INPUT PARAMETERS AND IMPLEMENTATION DETAILS

The marchenko_primaries program has the following parameters and options:

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MARCHENKO_primaries - Iterative primary reflections retrieval
marchenko_primaries file_tinv= file_shot= [optional parameters]
Required parameters:
 file_shot= ..... Reflection response: R
Optional parameters:
INTEGRATION
 ishot=nshots/2 ...... shot number(s) to remove internal multiples
 file_tinv= ..... shot-record (from R) to remove internal multiples
 file_src= ..... optional source wavelet to convolve selected ishot(s)
COMPUTATION
 tap=0 ...... lateral taper R_ishot(1), file_shot(2), or both(3)
 ntap=0 ..... number of taper points at boundaries
 fmin=0 ..... minimum frequency in the Fourier transform
 fmax=70 ..... maximum frequency in the Fourier transform
 plane_wave=0 ..... model plane wave
 src_angle=0 ..... angle with horizontal of plane source array
 src_velo=1500 ..... velocity to use in src_angle definition
 t0=0.1 ..... time shift in plane-wave source wavelet for migration
MARCHENKO ITERATIONS
 niter=22 ..... number of iterations to initialize and restart
 niterec=2 ..... number of iterations in recursive part of the time-samples
 niterskip=50 ...... restart scheme each niterskip samples with niter iterations
 istart=20 ..... start sample of iterations for primaries
 iend=nt ..... end sample of iterations for primaries
MUTE-WINDOW
 shift=20 ..... number of points to account for wavelet (epsilon in papers)
 smooth=shift/2 ..... number of points to smooth mute with cosine window
REFLECTION RESPONSE CORRECTION
 tsq=0.0 ..... scale factor n for t^n for true amplitude recovery
 Q=0.0 ...... Q correction factor
 f0=0.0 ..... for Q correction factor
 scale=2 ...... scale factor of R for summation of Mi with MO
 pad=0 ..... amount of samples to pad the reflection series
OUTPUT DEFINITION
 file_rr= ..... output file with primary only shot record
 file_iter= ..... output file with -Mi(-t) for each iteration: writes
           ..... MO.su=MO : initialisation of algorithm
           ..... RMi: iterative terms
           ..... u1min.su: u1min terms
 file_update= ..... output file with updates only => removed internal multiples
 T=0 .....: :1 compute transmission-losses compensated primaries
 verbose=0 ..... silent option; >0 displays info
```

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Defining file_iter writes for each iteration the focusing update term $-M_i(-t) = RM_i(t)$ in Algorithm 1 before applying the mute window. This same option will also write

 $k_{1,i}^-$ and $v_{1,i}^+$ after the update. By setting the verbose= option to 2 the energy of the focusing update term is printed out for each iteration and can be used to monitor the convergence of the scheme. When file_update= is given an output name the program writes the updates (= estimated internal multiples) to disk. The scale parameter can be useful when the (modeled) data does not have the correct amplitude.

The parameter niterskip= enables the fast algorithm when it is set larger than 1. The first instant time value istart= is run with niter= iterations. If niterskip= is set to a value > 1 the fast algorithm is in effect and the next niterskip iterations use only niterec=2 iterations. After niterskip fast iterations the scheme uses the full niter iterations to avoid possible cumulative numerical instabilities caused by amplified artefacts. The scheme continues with niterec fast algorithm iterations and the cycle repeats itself. By setting niterec=0 the scheme does not do any new iterations in the fast cycle and directly uses the result of the previous iteration. The niterec=0 setting will work well if niterskip= is set to ≈shift samples and is possible due to limited bandwidth of the data.

The T= parameter is a switch to enable the T-MME algorithm. The options plane_wave, src_angle, src_velo, xorig use plane-waves as input shot record as explained in Meles et al. (2018, 2020).

The commands to reproduce all figures in this paper can be found in the directory marchenko/demo/mme. The README_PRIMARIES in that directory explains in detail how to run the scripts. A more complicated (lateral varying) model can be found in the directory marchenko/demo/twoD. This example will take several hours to compute the reflection data and is not discussed here.

Besides the new Marchenko primaries removal program the package also contains the earlier published finite difference modeling code, that is used to model all data in the examples, in directory fdelmodc (Thorbecke and Draganov, 2011), and the standard Marchenko programs (Thorbecke et al. (2017)). The directory utils contains programs to calculate a gridded model (makemod), source wavelets (makewave) and programs for basic processing steps.

REFERENCES

- Meles, G.A., K. Wapenaar, and J. Thorbecke, 2018, Virtual plane-wave imaging via Marchenko redatuming: Geophysical Journal International, Vol. 214 (1), p. 508–519.
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- Thorbecke, J., E. Slob, J. Brackenhoff, J. van der Neut, and K. Wapenaar, 2017, Implementation of the Marchenko method: Geophysics, Vol. 82 (6), p. WB29–WB45.