

CS 240: Algorithm Design and Analysis

Kewei Tu
ShanghaiTech University
Fall 2017

Administrative Stuff

Classes

- Tue/Thu 10:15-11:55am @教学中心303
- 12 weeks (Sept 19 - mid Dec)

Instructor: 屠可伟

- Email: tukw@shanghaitech.edu.cn
- Office: SIST 1A-304B
- Office hours: TBA

TA: 周扬、梅俊、邹彦良、王丰

- Office hours: check your email and take a survey

Administrative Stuff

Textbook

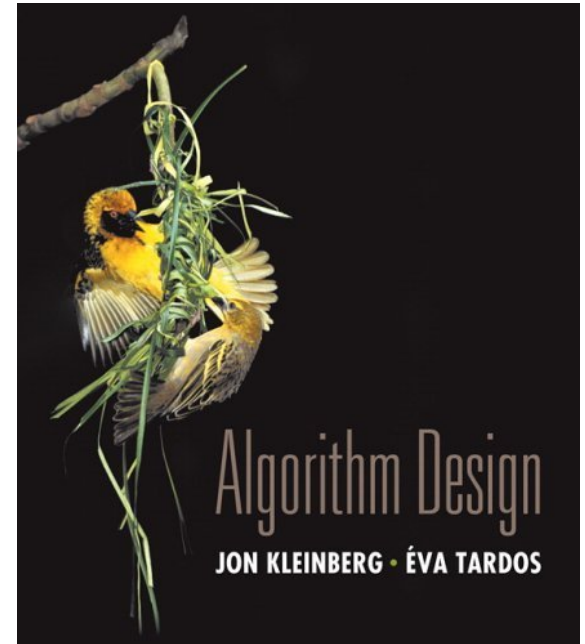
- Algorithm Design, Jon Kleinberg and Éva Tardos
- Reference
 - Introduction to Algorithms, C. E. Leiserson, C. Stein, T. H. Cormen, and R. Rivest, (third edition)

Prereq

- Computer Programming
- Data Structures
- Algorithms (undergraduate)

Survey

- <https://www.wenjuan.in/s/rYNBFvb/>



Administrative Stuff

Blackboard

- Announcements, homework assignments, slides, etc.
- Forum for discussion and QA
- Roster will be updated at the end of the 2nd week
- Students from 高研院: please check your email

Grading (percentages are tentative)

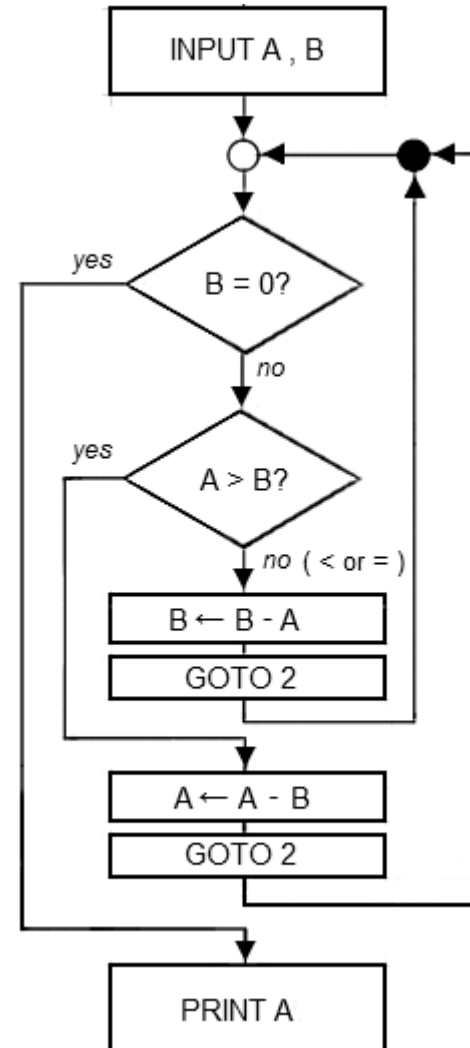
- Homework (20%): 5-6 homework assignments, due in one week
- Midterm (30%): in late Oct or early Nov
- Final (30%): in late Dec or early Jan
- Participation (10%): class, forum
- Project (10%): to be determined

Course Overview

Algorithms

Algorithm.

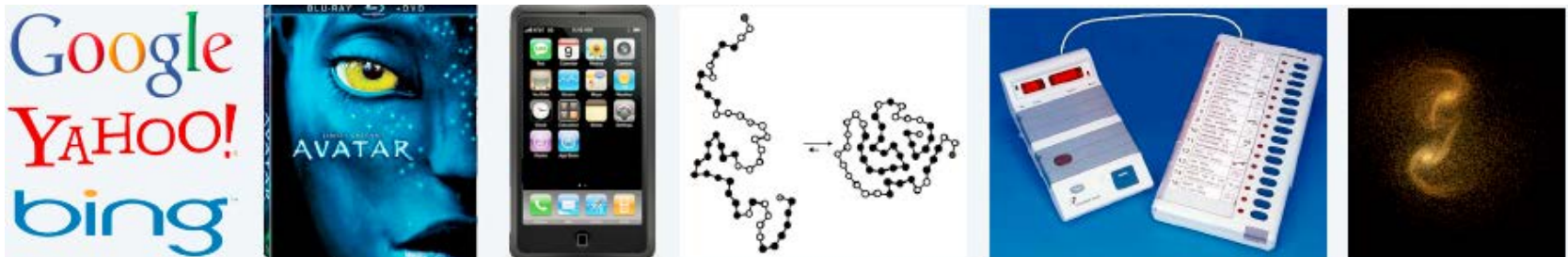
- [Wikipedia] In mathematics and computer science, an algorithm is an unambiguous specification of how to solve a class of problems.
- [Knuth, TAOCP] An algorithm is a finite, definite, effective procedure, with some input and some output.



Why study algorithms?

Wide range of applications.

- **Internet.** Web search, packet routing, distributed file sharing, ...
- **Biology.** Human genome project, protein folding, ...
- **Computers.** Circuit layout, databases, caching, networking, compilers, ...
- **Computer graphics.** Movies, video games, virtual reality, ...
- **Security.** Cell phones, e-commerce, voting machines, ...
- **Multimedia.** MP3, JPG, DivX, HDTV, face recognition, ...
- **Social networks.** Recommendations, news feeds, advertisements, ...
- **Physics.** N-body simulation, particle collision simulation, ...
- ...



Typical Undergraduate Algorithm Course

Understanding and implementing classic algorithms

- Sorting
- Searching
- String algorithms
- Graph algorithms

Critical thinking, problem-solving, coding

This Course

Design and analysis of computer algorithms

- Graph algorithms
- Greed
- Divide-and-conquer
- Dynamic programming
- Network flow
- Intractability (complexity classes)
- Coping with intractability
- Approximate algorithms
- Randomized algorithms
- Local search

Critical thinking, problem-solving, rigorous analysis

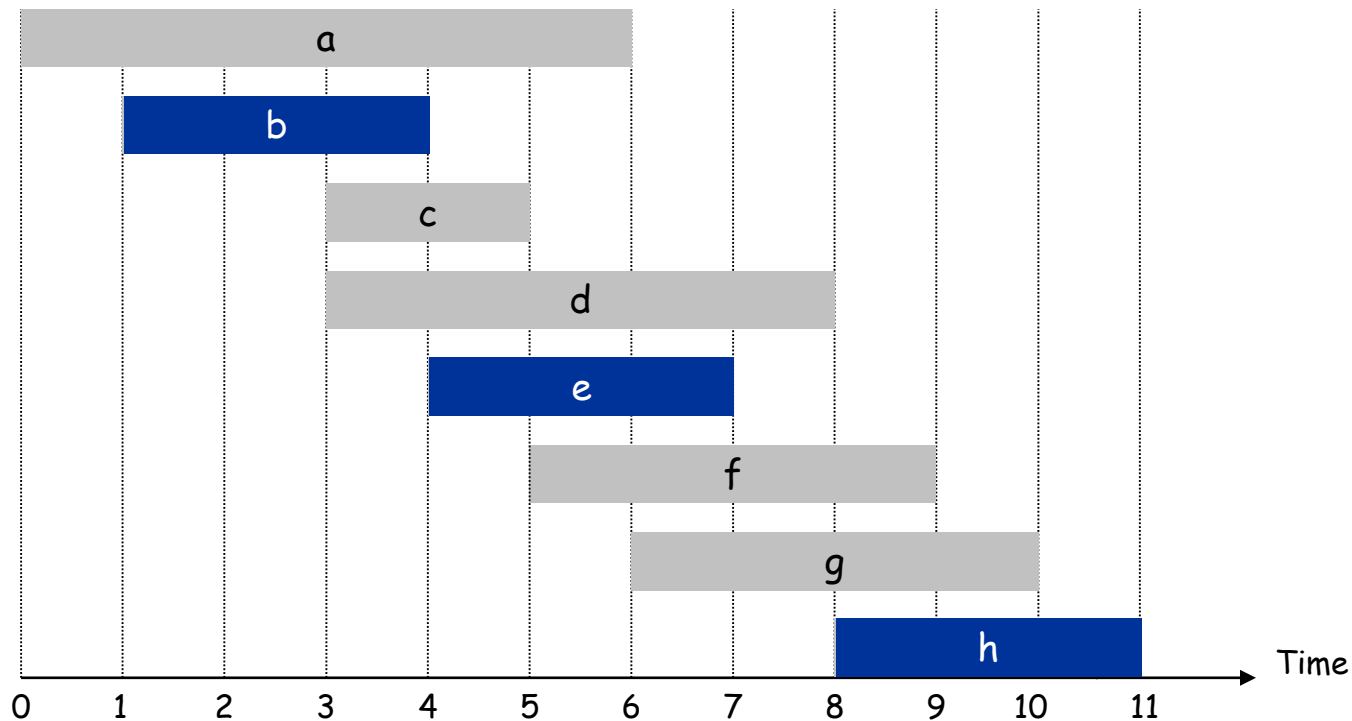
Five Representative Problems

Interval Scheduling

Input. Set of jobs with start times and finish times.

Goal. Find **maximum cardinality** subset of mutually compatible jobs.

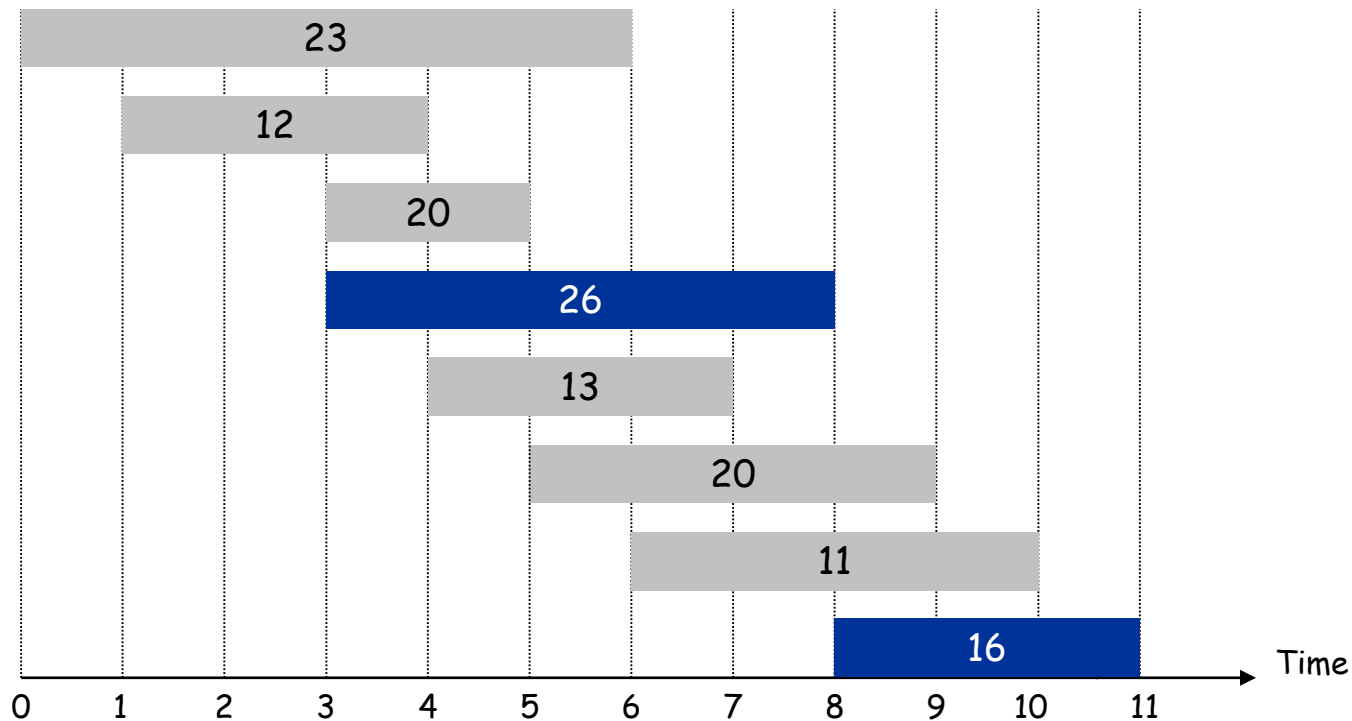
↑
jobs don't overlap



Weighted Interval Scheduling

Input. Set of jobs with start times, finish times, and weights.

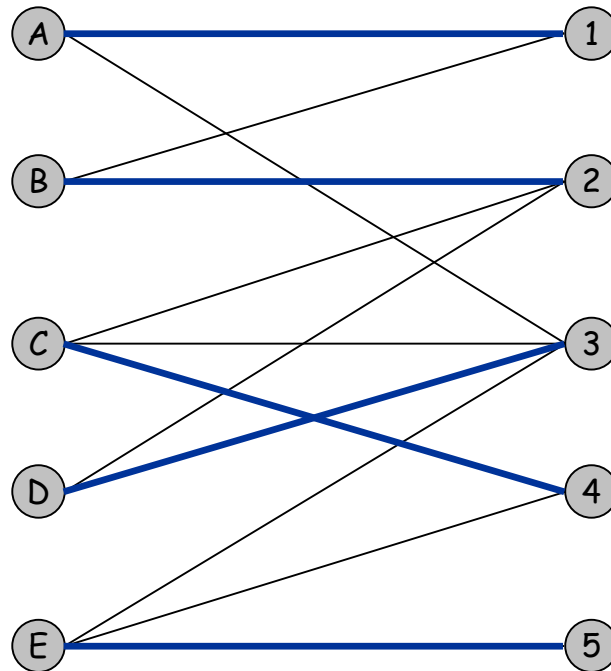
Goal. Find **maximum weight** subset of mutually compatible jobs.



Bipartite Matching

Input. Bipartite graph.

Goal. Find **maximum cardinality** matching.

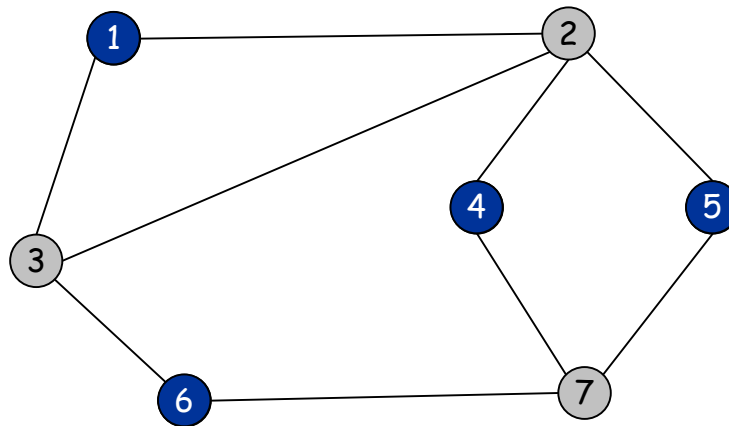


Independent Set

Input. Graph.

Goal. Find **maximum cardinality** independent set.

↑
subset of nodes such that no two
joined by an edge



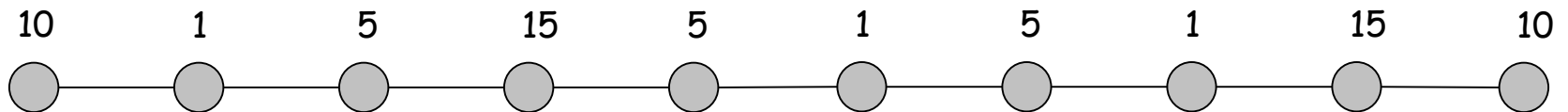
Extension: Weighted independent set.

Competitive Facility Location

Input. Graph with weight on each node.

Game. Two competing players alternate in selecting nodes. Not allowed to select a node if any of its neighbors have been selected.

Goal. Select a **maximum weight** subset of nodes.



Second player can guarantee 20, but not 25.

Five Representative Problems

Variations on a theme: independent set.

Interval scheduling: $n \log n$ greedy algorithm.

Weighted interval scheduling: $n \log n$ dynamic programming algorithm.

Bipartite matching: n^2 max-flow based algorithm.

Independent set: NP-complete.

Competitive facility location: PSPACE-complete.