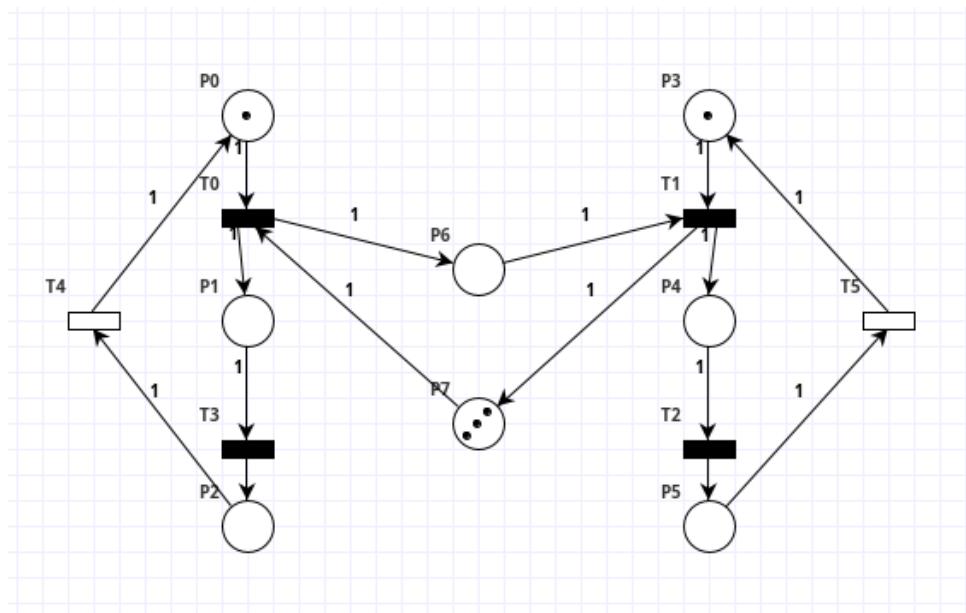
$$M(P_0) + M(P_1) + M(P_2) = 1$$

$$M(P_1) + M(P_3) = 1$$

$$M(P_2) + M(P_4) = 1$$

Równania niezmienników miejc pokazują ile znaczników zawsze bedzię w jakiejś grupie miejsc. Równanie $M(P_0) + M(P_1) + M(P_2) = 1$ to równanie sekcji krytycznej.

4 Zadanie 4



Petri net invariant analysis results

T-Invariants

T0	T1	T2	T3	T4	T5
1	1	1	1	1	1

The net is covered by positive T-Invariants, therefore it might be bounded and live.

P-Invariants

P0	P1	P2	P3	P4	P5	P6	P7
1	1	1	0	0	0	0	0
0	0	0	1	1	1	0	0
0	0	0	0	0	0	1	1

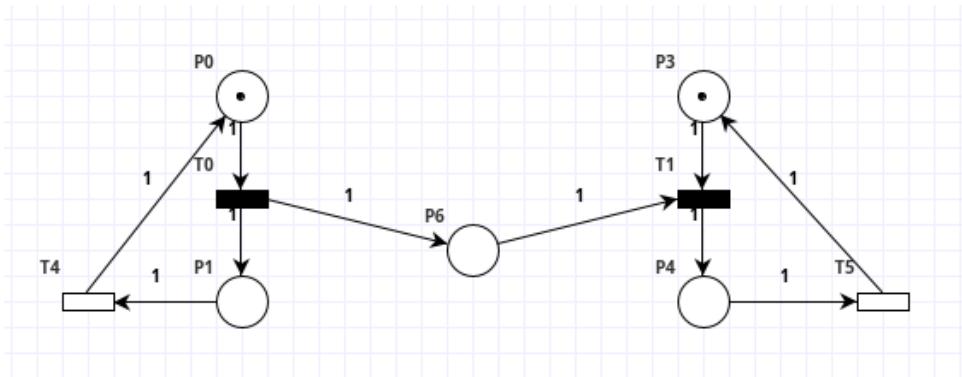
The net is covered by positive P-Invariants, therefore it is bounded.

P-Invariant equations

$$\begin{aligned} M(P_0) + M(P_1) + M(P_2) &= 1 \\ M(P_3) + M(P_4) + M(P_5) &= 1 \\ M(P_6) + M(P_7) &= 3 \end{aligned}$$

Sieć jest zachowawcza, widać to po 3 równaniach niezmienników miejsc, każde z tych równań ma rozłączne składniki. Równanie $M(P_6) + M(P_7) = 3$ mówi nam o rozmiarze bufora.

5 Zadanie 5



Petri net invariant analysis results

T-Invariants

T0	T1	T4	T5
1	1	1	1

The net is covered by positive T-Invariants, therefore it might be bounded and live.

P-Invariants

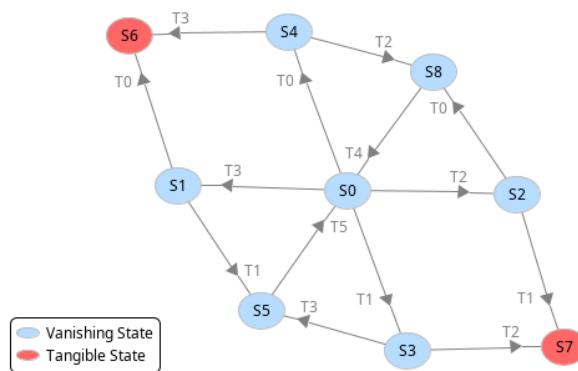
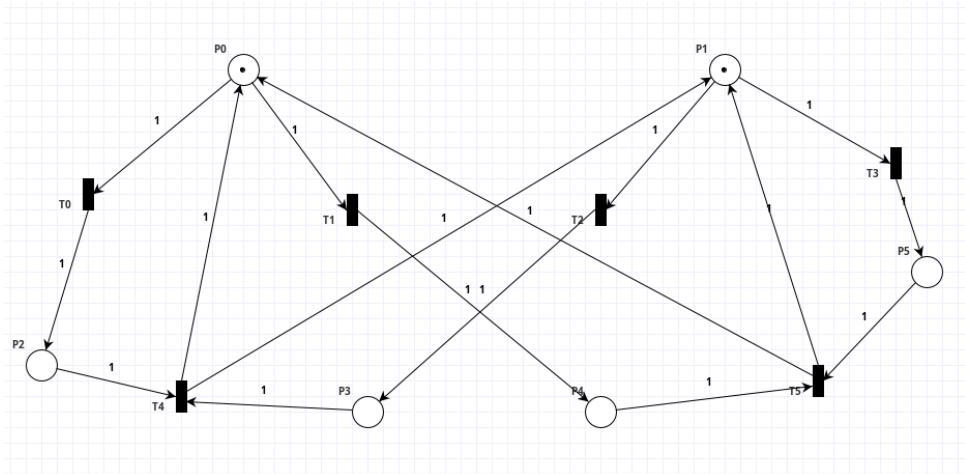
P0	P1	P3	P4	P6
1	1	0	0	0
0	0	1	1	0

The net is not covered by positive P-Invariants, therefore we do not know if it is bounded.

P-Invariant equations

$$\begin{aligned} M(P0) + M(P1) &= 1 \\ M(P3) + M(P4) &= 1 \end{aligned}$$

6 Zadanie 6

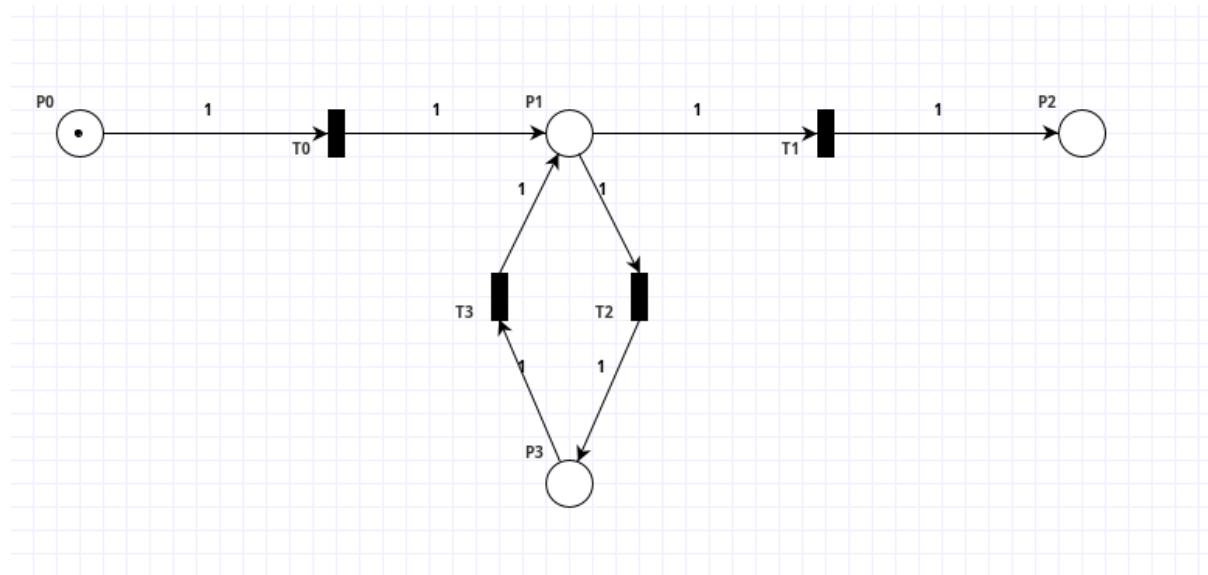


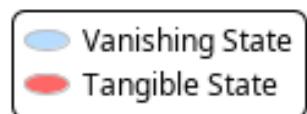
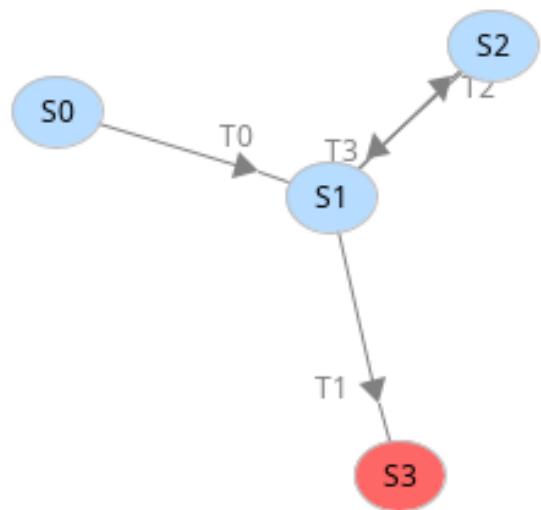
Petri net state space analysis results

Bounded	true
Safe	true
Deadlock	true

Shortest path to deadlock: T0 T3

7 Zadanie 7



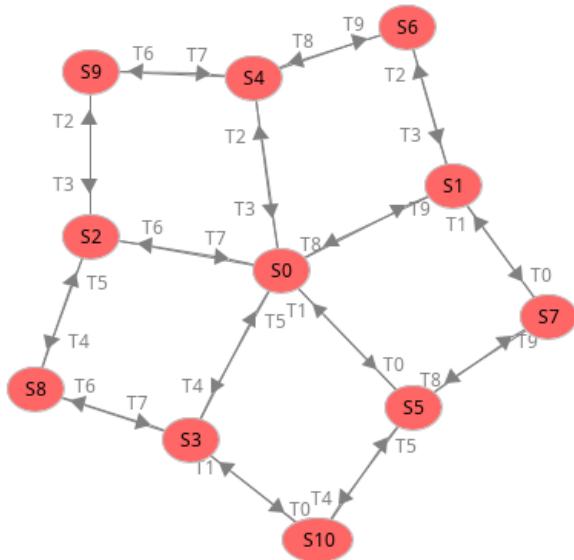
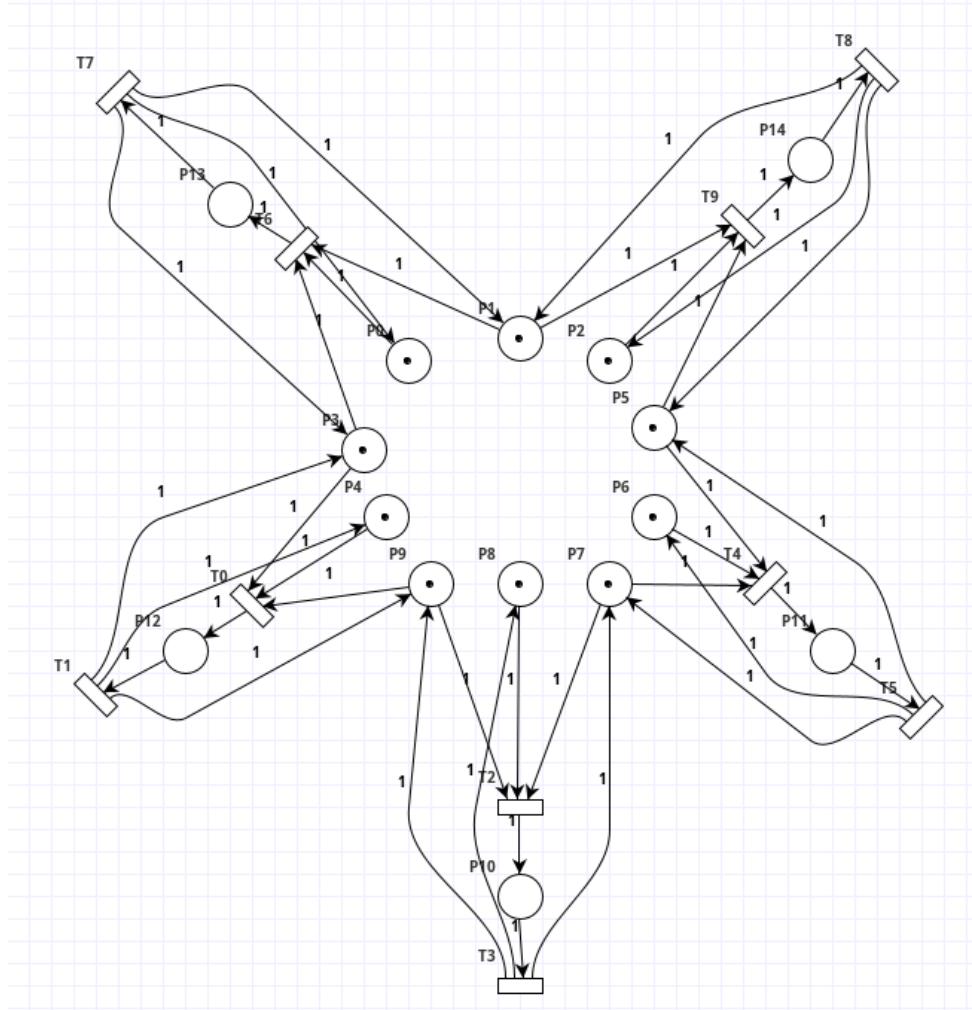


Petri net state space analysis results

Bounded	true
Safe	true
Deadlock	true

Shortest path to deadlock: T0 T1

8 Zadanie 8



Petri net invariant analysis results

T-Invariants

T0	T1	T2	T3	T4	T5	T6	T7	T8	T9
1	1	0	0	0	0	0	0	0	0
0	0	1	1	0	0	0	0	0	0
0	0	0	0	1	1	0	0	0	0
0	0	0	0	0	0	1	1	0	0
0	0	0	0	0	0	0	0	1	1

The net is covered by positive T-Invariants, therefore it might be bounded and live.

P-Invariants

P0	P1	P10	P11	P12	P13	P14	P2	P3	P4	P5	P6	P7	P8	P9
1	0	0	0	0	1	0	0	0	0	0	0	0	0	0
0	1	0	0	0	1	1	0	0	0	0	0	0	0	0
0	0	0	0	0	0	1	1	0	0	0	0	0	0	0
0	0	0	0	1	1	0	0	1	0	0	0	0	0	0
0	0	0	0	1	0	0	0	0	1	0	0	0	0	0
0	0	0	1	0	0	1	0	0	0	1	0	0	0	0
0	0	0	1	0	0	0	0	0	0	0	1	0	0	0
0	0	1	1	0	0	0	0	0	0	0	0	1	0	0
0	0	1	0	0	0	0	0	0	0	0	0	0	1	0
0	0	1	0	1	0	0	0	0	0	0	0	0	0	1

The net is covered by positive P-Invariants, therefore it is bounded.

P-Invariant equations

$$\begin{aligned}
 M(P0) + M(P13) &= 1 \\
 M(P1) + M(P13) + M(P14) &= 1 \\
 M(P14) + M(P2) &= 1 \\
 M(P12) + M(P13) + M(P3) &= 1 \\
 M(P12) + M(P4) &= 1 \\
 M(P11) + M(P14) + M(P5) &= 1 \\
 M(P11) + M(P6) &= 1 \\
 M(P10) + M(P11) + M(P7) &= 1 \\
 M(P10) + M(P8) &= 1 \\
 M(P10) + M(P12) + M(P9) &= 1
 \end{aligned}$$