

Spatial Economics – Assignment 1

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Exercise A

For our independent variables, we use per capita crime rate by town, average number of rooms per dwelling, Charles River dummy variable (= 1 if tract bounds river; 0 otherwise), nitrogen oxides concentration (parts per 10 million) and a constant.

Below we wrote a function which computes: OLS point estimates for the intercept, slope parameters, and the error variance. Suitable test statistics with corresponding p-values for the relevant coefficients. Intervals of the coefficients for a confidence level of 95%.

```
OLS <- function(X,Y){

  # OLS estimates for coefficients
  beta_hat <- solve(t(X) %*% X) %*% t(X) %*% Y
  Y_hat <- X %*% beta_hat    # Fitted values

  e <- Y - Y_hat            # residuals
  n <- nrow(X)              # Number of observations
  k <- ncol(X) - 1          # Number of covariates excluding intercept

  s <- as.numeric(t(e)%*%e / (n-k))      # SSR adjusted for degrees of freedom
  sigma <- s*solve(t(X) %*% X)          # VCV of Beta hat

  se <- sqrt(diag(sigma))               # standard error
  t_stat <- (beta_hat-0) / se            # Compute t-statistic
  p <- pt(abs(t_stat), n-k, lower.tail=FALSE) # Compute p-value

  # 95% Confidence interval
  th <- qt(0.975, n-k)
  conf <- cbind(beta_hat-th*se,beta_hat+th*se)

  colnames(beta_hat) <- "estimate"
  colnames(conf) <- c("2.5%","97.5%")
  colnames(t_stat) <- "t-statistic"
  colnames(p) <- "p-value"

  error_variance <- s

  list(rbind(beta_hat,error_variance), cbind(t_stat, p), conf)
}
```

The output of the function is presented below:

```
OLS(X,Y)
```

```
## [[1]]
##           estimate
## Constant    -17.259625
## Crime        -0.184610
## Rooms         7.706840
```

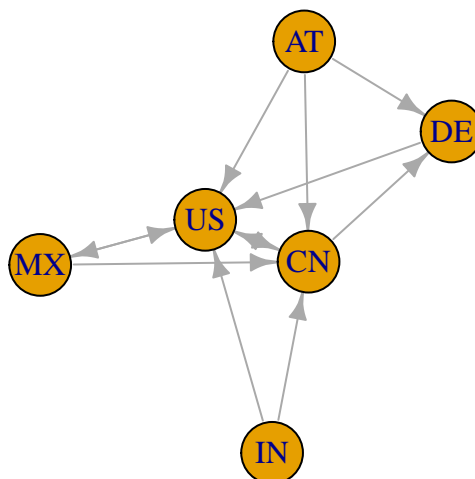
```
## Charles_River    4.673807
## NO_pp10m        -14.960358
## error_variance  35.771378
##
## [[2]]
##               t-statistic      p-value
## Constant      -5.373025 5.935625e-08
## Crime         -5.358215 6.414580e-08
## Rooms         19.155659 4.233091e-62
## Charles_River  4.388052 6.974274e-06
## NO_pp10m      -5.674181 1.178869e-08
##
## [[3]]
##               2.5%      97.5%
## Constant     -23.5707812 -10.9484684
## Crime        -0.2523012 -0.1169189
## Rooms         6.9163879  8.4972927
## Charles_River  2.5811627  6.7664511
## NO_pp10m     -20.1404236 -9.7802928
```

Exercise B

1. Draw a graph of the network; create the adjacency matrix in R.

We could consider 6 different countries and an indicator of a high trade between them. For illustration, we could consider a rule where there is directed edge from A to B, if B is one of the top 5 export destinations of A. We don't actually check for biggest trading partners empirically, but let's assume that such procedure gives rise to following network (arrows are mostly made up to achieve 10 edges and nice interpretations):

Trade network



The corresponding adjacency matrix is:

```
##      US MX DE AT CN IN
## US   0  1  0  0  1  0
## MX   1  0  0  0  1  0
```

```
## DE  1  0  0  0  0  0
## AT  1  0  1  0  1  0
## CN  1  0  1  0  0  0
## IN  1  0  0  0  1  0
```

2. Who are the most and least central agents in the network? Name, explain, and try to quantify different notions of centrality.

A very basic concept of centrality could define an agent as most central, if it has the highest number of directed edges pointing towards itself (i.e. if it is important export country for most other countries). Using this criterion we can see from the graph that or from columns of adjacency matrix that US the most central agents in this network, because it is top 5 trading partner for all 5 other countries. The least central agents would be Austria and India, since they are not a top 5 export country for any country from this network.

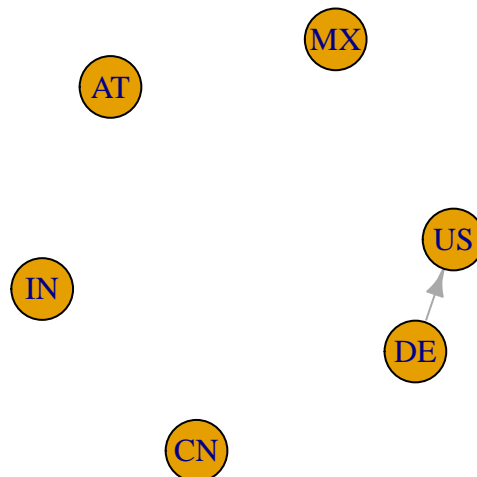
Another basic criterion of centrality could be the amount of outwards pointing arrows of an agent. Thus a country would be considered central if it exports to highest number of countries from this network. In this sense, Germany is least central with only 1 outward arrow, while Austria is most central with 3 outward arrows.

Eigenvector centrality: There is no sink, but not possible to get to Austria. ? Page Rank: weights (probs) need to be defined?

- How would centralities change if you considered a row-normalized network instead?

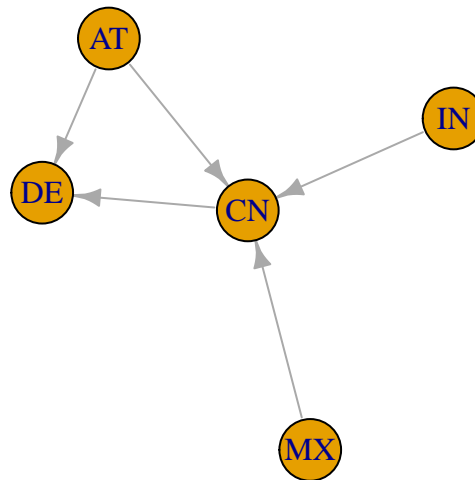
Germany which had only 1 connection, is the only row with sum of 1. Thus its the only edge which survives row normalization. Thus here depending on criterion US or Germany would be most central agent. Other countries would be all least central.

Trade network row normalized



- How would the network change if you removed or added a specific agent? Lets consider the case of removing US:

Trade network excl. US



Based on Inflowing arrows, China becomes the most central agent and India, Austria and Mexico the least central agents. Based on Outflowing arrows, Austria is still the most central agent, while Germany is the least central agent.

3. Simulate some agent characteristic based on a standard Normal distribution; use this characteristic to simulate responses following a liner-in-means model with your network.

- Repeat this a couple of times, and compare estimates of a standard linear model ($y_i = x_\beta + \varepsilon_i$) with the true values that you used to simulate the data

Exercise C

Download a suitable shapefile for NUTS2 regions (from here or using R directly) and some dataset of interest at the same level of aggregation (e.g. from here). Install and load the sf and ggplot2 packages together with their dependencies.

- Read in the shapefile, and find out what projection and CRS the file uses.

The projection used is WGS 84 (EPSG 4326).

Map the data to use another projection and/or CRS of your choosing: Since exclude everything except Austria, we decided for MGI Lambert Austria (equidistant equal-area specifically for AT).

```
# we exclude everything except Austria
shp <- shp[shp$CNTR_CODE %in% "AT", ]
#Therefore we decide for MGI Lambert Austria (equidistant equal-area specifically for AT)
#plot(st_geometry(shp))
st_geometry(shp) <- st_geometry(st_transform(shp,
                                             st_crs("epsg:31287")))
#plot(st_geometry(shp))
```

Exercise D

“Another way: Install and load the tmap and spDataLarge packages (available from GitHub). Load and review the pol_pres15 dataset on the Polish Presidential election in 2015 (see ?pol_pres15). Create three different, insightful visualizations of the underlying data.

- One visualization should compare the support for Komorowski and Duda.

Combine support for Komorowski and Duda into a single categorical variable

```
pol_pres15Support <- ifelse(pol_pres15I_Komorowski_share > pol_pres15$I_Duda_share, "Komorowski",
"Duda")
```

Visualize support for Komorowski and Duda in the first run

```
tm_shape(pol_pres15) + tm_borders(lwd = 0.5, alpha = 0.4) + tm_fill(col = "Support", style = "cat", palette
= "RdYlBu", title = "Support for Candidates") + tm_layout(legend.position = c("left", "bottom"))
```

- One visualization should investigate possible issues with postal voting envelopes. We want to investigate if Issues occurred because voting envelopes got lost on the way to the voters.

Visualization investigating possible issues with postal voting envelopes

Calculate the proportion of postal voting envelopes received to postal voting packages sent

```
pol_pres15EnvelopeProportion <- pol_pres15I_postal_voting_envelopes_received / pol_pres15$I_voters_sent_postal_voti
```

Define a threshold for the proportion indicating possible issues

```
threshold <- 0.99 # You can adjust this threshold as needed
```

Create a new column indicating possible issues with postal voting envelopes based on the proportion

```
pol_pres15EnvelopeIssues <- ifelse(pol_pres15EnvelopeProportion < threshold, "Possible Issues", "No
Issues")
```

```
tm_shape(pol_pres15) + tm_borders(lwd = 0.5, alpha = 0.4) + tm_fill(col = "Envelope_Issues", style = "cat",
palette = c("green", "red"), title = "Possible Issues with Postal Voting Envelopes") + tm_layout(legend.position
= c("left", "bottom"))
```

- Third visualization ## Visualize support for Komorowski and Duda in the second run `pol_pres15Support <- ifelse(pol_pres15II_Komorowski_share > pol_pres15$II_Duda_share, "Komorowski", "Duda")` `tm_shape(pol_pres15) + tm_borders(lwd = 0.5, alpha = 0.4) + tm_fill(col = "Support", style = "cat", palette = "RdYlBu", title = "Support for Candidates") + tm_layout(legend.position = c("left", "bottom"))`