

POPULATION GENETICS ANSWERS

Natural selection

Problem 4

A1A1	A1A2	A2A2	s	h	Favored allele
1	1	0.75	0.25	0	A1
1	0.6	0.6	0.4	1	A2
0.4	0.8	1	0.6	0.33	A2
0.8	1	0.55	$s_1 = 0.2$ $s_2 = 0.45$	Not applicable	A1 and A2

Problem 5

Relative fitness values: $w_{TT} = 1$, $w_{Tt} = 0.8717$, $w_{tt} = 0.1585$

Initial generation

Allele frequencies in newborns: $\text{Freq}(T) = p = 0.7667$, $\text{Freq}(t) = q = 0.2333$

Allele frequencies in adults: $\text{Freq}(T) = p = 0.8214$, $\text{Freq}(t) = q = 0.1786$

Next generation

Genotype frequencies in newborns:

$\text{Freq}(TT) = 0.6747$

$\text{Freq}(Tt) = 0.2934$

$\text{Freq}(tt) = 0.0319$

Genotype frequencies in adults:

$\text{Freq}(TT) = 0.7213$

$\text{Freq}(Tt) = 0.2733$

$\text{Freq}(tt) = 0.0054$

Problem 6

Situation	w		p		Equilibrium		
	Population 1	Population 2	Population 1	Population 2	p	q	Faster
Favored dominant allele	Same in both		$p = 0.8$	$p = 0.1$	1	0	Population 1
Favored dominant allele	$w_{aa} = 0.8$	$w_{aa} = 0.2$	Same in both		1	0	Population 2
Favored recessive allele	Same in both		$p = 0.8$	$p = 0.2$	0	1	Population 2
Favored recessive allele	$w_{AA} = 0.7$	$w_{AA} = 0.2$	Same in both		0	1	Population 2

Problem 7

Fitness values: $w_{A1A1} = 1$, $w_{A1A2} = 0.6$, $w_{A2A2} = 0.2$

Allele frequencies in next generation

Zygotes: $\text{Freq}(A1) = p = 0.4$, $\text{Freq}(A2) = q = 0.6$

Adults: $\text{Freq}(A1) = p = 0.5846$, $\text{Freq}(A2) = q = 0.4154$

Problem 8

Type of selection

Without warfarin: Directional selection favoring allele S

With warfarin: Heterozygote superiority

Allele frequencies in next generation adults

Without warfarin: $\text{Freq}(S) = p = 0.8435$, $\text{Freq}(R) = q = 0.1565$

With warfarin: $\text{Freq}(S) = p = 0.7730$, $\text{Freq}(R) = q = 0.2270$

Allele frequencies at equilibrium

Without warfarin: $\text{Freq}(S) = p = 1$, $\text{Freq}(R) = q = 0$

With warfarin: $\text{Freq}(S) = p = 0.6632$, $\text{Freq}(R) = q = 0.3368$

Problem 9

Current situation

$\text{Freq}(\text{PKU}) = q_{\text{eq}} = 0.00447$

Proportion of affected individuals at equilibrium = 0.00002 (1/50,000 individuals)

Increased fitness of affected individuals

$\text{Freq}(\text{PKU}) = q_{\text{eq}} = 0.00707$

Proportion of affected individuals at equilibrium = 0.00005 (1/20,000 individuals)

The frequency of PKU-causing alleles increases in the population when the fitness of the affected individuals increases because fewer alleles are being eliminated from the population by natural selection and mutation rate is still the same.

Problem 10

Totally recessive $\mu = 0.0003$

Partially dominant $\mu = 0.003464$

Natural selection is more efficient eliminating mutations that are partially dominant compared to recessive mutations, so a higher mutation rate is needed to maintain the observed frequency of blind mice in the situation where the disease is partially dominant (heterozygotes have lower fitness than homozygotes for the wild-type allele). The mutation rate is higher because more mutant alleles need to be created to compensate that a higher proportion are being eliminated by selection.