

# CODING WITH R

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# PROBABILITY DISTRIBUTIONS

One convenient use of R is to provide a comprehensive set of statistical tables.

Functions are provided

- to evaluate the cumulative distribution function  $P(X \leq x)$ , the probability density Function;
- to evaluate the quantile function (given  $q$ , the smallest  $x$  such that  $P(X \leq x) \geq q$ );
- to simulate from the distribution.

# PROBABILITY DISTRIBUTIONS

For normal distribution:

`dnorm(x,mean,sd,...)` ### calculate the pdf of normal distribution at the point x.

`pnorm(x,mean,sd,...)` ### calculate the cdf of normal distribution at the point x.

`qnorm(p,mean,sd,...)` ### calculate the point x at which  $P[X \leq x] > p$

`rnorm(n,mean,sd,...)` ### draw random sample of size n from a normal distribution.

Ex.

`pnorm(1.66,1,2)` ## calculate the pdf of normal distribution with mean = 1, sd = 2, at the point 1.66.

`qnorm(0.85,1,2)` ## calculate the point x at which  $P[X \leq x] > 0.85$  for normal(1,2) distribution.

`dnorm(3,1,2)` ## calculate the pdf of normal distribution with mean = 1, sd = 2, at the point 3.

`rnorm(1000,1,2)` ## draw random sample of size 1000 from a normal distribution with mean = 1, sd=2.

# PROBABILITY DISTRIBUTIONS

For uniform distribution:

`dunif(x,min,max)` ### calculate the pdf of uniform distribution at the point x.

`punif(x, min,max)` ### calculate the cdf of uniform distribution at the point x.

`qunif(p, min,max)` ### calculate the point x at which  $P[X \leq x] > p$

`runif(n, min,max)` ### draw random sample of size n from a uniform distribution.

Ex.

`punif(1.3,1,2)` ## calculate the pdf of uniform distribution with min = 1, max = 2, at the point x.

`qunif(0.85,1,2)` ## calculate the point x at which  $P[X \leq x] > 0.85$  for uniform distribution.

`dunif(1.87,1,2)` ## calculate the pdf of uniform distribution with min = 1, max = 2, at the point 1.87.

`runif(1000,1,2)` ## draw random sample of size 1000 from a normal distribution with min = 1, max=2.

# PROBABILITY DISTRIBUTIONS

For gamma distribution:

`dgamma(x,shape,rate)` ### calculate the pdf of gamma distribution at the point x.

`pgamma(x, shape,rate)` ### calculate the cdf of gamma distribution at the point x.

`qgamma(p, shape, rate)` ### calculate the point x at which  $P[X \leq x] > p$

`rgamma(n, shape, rate)` ### draw random sample of size n from a gamma distribution.

Ex.

`pgamma(1.3,1,2)` ## calculate the pdf of gamma distribution with shape = 1, rate = 2, at the point x.

`qgamma(0.85,1,2)` ## calculate the point x at which  $P[X \leq x] > 0.85$  for gamma distribution.

`dgamma(1.87,1,2)` ## calculate the pdf of gamma distribution with shape = 1, rate = 2, at the point 1.87.

`rgamma(1000,1,2)` ## draw random sample of size 1000 from a gamma distribution with shape = 1, rate=2.



# PROBABILITY DISTRIBUTIONS

For beta distribution:

`dgamma(x,shape,rate)` ### calculate the pdf of gamma distribution at the point x.

`pgamma(x, shape,rate)` ### calculate the cdf of gamma distribution at the point x.

`qgamma(p, shape, rate)` ### calculate the point x at which  $P[X \leq x] > p$

`rgamma(n, shape, rate)` ### draw random sample of size n from a gamma distribution.

Ex.

`pgamma(1.3,1,2)` ## calculate the pdf of gamma distribution with shape = 1, rate = 2, at the point x.

`qgamma(0.85,1,2)` ## calculate the point x at which  $P[X \leq x] > 0.85$  for gamma distribution.

`dgamma(1.87,1,2)` ## calculate the pdf of gamma distribution with shape = 1, rate = 2, at the point 1.87.

`rgamma(1000,1,2)` ## draw random sample of size 1000 from a gamma distribution with shape = 1, rate=2.

# PROBABILITY DISTRIBUTIONS

For beta distribution:

`dbeta(x, shape1, shape2) ### calculate the pdf of beta distribution at the point x.`

`pbeta(x, shape1, shape2) ### calculate the cdf of beta distribution at the point x.`

`qbeta(p, shape1, shape2) ### calculate the point x at which  $P[X \leq x] > p$`

`rbeta(n, shape1, shape2) ### draw random sample of size n from a beta distribution.`

Ex.

`pbeta(0.77,1,2) ## calculate the pdf of beta distribution with  $\text{shape1} = 1$ ,  $\text{shape2} = 2$ , at the point x.`

`qbeta(0.85,1,2) ## calculate the point x at which  $P[X \leq x] > 0.85$  for beta distribution.`

`dbeta (0.87,1,2) ## calculate the pdf of beta distribution with  $\text{shape1} = 1$ ,  $\text{shape2} = 2$ , at the point 0.87.`

`rbeta(1000,1,2) ## draw random sample of size 1000 from a beta distribution with  $\text{shape1} = 1$ ,  $\text{shape2}=2$ .`

You can also specify 'ncp' (non-centrality parameter) values if needed.

# PROBABILITY DISTRIBUTIONS

For student's t distribution:

`dt(x,df) ###` calculate the pdf of student's t distribution at the point x. df = degrees of freedom.

`pt(x, df) ###` calculate the cdf of student's t distribution at the point x.

`qt(p, df) ###` calculate the point x at which  $P[X \leq x] > p$

`rt(n, df) ###` draw random sample of size n from a student's t distribution.

Ex.

`pt(0.77,2) ##` calculate the pdf of student's t distribution with df = 2, at the point x.

`qt(0.85,2) ##` calculate the point x at which  $P[X \leq x] > 0.85$  for student's t distribution.

`dt(0.87,2) ##` calculate the pdf of student's t distribution with df = 2, at the point 0.87.

`rt(1000,2) ##` draw random sample of size 1000 from a student's t distribution with df = 2.



# PROBABILITY DISTRIBUTIONS

For F distribution:

`df(x,df1,df2)` ### calculate the pdf of F distribution at the point x. df1 and df2 = degrees of freedoms.

`pf(x, df1,df2)` ### calculate the cdf of F distribution at the point x.

`qf(p, df1,df2)` ### calculate the point x at which  $P[X \leq x] > p$

`rf(n, df1,df2)` ### draw random sample of size n from a F distribution.

Ex.

`pf(0.77,3,2)` ## calculate the pdf of F distribution with  $df1 = 3$ ,  $df2 = 2$ , at the point x.

`qf(0.85,3,2)` ## calculate the point x at which  $P[X \leq x] > 0.85$  for F distribution.

`df(0.87,3,2)` ## calculate the pdf of F distribution with  $df1 = 3$ ,  $df2 = 2$ , at the point 0.87.

`rf(1000,3,2)` ## draw random sample of size 1000 from a F distribution with  $df1 = 3$ ,  $df2 = 2$ .

# PROBABILITY DISTRIBUTIONS

For Cauchy distribution:

`dcauchy(x,location,scale)` ### calculate the pdf of Cauchy distribution at the point x.

`pcauchy(x, location,scale)` ### calculate the cdf of Cauchy distribution at the point x.

`qcauchy(p, location,scale)` ### calculate the point x at which  $P[X \leq x] > p$

`rcauchy(n, location,scale)` ### draw random sample of size n from a Cauchy distribution.

Ex.

`pcauchy(0.77,3,2)` ## calculate the pdf of Cauchy distribution with location =3, scale = 2, at the point x.

`qcauchy(0.85,3,2)` ## calculate the point x at which  $P[X \leq x] > 0.85$  for Cauchy distribution.

`dcauchy(0.87,3,2)` ## calculate the pdf of Cauchy distribution with location =3, scale = 2, at the point 0.87.

`rcauchy(1000,3,2)` ## draw random sample of size 1000 from a Cauchy distribution with location =3, scale = 2.

# PROBABILITY DISTRIBUTIONS

For log-normal distribution:

`dlnorm(x,meanlog,sdlog) ###` calculate the pdf of log-normal distribution at the point  $x$ .

`plnorm(x, meanlog,sdlog) ###` calculate the cdf of log-normal distribution at the point  $x$ .

`qlnorm(p, meanlog,sdlog) ###` calculate the point  $x$  at which  $P[X \leq x] > p$

`rlnorm(n, meanlog,sdlog) ###` draw random sample of size  $n$  from a log-normal distribution.

Ex.

`plnorm(0.77,3,2) ##` calculate the pdf of log-normal distribution with mean =3, sd = 2, at the point  $x$ .

`qlnorm(0.85,3,2) ##` calculate the point  $x$  at which  $P[X \leq x] > 0.85$  for log-normal distribution.

`dlnorm(0.87,3,2) ##` calculate the pdf of log-normal distribution with mean =3, sd = 2, at the point 0.87.

`rlnorm(1000,3,2) ##` draw random sample of size 1000 from a log-normal distribution with mean =3, sd = 2.

# PROBABILITY DISTRIBUTIONS

For binomial distribution:

`dbinom(x,size,prob)` ### calculate the pdf of binomial distribution at the point x.

`pbinom(x, size,prob)` ### calculate the cdf of binomial distribution at the point x.

`qbinom(p, size,prob)` ### calculate the point x at which  $P[X \leq x] > p$

`rbinom(n, size,prob)` ### draw random sample of size n from a binomial distribution.

Ex.

`pbinom(7,10,0.7)` ## calculate the pdf of binomial distribution with size =10, prob = 0.7, at the point x.

`qbinom(0.85,10,0.7)` ## calculate the point x at which  $P[X \leq x] > 0.85$  for binomial distribution.

`dbinom(7,10,0.7)` ## calculate the pdf of binomial distribution with size =10, prob = 0.7, at the point 7.

`rbinom(1000,10,0.7)` ## draw random sample of size 1000 from a binomial distribution with size =10, prob = 0.7.

# PROBABILITY DISTRIBUTIONS

For Poisson distribution:

`dpois(x,lambda)` ### calculate the pdf of Poisson distribution at the point x.

`ppois(x, lambda)` ### calculate the cdf of Poisson distribution at the point x.

`qpois(p, lambda)` ### calculate the point x at which  $P[X \leq x] > p$

`rpois(n, lambda)` ### draw random sample of size n from a Poisson distribution.

Ex.

`ppois(7, 3)` ## calculate the pdf of Poisson distribution with  $\lambda = 3$ , at the point x.

`qpois(0.85,3)` ## calculate the point x at which  $P[X \leq x] > 0.85$  for Poisson distribution.

`dpois(7,3)` ## calculate the pdf of Poisson distribution with  $\lambda = 3$ , at the point 7.

`rpois(1000,3)` ## draw random sample of size 1000 from a Poisson distribution with  $\lambda = 3$ .

# PROBABILITY DISTRIBUTIONS

Install the package 'e1071'. (mind the letter-case 'e'.)

```
library(e1071) ### call the package
```

```
a = rf(100,3,2) ### draw 100 random samples from a F distribution.
```

```
skewness(a)
```

```
kurtosis(a)
```

**\*\* More distributions are available in 'SuppDists' package.**

link: <https://cran.r-project.org/web/packages/SuppDists/index.html>

Also, you can search in google as 'SuppDists package in R'.



# PROBABILITY DISTRIBUTIONS

Alternatively,

#### install and call the following packages

```
library(timeDate)
```

```
library(fBasics)
```

```
a = rf(100,3,2) #### draw random sample from some distribution (not necessarily F)
```

```
skewness(a)
```

```
kurtosis(a)
```

# PROBABILITY DISTRIBUTIONS

Remember:

- 'p' for 'probability', the cdf of a distribution.
- 'q' for 'quantile', the inverse cdf.
- 'd' for 'density', the density function (pdf or pmf)
- 'r' for 'random', random sample from the specified distribution.

# PROBABILITY DISTRIBUTIONS

1. What is  $P(X = 1)$  when  $X$  has the  $\text{Bin}(25, 0.005)$  distribution?
2. What are the 10th, 20th, and so forth quantiles of the  $\text{Bin}(10, 1/3)$  distribution?
3. Suppose widgees produced at Acme Widgee Works have probability 0.005 of being defective. Suppose widgees are shipped in cartons containing 25 widgees. What is the probability that a randomly chosen carton contains no more than one defective widgee?