Coursera Nachine learning course Notes By June Shi

Estimated completion: Decade - Jan 2019.

Week 4

#### introduction

Definition of Machine learning.

A computer program is said to learn from experience E with respect to Some task T and some performance measure P if its performance on T as measured by P Improves with experience E.

Main two types: (explored in this course)

LA Superused machine learning is unsupervised machine learning

LA advice for practical uses of machine tearning

LA how to develop ML systems?

supervised learning

as a result of reloo between input &

It we gove a datoset (where the "right chaner" are given) we know what our consider looks tike

I regression problem: predict continuous value outlinet

Lt classification problem: predict discrete value output.

Latake account of voious number of inputs. I feedures linfaite may that attributes

Maylerised learning

It determine cludeing of data , where we have little , no idea about what result should bold like

LA Identify concluse groups of obta

H example: cooktaal party proden given two recording, with two bodys of different volume, output each sound tach

to can be written in one line (solution).

Levetere is good! built for In alg ! programming.

Model & cost function

#### Model representation

Lelinear regression model

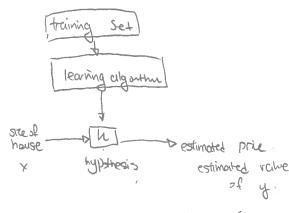
LA training set is the data - set.

H M: # of training example, x's input var/feature. 4's auticul var

(x,y) & training example

(x(i), y(i))\_ith triining example.

LA



Le ho(x) = 00+01x



Le trus is living will variable / universate living.

#### Cost function

re po(x) - 00 + 01 x

1 1 that training examples

god is to minimize of the (ho (xti)) -y (7))2

Le Minimite J(OO,OI) where J(OO,OI)= In Z(ho(xit))-y(i))2

H the squere evor function.

00

Le contour graphs or used for multiple features. (Pbl 3D graph)

01 global minima so that (90,0,7 line of best At.

Cost Amotion.

```
14 the graphs cannot always be visitatized as easily. Thus, we would need some other algo
LA Gradient descont algorithm.
        LA have function JIOS, OI
                   min 2(0,01)
         Layou start with some Do, D., then keep changing Do, D. -> reduce $100, D.) each Hooting
         Ho via calculus
          Let you can one up at town different load sptimums
                       (= > F assiding elector
 the algorithm.
          repeat with converge ?
                  \theta_{\tilde{J}} = \theta_{\tilde{J}} - \alpha \frac{3}{3\theta_{\tilde{J}}} J(\theta_0, \theta_1) for \tilde{J} = 0.1.
      cared simultaneous update:
       tempo := 00 - 01 300 J(00,01)
                                              Le or is the learning rate.
       tempi := \Theta_1 - \alpha \frac{\partial}{\partial \Theta_1} J(\Theta_2, \Theta_1)
                                                   how big step we go down hill?
                                                    big step / baby step?
        Oo=tempo
                                             Lt simultaneously ydate do and Di. od same time
       01=temp1
 Holmon updating, takes consideration of whether is positive or negative,
    So the new point is chosen to x axis. The absolute value of to approach to a gradually.
 Let need to charse of so it's not too small, not too large.
            if or to, small or also algorithm
            If a two large 17 may even dirage
 LA Dulling It altogether
     Gradient Descent alguntum
                                                        linear regression model.
        topech until converge L
          $ := 07-00- J(00,01)
                                                              ho(x) = 00+0,x
                                                             J(00,01) = In I (ho(x6)) - y6)) 2
                           for(j=1, 7-0)
                           apply to to minimize
```

Plug in the equation, we obtain

$$\frac{\partial}{\partial \theta_{i}} J(\theta_{0}, \theta_{1}) = \frac{\partial}{\partial \theta_{j}} \cdot \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2}$$

$$= \frac{\partial}{\partial \theta_{i}} \cdot \frac{1}{2m} \sum_{i=1}^{m} (\theta_{0} + \theta_{i} x^{(i)}) - y^{(i)})^{2}$$

$$\begin{array}{lll} \Theta_0: & \frac{\partial}{\partial \theta_0} \, \overline{J}(\theta_0,\theta_1) = & \frac{1}{m} \, \sum_{i=1}^m \, \left( h_\theta \left( \chi^{(i)} \right) - y^{(i)} \right) \\ \Theta_1: & \frac{\partial}{\partial \theta_0} \, J(\theta_0,\theta_1) = & \frac{1}{m} \, \sum_{i=1}^m \, \left( h_\theta \left( \chi^{(i)} \right) - y^{(i)} \right) \cdot \chi^{(i)} \end{array}$$

14's always a convex function. Our linear regression algorithm turns self to be

repeal until converge?

"Butch Gradient Descent" each step of gradient descent uses all training examples

Lende must use the model for J(Do, Di) where there's no other local sprima then the global or else it can set up at another local min

### Week a

Multi-fedure linear regression

Laharing multiple fratures

notation: n: # 2P feature

X(i): input feetures of 7th example (vector)

xj(i): value of feature j in the ith training Chample.

Hhypthesis:

for convenience, 4x, Xo=I

$$X = \begin{bmatrix} x & 0 \\ x & 2 \\ x & 0 \end{bmatrix} \in \mathbb{R}^{n+1}$$
  $\theta = \begin{bmatrix} \theta & 0 \\ \theta & 0 \end{bmatrix} \in \mathbb{R}^{n+1}$ 

Hypothesis:

or inner product, (0, x>

Percimeter: 0

Cost function:

J(0) = 2m = (ho (x (+))-4 (-)) 2

Gradient descent:

repeat !

0j:=0j-am = (ho(xil)-yil) xj (i)

Simultaneous update Oj, j=0,1,2,~~N since you're taking devotre with respect to the feature.

Gradient descent in practice:

Lo feetre scaling.

Lemake Sure features are on a similar scale.

H H+, -1<x=<1

Lemajor rates crond -3 v +3 ish not too little as in 10,1

4 Mean nomalization

- replace X-i with X1-ui, to make sure feature have no mean

LA do not city to Xo-1 though!

xit xi-ui trange value of xi

Le" debugging" make sure it works properly. He haw to choose your a?

Le "Debugging" make Pot whore # ito is x-axis, min J10) y,

Le J10) should always demose due to # of iter (every single iter).

Le 17 J10) ero increases, you want to decrease or

Le convergence test: choose & to declare when JID) < 2. 7 Converges!

L+ tip: to choose a, try 0.001, 0.01, 0.1,1, --- try a range of values.

# Peatures & polynmial regression

Ly condine multiple feetures into 1.

-> combine X1 and X2, by taking X3 = X1.1 X2

to polynomial regression if linear doesn't fit.

Leidens: ho(x)=00 + 0, x, +02x, 2+03x,3

feeture x2 feature x3

ho(x) = 00 + 01 x + 02 Jx1

Hewith this though, keep in mind, feather scaling is very importent.

Hamal equation (computing poom ancilytically)

H X= design motion. 
$$X^{(i)} = \begin{bmatrix} x_0^{(i)} \\ \vdots \\ x_n^{(i)} \end{bmatrix} \in \mathbb{R}^{n+1}$$
 then  $X = \begin{bmatrix} -(x^{(i)})^T \\ -(x^{(i)})^T - \end{bmatrix}$ 

Le optimum 0 gives by

 $\theta = (x^T x)^{-1} x^T y$ 

ictore: print (x' + x) \* x' \* y

x1: transpose \*: madax

He note with normal equation, you DONT need feature scaling.

V5

Gradient descent
Leneed to choose of
Le many iteration.
Le work well even
if n is large.

Normal equation.

Lens need to chare d

Lens Heating needed

LA (XTX) T takes o(n3)

LA Slaw when n is large (>(0,00)

M# training example

## Normal equation / minvotto/thy

Lewhol if XTX is non-involide?

ronze , binn, lustoof of inn, (bzengo-lurate)

List gives you of though XTX is singular foother. Or to many feather men, then use regularized

#### Vectorization

helps to compute vectors faster

Assignment questions include:

Li computing cost for multi/uni variable doctaset

4 computing lost for multiple variable

to gradient descent for multi/uni variables

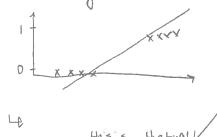
### Week 3

work with classification problem

LA yell Negative dans
Positive class.

Lehows binay class classification.

Does lin-reg work? no not a good idea.



threshold = 0.5

If ho(x) } & th predict } |

this is the byg! I mos up your linneg data! o

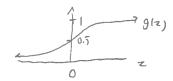
4 So don't use lin reg for classification.

Hogistic regression: 0 < ho(x) < 1

Ation is a dointholis algorithm

### logistic regression

g(z)= 1+e-2 //ogistic/signid Luction



Le Interpretation: ho(x) gives you probability that our output is 1 = p(y=1 | x;0) in probability notation.

decision benday is the line that spporate area when y=0, y=I ( line whore hol X) =0.5 exactry).)

non linear decision bendances, then you need more porches for higher dim. It there are als-



7 -1+x1+x2° 20 resultsin O boundary

### legistic regression model

$$ho(x) = \frac{1}{1 + e^{-bTx}}$$

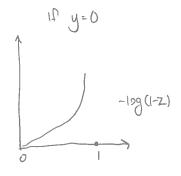
tin règ mont gire a correx, but we want a correx function

$$(ost (ho(x),y) = \begin{cases} -log ho(x) & if y=1 \\ -log cl-ho(x) & if y=0 \end{cases}$$



cost=0 if x=1 but as hown 70, cost > 00.

induction = if hown=0, but you predict t as I, you're paralized.



similar as the other intuition

this gives a conex & local optimum free function

nde: y=1 xy=0 always. -7 (an combine two equations

the compressed cost function is:

(ost (ho(x), y) = -y log (ho(x)) - (1-y) log (1-ho(x))

otal costJ: m (ost (he(x),y (i))

= -1 [ = y(i) log (he(x(i)) + (1-y(i)) log (1-he(x(i)))]

Want: MIN J(0)

gradient dexent algorini:

Repeat 
$$20j = 0j - \alpha \frac{\partial}{\partial 0j} J(0)$$

hereat  $l = 0j - \alpha \sum_{i=1}^{M} (ho(x^{(i)}) - y^{(i)}) x_j^{(i)}$  y simultnessy update works same as (in.reg's grad, des, but! ho(x) refers to  $\frac{1}{1+o^{-0.5}x}$  now.

### vectorized unperentation

(33)

h=g(x0) this computes quantity ho(x1i)

J(0)= th \(\Sigma\) =g(ho(x(i))) + (1-y(i)) log (1-ho(x(i)))]

J(0)=th. (-y \(\left\) log(h)-(1-y) \(\left\) log(1-h))

### the grudient downt

Idea: rearrage the vectors With it's easy to type into Mattab. "

0:=0-at 1= [(he(xi))-yiv)-xii] Colomirector

ロニロー 架 x T (g(Xの)-項)

do com vise colonation.

Dis a (in x 1) vector.

XO returns xin) On return corresponding whex.

The x (y(xy)-y)

Since: thus, xT makes each x(i) a column vector. x(i) [ x(i) ] [m

DENXI VAC x=mxn x0= mx1. MXM STX

ons: hx1.

diversed Optimization

disconsistent of the second of the Advance Optimization Le Conjugate gradient | footer, honed for of, but not complex.

4 BFGS

4 1-RECE

50 We use the library 4 L-BFGS

We Andry "fring(1)" Physin the SIB) & the gradients shall suffice

logistic aptiminates for multiple classes "me us all donsification" Multiclass donstitution. y=10,1, --- n's each are cotteny. Citign one days as positive, all other no, as "the rest" 48/0,1,2, ... NJ ho (N=P(y=0/xi0)

ho(1) (x) = P(y=1 | x) 0)

ho (m) (x) = p(y=n/x; 0)

predictionis: max ho (i) (x)

# Problem of over-fitting

under-fitting: hypothesis function maps to poorly to the trend of data. Too simple I tell the feature worfiting = not generalized enough. fits available data too well, but might have unhecessary angles/ e.e. to mggry (tail to generalized):

to resolve overfitting.

1) reduce that features. (model selection algorithm to ditch less-important features.)

2) regularization (reduce magnitude of 0;)

Cost function (thenew one with regularization, big n bumps up and furues of to be small Mino in Zin (ho (x(i)) - y(i))2 + 7 Zin 0;2 because big 0; will be penalized

Gradient docent

always less than 1 as it tredue by each time by a little bit

Normal equation

Where L= [0]

Note if men, XTX is inanvertible but adding L mater it invertible.

regularization solves non-invertibility as well:

Regularced logistic regression (advanced optimization works similarly)

regularized cost function for linear regression.

Advance function (regular cotion).

Jual: same as previous.

gradient 1: (Indexo)

In \( \frac{7}{1=1} \left( \he (\chi^{1/2}) - y^{1/2} \right) \chi\_0^{(12)} \)

gradient (2~nH) index (1,2,...n))

( In Inter (1,2,...n))

( In Inter (1,2,...n))

( In Inter (1,2,...n))

Wortchaut following when doing assignment:
La display dimensions might be in apposite order.

Ledraw out matches larefully to visualize the vectorization.

Ly motion matrix dimensions always.

### Week 4

#### Newal Networks - representation

LA computer vision - evaluate

Le 109 stic regression would have to many features. (like a femnilian : for mag La mimic the brain.

I lorge scale:

LA neural-rewiring experiment

LL adjust 1 learn the douta

### Model representation

=1, "bias mit" > (x)

Imputures

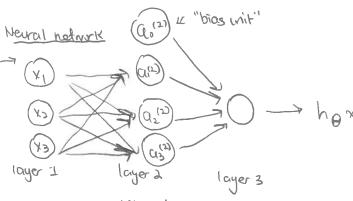
(x)

| New Particle | Murar model | bogistic unit

$$\begin{array}{c} (x_{2}) \\ (x_{3}) \end{array} \xrightarrow{\rho} \begin{array}{c} ho(x) = \frac{1}{1 + e^{-0\tau x}} \\ (x_{3}) \end{array} \begin{array}{c} \lambda = \begin{bmatrix} k_{0} \\ \kappa_{1} \\ \kappa_{2} \\ \kappa_{3} \end{bmatrix} \begin{array}{c} \theta = \begin{bmatrix} \theta_{0} \\ 0_{1} \\ 0_{2} \\ 0_{3} \end{array} \end{array}$$
the neuron.

$$X = \begin{bmatrix} x_0 \\ x_1 \\ x_2 \\ x_3 \end{bmatrix} \quad \emptyset = \begin{bmatrix} \theta & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

" signise activation function."



input layer hidden-layer authoritager

$$\begin{cases} Q_{i}^{(j)} = \text{``activation''' of out it in layer'j} \\ Q_{i}^{(j)} = \text{``matrix'} \text{ at weights controlling func mapping funclayer' j to j+1} \end{cases}$$

Vec representation

$$\begin{bmatrix} x_0 \\ y_1 \\ x_2 \\ y_3 \end{bmatrix} \rightarrow \begin{bmatrix} G_1(2) \\ G_2(2) \\ G_3(2) \end{bmatrix} \rightarrow h_0(x)$$

vector representation "activation nodes" arcomple

$$Q_{1}^{(2)} = Q(\theta_{10}^{(1)} \chi_{0} + \theta_{11}^{(1)} \chi_{1} + \theta_{12}^{(1)} \chi_{2} + \theta_{13}^{(1)} \chi_{3})$$

$$Q_{2}^{(2)} = Q(\theta_{20}^{(1)} \chi_{0} + \theta_{21}^{(1)} \chi_{1} + \theta_{22}^{(2)} \chi_{2} + \theta_{13}^{(1)} \chi_{3})$$

$$Q_{3}^{(2)} = Q(\theta_{30}^{(1)} \chi_{0} + \theta_{31}^{(1)} \chi_{1} + \theta_{32}^{(1)} \chi_{2} + \theta_{33}^{(1)} \chi_{3})$$

$$\log(x) = Q_1^{(3)} = Q_1^{(2)} Q_0^{(2)} + Q_{11}^{(2)} Q_1^{(2)} + Q_{12}^{(2)} Q_2^{(2)} + Q_{13}^{(2)} Q_3^{(2)})$$

qu (B)

La each layer has its own motion of weights

Le if network has Si layers in level J. Sitility on level Jt1, then 81) has dimension Sjul × (Sj+1)

Comes from bias node

Leloidout like this, blc mutipy 8, the rector will be on the right.

intuition: Neural network allows nodes in its hidden layer to "learn' its own features.

### Vectorization of computation

refer here

$$\Box Q_{2}^{(2)} = g(Z_{1}^{(2)})
 \Box Q_{2}^{(2)} = g(Z_{2}^{(2)})
 \Box Q_{3}^{(2)} = g(Z_{3}^{(2)})$$

for layer 
$$j_1$$
 nodek,  $Z_i$ 's
$$Z_{K}^{(j)} = \theta_{K,0}^{(j-1)} x_0 + \theta_{K,1} x_1 + \cdots + \theta_{K,n}^{(j)} x_n$$

$$X = \begin{bmatrix} x_0 \\ x_1 \\ \vdots \\ x_n \end{bmatrix} \qquad Z^{(n)} = \begin{bmatrix} Z^{(n)} \\ Z^{(n)} \\ \vdots \\ Z^{(n)} \end{bmatrix}$$

$$Z^{(i_1)} = \Theta^{(j_{-1})} \alpha^{(j_{-1})}$$

nde: dim (B(j-1)) is Six(n+1) dim (aiti) is (n+1)x1.

adding the bids wit: to layer j after combuting a (i) u. as (i) = 1.

to compute final hypothesis, compute z vector:

Z(it) = O(i) a(i) the last matrix O(i) has only I row, multipled by one column recal so the result is a real number.

17

Multi-class Classification Lane-us- all method holx) EIR 4 if those or 12 claimes

how≈[8] or [8] x [8] x [8]

with different INPUT X.

It returns one of the ei's vector given a particular input

[Week 5] Gual: learn har to train newed networks

the wat function for the neural network

LILE total # of layers mthe network

Le SI (#2 units not counting bias unit in layer L)

Lt K= #xl autput unit / closses.

J(0) = - = [ [ yk | log((ho(x(i)))k) + (1-y(i)) (log(1-ho(x(i)))k)] + = [ [ yk | log((ho(x(i)))k)] + [

Back propergation algorithm

Le goal is to compute min & J(A)

LA lost at ported derivative of J(8)

the back propagation against works as follows:

Ligivon training set  $\{(x^{(1)},y^{(1)}),\dots(x^{(m)},y^{(m)})\}$ Lit set  $\Delta^{(2)}$  :=0  $\forall \forall ij$ 

LA for training example &=1~M 1, set a(1):= x(1)

a perform forward propagation to compute all! , L= 1,2,3, --- L

(le set up z (inhamediate, use grz) to (alculate next layer)

3, 8(L) = 0 (L)-y(A)

4. Compute  $S^{(L^{-1})}$ ,  $S^{(L^{-2})}$ , ---  $S^{(2)}$  using  $S^{(L)} = ((\Theta^{(L)})^{T} S^{(L^{-1})}) \cdot * \alpha^{(L)} \cdot * (I-\alpha^{(L)})$   $G^{(1)} = Q^{(L)} \cdot * (I-\alpha^{(L)})$ 

5.  $\Delta_{ij}^{(l)} := \Delta_{ij}^{(l)} + Q_{ij}^{(l)} \delta_{j}^{(l+1)}$  with rectination,  $\Delta_{ij}^{(l)} := \Delta_{ij}^{(l)} + Q_{ij}^{(l+1)} (\alpha_{ij}^{(l+1)})^{T}$ Whate: } Dis(1) := m Dij(1) + N Oij(1)) , f J to

☆ Aij(1) はす=0

D'15 "accumulator". 30-19 J18) = D+11)

### Implementation details

Lenctor to holes and video

LAND need to write code for hand-withon neles.

reunding = you can make / convert between matrix / rector reprise matrices

Legradian checking: bug-free impl guarantee

Le use random to set initial thata

#### Week 61

## Evaluating a learning algorithm

ways to arrive at better hypothesis

LA more examples

LA MORCI 105 # of features

Lamorelless value of N.

70% 35%

to evaluate a hypothesis, we split date into triving set & test set.

We be learn 0, minimier Jerain (8) using training set

Le compute test set error Jtest (0)

computing tot set error

La lin. reg. : Jtest (0) = 1 Mest (ha(x) test - y test) a

Test error = 1 that cer (ha(x fest), y fest)

### Model Sclection

you can break down doto set into three dota sels:

training set, cross validation set, test set

dea: test different degree of polynomial, evaluate error function

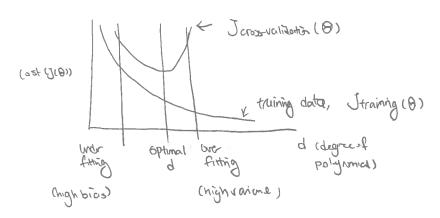
1, optimize proms in O using training set for each degree

2, find the polynomial degree of that produce least error by cross validation

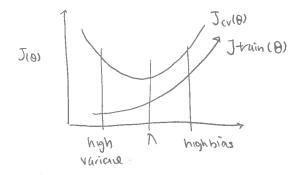
3. Estimate generalized error with Jtest (D(d)) using test set. (d:= deg returning /lowe: (this way, test set is NOT associated with the poam training.

# Diagnosing bias us Variane

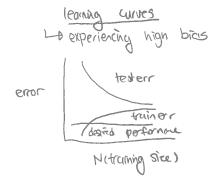
If you have bad predictor, you need to figure out whether it's high bios or variance.



Regularization vs bias/Varience



we use similar algorithm for testing regularization tom n.

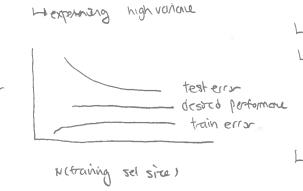


Lalow taking selsize causes Joan(0) low, Jev(0) high.

Lalorge training selsize causes both Joan(0), Jev(0) high

but also Joan(0) ≈ Jev(0)

Le getting more doubte won't help much.



Lalow training set size: Jtain(0) 10w, Jov(8) high
Lalorge training set size: Jtain(0) 11 crease with set

Size, and Jov(0) continue to derrose without
platearing. Jtain (0) & Jov(0), but difference
remains significant.

Lagetting more docter will likely to help

## Debugging learning again.

problem. try

getme training data high var

high var less features

get me features high blas

odd pdy features high bios

high bids dercool 1

increase n. highvar

( prone to under fitting) Small neural network: computationally chearp (prone to overfitting, (use A (regularization) to fre large neural network: computationary expensive

## Billidman a spam closisifier

Hosigning ML system. (building your own system)

Hidertify Features (X) and classifyer (y)

It ways to sport mre time

H collect lots of donta

LA MOR Sophisticated foothers

Le algoritms to process input data.

### Error analysis

Leimpenest a quick implementation

It use it to decide how to Spend your time

Le plat learning curves, and decide what to do.

Le manually examine errors, analyse

H Implanaria a metal that returns performance on different changelideas.

#### Skewed classes

It case when one class has very large size, another very little size.

It different error metric 7 use to t, true & false t, false - to classify (precision / recall) Precision: true + / pred + , \* Recall time + / actual +

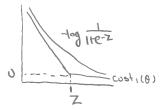
con change ho(x) threshold, which tade of precision / recoul precision netal: f. score: PR/(ptR)

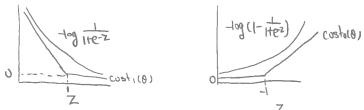
#### Week 7

Support vector machine (SVM)

H wing cost (1), costor similato has but easier computation wise

4 82. 18 4-1





minimização o givestoj: optimization projective:

L1 MM ( ) y(i) (ssl 1 (BT x(i)) + (1-y(i)) (sst 0 (BT x (i)))] + 2 = 0;

Lelorge margin dassifyer.

LAcillans a decision boundary that stays naturally for apart from destased. Ho the pertadiously vector is dosen to exemples



Kernels

label landmark (deliving factore) then use distance measure.   

$$f:=\exp\left(-\frac{||x||^{2}||y||^{2}}{20^{2}}\right)$$
 If  $||y|| \approx \frac{\text{Small}}{||y||} f_{\approx}^{2}$ 

team non-linear decisies boundary

details (overwith kernels)

Hypthesis given x, compute features fer Rmx1 predict "y=1" if 0"f>0

training using find's suniborty metric instead.

Min C = yillost, (OTfin) + (1-yin) (10sto (OTfin) + \$ = 07

note that since C= 1, large C > lowbias, highvar (le small n)

Small (> highbias, low var (le large T)

large 827 features fin, vary snoth, high bias, low var

Snowly > Leatures Phil vary less smooth, low bias, high yar

Man Jop 13 to choose c and Q5

using an SVM

Ly nice software libraries: librimor, libsum.

Lipsed to charse: kernel (use or nouse) and parameter C

Himer Kenel (no Kenel)

LA Floursian Kerner

Heed to chasse &

Lenced to do feating

lefor other choices of Kernel, it must satisfy Morcer's theorem. so it for sure do hot divege - Lywhiclassification

4 builtin SWA Package

Hone- 45-all

Hogistic regression us SVM.

which to choose?

M= # feetures N= # training example.

SVH7 carex function > reduct global optima

17 n large relative tom (norm, nx10,000 mx10~1000)

H use L. R. or siving wellinear Kennel

LA IP n Small, mintemediate (n=12100), M=102100)

H use SVM WI Growsian kernel

4 12n Small mlarge ( n=1~1017, n=50,000+) lin Kernel H add more feature, then use LAD or SVM with

14 nn works well with these settings, but is slower to train.