

DCA_Assignment3

September 28, 2016

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In [43]: # Imports
import numpy as np
from numpy import cos, sin, pi, absolute, arange, ndarray, dtype
from scipy.signal import kaiserord, lfilter, firwin, freqz
from pylab import figure, clf, plot, xlabel, ylabel, xlim, ylim, title, grid
from random import uniform
from decimal import *
import FixedPoint as FP
import matplotlib.patches as mpatches
import matplotlib.pyplot as plt
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0.1 Setting Cases

- 1 - NoAS - No altered storage
- 2 - Fl16 - 16 bit Floating Point storage
- 3 - Fl32 - 32 bit Floating Point storage
- 4 - Fi16 - 16 bit Fixed Point storage
- 5 - Fi32 - 32 bit Fixed Point storage

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In [45]: #Define class with multiple definitions
class Filter:
    #Define variables used in following definitions (def)
    def __init__(self, signal, t, Instance, plotinstance, ripple_db, cutoff_hz):
        self.signal = signal
        self.time = t
        self.Instance = Instance
        self.ripple_db = ripple_db
        self.cutoff_hz = cutoff_hz
        self.plotinstance = plotinstance
        self.taps = 0
        self.nyq_rate = 0
        self.filtersignal = 0
        self.N = 0
        c = getcontext() #return the current context for the active thread

    #set functions applied to self, will be detailed later
    def apply(self):
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self.createFIR() #create FIR filter
self.setInstance() #choose filter instance
self.filtersignal = lfilter(self.taps,1.0,self.signal) #applying lfilter
self.plot(self.plotinstance)

#defining what actions to be taken depending on type
#altering signal (self.signal) and taps (self.taps) of FIR filter
#taps: filter order + 1
def setInstance(self):
    if(self.Instance=='NoAS'):
        self.signal = self.signal
        self.taps = self.taps
    if(self.Instance=='F116'): #using Numpy float16 to alter to 16 bit
        self.signal = np.float16(self.signal)
        self.taps = np.float16(self.taps)
    if(self.Instance=='F132'): #using Numpy float16 to alter to 32 bit
        self.signal = np.float32(self.signal)
        self.taps = np.float32(self.taps)
    if(self.Instance=='Fi16'): #using FixedPoint to alter to 16 bit F
        for n, line in enumerate(self.signal):
            self.signal[n] = FP.FXnum(self.signal[n], FP.FXfamily(7,8))
        for n, line in enumerate(self.taps):
            self.taps[n] = FP.FXnum(self.taps[n], FP.FXfamily(7,8))
    if(self.Instance=='Fi32'): #using FixedPoint to alter to 16 bit F
        for n, line in enumerate(self.signal):
            self.signal[n] = FP.FXnum(self.signal[n], FP.FXfamily(15,16))
        for n, line in enumerate(self.taps):
            self.taps[n] = FP.FXnum(self.taps[n], FP.FXfamily(15,16))

#define FIR filter
def createFIR(self):
    self.nyq_rate = sample_rate / 2.0 #Nyquist rate
    width = 5.0 / self.nyq_rate #transition from pass to stop
    self.N, beta = kaiserord(ripple_db, width) #order and Kaiser param
    self.taps = firwin(self.N, self.cutoff_hz/self.nyq_rate, window=('

#defining plot init per instance
def plot(self,Instance):
    if(Instance == 1): #No action
        None
    if(Instance == 2): #Show plot for signal
        self.PlotSignal()
    if(Instance == 3): #Show plots for filter coefficients, magnitude
        self.PlotFirCoefficient()
        self.PlotFirMagnitude()
        self.PlotSignal()
    if(Instance == 4): #show plot for filter coefficients
        self.PlotFirCoefficient()

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        if(Instance == 5): #show plot for filter magnitude
            self.PlotFirMagnitude()
        show()

    #Plot for filter coefficients
    def PlotFirCoefficient(self):
        figure(1)
        plot(self.taps, 'bo-', linewidth=2)
        title('Filter Coefficients (%d taps)' % self.N)
        grid(True)

    #Plot for filter magnitude
    def PlotFirMagnitude(self):
        figure(2)
        clf()
        w, h = freqz(self.taps, worN=8000)
        plot((w/pi)*self.nyq_rate, absolute(h), linewidth=2)
        xlabel('Frequency (Hz)')
        ylabel('Gain')
        title('Frequency Response')
        ylim(-0.05, 1.05)
        grid(True)

        # Upper inset plot.
        ax1 = axes([0.42, 0.6, .45, .25])
        plot((w/pi)*self.nyq_rate, absolute(h), linewidth=2)
        xlim(0, 8.0)
        ylim(0.9985, 1.001)
        grid(True)

        # Lower inset plot
        ax2 = axes([0.42, 0.25, .45, .25])
        plot((w/pi)*self.nyq_rate, absolute(h), linewidth=2)
        xlim(12.0, 20.0)
        ylim(0.0, 0.0025)
        grid(True)

    #Plot for original signal
    def PlotSignal(self):
        # The phase delay of the filtered signal.
        delay = 0.5 * (self.N-1) / sample_rate

        figure(3)

        #Plot original signal
        plot(self.time, self.signal)

        #Plot filtered signal, shifted to compensate for phase delay

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        plot(self.time-delay, self.filtersignal, 'r-')

        #Remove first N-1 samples which are corrupted due to initial cond
        plot(self.time[self.N-1:]-delay, self.filtersignal[self.N-1:], 'g')
        xlabel('t')
        title('Signal')
        grid(True)

        #Returns taps when requested
        def getTaps(self):
            return self.taps

        #Returns signal when requested
        def getSignal(self):
            return self.signal

        #Returns filtered signal when requested
        def getFilterSignal(self):
            return self.filtersignal

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0.2 Creating Random Signal

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In [46]: sample_rate = 100.0
        nsamples = 300
        A1 = uniform(0,1); B1 = uniform(0,1); C1 = uniform(0,1); D1 = uniform(0,1)
        t = arange(nsamples) / sample_rate
        signal = cos(2*pi*0.5*t) + A1*sin(2*pi*2.5*t+0.1) + \
            B1*sin(2*pi*15.3*t) + C1*sin(2*pi*16.7*t + 0.1) + \
            D1*sin(2*pi*23.45*t+.8)

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0.3 Filtering

S/F/T1 - NoAS - No altered storage
 S/F/T2 - Fl16 - 16 bit Floating Point storage
 S/F/T3 - Fl32 - 32 bit Floating Point storage
 S/F/T4 - Fi16 - 16 bit Fixed Point storage
 S/F/T5 - Fi32 - 32 bit Fixed Point storage
 S = signal, F = filter, T = taps

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In [47]: #Desired attenuation in stop band, dB
        ripple_db = 60.0
        #Cutoff frequency of filter, Hz
        cutoff_hz = 10.0

        #Setup filters per instance as set in class __init__
        #For alternative plots use: 2 for signal, 3 for filter coefficients, magni
            #4 for filter coefficients, 5 or magnitude
        #Signal, time, instance, plotinstance, attenuunation, cutoff frequency

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F1 = Filter(signal,t,'NoAS',1,ripple_db,cutoff_hz)
F2 = Filter(signal,t,'F116',1,ripple_db,cutoff_hz)
F3 = Filter(signal,t,'F132',1,ripple_db,cutoff_hz)
F4 = Filter(signal,t,'Fi16',1,ripple_db,cutoff_hz)
F5 = Filter(signal,t,'Fi32',1,ripple_db,cutoff_hz)

#Unfiltered signal
F1.apply()
T1 = F1.getTaps()
S1 = F1.getSignal()
SF1 = F1.getFilterSignal()

#Floating point 16 bit
F2.apply()
T2 = F2.getTaps()
S2 = F2.getSignal()
SF2 = F2.getFilterSignal()

#Floating point 32 bit
F3.apply()
T3 = F3.getTaps()
S3 = F3.getSignal()
SF3 = F3.getFilterSignal()

#Fixed point 16 bit
F4.apply()
T4 = F4.getTaps()
S4 = F4.getSignal()
SF4 = F4.getFilterSignal()

#Fixed point 32 bit
F5.apply()
T5 = F5.getTaps()
S5 = F5.getSignal()
SF5 = F5.getFilterSignal()

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0.4 Calculating differences compared to original signal (no change in storage)

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In [48]: #Differences between taps
tapsdifference2 = T1 - T2
tapsdifference3 = T1 - T3
tapsdifference4 = T1 - T4
tapsdifference5 = T1 - T5

#Differences between signals
signaldifference2 = S1 - S2
signaldifference3 = S1 - S3
signaldifference4 = S1 - S4

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signaldifference5 = S1 - S5

#Differences between filtered signals
filtersignaldifference2 = SF1 - SF2
filtersignaldifference3 = SF1 - SF3
filtersignaldifference4 = SF1 - SF4
filtersignaldifference5 = SF1 - SF5

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0.5 Plotting differences

- 1 - NoAS - No altered storage
- 2 - Fl16 - 16 bit Floating Point storage
- 3 - Fl32 - 32 bit Floating Point storage
- 4 - Fi16 - 16 bit Fixed Point storage
- 5 - Fi32 - 32 bit Fixed Point storage

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In [55]: figure(5)
         #State what to plot
         plot(t,filtersignaldifference2,'r')

         #Define legend
         floatLegend = mpatches.Patch(color='red', label='16 bit Floating Point')
         legend(handles=[floatLegend])

         #Define title and axes
         title('Error of 16 bit Floating Point compared to original signal')
         xlabel('Time')
         ylabel('Error')

         figure(6)
         #State what to plot
         plot(t,filtersignaldifference3,'r')

         #Define legend
         floatLegend = mpatches.Patch(color='red', label='32 bit Floating Point')
         legend(handles=[floatLegend])

         #Define title and axes
         title('Error of 32 bit Floating Point compared to original signal')
         xlabel('Time')
         ylabel('Error')

         figure(7)
         #State what to plot
         plot(t,filtersignaldifference4,'r')

         #Define legend
         fixedLegend = mpatches.Patch(color='red', label='16 bit Fixed Point')

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legend(handles=[fixedLegend])

#Define title and axes
title('Error of 16 bit Fixed Point compared to original signal')
xlabel('Time')
ylabel('Error')

figure(8)
#State what to plot
plot(t, filtersignaldifference5, 'r')

#Define legend
fixedLegend = mpatches.Patch(color='red', label='32 bit Fixed Point')
legend(handles=[fixedLegend])

#Define title and axes
title('Error of 32 bit Fixed Point compared to original signal')
xlabel('Time')
ylabel('Error')

show()

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In []: