

4) Perform the following additions

a. $(2267)_8 + (1777)_8$

b. $(2267)_9 + (1777)_9$

c. $(2267)_{16} + (1777)_{16}$

* Solutions *

$$\begin{array}{r} \overset{1}{2} \ \overset{1}{2} \ \overset{1}{6} \ \overset{1}{7} \\ + (1 \ 7 \ 7 \ 7) \\ \hline \end{array}_8$$

$$\begin{array}{r} \\ (4 \ 2 \ 6 \ 5) \\ \hline \end{array}_8$$

$$\begin{array}{r} \overset{1}{2} \ \overset{1}{2} \ \overset{1}{6} \ \overset{1}{7} \\ + (1 \ 7 \ 7 \ 7) \\ \hline \end{array}_9$$

$$\begin{array}{r} \\ (4 \ 1 \ 5 \ 5) \\ \hline \end{array}_9$$

$$\begin{array}{r} (2 \ 2 \ 6 \ 7) \\ + (1 \ 7 \ 7 \ 7) \\ \hline \end{array}_{16}$$

$$\begin{array}{r} \\ (3 \ 9 \ D \ E) \\ \hline \end{array}_{16}$$

5) Perform the following subtractions

a. $(2267)_8 - (1777)_8$

b. $(2267)_9 - (1777)_9$

c. $(2267)_{16} - (1777)_{16}$

* Solutions *

$$\begin{array}{r} (2 \ 2 \ 6 \ 7) \\ - (1 \ 7 \ 7 \ 7) \\ \hline \end{array}_8$$

$$\begin{array}{r} (2 \ 2 \ 6 \ 7) \\ + (6 \ 0 \ 0 \ 1) \\ \hline \end{array}_8$$

$$\textcircled{X} (0 \ 2 \ 7 \ 0)_8$$

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$$\begin{array}{r} (2 \ 2 \ 6 \ 7) \\ - (1 \ 7 \ 7 \ 7) \\ \hline \end{array}_9$$

$$\begin{array}{r} (2 \ 2 \ 6 \ 7) \\ + (7 \ 1 \ 1 \ 2) \\ \hline \end{array}_9$$

$$\textcircled{X} (0 \ 3 \ 8 \ 2)_9$$

$$\begin{array}{r} (2 \ 2 \ 6 \ 7) \\ - (1 \ 7 \ 7 \ 7) \\ \hline \end{array}_{16}$$

$$(2 \ 2 \ 5 \ 7)_{16}$$

$$+ (E \ 8 \ 8 \ 9)_{16}$$

$$ $$

$$\textcircled{X} (0 \ A \ F \ 0)_{16}$$

$$c) ((A+B) \cdot D)' = (A+B)' + D'$$

$$= A' \cdot B' + D'$$

$$d) ((AB' + C) \cdot D + E)' = ((AB' + C) \cdot D)' \cdot E'$$

$$= ((AB' + C)' + D) \cdot E'$$

$$= ((AB')' \cdot C' + D) \cdot E'$$

$$= ((A' + B) \cdot C' + D) \cdot E'$$

$$= A'C'E + B'C'E + DE'$$

10) Simplify the following Boolean expressions to a minimum number of literals:

- $x(x+y)$
- $x'yz + xz$
- $xy + xy'$
- $(x+y)(x+y')$
- $xyz + x'y + xyz'$

* Solutions

$$a) x \cdot (x+y) = x \cdot x + x \cdot y = x + x \cdot y$$

$$= x(1+y) = x \cdot 1 = \boxed{x}$$

$$b) x'yz + xz = z \cdot (x'y + x)$$

$$= z \cdot (x' + x) \cdot (y + x) = z \cdot 1 \cdot (y + x)$$

$$= z \cdot (x + y)$$

$$c) xy + x\bar{y} = x \cdot (y + \bar{y}) = x \cdot 1 = \boxed{x}$$

$$d) (x+y)(x+\bar{y}) = x \cdot x + x \cdot \bar{y} + y \cdot x + y \cdot \bar{y} \\ = x + x\bar{y} + xy = x \cdot (1 + \bar{y} + y) \\ = \boxed{x}$$

$$e) xy\bar{z} + \bar{x}y + x\bar{y}z \\ = xy(\bar{z} + z) + \bar{x}y \\ = y(x + \bar{x}) = y \cdot 1 = \boxed{y}$$

Problem 2

1) Determine the value of the base x if, $(410)_x = (226)_8$.

* Solution: $4x^2 + x = 2 \cdot 8^2 + 2 \cdot 8 + 6 \cdot 8^0$

$\Rightarrow 4x^2 + x - 150 = 0 \Rightarrow \boxed{x = 6}$

2) Perform the following addition without converting to decimal

a. $(110110)_2 + (110101)_2$

b. $(15F)_{16} + (A7)_{16}$

c. $(35)_8 + (73)_8$

* Solution

a)

$$\begin{array}{r} 110110 \\ + 110101 \\ \hline 1001010 \end{array}_2$$

b)

$$\begin{array}{r} 15F \\ + A7 \\ \hline 206 \end{array}_{16}$$

c)

$$\begin{array}{r} 35 \\ + 73 \\ \hline 130 \end{array}_8$$

3) Perform the following multiplication

a. $(367)_8 * (20)_8$

b. $(b73)_{16} * (15)_{16}$

* Solution

a)

$$\begin{array}{r} 367 \\ * 20 \\ \hline 000 \\ 756 \\ \hline 7560 \end{array}_8$$

b)

$$\begin{array}{r} b73 \\ * 15 \\ \hline F3F \\ + b730 \\ \hline C50F \end{array}_{16}$$

7) Perform the subtraction of the following unsigned binary numbers using 2's complement

- a. 11010-1101
- b. 1011-1111
- c. 10011 - 10010
- d. 100010 - 100110

* Solutions:

$$\begin{array}{r} \text{a)} \quad 11010 \\ - 01101 \\ \hline \end{array}$$

$$\begin{array}{r} 11010 \\ + 10011 \\ \hline \end{array}$$

$$\textcircled{X} \quad \boxed{01101}$$

$$\begin{array}{r} \text{b)} \quad 1011 \\ - 1111 \\ \hline \end{array}$$

$$\begin{array}{r} 1011 \\ + 0001 \\ \hline \end{array}$$

$$\textcircled{-} \quad 1100$$

$$\boxed{-0100}$$

$$\begin{array}{r} \text{c)} \quad 10011 \\ - 10010 \\ \hline \end{array}$$

$$\begin{array}{r} 1'0'0'11 \\ + 01110 \\ \hline \end{array}$$

$$\textcircled{X} \quad \boxed{00001}$$

$$\begin{array}{r} \text{d)} \quad 100010 \\ - 100110 \\ \hline \end{array}$$

$$\begin{array}{r} 1000'10 \\ + 011010 \\ \hline \end{array}$$

$$\textcircled{-} \quad 111100$$

$$\boxed{-000100}$$

8) Follow the instructions

- Find the 16's complement of $(C3DF)_{16}$.
- Convert C3DF to binary.
- Find the 2's complement of the result in (b)
- Convert the answer in (c) to hexadecimal and compare with the answer in (a).

★ Solution:

$$\begin{array}{r} \boxed{a)} \quad C \quad 3 \quad D \quad F \\ \text{5 Comp:} \quad 3 \quad C \quad 2 \quad 0 \\ \text{16's Comp:} \quad \underline{3 \quad C \quad 2 \quad 1}_{16} \end{array}$$

$$b) \quad \begin{array}{c} C \quad 3 \quad D \quad F \\ (1100 \ 0011 \ 1101 \ 1111)_2 \end{array}$$

$$c) \text{ 2's Comp: } (00111100 \ 00100001)_2$$

$$d) \quad \begin{array}{c} 0011 \ 1100 \ 0010 \ 0001 \\ (3 \quad C \quad 2 \quad 1)_{16} \end{array}$$

9) Apply DeMorgan law to the following expressions

- $A + B'$
- $X'Y + XZ'$
- $((A+B).D)'$
- $((A B' + C).D' + E)'$

★ Solution:

$$a) A + B' = (A' . B)'$$

$$\begin{aligned} b) (X'Y + XZ') &= ((X'Y)' . (XZ')')' \\ &= [(X + Y') . (X' + Z)]' \end{aligned}$$

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