Coursera Machine learning handwritten neties.

Tought by: Prof. Andrew Ngs.

Gùthub: Jane Sliv 99 Summary of course

Supervised learning
Linear regression, logistio regression, heural networks, SVMS.

Unsuperised learning La K-means, PCA, Anomaly detection.

Special applications 1special topics
It recommender Systems, large Scale Marchine learning.

Addice for building a mathine learning system.

Let Brast ratione, regularization, deciding what to work on next evaluation of learning algorithms, learning curves, error analysis, ceiling analysis.

Coursera Nachine learning course Notes By Jane Shi

Estimated completion: Decade - Jan 2019.

Week 1

#### introduction

Definition of Machine learning.

A computer program is said to learn from experience E with respect to some task T and some performance measure P if its performance on T as measured by P improves with experience E.

Main two types: (explained in this course)

- Superused machine learning 15 unsupervised machine learning

LA advice for practical uses of machine tearning

I have to develop ML systems?

supervised rearning

as a result of relation between input & output

How gave a dataset (where the "right consider" are given) we know what our consider 12043 like

Hegressian problem predict continuous value outlinet.

Hollassification problem product discrete value output

Latake account of vonous number of inputs. I features linfinite may that attributes

# mayoused learning

It determine cludeing of data , where we have little 1 so idea about what result should bold like

Hi ldotty conedite groups of dota

given two recording, with two racks of different volume, output each sound tack

to can be written in one line (solution).

Laureteure is good! built for lin alg: programming.

## Hodel & cost function

#### Model representation

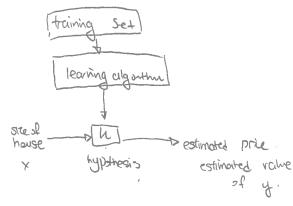
Lalinear regression model

4 training set is the dota -set.

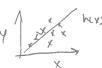
LA M: # of training example, x's input var/feature y's auticul var

(x(i), y(i))\_i+h training example.

14



Le he(x) = 00+017



La fins is lin-reg wil I vanishe / univende lin-reg

#### Cost function

He ho(x) = Bo + BIX

1 1 that training examples

goal is to minimize of the (he (xti)) -y (i))2

Le Minimire J(00,01) where J(00,01)= Im Z(ho(xii))-y(i)) 2

Cost Aunction

It the squere error function.

00

Le contour graphs are used for multiple features. (Pbl 3D graph)

Or global minima

-global minima so that loo, or > line of book fit.

If the graphs cannot always be visitalized as easily. Thus, we would need some other algo. Its Gradient descont algorithm.

LA have function J(00,01)

WOON MIN J(00,01)

Layou start with some Q.D., then keep though g Do.D. > reduce \$100.0.) each Hardhis. La via calculus

Le you can ore up at two different local optimins

the algorithm: (:= + assignment spector repeat with converge?

 $\theta_{j} = \theta_{j} - \alpha \frac{\partial}{\partial \theta_{j}} J(\theta_{0}, \theta_{1})$  for j = 0, 1.

cared simultaneous update:

temp0 :=  $\theta_0 - \alpha \frac{\partial}{\partial \theta_0} J(\theta_0, \theta_1)$ 

temp1 :=  $\theta_1 - \alpha \frac{\partial}{\partial \theta_1} J(\theta_0, \theta_1)$ 

Oo=temp 0

01=temp1

Le a is the learning rate.

how big step me go dann hill?

big step / baby step?

Lt simultaneously ydate to and Di. and same time.

La when updathing, takes consideration of whether to is positive or negative, So the new point is chosen to x axis. I the absolute value of to approach to a gradually. Le need to choose of so it's not too small, not too large.

if or too small or slow algorithm
if or two large in may even dirage

H Dulling It altugether:

Gradient Descent alguntum

repeat until converge l

4

linear regression model:

ho(x) = 00+01x J(00,01) = = = = (ho(x(i)) - y(i)) 2

apply to to minimize

Plug in the equation, we obtain

$$\frac{\partial}{\partial \theta_{j}} J(\theta_{0}, \theta_{1}) = \frac{\partial}{\partial \theta_{j}} \cdot \frac{1}{2m} \sum_{i=1}^{m} (h_{0}(x^{(i)}) - y^{(i)})^{2}$$

$$= \frac{\partial}{\partial \theta_{j}} \cdot \frac{1}{2m} \sum_{i=1}^{m} (\theta_{0} + \theta_{1} x^{(i)}) - y^{(i)})^{2}$$

$$\begin{array}{lll} \Theta_0: & \frac{\partial}{\partial \theta_0} \, \overline{J}(\Theta_0, \Theta_1) & = & \frac{1}{M} \, \sum_{i=1}^M \, \left( h_{\theta} \left( \chi^{(i)} \right) - y^{(i)} \right) \\ \Theta_1: & \frac{\partial}{\partial \Theta_1} \, J(\Theta_0, \Theta_1) & = & \frac{1}{M} \, \sum_{i=1}^M \, \left( h_{\theta} \left( \chi^{(i)} \right) - y^{(i)} \right) \cdot \chi^{(i)} \end{array}$$

14's always a convex function. Our linear regression algorithm turns sent to be

repeal until converge?

Butch Credited Descent " each step of gradient descent uses all training examples.

Lende must use the model for J(Do, O) where there's no other local sprima than the global or else it can end up at another local min

### Week a

Hutti-feature linear regression
Laharing multiple features
Natation: N: #2P feature

X(i): input feature of the example (vector)

Yj(i): value of feature j in the 7th training Champie.

thypothesis:

for convenence, 
$$\forall x$$
,  $x_0 = 1$   
So  $h_0(x) = \sum_{t=0}^{\infty} \theta + x_t$ 

Hypothesis:

or inner product, (0, x>

Perameter: 0

Cost function:

J(0) = 2m 2 (ho (x(4))-y(4))2

Gradient descant :

repeat !

since you're taking derivative with respect to the feature.

Gradient descent in practice:

Lo feetre scaling.

Lemake Sure features are on a similar scale.

H++, -15x251.

Lemajor rates crond -3 v +3 ish not too little as in 10,1

LeMean normalization

- replace X- with X1-ui, to make sure freature have no mean LA do not copy to Xo-1 though!

xit xi-li trange whe of xi

Le" debugging" make sure it with properly Le how to choose your a?

Le "Debugging" make Pot whore # ito is x-axis, min J10) y,

Le J(0) should always demose due to # of iter (every single iter!)

Le 17 J10) err incrases, you want to decrease a

Le convogence test: chose & to declare when J10) < E. 7 Converges!

L+ tip: to choose a, try 0.001, 0.01, 0.1,1, --- try a range of values.

# Peatures & polynmical regression

Ly Condine multiple feetures into I

-- combine x1 and x2, by taking X3 = X1.1 x

to Polynmial regression if linear doesn't fit

He change the behaviour, so it can be quadratic loubic etc.

Leidens: ho(x)=00 + 01x1+02x12+03x13

1

feetive x2 footre x3

ho(x) = 00 + 01 X + 02 Jx,

Lewith this though, keep in mind, feather scaling is very importent.

Marmal editogram (continued bacun outsitudity)

He X: design motion. 
$$x^{(i)} = \begin{bmatrix} x_0^{(i)} \\ \vdots \\ x_n^{(i)} \end{bmatrix} \in \mathbb{R}^{n+1}$$
 then  $X = \begin{bmatrix} -(x^{(i)})^T \\ -(x^{(i2)})^T - \end{bmatrix}$ 

Le optimen 0 gives by

 $\theta = (x^T x)^{-1} x^T y$ 

idenc: Print (x/\*x) \*x/\* y

x1: transpise \*: methix mult

He note with normal equation, you DONT need feature scaling

V5

Gradient descent
Leneed to choose of
Le many Iteration.
Le work well even
If n i= large.

Normal equation

Heno need to chare d

Hens Iteration needed

LA(XTX) - takes o(n3)

H Slaw when a is longe (>10,00)

M # training example

# Normal equation / minvotability

Lithrat if XTX is non-involide?

ranse , binn, lustery of inn, (beengalurase)

Last gives you & though XTX is singular /or delete features. thoppen when there's reducted feature, or to many featre: mkn, then use regularization)

#### Vectorization

helps to compute vectors faster

## Assignment questions include:

L+ computing cost for multi-/uni variable detaset L+ computing cost for multiple variable

to gradient descent for multi/uni variables

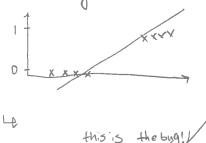
### Week 3

classification problem

LA yell Negative dass positive class.

Lanow binony class classification.

Does lin-reg mrk? no not a good idea.



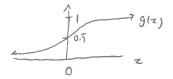
this is the byg! I mos up your linney data! o 4 So don't use lin reg for classification.

4 logistic regression: 0≤ ho(x) ≤1

this is a downloan algorithm

# logistic regression

g(z)= 1/1-2 //logistic/signid fuction



Le Interpretation: ho(x) gives you probability that our output is 1. = p(y=1 | x;0) in probability notation. = 1-P(y=01x;0)

(=7 p(y=1)x;0)+p(y=0|x;0)=1

Decision Boundary

decision benday is the line that spporate area when y=0, y=1 ( (ne whore holx)=0.5 exactry).)

non linear decision bendances, then you need more porches for higher dim. It there are als-

> -1+x1+x2 20 resultsin O boundary

legistic regression model

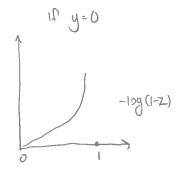
tin reg worlt give a convex, but we want a convex function

Cost (ho(x),y) = 
$$\begin{cases} -\log ho(x) & \text{if } y=1 \\ -\log cl - ho(x) & \text{if } y=0. \end{cases}$$



cost=0 if x=1 but as ho(x)=0, cost > 00.

intuition = if ho(x)=0, but you predict t as I, you're paralized.



similar as the other inhuition

this gives a conex 2 local optimum free function

note: y=1 ry=0 always. -7 (an combine two equotions

the compressed cost function is:

(05+ (ho(x),y)=-ylog(ho(x)) - (1-y)log(1-ho(x))

otal costJ: m (ost (he(x),y (i))

 $= \frac{-1}{m} \left[ \sum_{i=1}^{m} y^{(i)} \log \left( h_{\theta}(x^{(i)}) + (1-y^{(i)}) \log \left( l - h_{\theta}(x^{(i)}) \right) \right]$ Wand: MM J(\theta)

gradient dexent algoritim:

Repeat 
$$20j = 0j - \alpha \frac{\partial}{\partial 0j} J(0)$$

00

hepeat (0j:=0j- ox 1 (ho(x(i))-y(i))xj(i) y simultnessy update was same as lin.reg's grad, des, but! ho(x) refer to 1100x now.

### vectorized unpernentation

(38)  $h = g(x\theta)$  this computes quantity  $ho(x^{(i)})$   $J(\theta) = m \sum Ey^{(i)} = g(ho(x^{(i)})) + (1-y^{(i)}) = g(1-ho(x^{(i)}))$   $J(\theta) = m \cdot (-y^T + \log(h) - (1-y)^T + \log(1-h))$ 

# the grudient downt

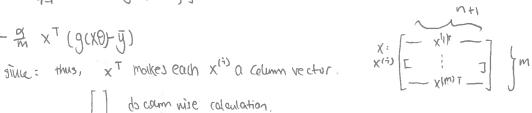
idea: rearrage the vectors With it's easy to type into Matlab. " 0:=0-am = [(ho(xi)-yi)-xi)7 collywestor

θ=θ-照 x<sup>T</sup> (g(Xθ)-ÿ)

do com wise calculation.

Dis a (In x I) vector.

XO returns xis) 0-1 returns corresponding whex.



DENXI VEC.

x=mxn X0= mx1.

XT: NXM

ons: hx1.

Advance Optimization

Advanced Optimization

Joseph function J(0), which mine J(0).

Two you can use the 12 functions

Given 0. If we can compute J(0), 20, J(0) than we can use the fielding algorithms

Le Conjugate gradient | footor, noneed for of, but not complex.

4 BFGS

50 We use the library

use Andron "faminuscl)"

Physin the 510) & the gradients sholl suffice

logistic optimization for multiple classes "ne us all donsification"

Multiclass dossification.

y=10,1,-- ny each are category.

Civign one days as positive, all other se, as "the rest"

yezo,1,1,-- n5

ho (N=P(y=0/x,0)

ho(1) (x) = P(y=1 | x; 0)

ho(") (x) = P(y=n(x;0) max ho(i)(x)

# Problem of over-fitting

under-fitting: hypothesis function maps to perry to the trend of data. Too simple I the little features Worfiting = not generalized enough. fits available dotestes well, but might have unhacesay angles/ Les too wigging come I.e. to viggry (tail to genorise):

to resolve overfitting.

1) reduce that features. (model selection algorithm to ditch less-importent features.)

2) regularization (reduce magnitude of 0;)

Cost function (the new one with regularization, big it bumps up and forces of to be small Mino In Zin (ho (x(i)) - y(i))2 + 7 Zin 0;2 because big 0; will be penalized

Gradient docent

Vepcat ? 
$$\theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^{m} (h_0(x^{(i)}) - y^{(i)}) x_0^{(i)}$$

$$\theta_j := \theta_j - \alpha \left[ \left( \frac{1}{m} \sum_{j=1}^{m} (h_0(x^{(i)}) - y^{(i)}) x_j^{(i)} \right) + \frac{\pi}{m} \theta_j \right] \quad j \in \{1,2,-n\}$$

always less than 1 as it treduce Dj each time by a little bit.

Normal equation

$$\theta = (X^T X + N \cdot L)^T X^T Y$$

Where L= [0]

[Mode if min, X7x is inamorative but adding L mates H invertible.

regularization solves not invertibility as well.

Regularced logistic regression (advened optimization works similarly)

regularized cost function for linear regression.

Chew term

$$J(\theta) = -\frac{1}{m} \sum_{i=1}^{m} \left[ y^{(i)} \log \left( ho(x^{(i)}) + (1 - y^{(i)}) \log \left( 1 - ho(x^{(i)}) \right) \right] + \sum_{i=1}^{m} \sum_{j=1}^{n} 0_j^2$$

Advance function (regularization)

Jual: same as provious.

gradient 1: (indexo)

In \( \sum\_{i=1}^{m} \left( \heta(\chi^{(i)}) - y^{(i)} \right) \chi\_0^{(z)} \)

gradient (2 ~ ntt) (ndex ((1), --n))

gradient (2~nH) Index ((1), --n))

( In many added from (ho(xi-1)-y(i)) x1(i) + (m 0)

watchaut following when doing assignment:

Letawent matries carefully to visualize the declarication.

Le motern matrix dimensions always.

# Week 4

### Newal Networks - representation

LA computer vision - example

Le 109 votic regression would have to many features. (like a femmilian : for mages) La minic the brain.

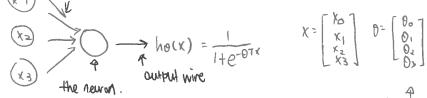
I lorge scale!

La neural-reviring experiment

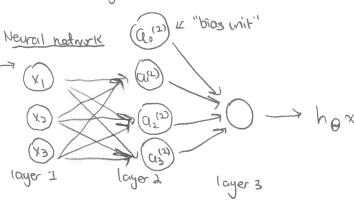
L+ Codynst / learn the docta

# Model representation

Hurar model: bogistic unit



$$X = \begin{bmatrix} x_0 \\ x_1 \\ x_2 \\ 0 \end{bmatrix} \quad \emptyset = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$



irput layer

hidden-layer awand layer

$$\int_{-\infty}^{\infty} Q_{i}(\dot{x}) = \frac{1}{2} \operatorname{activation}'' \text{ of and } \dot{x} \text{ in layer } \dot{y}$$

 $\begin{cases} Q_{i}^{(j)} = \text{``activation'' of ont is in layer'j} \\ Q_{i}^{(j)} = \text{matrix at weights controlling func mapping from layer j to j+1} \end{cases}$ 

## Vec representation

$$\begin{bmatrix} x_0 \\ y_1 \\ y_2 \\ y_3 \end{bmatrix} \rightarrow \begin{bmatrix} G_1^{(2)} \\ G_2^{(2)} \end{bmatrix} \rightarrow h_0(X)$$

vector representation "activation nodes" a remple

layer 1 to layer 2:

$$O_{3_{(5)}} = \partial \left( \theta_{(i)}^{30} \times^{0} + \theta_{(i)}^{31} \times^{1} + \theta_{(i)}^{37} \times^{5} + \theta_{(i)}^{39} \times^{9} \right)$$

$$O_{7_{(5)}} = \partial \left( \theta_{(i)}^{30} \times^{0} + \theta_{(i)}^{31} \times^{1} + \theta_{(i)}^{37} \times^{5} + \theta_{(i)}^{39} \times^{9} \right)$$

$$O_{3_{(5)}} = \partial \left( \theta_{(i)}^{30} \times^{0} + \theta_{(i)}^{31} \times^{1} + \theta_{(i)}^{37} \times^{5} + \theta_{(i)}^{39} \times^{9} \right)$$

 $|\alpha_{1}| = \frac{1}{2} \left( \frac{\partial_{1}}{\partial x} \left( \frac{\partial_{1}}{\partial x} \right) \left( \frac{\partial_{1}}{\partial x} \left( \frac{\partial_{1}}{\partial x} \right) + \frac{\partial_{1$ 

dn (8)

In each layer has its own matrix of weights

Le if network has Sy layers in level J. Syn layers in level J. Syn layers in level J+1, then  $\theta^{(j)}$  has dimension Syn  $\times$  (Sj+1)

Comes from bias node

Leloidout live this, b/c multiply 0, the rectur will be on the right.

Intuition: Neural network allows nodes in its hidden lays-to "learn' its own features.

# Vectorization of computation

refer here

$$\Box Q_{1}^{(2)} = g(Z_{1}^{(2)})
 \Box Q_{2}^{(2)} = g(Z_{2}^{(2)})
 \Box Q_{3}^{(2)} = g(Z_{3}^{(2)})$$

for layer j, radek, Zis
$$Z_{k}^{(j)} = \Theta_{k,0}^{(j-1)} x_{0} + \Theta_{k,1}^{(j-1)} x_{1} + \cdots + \Theta_{k,n}^{(i)} x_{n}$$

$$X = \begin{bmatrix} X_0 \\ X_1 \\ \vdots \\ X_n \end{bmatrix} \qquad Z^{(ij)} = \begin{bmatrix} Z_1^{(ij)} \\ Z_2^{(ij)} \\ \vdots \\ Z_n^{(ij)} \end{bmatrix}$$

$$Z^{(i_1)} = \Theta^{(i_2-1)} \alpha^{(i_2-1)}$$

nde: 
$$\dim(\Theta^{(\tilde{7}^{-1})})$$
 is  $S_{\tilde{7}} \times (n+1)$  dim $(\Omega^{(\tilde{7}^{-1})})$  is  $(n+1) \times 11$ .

adding the bias wit: to layer j after computing a (i) u. as'i'= 1.

to compute from hypothesis, compute z vector:

Z(it) = O(i) a(i) the last matrix O(i) has only I row, multipled by one column recalify so the result is a real number.

Multi-class Classification LAME-US- all method

holx) EIR 4 if throe are 4 claimes

hows[8] or [8] or [8]

with diffort INDUT X.

It returns one of the et's vector given a particular input

[Week 5] Gual: learn har to train neural networks

the wat function for the neural network

L+ L= total # of layers m the network

Le SI (#2) units not counting bias unit in layer 1)

Lt K= #x aut put wit / closses.

 $J(\Theta) = -\frac{1}{m} \sum_{i=1}^{m} \sum_{k=1}^{m} \left[ y_{k}^{(i)} \log \left( h_{\Theta} \left( x^{(i)} \right) \right)_{k} \right) + \left( 1 - y_{k}^{(i)} \right) \left( \log \left( 1 - h_{\Theta} \left( x^{(i)} \right) \right)_{k} \right) \right] + \frac{\lambda}{2m} \sum_{j=1}^{m} \frac{2^{j}}{j-1} \left( \Theta_{j,i}^{(i)} \right)^{2}$ 

Back propagation algorithm

Le goal is to compute min & J(0)

LA lost at portral derivative of J(B)

100 J(B)

the back propagation against works as follows:

Liginon training set  $l(x^{(1)}, y^{(1)}), \dots (x^{(m)}, y^{(m)})$  Lift Set  $\Delta_{i,j}^{(2)} := 0$   $\forall \forall i,j \in \mathbb{N}$ 

LA for training example &=1~M 1, set a(1):= x(2)

2. portron forward propagation to compute all, L=1,2,3,--- L (le set up & intempdiate, use giz) to colordoite next layer)

3, 8(L) = 01(L)-y(x)

Myate: } Dig(1) := m Aig(1) + N 8+17(1)) 189 to.

μ Δij(1) 1f j=0

D'15 "accumulator". 3 (10) = D. (1)

### Implementation datains

Lender to holes and video

LA No need to write code for hand-without neles.

reunolling = yeu can make / convert between matrix / rector repri of matrices

Legration checking: bug-free impl guarantee

Le use random to set initial thata

### Week 6

# Evaluating a learning algorithm

ways to arrive at better hypothesis

LA more examples

HP more / less # of features

Lamorelless valued 1.

70%. 30%

to evaluate a hypothesis, we split date into triving set & test set.

We to learn 0, minimier Jerain (8) using training set

Le compute test set error Jest (0)

computing test set error

La lin. reg. : Jtest (0) = 1 Mest (hackstert - ytest) 2

+ log, reg :

err (haix).y) = { | if (haix) > 0.5 && y=0) || (haix) = 0.5 && y=1)

Test error = 1 mtest cer (ha(x (+)), y test)

### Model Jelection

you can break down data set into three data sels:

trung set, cross validation set, test set

dea: test different degree of polynomial, evaluate error function

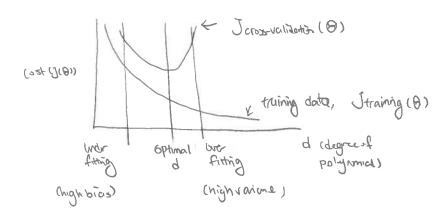
1, optimize porams in O using training set for each degree.

2, find the polynomial degree of that produce least error by cross validation /se.

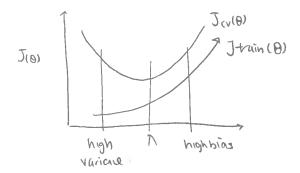
3. Estimate Generalized aron with Iteal (B(d)) using test set. (d:= deg victuming /se. (this way test set is NOT associated with the Poam training.

# Diagnosing bias us Variance.

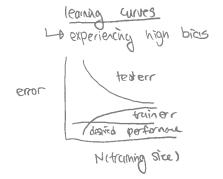
If you have bad predictor, you need to figure out whetherits high biois or variance.



### Regularization vs bias/Varione



we use similar algorithm for testing regularization tom n.



Lalow training selsite causes Jouin(0) low, Jev(0) high.
Lalorge training selsite causes both Joan(0), Jev(0) high
but also Jouin(0) & Jev(0)

Le getting more dotte won't help much.

test error

desired performance

train error

Hesterror

desired performance

Hexporning high variance

Latorge training set size: Itain(B) IDW, Jov (B) high
Latorge training set size: Itan(B) increase with set
Size, and Jov (B) continue to derrose without
plateaning. Itan (B) ( Jov (B), but difference
remains significant.

Lagetting more docter will likely to help

# Debugging learning algorithm.

problem.

try

high var

getme training data

high var

less features

high blas

get more features

high bias

odd paly features

high bids

descare 1

highvar

increase n.

Small neural network: computationally chearp

( Prone to underfitting)

large neural network: computationary expensive

(prone to overfitting, (use A (regularization) to fix)

## Building a spain clossifier

Hæsigning ML system. (building year own system)

LA identify features (X) and classifyer (y)

LA Ways to spand mre time

LA collect lots of donter

LA more sophisticated features

Le algoritms to process input data.

### Error analysis

Leimpenest a quick implementation

It use it to decide how to Spend your time

Le plat learning curves, and decide what to do.

Le manually exornine errors, analyse

Le implement a metric that returns performance on different changelideas.

#### Skewed classes

It case when one class has very large size, another very little size.

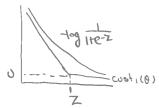
It different error metric 7 use to t, true & false t, false - to classify (precision / recall) Precision: true + / pred + , \* Recall true + / actual +

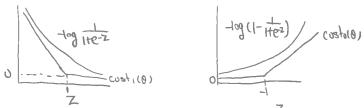
con change ho(x) threshold, which tade off precision / recoul precision netal: f. score: PR/(ptR)

#### Week 7

Support vector machine (SVM)

Ly wing cost (1), costor similarto has but easier computation wise





minimizing o gives by: optimization projective:

Lelorge margin dassifyer.

LACULONS a decision boundary that stays naturally for aport from destased. 40 the pertodicular vector is dosent to exemples



#### Kernels

label landmark (defining facture) then use distance measure 
$$f_i = \exp\left(-\frac{||x||^2}{29^2}\right)$$
 if  $||x|| \leq \frac{small}{1 \times 9^6}$  fixe

tearn my linear decisies beendary

details (over with kernels)

given x, compute features fe IR mail predict "y=1" if 0" f≥0 training using fail's strillouty metric instead. Min C = yilkost, (O'fi) + (1-yil) (35+0 (O'f(")) + \$ = 0; note that since Cot, large Co lumbias, highvar (le small n) Small (> highbias, low var (le large T) large 82 7 features fin, vary smoth, high bias, low var Snowly > Leatures Phil vary less smooth, low bias, high yar Man Jop 13 to choose c and Q5 using an SVM Ly nive software libraries: liblimar, libsum. Lyneed to chause: Kernel Lusear nouse, and parameter C Himer Konel (no Kenel) LA Floursian Kornel 6 secens ut bosn & Leneed to do featire scaling Lefor other choices of Kernel, it must satisfy Mercer's theorem so It for sure do hot diverge -A putticlassification 4 builtin SUM Package LA one- 45-all Hogistic regression us SVM. which to choose? M= # features

N= # training example. SVH-7 covex function > reduct global aptima 17 1/2 n large relative to m ( nr7m, nx10,000 mx10~1000) LI use L. R. or sivin Willinear Kenel. LA IP n Small, mintemediate (n=1~1000, M=10~1000) H use gVM WI Growsian kernel L+ 12n Small mlarge ( 12/1/01), n=50,000+) lin Kernel H add more feature, then use LA or SVH with

14 nn works well with these settings, but is slower to train.

#### Week 81

### unsuperised learning

4 given input has no labels

LA algorithm firds clustering data 1 structure (as example of manpoised learning algorithm Le used for identifying market segmentation, social network analysis, organize computer clusters. galaxy formation / Ostrononical data analysis

### K-means algorithm

Let for clustering

Let Step I: Initial cluster catroids tendomly

Step 2: Norm loop each point to centroid that's closer to it (assign ct, to index of closest cluster controid)

Keep on a step 3: More the centroids, to new mean of ossigned points. Mean = MK

Herating a step 3: more the centroids, to new mean of ossigned points.

LA IMPUT: K(# of clusters) toing set {x', ... xm'} xi EIR"

Lads with for non-separated consters.

it can still separate and clusters, although may not seem like a obvious separation

### Optimization objective

c (i) = index of cluster (INK) that x (i) is currently ossigned to MK = cluster centraid K (UKEIRK) Mc(i) = cluster (extrains of cluster that x(i) is assigned to.

objective  $J(C^{(1)}, -C^{(m)}, M_1, -M_K) = \frac{1}{m} \sum_{i=1}^{m} ||x^{(i)} - M_C^{(i)}||^2$   $C^{(1)}, -C^{(m)}, J(C^{(1)}, -C^{(m)}, M_1, -M_K)$ 

hate that I does not increase ! as a fine of iteration.

### rondom initialize clustering lentroll

steps: Lasel KKM

Hrandonly choose K training examples

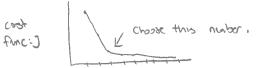
1-1 k-neers may not always end at global sptima.

H set My ... Mk to these exemples.

Havid bad clustering, can initialize many times! compute I each time & pick are that gives when having small # of cluster, multiple/

### Ack # of clustors

LA Charang # of clusters "elban method"



# clisters.

Le But ofte, the 'elbon does not appear.

Ht donitexpect It to work.

Hobertoway: pick K from "what you want to do with result of the learning" LARIE. how many groups you want? for what purpose are you running this algorithm

## Data comprosion & dimestrating reduction

Hexample: 20-10

Historial Leginday godes

Harepresent doutepoints in a line by the line (20-10) and project each point to the ine

for each hi, XiER 72-EIR

example: 30 space roughly on plane or lie on plane

you ca generally reduce from high tolow dimersion given that data roughly lie on like-dimensions

# <u>Visualitation</u> + dimensionally reduction.

their with data usualization that was very complex

Le houng parish smaller direction to corpture into in more impertent feature in data

GOP Per person .... exemple: country's conmy

Husually reduce to 20 or 3.0 so it's easy to visualize.

## PCA(Principle component analysis)

Lagoral = Fire surface of lower dimension that has smallest own of districe (from actual Pt to projection error)

Le hate: PCA is NOT linear regression.

A is NOT linear regression.

lin reg minimize vertical distance (predict y)

pca minimize perpendicular distance (nothing to do with y)

### PCA algorithm

replace each xj(i) with xj-lij

also Scale the features

LA then, we need to compute the vector ui, and the projections, new representations.

Reduce data from dim n to dimk.

covariance moting: 
$$\Sigma = \frac{1}{m} \sum_{i=1}^{n} (x^{(i)})(x^{(i)})^T$$
 when moting

U will be a nxn mostrix whose columns ore u', us, -- um

LACHONGE XCIR"> ZEIRK

# retorstruction from compressed representation

## Applying PCA

chasing K (# of principle components)

LA avarage squar projection error = 
$$\frac{1}{m} \sum_{i=1}^{m} ||x^{(i)}| - x_{approx}||^2$$

Let total review in data 
$$=\frac{1}{m}\sum_{i=1}^{m}\|x^{(i)}\|^2$$
 choose K to be smallest value, s.t.

# algorithm

[UISIV] = Sid(sigma) sis adiagnal matrix

Pick smallest K s.t.

(0.00 varione retained).

# we PCA to speed up learning algorithm

when runnling PCA, only I'm it on the training set.

to speed up:

input: {(x1,y1), (x2,y2), --- (xm,ym)}

extracted input: x1, x2, ... xm ER (0000

z', z ?, -- zm e R 1000

than train ((z'y'), -- (zmym)) by ho(z)

# Summary of Application of PCA

He combussion

Leredue storage to store data J choose K by % variane

HUSuchization

HK=2 or K=3

LINOTE: DON'T use PCA to prevent wantithing. Letts abad way of using PCA

House regularization instead.

Lenote: when designing system

Lefist try without PCA.

Harry of 14 does not work, Utilize PCA

Helf you need to sove storage space or time.

#### Week 9

# Anonaly detection

Ladeted abnormally behaving doute

Huse Gaussian distribution (probability distribution)

Le Donsity estimation

Lytraining set =  $1 \times 1, \times^2, -- \times^m y$  each traing  $X \in \mathbb{R}^n$ 

Annaly detection algorithm

It I, choose features Xi that you think might be aromaly.

~ 2, fit params Wi, --- Mn, Θ², -- ση², => Mj= m ∑ xj(i) Θj=m∑ (xj(i)-uj)²

Le 3, given new example x, computerix)

 $P(x) = \prod_{j=1}^{n} p(x_j) u_j(\theta_j^2)$ P(x) L &

#### defection system & evaluating an armaly

training set, cross varidation set, and test set. Lause the

Le algorith evaluation:

fit model PIXI on test set x' .- xm

con CV/test example)

predict:

(comal)

Lecon use or set to chose &

4 Use precision recall 8 Fi-score

When to use annuly detection, when to use superused learning?

OA

Le very small # of positive Glowblez= (A=1) (2050) large number of negative

Cramples.

He may types of annaly ( difficult for learning)

4 possible chomoly in future that we've now seen.

SL

Le large # of positive Inegative examples

Le future anomaly look like previous ones.

LA enough positive examples for the algorith to Learn.

Le Multivanate Gaussian distribution con detect abromal relationship between features. Leits more computationally expassive. Lemust have mon or else Z is sugular.

### Recommader systems

Hegive recommendation to subscribers to a sorber His a high priority to many companies. Lexemple- predicting movies Lemantes:

> Le & Corter bused resurchation both or included in videos. Comprenetation)

Collaborative fitting algorithm

(initialize X', - Xnn, 0', - 0 hu EIRn to small values.

2, minimize  $J(x', -x^{nm}, \theta', -\theta^{nn})$  using gradient dexast or other advanced optimization algoritm, lie

$$\chi_{\vec{k}}^{\vec{i}} = \chi_{\vec{k}}^{\vec{i}} - \alpha \left( \sum_{\vec{j} \in r(\vec{i}, j) = 1} ((g^{(j)})^{T} \chi^{(i)}) - y^{(ij)} \right) \theta_{\vec{k}}^{(i)} + \Lambda \chi_{\vec{k}}^{(i)}$$

$$\theta_{\vec{k}}^{\vec{i}} = \theta_{\vec{k}}^{\vec{i}} - \alpha \left( \sum_{\vec{i} = r(\vec{i}, j) = 1} ((\theta^{(i)})^{T} \chi^{(i)}) - y^{(ij)} \chi_{\vec{k}}^{(i)} + \Lambda \chi_{\vec{k}}^{(i)} \right)$$

3. For a user with parameters of and a movie with clearned) features x, predict a star rating of otx.

restorced implementation is in videos.

"Now reak moths factorization"

Use mean rumalization to predict entres with no previous dates

# Week 10

Note

More deda, the better algorithm it is.

Stochastic gradient descent

14 updating data as duta come along.

But in gradient descent VS.  $h_{\theta}(x) = \sum_{k=0}^{n} f_{j}^{k} X_{j}^{n}$   $J_{f}(h_{\theta}(x^{i}) - y^{i})^{2}$ 

Repeat \( \text{\$g:=0g-\$at \$\frac{m}{2}\$ (ho(x\frac{1}{2})-y\frac{1}{2})xy^\frac{1}{2}\$ for every \$\hat{g}=0,\dots M\$

Stochastic gradient dexent cost (0, xi, yi) = 1/2 (0st (0, (xi, yi))) a

Train(0)= 1/2 22 (0st (0, (xi, yi)))

O randomly Shuffle set

(a) repeat  $\xi$ for i = 0, ...  $m \in 0$ for j = 0, ...  $n \in 0$ for j = 0, ...  $n \in 0$ 

### Mini-batch gradient descent

Laborith good des. Use all m examples each Hoation.

18 sto chastic grad des. Use 1 example each time (Iteration)

He mini batch grad-des use <u>b</u> examples each iteration

## Checking for convergence

4 check frend/convergence over time.

# large scale machine learning

Mapredue & dota parallelism.

Map reduce is to split batch gradient descent over different computers for computation. then the control machine combines the result.

#### Week II

Example: photo OCR problem.

He design a <u>pipeline</u> that goes through multiple step of machine learning algorithm.

Goething lats of data, Artificial data analysis.

Hadistart the deuter to generate more text examples

Lethus more douter and better ML algorithm.

Cieling analysis

Let for each process in the pipeline, take its maximum performance and see how it improves the algorithm. Then componed use improve the process by their priorities.