

# Bachelor Thesis

Comparison of Hamming- and Variation of Information-Loss  
based structured learning on the Multicut Problem

Jan Lammel

16. Februar 2016

# Table of Contents

1 Introduction

2 Theory

3 Experimental Setup

4 Experiments and Results

5 Conclusion

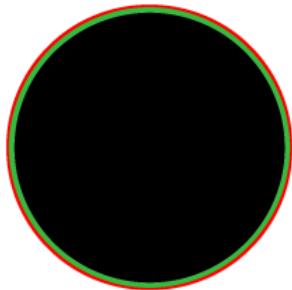
# Segmentation



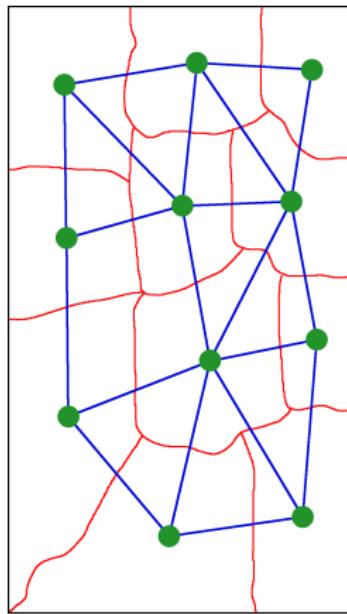
# Motivation Variation of Information



- Hamming Loss strongly dependend on exact path of segmentation
- But: Path of segmentation often not unique
- Idea VOI: Consider labels of segmentation and penalize area-dependend



# Region Adjacency Graph (RAG)



- Image partitioned into **Superpixel** (SP) via SLIC
- Each Superpixel  $\hat{=}$  **Node** in RAG
- Nodes of adjacent SP are linked by an **Edge**

# Multicut Problem (MP)

$$\begin{aligned} \min_y \quad & \sum_{y_e \in E} \langle w, \beta_e \rangle \cdot y_e \\ \text{s.t.} \quad & y - \sum_{y_i \in P(y)} y_i \leq 0 \quad \forall y \in E \end{aligned}$$

- $w$ : Weights to be learned
- $\beta_e$ : Features of edge  $e$
- $y_e$ : Activity of edge  $e$
- Constraint to enforce consistency

Introduction

## Theory

Experimental Setup

Experiments and Results

Conclusion

Region Adjacency Graph

Multicut Problem

## Learning

# Training- and Test data

- Natural Images from Berkeley Segmentation Dataset (BSD-500)
- Took thereof the 200 images from the testset due to availability of state-of-the-art contour detectors → 100 training- and test-images
- Ground Truth as well from BSD-500 dataset (determined label of SP via majority vote)

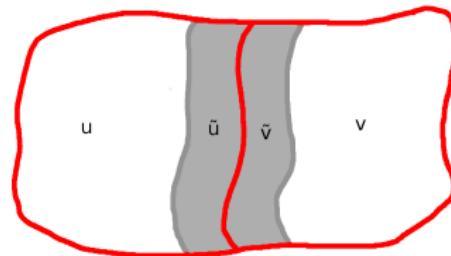
# Feature Space

- Gaussian Gradient Magnitude
- Hessian of Gaussian Eigenvalues
- Laplacian of Gaussian
- Structure Tensor Eigenvalues
- Canny Filter
- $N^4$ -Fields [?] with and without edge length weighting
- Dollár et. al [?] Kantendetektor with and without edge length weighting

# Feature Space

- Statistics in area  $\tilde{u}$  und  $\tilde{v}$  around edge of SP u and v:

- Mean( $\tilde{u} + \tilde{v}$ )
- Variance( $\tilde{u} + \tilde{v}$ )
- $\frac{\max \{\text{Mean}(\tilde{u}), \text{Mean}(\tilde{v})\}}{\min \{\text{Mean}(\tilde{u}), \text{Mean}(\tilde{v})\}}$
- $\frac{\max \{\text{Median}(\tilde{u}), \text{Median}(\tilde{v})\}}{\min \{\text{Median}(\tilde{u}), \text{Median}(\tilde{v})\}}$
- Skewness( $\tilde{u} + \tilde{v}$ )
- Kurtosis( $\tilde{u} + \tilde{v}$ )



- Random Forest Feature

# Stochastic Gradient with RF Feature

- Varying configurations:
  - Domain Feature Space
  - Constraint on RF Feature
  - Subgradient Descent with/without RF Feature
- Results:
  - Decrease of VOI Loss leads to decline of Hamming Loss in Trainingsset
  - Rate of decrease sensible to configuration,  
besides strong fluctuations due to stochastic process
  - Loss decrease on Trainingset  $\propto$  Loss increase on Testset  
 $\Rightarrow$  Overfit of training data

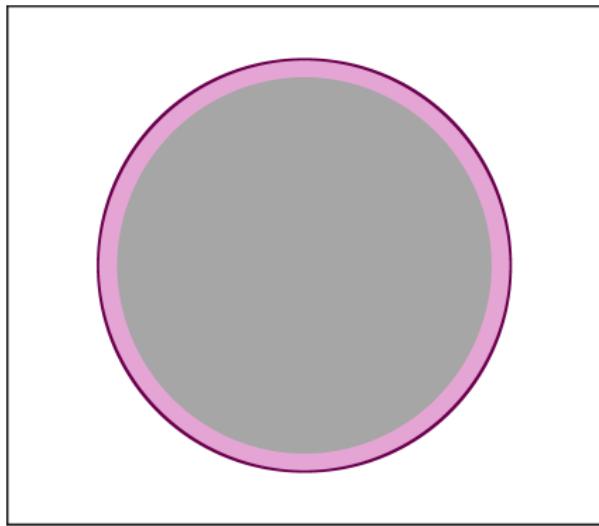
# Stochastic Gradient without RF Feature

- Varying configurations:
  - Domain Feature Space
  - Constraint on  $N^4$  Feature
- Results:
  - VOI Loss decrease on Trainingset of approximately 4%
  - Change of Loss on Testset within  $1\sigma$  range of error

# Cross Validation Measurement 10

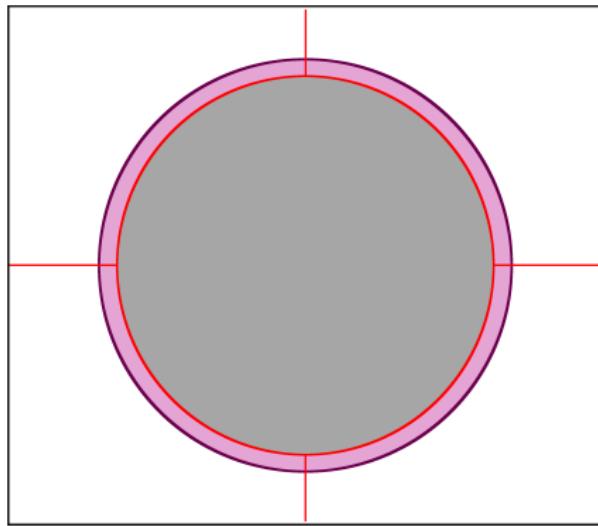
- Cross validation to minimize measurement errors
  - Results on Testset:
    - $\mathcal{L}_H: \frac{\text{StochGrad}}{\text{SubGrad}} = 0.989 \pm 0.005$
    - $\mathcal{L}_{VOI}: \frac{\text{StochGrad}}{\text{SubGrad}} = 1.0025 \pm 0.0084$
- No significant change

# Explanation by SLIC



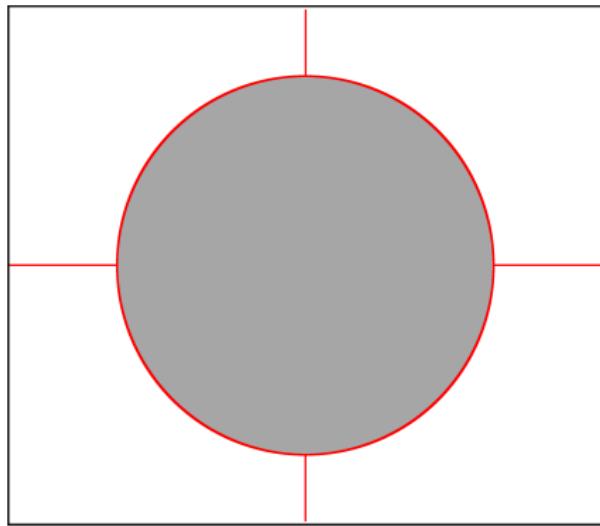
█ Ground Truth Edge  
█ Ground Truth Area  
█ Structure

# Explanation by SLIC



- Ground Truth Edge
- Ground Truth Area
- Structure
- Super Pixel Edges

# Explanation by SLIC



Structure  
Super Pixel- &  
Ground Truth Edges

# Conclusion

- Stochastic Gradient with RF Feature leads to Overfit of training data
- No significant change without RF Feature
  - Bad Ground Truth compensated by SLIC
  - Examination on Pixel-level would be interesting
- Examples were found which confirm theoretical behavior of VOI