Practical 7 - Stochastic simulations

Jan Izquierdo Ramos, Carmen Samedi Gamboa November 2024

Name: Jan Izquierdo, Carmen Samedi

SYSTEMS AND NETWORK BIOLOGY - PRACTICAL 6

Stochastic description of protein expression

To submit your report, answer the questions below and save the *notebook* clicking on File > Download as > iPython Notebook in the menu at the top of the page. Rename the notebook file to ''practicalN_name1_name2.ipynb'', where N is the number of the practical, and name1 and name2 are the first surnames of the two team members (only one name if the report is sent individually). Finally, submit the resulting file through the *Aul@-ESCI*.

Remember to label the axes in all the plots.

IMPORTANT REMINDER: Before the final submission, remember to **reset the kernel** and re-run the whole notebook again to check that it works.

Here we implement a stochastic description of simple protein expression processes, using a stochastic simulation algorithm know as the *next-reaction method*. We will consider a biochemical process constituted by M reactions, denoted by $\mu = 1, 2, ..., M$, and N biomolecular species, denoted by i = 1, 2, ..., N.

Let the rate of reaction μ be k_{μ} , and their corresponding reactants $x_{i}^{(\mu)}$. The probability that this reaction occurs in the interval (t, t + dt) given the state of the system at time t is given by $a_{\mu}dt$, where a_{μ} is the *propensity* of the reaction. Following the law of mass action, and assuming that only one molecule of each reactant species is involved, the propensity of reaction μ has the form:

$$a_{\mu} = k_{\mu} \prod_{i=1}^{N} x_i^{(\mu)}$$

Another important piece of information that characterizes the reactions is the *stoichiometry matrix* $S_{\mu,i}$. The columns of this matrix are the reactions and the rows are the biomolecular species. The elements of the matrix represent how each reaction affect each species (e.g. a species that loses one molecule in a reaction has a value -1 in the corresponding matrix location, while if the reaction produces two molecules of a species, the corresponding matrix element is 2). Once the propensities and

the stoichimetry matrix are known, the steps of the next-reaction stochastic simulation algorithm are:

- 1. Initialize the system (number of molecules and time)
- 2. Calculate the propensities of all reactions
- 3. Calculate the time τ at which the next reaction happens, using the expression:

$$\tau = \frac{1}{a_{tot}} \ln \frac{1}{z_1}$$

where $a_{tot} = \sum_{\nu=1}^{M} a_{\nu}$ and z_1 is a random number uniformly distributed between 0 and 1.

4. Determine the reaction that occurs at time τ by calculating the smallest integer λ such that

$$\sum_{\nu=1}^{\lambda} a_{\nu} > z_2 \sum_{\nu=1}^{M} a_{\nu}$$

where z_2 is another random number uniformly distributed between 0 and 1.

- 5. Update the molecule numbers according to the stoichimetry coefficients $S_{\mu,i}$.
- 6. Go to step 2 to compute the next reaction.

Let us implement this algorithm for a simple birth-death process representing protein expression and degradation:

$$\emptyset \stackrel{k_{exp}}{\to} A, \quad A \stackrel{k_{deg}}{\to} \emptyset$$

First, we load all necessary Python packages.

```
[21]: import numpy as np import matplotlib.pyplot as plt from scipy.stats import poisson, norm
```

Next, we define the values of the parameters, the stoichimetry matrix and the initial conditions (step 1 above). We consider first that $k_{exp} = 100$ and $k_{deg} = 1$.

```
[22]: k_exp=100
k_deg=1

c_time=0 #current time
tmax=200
mt=0.1
num_molec=0 #At t0 we have 0 A molecules
```

Now we compute the propensities (step 2 above), calculate the next reaction time (step 3), and determine the reaction that takes place (step 4). For steps 3 and 4 use the function uniform from the module numpy.random.

```
[23]: #Step2: Propensities for producing and degrading A def calculate_prop(n_mol, k_exp, k_deg):
```

```
a_exp=k_exp #Propensity for producing A (reaction expresed)
a_deg=k_deg*n_mol #Prop for degradating A
return a_exp, a_deg

#Step3: Calc next reaction time

def next_Rtime(a_tot):
    z=np.random.uniform(0,1)
    t=(1/a_tot)*np.log(1/z) #a_tot=a_exp+a_deg
    return t

#Step4: Reaction to take place

def Rdecide(a_exp, a_tot):
    z2=np.random.uniform(0,1)

if a_exp > z2*a_tot:
    return 1 #expression
return 0 #degradation
```

Finally, we update the molecule numbers and the time variable (step 5 above).

```
[24]: def update_molec(reaction, n_molec):
    if reaction==1: #expression
        n_molec+=1 #more molec
    elif reaction==0 and n_molec>0: #degradation, but n_molec cant be negative
        n_molec-=1
    return n_molec
```

Now put together steps 2-5 above in a loop, and generate output every mt time units (you might need to save the same state of the system for multiple output times, if no reaction happens in a given mt interval). Run the simulation for 200 time units with sampling period mt = 0.1.

```
[25]: c_time=0 #current time
tmax=200
mt=0.1

timeList=[]
n_molec=[]
while c_time < tmax:
    timeList.append(c_time)
    n_molec.append(num_molec)
    a_exp, a_deg=calculate_prop(num_molec, k_exp, k_deg)
    a_tot=a_exp+a_deg

#add break in case of emergency</pre>
```

```
if a_tot==0:
    break

Rtime=next_Rtime(a_tot)
#add R time to time, so steps in range are irregular, they depend on
→previous reation
    c_time+=Rtime

R=Rdecide(a_exp, a_tot)
    num_molec=update_molec(R, num_molec)

print(n_molec)
```

```
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 13, 14, 15, 14, 15, 16, 17,
16, 17, 18, 19, 20, 21, 20, 21, 20, 21, 22, 23, 24, 25, 26, 25, 26, 25, 26, 27,
28, 29, 28, 29, 30, 31, 32, 31, 32, 31, 32, 33, 34, 33, 34, 35, 36, 37, 38, 39,
40, 41, 42, 43, 42, 43, 44, 45, 46, 45, 46, 47, 48, 49, 48, 49, 48, 49, 50, 49,
50, 51, 50, 49, 48, 49, 48, 47, 48, 49, 50, 49, 50, 51, 52, 51, 52, 53, 54, 55,
54, 55, 56, 57, 56, 57, 58, 59, 58, 57, 58, 59, 58, 59, 60, 61, 60, 61, 62, 63,
64, 63, 64, 65, 64, 65, 66, 67, 66, 65, 64, 63, 62, 63, 64, 65, 64, 63, 62, 63,
64, 65, 66, 65, 66, 67, 68, 69, 70, 69, 68, 69, 70, 71, 72, 71, 72, 73, 72, 73,
74, 73, 74, 73, 74, 73, 74, 73, 72, 71, 72, 71, 70, 71, 70, 71, 72, 71, 70, 71,
72, 73, 74, 73, 72, 73, 72, 71, 72, 73, 74, 75, 76, 75, 74, 73, 74, 73, 74, 75,
76, 75, 76, 77, 78, 77, 78, 77, 76, 77, 76, 77, 78, 79, 78, 77, 78, 79, 78, 77,
76, 77, 78, 77, 78, 77, 76, 75, 76, 77, 78, 77, 78, 79, 80, 79, 78, 77, 76, 77,
78, 77, 78, 79, 80, 79, 80, 81, 82, 81, 80, 79, 80, 81, 82, 83, 84, 85, 84, 85,
86, 85, 84, 85, 86, 87, 86, 85, 86, 85, 86, 87, 86, 85, 86, 87, 86, 87, 86, 85,
84, 85, 84, 83, 84, 83, 84, 85, 84, 85, 86, 87, 86, 87, 88, 87, 86, 87, 88, 89,
88, 87, 88, 89, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 96, 95, 96, 95, 94, 93,
92, 91, 92, 93, 92, 93, 92, 93, 92, 91, 90, 91, 92, 93, 92, 91, 90, 91, 90, 91,
92, 93, 92, 93, 92, 91, 90, 89, 88, 89, 88, 89, 88, 89, 90, 91, 90, 91, 90, 89,
90, 91, 90, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 97, 96, 97, 98, 99, 98, 99,
98, 99, 100, 99, 98, 97, 96, 97, 96, 97, 98, 97, 98, 99, 100, 101, 102, 101,
100, 99, 98, 99, 98, 97, 98, 97, 98, 97, 98, 99, 98, 97, 98, 99, 100, 101, 100,
101, 102, 101, 100, 101, 102, 103, 102, 101, 100, 101, 102, 103, 102, 103, 104,
103, 102, 101, 100, 99, 100, 101, 102, 101, 100, 101, 100, 99, 98, 99, 100, 101,
102, 103, 102, 101, 102, 101, 100, 99, 100, 101, 100, 99, 98, 99, 100, 99, 98,
99, 100, 99, 100, 99, 100, 99, 100, 99, 98, 99, 98, 97, 98, 97, 96, 95, 96, 97,
98, 99, 98, 97, 96, 95, 96, 97, 96, 97, 98, 99, 98, 97, 98, 99, 100, 99, 100,
101, 100, 99, 100, 99, 100, 99, 98, 99, 100, 99, 100, 99, 98, 99, 100, 99, 100,
99, 100, 99, 98, 97, 98, 99, 98, 97, 98, 99, 100, 99, 98, 99, 100, 101, 102,
101, 102, 101, 100, 101, 100, 99, 100, 99, 100, 99, 98, 97, 96, 95, 94, 95, 94,
93, 94, 95, 94, 95, 96, 95, 96, 97, 98, 97, 98, 99, 100, 101, 100, 101, 102,
101, 102, 101, 102, 103, 102, 103, 102, 101, 100, 101, 100, 101, 100, 99, 98,
99, 100, 101, 102, 103, 102, 101, 100, 99, 100, 101, 100, 101, 100, 101, 100,
101, 102, 103, 104, 103, 104, 103, 104, 105, 106, 107, 106, 107, 106, 107, 106,
105, 104, 105, 104, 103, 102, 103, 102, 103, 102, 101, 102, 101, 102, 103, 104,
```

105, 104, 105, 106, 107, 106, 107, 108, 107, 108, 109, 108, 107, 106, 105, 104, 103, 102, 103, 102, 101, 102, 101, 100, 99, 100, 99, 98, 99, 98, 97, 98, 99, 100, 101, 102, 101, 102, 101, 100, 101, 100, 101, 100, 99, 100, 99, 98, 99, 98 97, 96, 95, 94, 93, 92, 93, 92, 91, 92, 91, 90, 91, 92, 91, 90, 89, 90, 91, 92, 93, 94, 95, 96, 97, 96, 97, 98, 99, 100, 99, 100, 99, 98, 97, 98, 99, 100, 101, 100, 101, 102, 101, 102, 101, 100, 99, 100, 101, 102, 101, 102, 103, 102, 103, 104, 103, 102, 101, 100, 101, 102, 101, 102, 101, 100, 101, 102, 101, 100, 101, 102, 101, 100, 99, 100, 99, 98, 97, 96, 97, 98, 97, 98, 99, 98, 97, 96, 97, 96, 95, 96, 95, 94, 95, 94, 95, 96, 97, 98, 99, 100, 101, 100, 99, 100, 101, 100, 99, 98, 97, 96, 95, 96, 95, 96, 95, 96, 97, 98, 97, 98, 99, 98, 97, 96, 95, 96, 95, 96, 97, 96, 97, 96, 95, 94, 95, 96, 95, 96, 95, 96, 97, 96, 97, 98, 99, 100, 99, 100, 99, 98, 97, 96, 97, 98, 97, 96, 95, 96, 97, 96, 97, 98, 97, 98, 97, 98, 97, 96, 97, 98, 99, 98, 97, 96, 97, 98, 99, 100, 99, 100, 99, 98, 99, 98, 97, 98, 99, 98, 97, 96, 97, 96, 95, 96, 95, 96, 95, 96, 95, 94, 95, 94, 93, 94, 95, 94, 95, 96, 97, 98, 97, 96, 97, 96, 97, 96, 97, 96, 97, 98, 99, 98, 97, 98, 99, 98, 99, 98, 99, 98, 99, 100, 99, 98, 97, 96, 95, 96, 95, 96, 95, 96, 97, 98, 97, 98, 99, 100, 99, 98, 99, 98, 99, 98, 99, 100, 99, 100, 101, 100, 101, 102, 103, 102, 101, 102, 101, 100, 101, 100, 99, 100, 99, 100, 101, 100, 99, 100, 101, 102, 103, 104, 103, 102, 101, 100, 101, 100, 99, 100, 99, 100, 99, 100, 101, 100, 101, 100, 101, 102, 101, 102, 101, 100, 99, 100, 101, 102, 103, 102, 103, 104, 103, 104, 103, 104, 103, 104, 105, 104, 103, 104, 105, 104, 103, 102, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 109, 110, 109, 110, 109, 110, 109, 110, 111, 110, 109, 110, 109, 110, 109, 108, 107, 106, 105, 104, 103, 102, 103, 104, 103, 102, 101, 100, 99, 98, 99, 100, 101, 102, 101, 102, 103, 102, 101, 102, 103, 104, 103, 102, 101, 102, 101, 100, 101, 100, 99, 100, 101, 100, 101, 102, 101, 100, 101, 100, 101, 100, 101, 102, 101, 102, 103, 104, 103, 104, 103, 102, 101, 100, 101, 102, 103, 102, 103, 102, 101, 102, 103, 104, 105, 104, 103, 102, 101, 100, 99, 100, 101, 100, 99, 98, 99, 100, 101, 102, 101, 102, 101, 100, 99, 100, 99, 100, 99, 100, 101, 100, 99, 100, 101, 100, 101, 100, 101, 100, 99, 98, 99, 98, 97, 96, 97, 96, 97, 96, 95, 96, 97, 96, 95, 96, 97, 98, 97, 98, 97, 98, 99, 100, 99, 98, 99, 98, 99, 100, 101, 102, 103, 102, 101, 100, 99, 100, 99 100, 99, 98, 99, 100, 101, 100, 99, 100, 101, 100, 101, 100, 99, 100, 101, 102, 103, 104, 105, 106, 105, 104, 105, 104, 103, 104, 105, 104, 103, 104, 105, 106, 105, 104, 103, 102, 101, 100, 101, 100, 99, 100, 101, 102, 101, 102, 103, 104, 105, 104, 103, 102, 103, 102, 103, 102, 103, 102, 103, 102, 103, 104, 105, 104, 105, 104, 105, 104, 105, 106, 105, 106, 105, 106, 105, 104, 103, 104, 103, 104, 105, 104, 105, 106, 105, 104, 105, 106, 107, 106, 107, 106, 105, 104, 103, 102, 103, 102, 101, 100, 99, 98, 99, 100, 101, 102, 103, 102, 103, 102, 101, 100, 99 98, 97, 96, 95, 96, 95, 94, 95, 94, 95, 94, 93, 94, 95, 96, 97, 98, 97, 96, 97, 98, 99, 100, 99, 98, 99, 98, 99, 100, 99, 98, 97, 98, 97, 96, 97, 98, 97, 98, 97, 96, 97, 98, 97, 98, 99, 100, 101, 102, 103, 104, 103, 102, 101, 102, 101, 100, 101, 102, 103, 102, 101, 100, 101, 100, 99, 100, 101, 100, 101, 102, 103, 102, 103, 102, 103, 102, 103, 104, 103, 102, 103, 104, 105, 106, 105, 104, 103, 104, 103, 104, 103, 102, 101, 102, 103, 102, 101, 100, 99, 98, 99, 100, 101, 102, 103, 102, 101, 100, 101, 102, 103, 104, 105, 104, 103, 104, 103, 104, 105 104, 105, 104, 105, 104, 105, 104, 103, 102, 101, 102, 101, 100, 99, 100, 101, 102, 103, 102, 101, 100, 99, 100, 99, 98, 97, 96, 95, 94, 95, 94, 95, 96, 97, 96, 95, 94, 93, 92, 91, 90, 91, 92, 93, 94, 95, 96, 97, 96, 95, 94, 93, 92, 93,

```
92, 91, 92, 93, 94, 95, 96, 97, 96, 95, 94, 93, 94, 95, 96, 95, 94, 93, 92, 91,
90, 89, 90, 91, 92, 93, 92, 91, 90, 89, 88, 89, 90, 91, 90, 91, 90, 89, 88, 87,
86, 85, 86, 87, 88, 87, 88, 89, 88, 89, 90, 91, 92, 93, 92, 93, 92, 93, 94, 95,
96, 97, 96, 97, 98, 99, 100, 101, 102, 103, 102, 101, 102, 101, 102, 101, 102,
101, 100, 99, 98, 99, 98, 99, 100, 101, 100, 101, 100, 99, 100, 99, 100, 99,
100, 99, 100, 101, 102, 103, 104, 105, 106, 107, 106, 107, 108, 107, 106, 107,
108, 109, 108, 109, 110, 111, 112, 113, 114, 115, 116, 115, 114, 113, 112, 113,
112, 111, 112, 111, 110, 111, 112, 113, 112, 111, 112, 113, 114, 113, 114, 115,
114, 115, 114, 115, 114, 115, 116, 117, 118, 119, 120, 119, 118, 117, 116, 115,
116, 117, 118, 117, 116, 117, 118, 119, 118, 117, 116, 115, 114, 113, 112, 111,
110, 109, 108, 109, 108, 109, 108, 107, 106, 105, 106, 105, 104, 103, 102, 103,
102, 103, 102, 101, 100, 99, 98, 99, 98, 97, 96, 97, 98, 97, 96, 97, 98, 97, 96
97, 96, 95, 96, 95, 94, 95, 94, 93, 92, 93, 92, 91, 90, 91, 90, 91, 90, 89, 90
89, 90, 89, 88, 87, 86, 87, 86, 85, 84, 85, 84, 85, 86, 87, 86, 87, 88, 89, 88,
89, 88, 87, 88, 89, 90, 91, 90, 89, 90, 91, 90, 91, 92, 93, 94, 95, 96, 95, 94,
93, 92, 93, 92, 91, 92, 91, 92, 93, 94, 95, 94, 93, 92, 91, 90, 91, 92, 91, 92,
91, 92, 91, 92, 93, 94, 93, 92, 93, 92, 91, 90, 89, 90, 91, 92, 91, 90, 91, 90,
91, 90, 91, 92, 91, 92, 91, 90, 89, 88, 87, 88, 89, 90, 91, 92, 91, 90, 89, 90,
89, 90, 91, 90, 89, 90, 91, 90, 89, 88, 89, 90, 89, 90, 89, 88, 89, 90, 91, 92,
93, 92, 93, 92, 91, 92, 93, 92, 91, 90, 89, 88, 89, 88, 87, 86, 85, 84, 85, 86
87, 88, 87, 88, 87, 86, 87, 86, 85, 86, 85, 84, 83, 84, 85, 84, 83, 84, 83, 82,
83, 82, 83, 82, 81, 82, 81, 82, 81, 82, 83, 84, 85, 84, 83, 82, 81, 80, 79, 78,
79, 80, 79, 78, 77, 76, 77, 76, 77, 76, 75, 76, 77, 76, 77, 78, 79, 78, 79, 78,
77, 76, 77, 78, 79, 80, 81, 82, 81, 82, 81, 82, 83, 82, 83, 82, 83, 82, 83, 84,
83, 82, 81, 82, 83, 84, 83, 84, 85, 86, 87, 86, 85, 84, 85, 86, 87, 86, 85, 84,
83, 84, 83, 82, 83, 82, 83, 82, 83, 82, 81, 80, 79, 80, 79, 80, 81, 80, 79, 78,
77, 78, 79, 80, 79, 80, 81, 80, 81, 82, 83, 82, 83, 84, 83, 84, 83, 82, 83, 84
83, 84, 85, 84, 85, 84, 85, 84, 85, 86, 85, 86, 85, 84, 85, 84, 85, 86, 85, 86
87, 86, 87, 88, 87, 88, 87, 86, 85, 84, 83, 82, 81, 80, 79, 78, 79, 78, 79, 78,
79, 80, 79, 80, 81, 80, 81, 80, 79, 78, 79, 78, 79, 78, 79, 78, 77, 78, 77, 78
77, 76, 77, 78, 77, 78, 79, 80, 81, 82, 83, 84, 85, 84, 85, 84, 85, 84, 83, 82,
81, 80, 81, 80, 81, 82, 83, 82, 83, 84, 83, 82, 83, 82, 83, 82, 83, 84, 83, 84,
85, 86, 85, 86, 87, 88, 87, 86, 85, 86, 85, 84, 83, 84, 85, 84, 83, 82, 81, 80
81, 82, 81, 80, 81, 82, 83, 82, 83, 84, 83, 82, 83, 84, 85, 84, 85, 86, 85, 86
87, 88, 87, 88, 89, 90, 91, 90, 89, 88, 87, 86, 87, 86, 85, 86, 87, 88, 87, 88,
89, 90, 89, 90, 89, 90, 89, 90, 89, 90, 91, 90, 91, 92, 93, 92, 93, 94, 93, 94,
93, 94, 95, 96, 95, 94, 93, 92, 93, 92, 93, 94, 93, 94, 95, 96, 95, 94
93, 92, 91, 90, 89, 88, 89, 90, 89, 88, 87, 88, 89, 90, 91, 90, 89, 88, 89, 88,
87, 86, 87, 88, 87, 86, 87, 88, 89, 90, 91, 92, 93, 92, 91, 90, 89, 90, 91, 90,
89, 88, 87, 88, 89, 88, 87, 86, 87, 88, 89, 90, 91, 92, 91, 92, 91, 92, 91, 90
91, 90, 89, 90, 89, 88, 87, 86, 87, 86, 87, 86, 85, 86, 85, 86, 87, 88, 89, 90,
89, 90, 89, 90, 91, 90, 91, 90, 91, 92, 91, 90, 89, 90, 91, 92, 93, 94, 93, 92,
93, 92, 91, 92, 93, 94, 95, 94, 95, 94, 95, 94, 95, 96, 97, 96, 97, 96, 95, 94
95, 96, 97, 98, 97, 96, 95, 94, 93, 94, 93, 92, 91, 90, 89, 88, 87, 86, 87, 86
87, 88, 87, 88, 87, 86, 87, 86, 85, 86, 85, 84, 85, 84, 85, 86, 87, 88, 89, 88,
89, 90, 89, 90, 89, 88, 89, 90, 91, 90, 91, 92, 91, 92, 93, 92, 91, 92, 91, 90,
91, 90, 91, 92, 91, 92, 93, 94, 93, 92, 93, 92, 91, 92, 91, 92, 91, 90, 91, 90,
89, 90, 91, 90, 89, 90, 89, 88, 87, 86, 85, 86, 85, 86, 87, 86, 87, 86, 87, 88,
```

```
89, 88, 89, 88, 89, 90, 89, 90, 91, 92, 93, 92, 93, 92, 91, 90, 89, 90, 89, 88,
87, 86, 87, 88, 89, 90, 89, 88, 87, 86, 87, 88, 89, 88, 87, 88, 89, 90, 89, 88,
87, 88, 89, 90, 89, 90, 91, 90, 91, 90, 91, 90, 89, 90, 91, 92, 91, 90, 89, 88,
89, 90, 91, 92, 93, 92, 93, 94, 95, 94, 93, 92, 93, 92, 91, 92, 93, 92, 93, 94,
93, 94, 95, 94, 93, 92, 93, 94, 93, 94, 93, 92, 93, 92, 91, 92, 93, 94, 93, 94
95, 96, 95, 94, 93, 92, 91, 92, 93, 94, 93, 94, 93, 92, 93, 94, 95, 94, 95, 96,
95, 94, 93, 92, 93, 92, 91, 90, 91, 90, 91, 92, 93, 92, 93, 92, 91, 90, 89, 90,
91, 90, 91, 92, 93, 92, 93, 92, 93, 94, 95, 94, 93, 92, 93, 92, 91, 90, 89, 90,
91, 92, 91, 92, 93, 94, 93, 94, 93, 94, 93, 94, 93, 92, 91, 90, 89, 88, 89, 88,
87, 86, 87, 86, 85, 84, 83, 82, 81, 80, 81, 80, 81, 80, 79, 78, 79, 80, 81, 80,
81, 80, 79, 78, 79, 80, 81, 82, 83, 84, 85, 84, 85, 84, 83, 82, 83, 84, 83, 84,
85, 86, 85, 86, 85, 84, 83, 84, 85, 86, 85, 86, 87, 88, 87, 88, 89, 88, 89, 90
91, 90, 91, 90, 91, 92, 93, 94, 95, 94, 95, 96, 97, 98, 97, 96, 97, 98, 99, 98,
99, 98, 99, 98, 97, 96, 95, 94, 95, 94, 93, 94, 95, 94, 93, 94, 93, 94, 93, 94,
95, 94, 93, 92, 93, 94, 95, 96, 97, 98, 97, 98, 97, 96, 95, 96, 95, 94, 95, 94,
93, 94, 93, 92, 93, 94, 93, 92, 93, 92, 93, 92, 91, 92, 93, 92, 93, 92, 93, 92,
91, 90, 91, 92, 91, 90, 91, 92, 91, 92, 91, 92, 93, 92, 91, 92, 91, 92, 91, 92,
93, 92, 93, 92, 93, 92, 91, 90, 89, 90, 91, 90, 89, 90, 91, 90, 89, 88, 89, 88,
87, 86, 87, 88, 87, 86, 87, 86, 87, 88, 89, 90, 91, 92, 93, 92, 93, 92, 91, 90,
91, 92, 93, 92, 93, 94, 93, 92, 91, 92, 91, 90, 91, 90, 91, 92, 91, 90, 91, 92
93, 92, 93, 92, 93, 92, 93, 94, 95, 96, 95, 94, 93, 92, 93, 94, 93, 92, 91, 92,
93, 94, 93, 94, 95, 94, 93, 94, 93, 92, 93, 94, 95, 96, 95, 94, 93, 94, 95, 94,
95, 94, 93, 94, 95, 94, 95, 96, 95, 94, 95, 96, 97, 96, 97, 96, 95, 94, 93, 94,
95, 96, 95, 96, 97, 98, 97, 98, 99, 98, 99, 100, 99, 100, 101, 100, 101, 100,
99, 100, 99, 98, 97, 98, 99, 98, 97, 98, 99, 100, 99, 100, 101, 102, 103, 102,
101, 100, 99, 98, 99, 98, 99, 98, 97, 96, 97, 96, 95, 94, 93, 92, 93, 94, 95,
96, 95, 96, 95, 96, 95, 96, 97, 98, 97, 96, 95, 96, 97, 96, 97, 98, 97, 98, 99
100, 99, 100, 99, 98, 99, 100, 101, 100, 101, 100, 99, 98, 97, 98, 99, 100, 101,
102, 103, 104, 105, 104, 105, 104, 105, 106, 105, 104, 105, 106, 105, 104, 103,
104, 105, 106, 107, 106, 105, 104, 105, 104, 103, 104, 105, 104, 105, 104, 105,
104, 105, 106, 105, 104, 103, 102, 103, 102, 101, 102, 101, 100, 99, 100, 101,
100, 101, 102, 103, 104, 103, 104, 103, 104, 105, 104, 103, 102, 103, 102, 103,
102, 103, 104, 103, 104, 105, 104, 105, 106, 105, 104, 103, 102, 101, 100, 99,
100, 101, 102, 103, 102, 101, 102, 101, 100, 99, 98, 97, 98, 99, 98, 99, 100,
99, 98, 99, 100, 99, 98, 97, 98, 97, 98, 99, 100, 99, 100, 99, 98, 99, 98, 99,
100, 101, 100, 99, 100, 99, 100, 101, 100, 101, 102, 103, 104, 105, 104, 105,
104, 105, 104, 103, 104, 103, 102, 101, 100, 101, 102, 101, 100, 99, 100, 101,
100, 101, 102, 101, 100, 101, 100, 99, 100, 101, 102, 103, 102, 101, 102, 103,
102, 103, 104, 103, 104, 105, 104, 103, 104, 103, 102, 103, 102, 103, 102, 101,
102, 101, 102, 103, 104, 103, 104, 103, 104, 105, 104, 105, 104, 103, 102, 101,
102, 103, 104, 103, 104, 103, 102, 103, 104, 103, 102, 103, 102, 103, 104, 103,
104, 105, 104, 103, 102, 101, 100, 99, 98, 99, 100, 101, 102, 101, 102, 103,
104, 105, 104, 103, 102, 101, 100, 99, 98, 97, 96, 95, 94, 95, 96, 95, 96, 95,
96, 97, 96, 95, 94, 95, 96, 95, 94, 93, 94, 95, 94, 95, 94, 93, 92, 91, 92, 91,
92, 91, 90, 89, 90, 91, 90, 89, 88, 87, 86, 85, 84, 83, 82, 83, 84, 85, 84, 85,
84, 85, 86, 85, 86, 85, 86, 87, 86, 87, 88, 89, 90, 89, 90, 91, 90, 91, 92, 91,
90, 91, 90, 89, 90, 89, 88, 87, 86, 87, 86, 87, 88, 87, 88, 87, 86, 87, 88, 87
86, 87, 86, 87, 88, 89, 88, 89, 88, 89, 88, 87, 88, 87, 88, 87, 86, 85, 86, 87,
```

88, 87, 88, 89, 88, 87, 88, 89, 90, 91, 92, 91, 92, 91, 92, 93, 92, 93, 92, 91, 90, 91, 90, 89, 88, 87, 88, 89, 88, 87, 88, 87, 86, 87, 88, 89, 88, 89, 88, 89, 90, 89, 88, 89, 88, 89, 88, 87, 86, 87, 88, 89, 88, 89, 88, 89, 88, 89, 88, 87, 86, 87, 86, 85, 86, 85, 86, 87, 88, 89, 90, 91, 90, 89, 88, 87, 88, 89, 88, 87, 88, 87, 88, 89, 90, 91, 92, 91, 90, 91, 92, 91, 92, 91, 92, 93, 92, 91, 90, 91 92, 91, 92, 91, 90, 91, 90, 91, 92, 91, 90, 89, 88, 87, 86, 87, 86, 87, 86, 85, 86, 85, 84, 83, 84, 85, 86, 87, 88, 89, 90, 89, 90, 89, 88, 89, 88, 89, 90, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 104, 105 106, 107, 106, 105, 104, 105, 106, 107, 106, 105, 106, 107, 106, 107, 108, 109, 108, 107, 106, 105, 106, 107, 106, 107, 106, 105, 104, 103, 102, 101, 100, 101, 100, 99, 100, 99, 98, 97, 98, 99, 100, 101, 100, 99, 100, 101, 102, 101, 100, 99, 100, 99, 98, 97, 98, 99, 100, 101, 100, 99, 100, 99, 98, 99, 98, 97, 98, 99 98, 97, 98, 97, 96, 97, 96, 97, 96, 95, 96, 95, 96, 95, 96, 95, 96, 97, 98, 99, 98, 97, 98, 99, 98, 99, 100, 99, 100, 99, 98, 97, 96, 95, 96, 95, 94, 93, 92, 91, 90, 91, 92, 93, 92, 91, 92, 91, 92, 93, 92, 91, 90, 91, 90, 91, 92, 91, 92, 91, 92, 91, 92, 91, 92, 91, 92, 93, 92, 91, 92, 93, 94, 93, 92, 93, 94, 95, 96, 97, 98, 97, 96, 97, 98, 97, 96, 95, 94, 95, 96, 95, 96, 97, 96, 97, 96, 97, 96, 95, 96, 95, 96, 97, 98, 99, 100, 101, 102, 101, 102, 101, 102, 101, 100, 99, 100, 101, 100, 101, 102, 101, 102, 101, 100, 99, 100, 101, 100, 101, 100, 99, 98, 99, 100, 99, 100, 101, 100, 101, 102, 101, 102, 101, 100, 101, 102, 103, 102, 101, 100, 101, 100, 99, 100, 99, 100, 101, 102, 101, 100, 99, 100, 99, 100, 101, 100, 99, 98, 97, 96, 95, 96, 95, 96, 95, 96, 97, 96, 95, 96, 95, 94, 93, 94, 95, 94, 95, 96, 95, 96, 95, 96, 95, 96, 95, 94, 95, 94, 93, 94, 95, 96, 97, 98, 97, 96, 95, 96, 95, 96, 95, 96, 95, 94, 93, 94, 95, 94, 95, 96, 97, 98, 99, 98, 97, 98, 99, 100, 99, 98, 99, 98, 97, 98, 99, 98, 99, 100, 101, 102, 103, 102, 103, 102, 101, 102, 103, 104, 105, 106, 107, 106, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 114, 113, 112, 113, 114, 113, 112, 111, 110, 111, 112, 111, 110, 109, 108, 107, 108, 107, 108, 107, 106, 107, 106, 105, 106, 105, 106, 107, 106, 105, 104, 105, 106, 107, 106, 107, 106, 105, 104, 105, 104, 105 104, 103, 102, 103, 102, 101, 102, 103, 104, 105, 104, 105, 104, 103, 104, 105, 106, 105, 104, 105, 104, 103, 102, 101, 100, 101, 100, 101, 100, 99, 100, 101, 100, 101, 100, 101, 100, 101, 102, 101, 102, 103, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 110, 109, 110, 111, 112, 113, 112, 111, 110, 109, 108, 109, 110, 111, 110, 111, 112, 113, 114, 113, 114, 113, 114, 113, 114, 113, 112, 113, 114, 115, 116, 115, 116, 115, 116, 117, 116, 115, 116, 115, 116, 117, 118, 119, 120, 121, 120, 121, 122, 121, 120, 119, 120, 121, 120, 121, 120, 119, 118, 119, 120, 119, 118, 117, 118, 119, 120, 121, 122, 123, 124, 123, 124, 123, 122, 121, 122, 121, 120, 121, 120, 121, 120, 119, 118, 117, 116, 117, 118, 119, 120, 121, 120, 119, 118, 117, 116, 117, 118, 117, 116, 117, 118, 117, 118, 119, 118, 117, 116, 115, 114, 115, 116, 115, 114, 115, 114, 115, 116, 115, 114, 113, 112, 111, 112, 111, 110, 111, 110, 109, 108, 109, 108, 107, 106, 105, 104, 105, 104, 105, 106, 105, 106, 105, 106, 105, 104, 103, 102, 101, 102, 103, 102, 103, 102, 103, 102, 101, 102, 101, 102, 101, 100, 99, 100, 101, 100, 99, 100, 99, 100, 101, 102, 101, 100, 99, 98, 99, 98, 97, 96, 97, 96, 97, 98, 99, 100, 101, 102, 101, 100, 99, 100, 101, 100, 99, 98, 99, 100, 99, 98, 99, 98, 97, 98, 99, 98, 97, 98, 99, 100, 99, 98, 99, 100, 99, 98, 97, 96, 95, 96, 95, 94, 95, 96, 97, 96, 97, 98, 99, 100, 99, 100, 99, 98, 97, 98, 97, 96, 95, 94, 93, 94, 93, 94, 93, 92, 93, 92, 91, 90, 89, 88, 87, 86, 87, 88, 87, 88, 87, 88, 89, 90, 91, 90, 89, 90,

91, 92, 93, 94, 93, 94, 95, 96, 95, 94, 93, 92, 93, 92, 93, 94, 95, 94, 93, 94, 93, 94, 95, 96, 97, 98, 99, 100, 99, 98, 99, 98, 99, 98, 97, 96, 95, 96, 95, 94, 93, 92, 93, 92, 91, 90, 89, 90, 91, 92, 91, 90, 91, 92, 91, 92, 93, 92, 91, 92, 93, 94, 95, 94, 95, 94, 93, 94, 93, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 101, 100, 101, 100, 101, 102, 103, 102, 101, 102, 103, 102, 101, 100, 101, 100, 99, 98, 99, 98, 99, 98, 99, 98, 99, 100, 99, 98, 97, 96, 97, 98, 97, 98, 97, 98, 99, 98, 99, 100, 101, 100, 101, 100, 101, 102, 103, 104, 105, 104, 103, 104, 105, 106, 105, 104, 103, 102, 103, 102, 103, 102, 101, 100, 99, 98, 99, 100, 99, 100, 101, 100, 99, 100, 101, 102, 103, 104, 103, 102, 101, 102, 103, 102, 101, 102, 101, 102, 101, 102, 103, 102, 103, 102, 101, 102, 103, 102, 101, 102, 101, 100, 101, 100, 99, 98, 99, 100, 99, 100, 99, 100, 101, 100, 99, 98, 97, 98, 97, 98, 97, 98, 99, 98, 97, 98, 97, 98, 97, 98, 99, 100, 99, 100, 99, 100, 101, 102, 103, 102, 103, 104, 105, 104, 105, 104, 105, 106, 107, 106, 107 106, 107, 106, 107, 106, 105, 106, 105, 104, 103, 102, 101, 102, 103, 104, 103, 104, 103, 102, 103, 104, 105, 106, 105, 106, 107, 108, 107, 106, 107, 106, 105, 104, 103, 102, 103, 104, 105, 104, 103, 102, 101, 102, 103, 102, 101, 100, 99, 100, 99, 98, 99, 100, 101, 100, 101, 102, 103, 104, 105, 106, 105, 106, 105, 104, 103, 102, 103, 102, 101, 102, 103, 102, 101, 100, 101, 100, 101, 100, 99, 100, 101, 102, 101, 100, 99, 98, 97, 98, 99, 100, 101, 102, 103, 104, 103, 102, 103, 104, 103, 102, 103, 102, 101, 100, 101, 100, 99, 98, 97, 98, 97, 98, 97, 98, 97, 98, 97, 96, 95, 94, 93, 94, 95, 94, 93, 92, 91, 92, 91, 92, 91, 92, 93, 94, 93, 92, 93, 94, 95, 96, 95, 94, 93, 94, 95, 96, 95, 94, 93, 94, 93, 94, 95, 94, 93, 92, 91, 92, 91, 92, 91, 92, 93, 92, 93, 92, 93, 94, 95, 94, 95, 94, 95, 94, 95, 94, 93, 92, 93, 94, 93, 94, 95, 96, 97, 96, 97, 96, 95, 94, 95, 96, 97, 98, 99, 100, 99, 98, 99, 100, 101, 102, 103, 104, 103, 102, 103, 102, 103, 102, 103, 102, 101, 102, 101, 102, 103, 102, 101, 102, 103, 104, 103, 102, 103, 104, 105, 104, 105, 104, 103, 102, 103, 104, 105, 106, 107, 106, 105, 106, 107, 108, 109, 108, 109, 108, 107, 108, 109, 108, 109, 108, 109, 110, 109, 108, 107, 108, 109, 110, 109, 108, 109, 108, 109, 108, 107, 106, 107, 106, 107, 106, 107, 106, 107, 108, 109, 110, 109, 110, 111, 110, 111, 110, 109, 108, 109, 110, 111, 112, 111, 112, 111, 112, 113, 112, 113, 114, 115, 116, 117, 116, 115, 114, 115, 114, 115, 114, 113, 114, 113, 112, 111, 110, 111, 112, 111, 110, 109, 108, 107, 106, 107, 108, 109, 110, 111, 110, 111, 112, 111, 110, 109, 108, 109, 110, 111, 110, 111, 112, 111, 112, 111, 110, 109, 108, 109, 108, 109, 108, 109, 108, 107, 106, 105, 104, 105, 104, 103, 102, 101, 100, 101, 100, 99, 98, 99, 100, 101, 102, 101, 102, 101, 102, 103, 102, 101, 102, 101, 100, 101, 102, 103, 104, 105, 104, 103, 102, 103, 104, 103, 104, 105, 106, 107, 106, 107, 106, 107, 108, 109, 108, 109, 110, 109, 110, 109, 110, 109, 108, 107, 108, 109, 110, 109, 108, 107, 108, 109, 110, 109, 108, 107, 108, 107, 106, 105, 106, 105, 104, 105, 104, 105, 104, 105, 104, 103, 104, 103, 104, 103, 102, 101, 102, 101, 100, 101, 102, 101, 102, 103, 102, 103, 102, 103, 102, 101, 102, 101, 102, 101, 100, 99, 98, 99, 98, 99, 100, 101, 102, 101, 100, 101, 102, 103, 102, 101, 102, 101, 102, 101, 102, 101, 100, 101, 102, 103, 102, 103, 102, 101, 102, 101, 102, 101, 100, 99, 98, 97, 98, 97, 98, 99, 98, 99, 98, 99, 98, 97, 98, 99, 100, 99, 98, 97, 96, 95, 96, 95, 94, 95, 96, 95, 96, 97, 98, 97, 98, 99, 98, 97, 98, 99, 98, 99, 100, 101, 100, 99, 100, 99, 100, 99, 100, 99, 100, 99, 100, 101, 100, 101, 102, 101, 102, 101, 102, 103, 102, 101, 100, 101, 102, 103, 102, 103, 104, 103, 102, 101, 100, 101, 102, 101, 100, 101, 102, 103, 102, 101, 102, 103, 102, 103, 102, 103, 102, 103, 104,

```
103, 104, 103, 104, 105, 104, 105, 106, 105, 104, 105, 106, 105, 106, 107, 108,
107, 108, 109, 110, 109, 108, 107, 108, 109, 108, 109, 110, 111, 112, 113, 112,
111, 112, 111, 112, 111, 112, 111, 112, 111, 110, 109, 110, 111, 112, 113, 114,
113, 112, 111, 112, 111, 110, 111, 112, 111, 112, 113, 114, 113, 112, 113, 112,
111, 110, 111, 112, 113, 112, 113, 114, 113, 112, 111, 110, 111, 110, 109, 110,
109, 108, 109, 108, 107, 108, 107, 106, 107, 108, 109, 110, 109, 110, 111, 110,
109, 110, 111, 110, 111, 110, 111, 112, 113, 114, 115, 116, 115, 114, 113, 114,
115, 116, 117, 118, 119, 120, 121, 120, 119, 118, 119, 120, 119, 120, 119, 118,
117, 118, 119, 118, 117, 116, 117, 116, 117, 116, 117, 118, 119, 120, 121, 120,
121, 122, 121, 120, 119, 118, 117, 118, 117, 116, 117, 118, 117, 118, 119, 120,
119, 118, 119, 118, 117, 116, 115, 114, 115, 114, 115, 114, 113, 114, 115, 114,
113, 112, 111, 112, 113, 112, 111, 112, 113, 112, 111, 112, 113, 112, 113, 114,
113, 112, 111, 110, 111, 112, 113, 112, 111, 110, 111, 112, 113, 114, 113, 112,
113, 112, 111, 110, 111, 110, 111, 110, 109, 110, 111, 110, 109, 110, 109, 110,
111, 112, 113, 114, 113, 112, 111, 110, 109, 108, 107, 106, 107, 108, 107, 108,
109, 108, 107, 106, 107, 108, 109, 110, 111, 110, 109, 110, 109, 108, 107, 106,
107, 108, 109, 108, 109, 108, 107, 106, 105, 106, 105, 104, 105, 106, 105, 106,
107, 108, 107, 106, 107, 108, 107, 106, 105, 106, 105, 104, 103, 102, 103, 104,
105, 106, 107, 106, 105, 106, 105, 104, 105, 106, 107, 106, 107, 106, 107, 106,
107, 106, 107, 108, 107, 106, 105, 104, 103, 104, 103, 104, 103, 102, 101, 100,
99, 100, 101, 102, 103, 104, 103, 104, 103, 104, 103, 104, 103, 104, 105, 106,
105, 104, 103, 102, 103, 104, 103, 102, 103, 102, 101, 102, 101, 102, 101, 100,
99, 98, 97, 96, 97, 96, 95, 94, 93, 94, 95, 94, 95, 94, 95, 94, 93, 92, 93, 94,
95, 96, 95, 96, 95, 96, 95, 96, 97, 96, 97, 96, 95, 96, 95, 94, 95, 96, 97, 96,
97, 98, 99, 100, 101, 100, 101, 102, 103, 104, 105, 104, 105, 104, 103, 104,
105, 104, 103, 104, 103, 102, 103, 102, 103, 104, 105, 106, 105, 106, 107, 106,
105, 106, 105, 104, 103, 104, 103, 104, 105, 104, 103, 102, 103, 104, 105, 104,
105, 106, 105, 106, 105, 104, 105, 104, 103, 102, 103, 102, 103, 102, 103, 102,
101, 100, 101, 102, 103, 102, 103, 104, 105, 106, 105, 104, 105, 104, 103, 104,
105, 104, 105, 106, 107, 108, 109, 108, 107, 106, 107, 106, 107, 106, 105, 104,
105, 104, 103, 104, 103, 102, 101, 100, 99, 100, 99, 98, 97, 98, 97, 96, 97, 98
99, 98, 99, 98, 99, 98, 99, 98, 99, 100, 101, 102, 103, 102, 103, 102, 101, 100,
99, 98, 97, 96, 97, 98, 97, 98, 97, 98, 97, 98, 97, 96, 97, 96, 95, 94, 95, 96,
97, 98, 99, 100, 101, 100, 99, 98, 99, 100, 99, 100, 99, 100, 99, 98, 97, 96,
97, 96, 97, 98, 99, 100, 99, 98, 99, 98, 97, 96, 97, 96, 97, 96, 97, 98, 99,
100, 99, 100, 99, 98, 99, 100, 101, 100, 99, 98, 97, 98, 99, 100, 99, 98, 99,
100, 101, 100, 101, 102, 103, 102, 101, 100, 101, 100, 101, 102, 103, 102, 101,
102, 103, 102, 103, 104, 103, 104, 103, 104, 103, 102, 101, 102, 103, 102, 101,
102, 103, 104, 103, 104, 103, 102, 103, 102, 101, 100, 101, 102, 101, 100, 99,
100, 101, 102, 101, 100, 101, 100, 101, 102, 103, 104, 103, 102, 101, 100, 101,
102, 103, 104, 103, 104, 105, 104, 103, 102, 103, 104, 103, 104, 103, 104, 105,
106, 105, 104, 105, 104, 103, 102, 101, 102, 101, 102, 103, 102, 101, 102, 103,
102, 103, 104, 105, 104, 105, 106, 107, 106, 107, 106, 107, 108, 107, 106, 105,
106, 107, 108, 109, 108, 107, 106, 107, 108, 109, 108, 107, 106, 107, 106, 105,
104, 103, 104, 105, 104, 105, 104, 105, 104, 103, 102, 101, 102, 103, 102, 101,
100, 99, 98, 97, 96, 95, 96, 97, 98, 97, 98, 97, 96, 95, 94, 95, 96, 97, 98, 99,
98, 99, 98, 99, 98, 99, 98, 97, 96, 95, 96, 95, 94, 93, 92, 91, 90, 91, 92, 91,
90, 91, 90, 89, 90, 89, 90, 91, 92, 93, 94, 93, 94, 95, 96, 95, 94, 93, 94, 93,
```

92, 93, 94, 95, 96, 95, 94, 95, 94, 95, 96, 95, 96, 97, 96, 97, 98, 97, 98, 99, 98, 99, 98, 97, 98, 97, 98, 97, 96, 97, 98, 97, 98, 97, 96, 97, 96, 97, 96, 95, 94, 95, 94, 95, 94, 95, 96, 95, 94, 95, 96, 95, 96, 95, 96, 97, 96, 97, 98, 99, 98, 99, 100, 99, 98, 99, 100, 99, 100, 99, 100, 99, 100, 101, 100, 99, 100, 101, 102, 103, 104, 105, 106, 105, 104, 103, 104, 103, 102, 103, 102, 103, 102, 103, 102, 103, 104, 105, 106, 107, 106, 105, 106, 105, 104, 103, 102, 101, 102, 103, 102, 103, 102, 103, 102, 101, 100, 99, 100, 99, 98, 99, 100, 101, 100, 99, 100, 99, 98, 99, 98, 99, 98, 99, 98, 99, 100, 101, 100, 99, 100, 101, 102, 103, 102, 103, 102, 101, 100, 99, 98, 99, 100, 101, 100, 99, 100, 99, 98, 97, 98, 97, 98, 97, 96, 97, 98, 97, 98, 99, 98, 97, 98, 97, 96, 97, 96, 97, 96, 97, 98, 97, 96, 97, 96, 95, 96, 97, 96, 97, 98, 97, 96, 97, 98, 99, 98, 97, 98, 99, 100, 101, 102, 101, 100, 101, 100, 99, 98, 97, 98, 97, 96, 97, 98, 99, 100, 101, 100, 99, 100, 101, 100, 99, 98, 97, 96, 97, 96, 97, 98, 99, 98, 97, 98, 97, 96, 95, 94, 93, 94, 95, 94, 95, 96, 97, 96, 95, 94, 93, 94, 95, 94, 93, 94, 95, 96, 95, 96, 97, 96, 97, 96, 97, 98, 99, 98, 99, 98, 99, 98, 99, 100, 101, 102, 101, 100, 101, 100, 99, 100, 99, 100, 99, 98, 99, 100, 101, 100, 99, 98, 99, 100, 101, 102, 103, 104, 105, 104, 103, 104, 103, 104, 105, 104, 103, 102, 101, 102, 103, 104, 105, 106, 105, 104, 103, 104, 103, 104, 105, 104, 105, 106, 105, 104, 103, 104, 105, 104, 105, 104, 105, 104, 105, 106, 105, 104, 105, 106, 107, 108, 107, 106, 107, 106, 105, 104, 105, 106, 107, 106, 105, 104, 103, 104, 103, 102, 101, 100, 99, 98, 97, 98, 97, 96, 95, 96, 97, 98, 97, 96, 95, 94, 95, 94, 93, 94, 93 94, 93, 94, 93, 92, 91, 90, 89, 90, 89, 90, 91, 90, 89, 90, 91, 90, 89, 88, 87, 86, 85, 86, 85, 86, 87, 86, 87, 88, 89, 90, 91, 90, 89, 90, 89, 90, 89, 90, 89, 88, 89, 88, 89, 88, 89, 88, 89, 90, 89, 88, 89, 90, 89, 88, 89, 90, 91, 90, 91, 92, 93, 94, 95, 94, 93, 92, 93, 92, 91, 92, 93, 92, 91, 90, 91, 90, 89, 88, 89, 88, 89, 90, 91, 90, 89, 90, 89, 90, 88, 88, 89, 90, 91, 92, 93, 92, 91, 92, 93, 94, 93, 92, 93, 92, 91, 90, 91, 92, 91, 92, 93, 94, 95, 96, 95, 96, 95, 94, 95, 94, 95, 94, 95, 94, 93, 92, 93, 94, 93, 92, 93, 92, 91, 92, 91, 90, 89, 90, 89, 88, 89, 88, 87, 86, 85, 84, 85, 84, 85, 86, 87, 86, 85, 86, 85, 86, 85, 84, 85, 84, 85, 86, 87, 86, 87, 86, 85, 84, 83, 84, 85, 84, 85, 86, 85, 86, 85, 86, 87, 86, 85, 86, 87, 88, 89, 90, 89, 88, 87, 86, 87, 88, 89, 90, 89, 88, 89, 88, 87, 88, 89, 90, 89, 90, 91, 90, 91, 90, 89, 90, 91, 92, 91, 92, 91, 90, 89, 90, 91, 92, 93, 92, 93, 92, 91, 92, 91, 90, 91, 90, 91, 90, 89, 90, 89, 90, 91, 90, 89, 88, 89, 88, 89, 90, 91, 92, 93, 92, 91, 90, 89, 88, 89, 88, 87, 88, 87, 86, 85, 86, 85, 86, 85, 86, 85, 86, 85, 84, 85, 86, 87, 86, 85, 86, 87, 88, 89, 88, 89, 90, 89, 88, 89, 88, 87, 86, 85, 86, 87, 88, 89, 90, 89, 90, 89, 88, 89, 90, 91, 92, 93, 92, 93, 92, 93, 94, 95, 96, 97, 96, 95, 96, 95, 94, 95, 96, 95, 94, 93, 92, 91, 90, 89, 90, 89, 88, 89, 90, 89, 90, 89, 90, 89, 88, 89, 90, 91, 92, 93, 94, 95, 94, 93, 94, 95, 94, 93, 94, 95, 96, 95, 96, 97, 96, 97, 98, 99, 100, 99, 98, 99, 98, 97, 96, 95, 94, 93, 94, 93, 94, 93, 92, 93, 94, 93, 94, 95, 96, 97 98, 97, 98, 97, 98, 97, 98, 97, 96, 95, 96, 97, 98, 99, 98, 97, 96, 97, 96, 95, 96, 97, 96, 95, 94, 95, 94, 93, 92, 91, 92, 91, 92, 93, 94, 95, 96, 97, 98, 97, 96, 95, 96, 95, 96, 95, 94, 95, 96, 97, 98, 99, 100, 99, 98, 99, 100, 101, 100, 101, 102, 101, 100, 101, 102, 101, 102, 103, 102, 103, 104, 105, 106, 107, 108, 109, 108, 109, 110, 109, 108, 107, 108, 109, 108, 109, 110, 109, 110, 109, 108, 109, 108, 107, 106, 107, 106, 107, 108, 109, 108, 109, 110, 111, 110, 109, 108, 107, 106, 105, 106, 107, 108, 107, 106, 107, 106, 107, 108, 107, 106, 105, 106, 107, 106, 107, 106, 105, 106, 107, 106, 107, 106, 105, 106, 107, 108, 109, 110,

```
109, 110, 111, 112, 113, 112, 111, 112, 111, 110, 111, 110, 111, 112, 111, 110,
109, 110, 111, 110, 109, 108, 109, 110, 111, 112, 113, 112, 113, 112, 113, 112,
113, 112, 113, 112, 113, 112, 113, 112, 113, 114, 113, 112, 113, 112, 111, 112,
111, 110, 111, 112, 111, 110, 111, 110, 111, 112, 113, 114, 115, 114, 113, 112,
111, 110, 111, 110, 111, 112, 111, 112, 111, 112, 113, 112, 111, 112, 111, 112
113, 112, 113, 114, 113, 112, 111, 110, 111, 110, 109, 110, 109, 108, 109, 110,
111, 110, 111, 110, 111, 110, 109, 110, 111, 110, 109, 110, 109, 110, 111, 112,
111, 112, 111, 112, 111, 112, 113, 112, 111, 110, 111, 112, 111, 112, 111, 110,
109, 110, 109, 110, 111, 112, 111, 110, 111, 110, 111, 112, 111, 112, 111, 110,
111, 110, 109, 108, 109, 110, 109, 110, 109, 110, 109, 110, 111, 110, 109, 110,
111, 112, 111, 112, 113, 112, 113, 114, 113, 112, 113, 114, 113, 112, 111, 112,
111, 110, 111, 110, 109, 108, 109, 110, 111, 112, 111, 112, 113, 114, 115, 114
113, 112, 111, 112, 111, 110, 111, 110, 109, 108, 109, 110, 109, 108, 107, 108,
109, 108, 109, 108, 107, 106, 105, 106, 107, 108, 107, 108, 109, 108, 107, 106,
107, 108, 107, 106, 105, 104, 103, 102, 101, 102, 103, 104, 103, 104, 105, 106,
105, 104, 105, 104, 105, 106, 107, 106, 105, 106, 107, 106, 105, 104, 103, 104,
105, 104, 103, 102, 101, 102, 101, 102, 101, 100, 99, 100, 99, 100, 101, 102,
103, 102, 101, 100, 101, 100, 101, 100, 99, 100, 99, 100, 99, 98, 97, 98, 97,
98, 97, 96, 97, 96, 95, 94, 95, 94, 95, 94, 95, 94, 95, 94, 93, 92, 91, 90, 91,
90, 91, 92, 93, 94, 95, 94, 95, 96, 95, 96, 95, 94, 95, 94, 93, 92, 93, 94, 95
96, 97, 98, 99, 98, 99, 100, 99, 98, 99, 98, 99, 98, 97, 98, 97, 96, 97, 98, 97,
98, 97, 96, 97, 98, 97, 98, 99, 100, 99, 98, 99, 98, 97, 96, 97, 96, 95, 94, 93,
92, 91, 90, 89, 90, 89, 88, 87, 86, 85, 86, 87, 88, 89, 88, 87, 86, 87, 86, 85,
84, 83, 82, 83, 82, 83, 82, 81, 80, 81, 80, 79, 78, 77, 78, 77, 76, 75, 74, 75,
74, 75, 74, 75, 76, 77, 76, 77, 78, 77, 78, 79, 80, 81, 82, 81, 80, 79, 80, 79,
80, 81, 80, 79, 80, 81, 82, 83, 82, 81, 82, 83, 82, 81, 82, 81, 80, 81, 80, 79,
80, 81, 82, 81, 80, 81, 82, 81, 80, 81, 82, 81, 80, 79, 78, 79, 78, 79, 78, 77,
78, 79, 80, 81, 82, 83, 82, 83, 82, 81, 82, 83, 82, 81, 82, 83, 82, 83, 82, 81,
82, 83, 82, 81, 80, 79, 80, 81, 82, 83, 84, 83, 84, 83, 84, 85, 86, 87, 86, 87,
86, 85, 84, 83, 82, 81, 80, 81, 82, 81, 80, 79, 80, 81, 82, 83, 84, 85, 84, 85
84, 85, 86, 87, 86, 85, 86, 85, 86, 87, 86, 87, 86, 87, 86, 87, 88, 89, 90, 91,
92, 91, 92, 91, 92, 93, 94, 93, 94, 93, 92, 93, 92, 93, 92, 91, 90, 89, 88, 87,
86, 87, 88, 87, 86, 87, 86, 87, 88, 87, 88, 87, 88, 87, 88, 87, 88, 87, 88, 87,
86, 87, 88, 87, 88, 89, 88, 87, 86, 85, 86, 87, 86, 87, 86, 85, 86, 85, 84, 83,
84, 83, 84, 85, 84, 83, 82, 83, 82, 83, 84, 85, 86, 87, 88, 87, 86, 87, 88, 87
86, 85, 86, 87, 88, 89, 88, 87, 86, 87, 86, 85, 84, 85, 86, 87, 88, 89, 88, 89
88, 87, 88, 87, 88, 89, 90, 91, 90, 89, 88, 89, 90, 91, 92, 91, 90, 89, 90, 91,
92, 91, 90, 91, 90, 91, 90, 89, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 96, 97,
98, 99, 100, 99, 98, 99, 98, 99, 98, 99, 100, 101, 100, 99, 100, 101, 102, 101,
100, 99, 100, 99, 100, 101, 100, 101, 102, 101, 102, 101, 100, 99, 98, 99, 98,
97, 96, 97, 98, 97, 98, 99, 100, 101, 100, 101, 102, 103, 104, 103, 102, 103,
104, 103, 102, 103, 104, 105, 106, 105, 106, 105, 106, 105, 104, 103, 104, 103,
104, 105, 104, 103, 102, 103, 102, 103, 104, 103, 102, 103, 104, 103, 104, 105,
106, 107, 106, 105, 104, 105, 104, 105, 104, 105, 106, 107, 106, 105, 106, 107,
106, 105, 104, 103, 102, 101, 102, 103, 104, 105, 104, 105, 104, 103, 104, 105,
106, 107, 108, 107, 108, 109, 110, 111, 112, 113, 114, 115, 114, 113, 114, 115,
114, 115, 114, 113, 112, 113, 112, 113, 114, 115, 114, 115, 114, 113, 112, 111,
112, 111, 112, 111, 110, 109, 108, 107, 108, 109, 108, 107, 108, 107, 106, 105,
```

104, 103, 104, 105, 106, 105, 104, 103, 104, 105, 106, 105, 104, 103, 102, 101, 102, 101, 102, 101, 102, 103, 102, 103, 102, 101, 102, 101, 102, 101, 102, 101, 100, 99, 100, 99, 100, 101, 102, 103, 104, 105, 104, 103, 104, 105, 106, 105, 104, 103, 102, 103, 104, 103, 102, 103, 104, 103, 104, 105, 104, 105, 104, 105, 104, 103, 102, 103, 104, 105, 104, 103, 104, 103, 104, 105, 104, 105, 104, 103, 104, 103, 104, 105, 106, 107, 108, 109, 108, 109, 110, 111, 110, 111, 110, 109, 108, 109, 110, 111, 112, 111, 110, 109, 110, 109, 108, 109, 108, 107, 108, 107, 108, 107, 106, 105, 106, 105, 106, 107, 106, 105, 106, 107, 108, 107, 108, 109, 110, 111, 110, 111, 112, 111, 110, 109, 110, 109, 110, 109, 108, 107, 106, 105, 106, 107, 108, 109, 110, 111, 110, 111, 110, 111, 110, 111, 110, 111, 110, 109, 108, 109, 110, 109, 110, 111, 110, 111, 112, 111, 110, 111, 110, 111, 112, 111, 112, 113, 112, 111, 112, 111, 112, 111, 110, 111, 110, 111, 112, 113, 114, 113, 112, 113, 112, 113, 112, 111, 110, 111, 110, 111, 110, 111, 110, 111, 110, 109, 108, 109, 108, 109, 108, 109, 108, 107, 106, 105, 104, 103, 104, 103, 104, 103, 104, 105, 104, 105, 106, 105, 104, 103, 102, 101, 102, 103, 102, 103, 104, 103, 102, 103, 102, 101, 100, 99, 100, 101, 102, 101, 100, 101, 102, 103, 102, 101, 100, 99, 98, 99, 100, 101, 100, 101, 100, 101, 100, 101, 100, 99, 98, 97, 96, 97, 96, 95, 96, 97, 98, 99, 100, 99, 98, 97, 98, 99, 98, 99, 98, 99, 98, 97, 96, 95, 96, 95, 96, 97, 96, 97, 96, 95, 96, 97, 96, 97, 96, 97, 96, 97, 98, 99, 98 97, 98, 99, 100, 101, 102, 101, 100, 99, 98, 97, 98, 99, 100, 99, 100, 101, 102, 101, 100, 101, 102, 101, 100, 99, 100, 99, 98, 99, 100, 99, 98, 97, 96, 97, 96, 95, 96, 95, 96, 97, 98, 99, 100, 101, 100, 101, 100, 101, 100, 101, 100, 101, 102, 103, 104, 103, 102, 101, 102, 103, 102, 101, 100, 101, 102, 101, 100, 101, 102, 101, 100, 101, 102, 101, 100, 99, 98, 97, 98, 97, 96, 97, 96, 97, 98, 99, 100, 101, 102, 103, 102, 103, 104, 103, 102, 101, 100, 101, 100, 99, 100, 101, 102, 101, 100, 99, 98, 97, 98, 97, 98, 97, 98, 99, 100, 99, 98, 99, 98, 99, 100, 99, 98, 99, 100, 101, 102, 103, 102, 103, 104, 105, 106, 105, 106, 105, 106, 107, 106, 105, 104, 105, 106, 105, 104, 105, 106, 105, 104, 103, 104, 103, 104, 103, 102, 101, 102, 101, 100, 99, 98, 97, 98, 99, 98, 99, 100, 99, 100, 99, 98, 97, 96, 95, 94, 93, 92, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 100, 99, 98, 99, 98, 99, 100, 101, 102, 101, 100, 101, 100, 99, 98, 97, 96, 97, 98, 99, 100, 101, 102, 101, 100, 101, 100, 101, 100, 101, 100, 101, 100, 99, 100, 101, 100, 101, 100, 99, 98, 97, 98, 97, 96, 95, 96, 95, 94, 95, 94, 93, 94, 93, 92, 93, 92, 91, 92, 93, 92, 93, 94, 93, 94, 95, 94, 95, 94, 93, 92, 93, 94, 95, 96 97, 98, 97, 98, 99, 98, 97, 98, 99, 98, 97, 96, 95, 96, 95, 94, 95, 96, 95, 96, 97, 98, 97, 96, 97, 98, 99, 98, 99, 98, 99, 98, 99, 100, 101, 100, 101, 100, 101, 100, 99, 100, 101, 100, 101, 100, 101, 102, 101, 100, 99, 100, 101, 100, 101, 100, 101, 100, 99, 100, 101, 100, 101, 100, 99, 100, 101, 102, 101, 102, 103, 102, 101, 100, 99, 98, 99, 98, 99, 100, 101, 100, 101, 100, 99, 100, 99, 98, 97, 98, 99, 98, 97, 98, 97, 96, 97, 96, 97, 96, 95, 96, 95, 96, 97, 96, 97, 98, 97, 98, 97, 96, 95, 94, 95, 96, 97, 98, 99, 98, 97, 96, 95, 94, 95, 94, 93, 92, 91, 90, 89, 90, 91, 92, 91, 90, 89, 88, 89, 90, 89, 90, 89, 90, 89, 88, 87, 88, 89, 88, 89, 88, 89, 88, 87, 88, 87, 86, 85, 86, 85, 84, 85, 84, 85, 84, 85, 84, 83, 84, 85, 86, 85, 86, 85, 84, 83, 84, 85, 84, 85, 86, 85, 84, 85, 86, 87, 88, 89, 88, 87, 86, 87, 86, 87, 88, 87, 88, 87, 88, 87, 86, 85, 86, 87, 88, 87, 88, 89, 88, 87, 86, 87, 88, 87, 86, 87, 86, 87, 88, 89, 88, 87, 88, 89, 88, 87, 88, 87, 88, 89, 88, 87, 88, 87, 86, 85, 84, 85, 84, 83, 84, 83, 82, 83, 82, 81, 82, 81, 82, 83, 82, 83, 84, 85, 86, 85, 84, 83, 82, 83, 84, 85, 84, 85, 84, 85,

```
84, 83, 84, 85, 86, 85, 84, 85, 84, 83, 82, 83, 84, 83, 84, 85, 86, 87, 88, 89,
88, 89, 88, 87, 86, 87, 88, 87, 86, 87, 86, 85, 84, 83, 84, 85, 84, 83, 82, 81,
82, 81, 82, 83, 84, 83, 84, 83, 84, 83, 84, 85, 86, 87, 88, 87, 88, 87, 88, 87,
88, 89, 90, 91, 90, 91, 90, 91, 90, 89, 88, 87, 88, 89, 90, 89, 88, 89, 90, 89,
88, 89, 90, 89, 88, 89, 88, 89, 88, 89, 88, 87, 86, 85, 86, 87, 88, 89, 88, 87,
86, 87, 88, 89, 90, 89, 90, 89, 90, 91, 92, 93, 92, 93, 94, 95, 94, 95, 94, 93,
94, 93, 92, 93, 94, 95, 94, 95, 94, 93, 94, 95, 94, 95, 94, 93, 92, 93, 92, 91,
90, 91, 90, 91, 90, 89, 90, 91, 92, 93, 94, 93, 92, 93, 92, 93, 92, 93, 94, 95,
94, 93, 94, 95, 96, 97, 96, 97, 96, 97, 98, 99, 100, 101, 102, 101, 102, 101,
100, 99, 98, 97, 96, 97, 98, 99, 98, 99, 100, 101, 100, 99, 98, 97, 96,
95, 94, 95, 96, 95, 94, 93, 92, 91, 90, 89, 88, 89, 90, 89, 90, 91, 92, 91, 92
93, 92, 91, 90, 89, 90, 89, 90, 91, 92, 91, 90, 89, 88, 87, 88, 87, 88, 87, 88
89, 90, 89, 88, 87, 86, 87, 88, 87, 88, 87, 88, 89, 88, 89, 90, 89, 90, 89, 90
91, 92, 93, 94, 95, 96, 97, 98, 99, 98, 99, 98, 97, 96, 95, 94, 93, 92, 93, 92,
91, 90, 89, 90, 89, 88, 89, 88, 87, 88, 89, 88, 87, 88, 87, 86, 85, 86, 85, 84,
83, 82, 83, 82, 83, 82, 81, 82, 81, 82, 83, 82, 83, 84, 83, 84, 85, 84, 85, 84
83, 84, 85, 86, 85, 86, 85, 84, 85, 84, 83, 84, 83, 82, 83, 84, 85, 86, 85, 84,
85, 86, 87, 86, 87, 88, 89, 88, 89, 88, 89, 90, 89, 90, 89, 88, 87, 86, 87, 86,
87, 88, 87, 88, 87, 86, 85, 86, 87, 88, 89, 90, 89, 90, 91, 92, 93, 94, 93, 94
93, 92, 93, 94, 95, 94, 93, 94, 93, 94, 93, 94, 93, 94, 95, 96, 95, 96, 95, 96
95, 94, 95, 94, 95, 96, 97, 98, 99, 100, 99, 98, 99, 100, 99, 100, 101, 100,
101, 102, 103, 104, 103, 104, 103, 102, 103, 102, 101, 102, 103, 102, 103, 102,
101, 102, 103, 102, 101, 102, 103, 104, 105, 106, 107, 106, 105, 106, 105, 106,
105, 106, 107, 108, 109, 110, 109, 110, 109, 108, 109, 108, 107, 106, 105, 104,
103, 104, 105, 104, 105, 106, 105, 106, 105, 104, 105, 104, 105, 106, 107, 106,
105, 104, 105, 104, 105, 104, 105, 104, 103, 104, 105, 106, 105, 104, 103, 102,
103, 104, 105, 104, 105, 104, 105, 104, 103, 102, 103, 102, 103, 104, 105, 106,
105, 106, 105, 106, 105, 106, 107, 108, 107, 106, 105, 106, 105, 104, 105, 106,
105, 104, 103, 104, 105, 106, 105, 104, 103, 102, 101, 100, 99, 98, 99, 98, 99
100, 99, 100, 101, 100, 99, 98, 99, 98, 99, 100, 99, 98, 97, 98, 97, 98, 97, 98
97, 96, 97, 96, 95, 96, 97, 98, 99, 100, 99, 100, 101, 102, 103, 104, 103, 102,
103, 102, 103, 104, 103, 104, 105, 104, 105, 104, 105, 106, 105, 104, 105, 106,
107, 106, 107, 106, 107, 108, 109, 108, 107, 106, 105, 106, 107, 106, 105, 104,
103, 104, 105, 104, 105, 106, 105, 106, 105, 106, 107, 106, 107, 106, 107, 108,
107, 106, 105, 106, 107, 108, 109, 110, 109, 110, 109, 110, 109, 110, 109, 110,
111, 112, 111, 112, 111, 110, 109, 108, 107, 108, 109, 110, 111, 112, 111, 112,
113, 112, 111, 110, 109, 108, 107, 106, 107, 106, 105, 104, 105, 106, 105, 104,
103, 102, 103, 102, 103, 102, 101, 102, 103, 102, 103, 102, 103, 104, 105, 106,
105, 104, 103, 102, 103, 102, 101, 100, 101, 100, 99, 98, 99, 100, 101, 102,
101, 100, 101, 102, 101, 102, 101, 100, 99, 98, 99, 98, 99, 98, 99, 98, 99, 100,
101, 102, 103, 102, 101, 100, 101, 100, 101, 100, 99, 100, 101, 102, 103, 104,
105, 104, 105, 106, 107, 108, 107, 108, 109, 108, 107, 106, 107, 106, 105, 104,
105, 104, 103, 102, 103, 104, 103, 104, 103, 104, 103, 104, 103, 102, 103, 102,
103, 104, 105, 106, 105, 106, 107, 106, 107, 108, 107, 106, 105, 106, 105, 104,
103, 104, 105, 106, 107, 106, 107, 106, 105, 106, 105, 106, 105, 104, 105, 106,
105, 106, 107, 108, 107, 106, 105, 104, 103, 104, 105, 104, 103, 104, 103, 104,
103, 102, 103, 104, 103, 102, 103, 102, 101, 100, 101, 100, 99, 100, 99, 98, 97
96, 95, 96, 97, 96, 97, 96, 95, 96, 97, 98, 97, 98, 99, 100, 99, 98, 99, 98, 99,
```

```
98, 97, 96, 97, 98, 99, 98, 99, 98, 99, 100, 99, 100, 101, 100, 101, 100, 99,
98, 99, 100, 99, 100, 99, 98, 97, 96, 95, 96, 95, 96, 97, 98, 97, 98, 97, 98,
99, 100, 99, 100, 99, 98, 97, 96, 95, 96, 97, 98, 99, 100, 99, 100, 99, 100, 99
98, 97, 98, 97, 96, 97, 96, 95, 96, 95, 94, 95, 94, 93, 92, 91, 92, 93, 92, 91,
92, 91, 90, 89, 88, 87, 88, 87, 88, 87, 86, 85, 86, 87, 86, 87, 88, 89, 90, 89,
88, 89, 88, 89, 88, 87, 86, 87, 86, 87, 88, 89, 90, 91, 92, 91, 92, 91, 92, 91,
90, 91, 92, 91, 92, 93, 94, 93, 94, 95, 96, 95, 94, 95, 94, 95, 96, 95, 94, 93,
92, 91, 92, 91, 92, 93, 92, 91, 90, 89, 90, 91, 92, 93, 92, 93, 94, 93, 94, 95
94, 93, 94, 93, 92, 93, 92, 91, 90, 89, 90, 91, 92, 91, 90, 91, 90, 89, 90, 91,
90, 91, 90, 89, 88, 87, 88, 89, 90, 91, 90, 91, 92, 93, 92, 91, 90, 89, 88, 89,
90, 91, 92, 93, 94, 93, 94, 93, 94, 93, 94, 93, 94, 93, 94, 93, 92, 91, 92, 93, 92, 93
92, 93, 94, 93, 92, 93, 92, 93, 92, 91, 92, 93, 94, 93, 92, 93, 94, 93, 92, 93
94, 95, 94, 95, 96, 97, 96, 95, 94, 95, 94, 93, 92, 91, 92, 91, 90, 89, 90, 89
90, 89, 88, 89, 88, 89, 88, 89, 90, 89, 90, 89, 88, 89, 90, 91, 90, 91, 92, 93,
92, 91, 90, 91, 90, 91, 90, 91, 90, 91, 90, 89, 90, 89, 90, 89, 88, 89, 90, 89,
88, 87, 88, 87, 86, 85, 84, 85, 86, 87, 88, 87, 88, 87, 86, 85, 86, 85, 84, 83,
82, 81, 80, 79, 78, 79, 78, 77, 78, 79, 78, 79, 78, 79, 80, 81, 82, 83, 82, 81,
82, 83, 84, 85, 86, 85, 86, 87, 88, 87, 88, 87, 86, 87, 88, 87, 86, 87, 88, 87,
86, 87, 88, 87, 86, 87, 86, 87, 88, 89, 88, 87, 86, 85, 84, 85, 84, 83, 82, 81,
80, 79, 78, 79, 80, 79, 78, 79, 80, 79, 78, 79, 80, 79, 78, 79, 80, 81, 82, 81,
80, 81, 80, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 87, 88, 89, 90, 91, 92, 91,
92, 93, 94, 95, 94, 93, 94, 93, 92, 93, 92, 91, 92, 91, 92, 93, 92, 91, 90, 91,
92, 91, 92, 91, 92, 93, 92, 93, 94, 95, 94, 93, 94, 93, 92, 93, 94, 93, 94, 93,
92, 93, 94, 93, 94, 93, 94, 93, 92, 93, 92, 91, 92, 93, 92, 93, 94, 93, 92, 91,
90, 91, 92, 91, 92, 91, 92, 93, 94, 95, 96, 97, 98, 99, 98, 97, 96, 97, 96, 95,
94, 93, 92, 91, 90, 89, 90, 89, 90, 88, 88, 89, 90, 91, 92, 93, 92, 93, 92, 93,
94, 93, 92, 93, 94, 95, 94, 95, 96, 97, 98, 97, 98, 97, 96, 97, 96, 97, 98, 97
98, 97, 96, 95, 96, 95, 94, 93, 94, 93, 94, 93, 94, 95, 94, 95, 96, 97, 96, 95
94, 95, 94, 93, 92, 91, 92, 93, 94, 95, 94, 95, 96, 95, 94, 95, 96, 97, 98, 99
100, 101, 102, 103, 104, 103, 102, 103, 102, 101, 102, 103, 104, 103, 104, 103,
102, 101, 102, 101, 102, 103, 104, 103, 102, 101, 100, 101, 102, 103, 104, 105,
106, 107, 108, 107, 106, 105, 106, 107, 106, 107, 106, 107, 108, 109, 108, 109,
110, 109, 108, 109, 110, 109, 108, 107, 106, 105, 106, 107, 108, 107, 108, 109,
108, 109, 110, 111, 112, 111, 110, 109, 110, 109, 110, 109, 110, 109, 110, 109,
110, 109, 110, 109, 108, 109, 110, 111, 112, 111, 112, 113, 114, 115, 114, 113,
114, 113, 112, 111, 110, 109, 110, 109, 110, 111, 110, 111, 112, 113, 114, 113,
112, 111, 110, 109, 110, 109, 110, 109, 110, 109, 108, 109, 110, 109, 110, 109,
110, 109, 110, 109, 108, 109, 110, 111, 110, 109, 108, 109, 110, 111, 110, 109,
108, 107, 106, 105, 104, 103, 102, 101, 100, 101, 100, 101, 102, 103, 104, 103,
104, 105, 104, 103, 104, 103, 102, 103, 104, 105, 106, 105, 106, 107, 106, 105,
104, 103, 104, 105, 104, 105, 106, 105, 106, 107, 106, 107, 106, 105, 106, 107,
108, 107, 106, 107, 106, 105, 104, 103, 104, 105, 106, 105, 106, 107, 106, 105,
104, 103, 102, 103, 102, 101, 100, 101, 102, 103, 104, 103, 102, 101, 100, 99,
98, 97, 98, 99, 98, 97, 98, 97, 96, 95, 96, 95, 94, 93, 92, 93, 92, 93, 94, 93
94, 93, 94, 95, 96, 95, 96, 97, 96, 95, 96, 97, 96, 97, 96, 97, 98, 99, 100,
101, 100, 99, 100, 101, 102, 103, 102, 103, 104, 103, 102, 103, 104, 103, 104,
103, 104, 105, 106, 105, 106, 107, 106, 105, 106, 105, 106, 105, 106, 105, 104,
105, 106, 107, 106, 105, 104, 103, 102, 101, 100, 99, 98, 97, 96, 97, 96, 95,
```

```
94, 93, 94, 95, 96, 95, 96, 97, 96, 97, 96, 95, 96, 97, 98, 97, 98, 99, 100, 99,
100, 101, 100, 99, 98, 99, 98, 99, 100, 99, 98, 99, 98, 99, 98, 97, 98, 99, 98,
97, 96, 97, 98, 99, 98, 97, 96, 95, 96, 97, 98, 97, 96, 97, 98, 97, 98, 97, 96,
95, 94, 95, 96, 97, 98, 97, 98, 99, 100, 101, 100, 101, 102, 103, 104, 105, 104,
105, 106, 105, 106, 105, 104, 105, 106, 105, 106, 105, 106, 107, 108, 109, 108
107, 108, 107, 108, 107, 106, 107, 106, 107, 106, 105, 106, 107, 108, 107, 106,
107, 106, 105, 104, 103, 104, 105, 104, 105, 104, 105, 104, 103, 102, 103, 102,
103, 102, 103, 102, 101, 100, 101, 100, 101, 102, 103, 104, 105, 106, 105, 106
107, 106, 107, 108, 109, 110, 111, 110, 111, 110, 109, 108, 109, 110, 109, 110,
109, 108, 107, 106, 105, 106, 105, 106, 105, 104, 103, 102, 101, 100, 99, 98,
97, 96, 97, 96, 97, 98, 97, 98, 97, 96, 95, 94, 95, 94, 95, 94, 95, 96, 97, 98,
97, 96, 97, 96, 95, 94, 93, 94, 95, 94, 95, 94, 93, 92, 93, 94, 95, 96, 97, 96
97, 96, 95, 94, 93, 92, 93, 94, 95, 96, 97, 98, 99, 98, 99, 100, 99, 98, 99, 98
97, 98, 97, 96, 95, 96, 97, 98, 97, 98, 99, 98, 97, 96, 95, 94, 95, 96, 95, 96,
97, 98, 97, 96, 95, 94, 93, 94, 95, 94, 93, 92, 91, 90, 91, 90, 91, 92, 93, 94,
95, 94, 93, 94, 95, 96, 97, 96, 97, 98, 99, 98, 97, 96, 95, 94, 93, 92, 93, 94
95, 94, 93, 92, 91, 92, 91, 90, 89, 88, 89, 90, 89, 88, 87, 86, 85, 86, 87, 88,
89, 88, 89, 88, 87, 88, 87, 88, 89, 90, 91, 92, 91, 92, 93, 92, 91, 90, 89, 90,
91, 90, 89, 90, 91, 92, 91, 92, 91, 92, 93, 94, 95, 94, 95, 96, 95, 94, 95, 94,
95, 96, 95, 96, 95, 94, 93, 92, 93, 94, 93, 92, 91, 92, 93, 92, 91, 92, 91, 90,
89, 90, 89, 88, 87, 88, 89, 88, 87, 88, 87, 86, 85, 86, 85, 84, 85, 86, 87, 88,
89, 88, 89, 90, 91, 92, 91, 92, 93, 94, 95, 96, 95, 94, 93, 94, 95, 96, 95, 94
93, 92, 93, 94, 93, 92, 93, 94, 95, 94, 95, 94, 95, 94, 93, 94, 93, 94, 93, 92,
91, 90, 89, 90, 89, 88, 89, 88, 89, 88, 89, 90, 89, 90, 91, 90, 91, 90, 91, 90,
91, 92, 93, 92, 93, 94, 95, 96, 97, 98, 99, 100, 99, 100, 99, 98, 97, 98, 99,
100, 99, 98, 99, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110,
109, 108, 109, 108, 107, 108, 107, 106, 105, 106, 107, 108, 109, 110, 109, 110,
109, 110, 109, 108, 107, 108, 109, 108, 107, 106, 107, 108, 107, 106, 105, 106,
105, 106, 107, 106, 107, 108, 107, 108, 109, 110, 111, 110, 111, 112, 111, 112,
113, 112, 111, 112, 111, 110, 111, 112, 113, 114, 113, 114, 113, 114, 113, 112,
111, 110, 111, 110, 111, 110, 109, 108, 109, 110, 109, 108, 107, 106, 107, 106,
105, 106, 105, 104, 105, 106, 105, 106, 105, 106, 107, 106, 107, 106, 105, 104,
105, 104, 105, 106, 107, 106, 107, 108, 107, 108, 107, 106, 105, 106, 107, 108,
113, 112, 111, 112, 113, 114, 113, 112, 113, 112, 113, 114, 115, 116, 115, 116
117, 118, 117, 118, 119, 118, 119, 120, 119, 118, 117, 118, 117, 116, 115, 114,
113, 114, 115, 114, 113, 112, 113, 112, 111, 112, 113, 114, 115, 114, 115, 116,
115, 114, 113, 112, 113, 112, 113, 112, 111, 110, 109, 108, 109, 108, 107, 108,
109, 110, 111, 112, 111, 110, 111, 112, 113, 112, 111, 112, 113, 112, 113, 112,
113, 112, 113, 114, 113, 114, 113, 114, 113, 112, 111, 112, 111, 112, 113, 112,
111, 112, 111, 110, 111, 110, 111, 110, 109, 110, 111, 112, 113, 112, 111, 110,
109, 110, 109, 110, 111, 112, 111, 112, 111, 110, 111, 112, 111, 112, 113, 112,
111, 112, 111, 110, 111, 112, 113, 112, 113, 112, 111, 110, 109, 110, 111, 110,
109, 110, 109, 110, 111, 110, 111, 110, 111, 112, 113, 114, 115, 116, 117, 118,
117, 118, 119, 118, 119, 120, 119, 118, 117, 116, 117, 118, 119, 120, 119, 118,
119, 118, 117, 116, 117, 118, 119, 120, 119, 120, 121, 120, 119, 118, 119, 120,
121, 120, 119, 118, 119, 118, 117, 116, 115, 114, 113, 114, 115, 114, 115, 116,
115, 116, 117, 116, 115, 114, 115, 116, 115, 114, 113, 112, 111, 112, 113, 112,
```

```
111, 110, 109, 108, 109, 110, 109, 108, 107, 106, 107, 108, 109, 108, 107, 108,
109, 110, 109, 108, 107, 106, 105, 106, 105, 104, 105, 106, 105, 106, 105, 106,
107, 106, 107, 106, 105, 104, 105, 104, 105, 106, 105, 106, 107, 108, 109, 110,
111, 112, 111, 110, 111, 110, 109, 108, 107, 106, 105, 104, 103, 104, 103, 104,
103, 104, 103, 104, 105, 106, 107, 108, 109, 108, 107, 108, 107, 106, 105, 104,
103, 102, 103, 102, 103, 104, 105, 106, 107, 106, 107, 108, 107, 106, 107, 106,
105, 104, 105, 106, 105, 106, 105, 106, 105, 104, 103, 104, 103, 102, 103, 102,
103, 104, 105, 106, 105, 106, 105, 106, 107, 106, 105, 106, 107, 108, 107, 106,
105, 104, 105, 104, 105, 106, 105, 104, 103, 102, 101, 100, 101, 100, 101, 102,
101, 102, 103, 104, 105, 104, 103, 104, 105, 104, 105, 104, 103, 102, 103, 102,
101, 102, 101, 102, 101, 102, 101, 102, 101, 102, 103, 102, 101, 100, 99, 100,
101, 100, 99, 100, 101, 102, 101, 102, 103, 102, 101, 100, 101, 102, 103, 102,
101, 102, 101, 102, 103, 104, 105, 106, 105, 106, 105, 106, 107, 108, 109, 108,
109, 108, 107, 106, 105, 106, 107, 106, 105, 104, 105, 106, 105, 106, 105, 104,
105, 104, 103, 104, 103, 104, 105, 104, 103, 104, 103, 102, 103, 102, 101, 100,
99, 98, 99, 98, 97, 96, 95, 94, 95, 96, 95, 94, 93, 92, 91, 92, 91, 90, 91, 90,
91, 92, 91, 92, 93, 94, 93, 92, 93, 94, 93, 92, 93, 92, 93, 92, 91, 90, 89, 88,
87, 88, 87, 86, 87, 88, 89, 88, 87, 88, 87, 88, 87, 86, 85, 86, 87, 86, 85, 86,
87, 86, 85, 84, 85, 86, 87, 88, 89, 90, 91, 90, 91, 90, 91, 92, 93, 94, 93, 92,
93, 92, 91, 90, 89, 90, 91, 92, 93, 94, 95, 96, 95, 96, 97, 98, 97, 98, 99, 100
99, 100, 99, 98, 99, 98, 99, 98, 99, 100, 99, 98, 97, 98, 97, 96, 97, 98, 97,
96, 95, 96, 97, 96, 95, 94, 93, 92, 93, 94, 93, 92, 91, 90, 91, 90, 91, 90, 89,
90, 91, 92, 93, 92, 91, 90, 89, 88, 89, 88, 89, 90, 89, 88, 87, 88, 87, 88, 87,
86, 87, 88, 87, 88, 89, 90, 89, 90, 91, 92, 91, 90, 91, 90, 89, 88, 87, 88, 87,
86, 85, 86, 85, 86, 87, 86, 85, 84, 85, 86, 85, 86, 87, 88, 87, 86, 85, 84, 83,
84, 85, 84, 85, 84, 85, 86, 85, 86, 85, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93
92, 93, 94, 93, 92, 93, 92, 91, 90, 89, 88, 89, 88, 89, 88, 87, 88, 89, 88, 87
88, 87, 86, 87, 88, 87, 88, 89, 90, 91, 90, 89, 88, 87, 86, 85, 84, 83, 82, 83,
84, 85, 84, 83, 84, 85, 84, 85, 86, 85, 84, 83, 82, 81, 82, 83, 84, 85, 86, 85,
86, 85, 84, 85, 84, 85, 84, 83, 82, 83, 84, 83, 84, 85, 86, 85, 86, 87, 88, 87,
86, 87, 88, 87, 88, 89, 88, 89, 90, 91, 92, 93, 94, 93, 94, 93, 94, 93, 94, 95,
94, 93, 92, 91, 92, 93, 92, 93, 92, 93, 92, 91, 90, 91, 92, 91, 90, 91, 92, 93,
92, 93, 94, 93, 94, 95, 94, 95, 96, 97, 96, 97, 96, 97, 96, 95, 94, 93, 94, 95
94, 95, 94, 95, 96, 97, 98, 97, 96, 97, 96, 97, 96, 97, 98, 99, 98, 97, 98, 99,
98, 97, 98, 99, 100, 101, 100, 101, 102, 101, 100, 99, 98, 99, 100, 101, 100,
99, 98, 97, 96, 97, 96, 97, 96, 95, 94, 95, 96, 97, 98, 99, 98, 97, 96, 95, 94,
95, 96, 97, 96, 97, 96, 95, 96, 97, 98, 99, 98, 99, 98, 97, 96, 95, 96, 97, 96
97, 96, 95, 96, 97, 96, 95, 96, 95, 94, 93, 92, 91, 92, 93, 94, 95, 94, 93, 92,
93, 92, 93, 94, 93, 92, 93, 92, 93, 92, 91, 92, 91, 92, 93, 94, 95, 96, 97, 96,
95, 94, 93, 92, 91, 92, 93, 92, 91, 92, 91, 92, 93, 94, 95, 94, 93, 92, 93, 94
95, 96, 97, 98, 99, 98, 97, 96, 95, 96, 95, 96, 95, 94, 95, 94, 95, 96, 95, 94,
93, 94, 93, 92, 93, 92, 93, 94, 93, 94, 93, 94, 95, 96, 97, 96, 97, 96, 95, 96,
95, 94, 95, 96, 95, 94, 95, 96, 97, 96, 95, 94, 95, 94, 95, 94, 95, 96, 95, 94,
95, 96, 97, 98, 97, 98, 99, 98, 99, 100, 99, 98, 99, 98, 99, 98, 97, 98, 97, 98
99, 98, 97, 98, 99, 100, 99, 98, 99, 100, 101, 100, 101, 102, 101, 102, 101,
102, 103, 104, 103, 102, 103, 102, 103, 102, 101, 100, 101, 102, 103, 104, 105,
104, 105, 106, 105, 106, 107, 108, 109, 108, 107, 106, 107, 108, 109, 110, 111,
112, 113, 114, 113, 114, 115, 116, 117, 118, 117, 118, 119, 118, 119, 118, 117,
```

```
118, 119, 120, 119, 118, 119, 120, 119, 120, 119, 120, 121, 120, 121, 120, 121,
122, 121, 122, 121, 120, 121, 122, 121, 122, 123, 124, 123, 122, 123, 122, 123,
122, 123, 124, 125, 124, 125, 126, 125, 124, 125, 124, 125, 126, 125, 124, 125
124, 123, 122, 121, 120, 119, 118, 117, 118, 119, 120, 119, 118, 117, 118, 117,
118, 117, 118, 117, 116, 115, 116, 117, 118, 117, 118, 117, 118, 117, 116, 117,
118, 119, 118, 117, 116, 117, 116, 115, 114, 115, 116, 117, 116, 117, 118, 117,
118, 119, 118, 117, 118, 119, 120, 119, 118, 117, 118, 119, 118, 117, 118, 117,
118, 119, 120, 119, 120, 121, 120, 121, 120, 119, 120, 119, 118, 117, 118, 117,
116, 115, 116, 117, 116, 117, 116, 115, 114, 113, 112, 111, 110, 111, 110, 111,
112, 111, 112, 113, 114, 113, 114, 115, 116, 115, 116, 115, 114, 113, 112, 111,
110, 111, 110, 111, 112, 111, 112, 113, 112, 113, 114, 115, 114, 113, 114, 115,
114, 115, 114, 115, 114, 113, 114, 115, 116, 117, 116, 115, 116, 117, 118, 117
116, 117, 118, 119, 118, 119, 120, 119, 118, 119, 118, 117, 116, 117, 116, 117,
116, 115, 114, 113, 112, 113, 112, 111, 112, 113, 112, 111, 110, 111, 110, 109,
108, 109, 110, 111, 110, 109, 108, 107, 108, 107, 106, 107, 106, 105, 106, 105
104, 105, 104, 103, 102, 103, 102, 101, 102, 103, 104, 103, 104, 103, 102, 103,
104, 103, 102, 101, 100, 101, 102, 101, 102, 103, 102, 101, 100, 99, 98, 99,
100, 101, 102, 101, 100, 101, 100, 99, 100, 101, 100, 99, 98, 97, 98, 99, 98,
97, 96, 97, 98, 97, 96, 97, 96, 97, 98, 99, 98, 97, 98, 97, 98, 97, 98, 97, 98,
99, 98, 97, 98, 99, 100, 101, 102, 101, 102, 103, 104, 103, 104, 103, 104, 105,
104, 103, 102, 101, 100, 99, 98, 99, 100, 101, 100, 101, 102, 101, 102, 103,
102, 101, 100, 99, 100, 99, 100, 99, 98, 97, 98, 99, 100, 99, 98, 97, 98, 97,
98, 97, 98, 97, 96, 95, 96, 95, 94, 95, 96, 97, 98, 99, 98, 99, 100, 101, 102,
101, 100, 101, 100, 101, 102, 101, 102, 103, 102, 103, 104, 105, 104, 103, 104,
105, 104, 103, 102, 101, 102, 101, 100, 99, 98, 99, 100, 99, 98, 99, 98, 99,
100, 101, 100, 101, 100, 99, 98, 99, 98, 99, 98, 97, 96, 95, 96, 97, 96, 97, 98,
97, 96, 95, 94, 95, 96, 95, 96, 95, 96, 97, 98, 99, 98, 97, 96, 97, 98, 97, 98
99, 98, 97, 98, 97, 96, 97, 98, 99, 100, 101, 102, 103, 102, 103, 102, 103, 104,
105, 106, 107, 108, 107, 106, 105, 106, 105, 104, 103, 104, 105, 104, 103, 104,
105, 106, 107, 106, 105, 104, 105, 104, 105, 106, 105, 106, 107, 106, 105, 104,
103, 102, 101, 100, 101, 102, 101, 102, 103, 102, 101, 100, 99, 100, 99, 98, 99
98, 99, 98, 97, 98, 97, 96, 95, 96, 97, 96, 97, 98, 97, 96, 97, 98, 97, 96, 97,
96, 97, 98, 99, 100, 99, 100, 101, 102, 103, 104, 105, 104, 105, 106, 107, 108,
107, 108, 109, 110, 111, 110, 109, 110, 111, 112, 113, 112, 113, 112, 113, 112,
111, 110, 109, 108, 107, 106, 107, 106, 105, 104, 105, 106, 105, 104, 105, 104,
105, 104, 103, 102, 101, 100, 101, 102, 103, 104, 105, 104, 103, 104, 103, 102,
103, 102, 103, 102, 103, 102, 103, 102, 101, 102, 103, 104, 105, 106, 107, 108,
109, 108, 109, 108, 109, 108, 109, 108, 109, 110, 111, 112, 113, 114, 113, 112,
111, 112, 113, 114, 115, 116, 115, 116, 115, 114, 113, 114, 113, 112, 111, 110,
109, 110, 111, 110, 111, 110, 111, 110, 109, 108, 109, 110, 109, 110, 109, 110,
109, 108, 109, 110, 111, 112, 113, 112, 113, 112, 111, 110, 109, 108, 109, 108,
107, 108, 109, 110, 109, 110, 111, 110, 111, 112, 111, 110, 109, 108, 107, 106,
105, 104, 103, 102, 103, 104, 105, 104, 103, 102, 103, 102, 101, 102, 101, 100,
101, 102, 101, 100, 101, 100, 99, 100, 101, 102, 101, 100, 99, 98, 97, 96, 97,
98, 99, 98, 97, 96, 95, 94, 95, 96, 95, 94, 95, 94, 93, 94, 95, 94, 93, 92, 91,
92, 91, 90, 91, 92, 91, 90, 89, 90, 91, 92, 91, 90, 89, 88, 87, 86, 87, 88, 89,
88, 87, 86, 87, 86, 85, 84, 83, 82, 83, 84, 85, 86, 87, 86, 87, 88, 89, 90, 91,
92, 91, 90, 91, 90, 91, 92, 91, 92, 91, 92, 93, 92, 93, 92, 93, 94, 93, 94, 95,
```

```
94, 95, 94, 95, 94, 93, 94, 93, 92, 91, 90, 89, 90, 89, 88, 87, 88, 87, 88, 87,
86, 87, 86, 85, 86, 85, 86, 87, 86, 85, 86, 87, 88, 89, 88, 89, 88, 87, 88, 89,
88, 89, 90, 89, 88, 87, 88, 89, 88, 87, 86, 87, 88, 89, 90, 89, 90, 91, 90, 89,
88, 89, 88, 89, 90, 91, 92, 93, 94, 93, 92, 93, 92, 91, 90, 89, 90, 89, 90, 89,
88, 89, 90, 89, 90, 89, 90, 91, 90, 91, 92, 93, 92, 91, 92, 91, 90, 89, 90, 89
90, 89, 88, 87, 88, 87, 86, 87, 88, 87, 88, 89, 90, 91, 90, 91, 92, 93, 92, 91,
92, 93, 92, 91, 92, 93, 94, 95, 96, 97, 96, 97, 98, 99, 100, 99, 98, 99, 98, 97,
98, 99, 100, 101, 100, 99, 98, 97, 98, 97, 98, 97, 96, 95, 94, 93, 92, 91, 92,
93, 92, 91, 92, 93, 92, 91, 92, 93, 94, 93, 92, 91, 90, 91, 92, 93, 94, 95, 96,
95, 94, 93, 94, 93, 94, 95, 94, 95, 96, 95, 96, 97, 98, 99, 98, 99, 98, 97, 96,
95, 96, 97, 96, 95, 94, 95, 96, 95, 94, 95, 94, 95, 94, 93, 92, 93, 94, 95, 96,
97, 96, 95, 96, 95, 94, 93, 92, 93, 92, 93, 92, 91, 92, 93, 94, 95, 94, 93, 92,
93, 92, 91, 90, 89, 90, 91, 90, 89, 90, 91, 90, 89, 88, 89, 88, 89, 90, 91, 90,
91, 90, 89, 90, 91, 90, 91, 90, 89, 88, 87, 88, 89, 90, 89, 90, 89, 90, 91, 92,
91, 92, 91, 92, 91, 90, 91, 90, 89, 88, 89, 88, 89, 90, 91, 92, 91, 92, 93, 92,
93, 92, 93, 92, 93, 92, 91, 90, 89, 90, 91, 92, 91, 90, 89, 90, 91, 90, 89, 88,
87, 88, 87, 86, 87, 88, 87, 86, 85, 86, 85, 84, 83, 82, 83, 84, 83, 82, 83, 82,
81, 82, 83, 84, 85, 84, 83, 82, 81, 80, 79, 80, 79, 80, 81, 80, 81, 82, 83, 84,
83, 84, 85, 86, 85, 86, 85, 86, 87, 86, 87, 88, 89, 90, 89, 88, 89, 90, 89, 88
87, 86, 87, 88, 89, 90, 89, 88, 87, 86, 87, 88, 87, 88, 87, 86, 85, 86, 87, 86
87, 86, 87, 88, 87, 86, 85, 86, 85, 84, 83, 84, 83, 84, 85, 84, 83, 84, 83, 82,
83, 82, 83, 84, 83, 84, 83, 82, 83, 84, 85, 86, 85, 84, 83, 82, 81, 80, 81, 82,
81, 82, 83, 82, 81, 82, 83, 82, 81, 82, 81, 82, 83, 82, 83, 82, 83, 84,
83, 82, 83, 82, 83, 84, 83, 82, 81, 80, 79, 80, 79, 80, 81, 80, 81, 80, 81, 82,
81, 82, 83, 82, 81, 82, 81, 80, 79, 78, 79, 80, 81, 80, 79, 78, 79, 80, 81, 80,
79, 78, 77, 76, 75, 76, 75, 76, 77, 76, 77, 76, 75, 74, 73, 74, 73, 74, 73, 74,
75, 74, 73, 74, 73, 74, 75, 76, 77, 78, 79, 78, 79, 78, 79, 78, 79, 78, 79, 80,
81, 80, 81, 80, 79, 78, 79, 80, 79, 78, 77, 76, 75, 76, 75, 74, 73, 74, 75, 76,
75, 74, 73, 74, 75, 76, 77, 76, 75, 76, 77, 76, 77, 78, 77, 76, 75, 76, 77, 78,
79, 78, 77, 76, 77, 76, 75, 74, 73, 74, 73, 74, 73, 72, 73, 72, 73, 74, 75, 76,
75, 76, 77, 76, 75, 74, 73, 74, 75, 74, 75, 76, 75, 76, 75, 74, 73, 74, 75, 74,
73, 74, 75, 76, 75, 74, 75, 76, 77, 76, 75, 74, 73, 72, 71, 72, 71, 72, 73, 72,
73, 74, 73, 72, 71, 72, 71, 72, 73, 74, 75, 76, 77, 76, 75, 74, 75, 74, 75, 76,
77, 78, 77, 76, 77, 76, 75, 76, 77, 76, 77, 76, 77, 78, 79, 78, 77, 78, 79, 80,
79, 80, 79, 78, 77, 76, 77, 76, 77, 76, 77, 78, 77, 76, 75, 76, 77, 78, 77, 76,
77, 78, 79, 78, 79, 80, 79, 78, 77, 78, 79, 80, 79, 78, 77, 76, 75, 76, 75, 76
77, 78, 77, 76, 75, 74, 73, 74, 75, 74, 73, 74, 73, 74, 75, 74, 73, 72, 73, 72,
71, 72, 73, 72, 71, 70, 69, 68, 67, 68, 67, 68, 69, 70, 71, 72, 73, 72, 71, 72,
71, 70, 71, 70, 69, 68, 67, 68, 67, 66, 67, 66, 65, 66, 67, 68, 69, 70, 69, 68,
69, 70, 71, 72, 73, 74, 75, 74, 73, 74, 75, 74, 75, 76, 75, 76, 77, 76, 77, 78,
77, 76, 77, 76, 75, 76, 77, 76, 75, 74, 73, 72, 71, 70, 71, 72, 73, 72, 71, 72,
71, 70, 69, 68, 67, 66, 65, 64, 65, 64, 63, 64, 63, 64, 65, 64, 65, 64, 63, 64,
65, 66, 67, 68, 69, 70, 71, 72, 71, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80,
81, 80, 81, 80, 81, 80, 79, 80, 81, 80, 79, 80, 81, 82, 81, 80, 79, 78, 79, 78,
79, 78, 79, 78, 77, 76, 77, 78, 77, 78, 77, 78, 79, 80, 79, 78, 77, 78, 77, 78,
77, 76, 77, 78, 77, 76, 77, 76, 77, 76, 75, 76, 77, 76, 75, 74, 75, 74, 73, 74,
73, 74, 75, 76, 75, 76, 77, 76, 77, 76, 77, 78, 79, 78, 79, 78, 77, 78, 77, 76
75, 76, 75, 76, 77, 78, 79, 80, 79, 80, 81, 80, 79, 78, 77, 78, 77, 78, 77, 78,
```

```
79, 80, 81, 82, 81, 82, 83, 82, 81, 80, 79, 78, 79, 78, 77, 78, 77, 78, 79, 78,
79, 80, 81, 80, 79, 80, 79, 78, 79, 78, 79, 80, 81, 80, 79, 80, 79, 80, 79, 80,
81, 80, 81, 82, 81, 82, 83, 82, 81, 80, 79, 78, 79, 78, 77, 76, 75, 74, 73, 72,
73, 72, 71, 70, 71, 70, 69, 68, 69, 70, 71, 70, 71, 72, 73, 72, 71, 72, 71, 70,
69, 68, 67, 68, 69, 68, 69, 68, 69, 70, 71, 70, 69, 68, 67, 68, 69, 68, 69, 68
67, 68, 69, 68, 69, 70, 69, 70, 69, 70, 69, 70, 71, 72, 71, 70, 69, 70, 71, 72,
73, 72, 73, 74, 75, 76, 77, 78, 77, 76, 75, 76, 77, 76, 77, 76, 77, 78, 79, 78,
79, 78, 79, 80, 79, 78, 79, 80, 79, 80, 81, 80, 81, 82, 81, 82, 81, 82, 83, 84,
85, 84, 85, 84, 85, 86, 85, 86, 87, 88, 87, 88, 89, 90, 91, 92, 91, 90, 91, 90,
89, 90, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 97, 96, 95, 94, 93, 92, 91, 92,
93, 94, 93, 92, 91, 92, 91, 92, 91, 90, 91, 90, 91, 92, 93, 94, 95, 96, 95, 94,
93, 92, 93, 92, 91, 90, 89, 88, 87, 86, 85, 86, 85, 86, 85, 84, 85, 86, 87, 88
89, 90, 91, 90, 91, 90, 89, 90, 91, 90, 91, 90, 91, 92, 93, 94, 93, 94, 95, 94
95, 94, 93, 94, 95, 94, 93, 92, 91, 90, 89, 88, 87, 86, 87, 88, 87, 88, 87, 88,
87, 86, 85, 84, 85, 86, 85, 84, 85, 84, 85, 86, 87, 88, 87, 88, 89, 88, 89, 90,
89, 90, 89, 90, 89, 90, 91, 92, 91, 90, 89, 88, 87, 86, 87, 88, 89, 90, 91, 92,
93, 94, 95, 96, 97, 98, 99, 100, 99, 98, 97, 96, 95, 96, 97, 96, 97, 96, 95, 96
97, 98, 97, 98, 97, 96, 95, 96, 95, 96, 95, 96, 97, 98, 97, 98, 99, 98, 97, 98,
97, 98, 97, 96, 97, 96, 97, 96, 97, 98, 97, 98, 99, 98, 99, 98, 99, 98, 97, 98,
97, 98, 99, 98, 99, 100, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 107,
106, 105, 104, 105, 104, 103, 104, 105, 106, 105, 106, 105, 106, 107, 108, 107,
106, 105, 106, 107, 108, 109, 110, 109, 110, 109, 108, 107, 106, 107, 106, 107,
108, 109, 108, 107, 108, 107, 106, 107, 106, 107, 108, 109, 110, 109, 110, 111,
112, 113, 114, 113, 114, 113, 112, 113, 114, 115, 116, 117, 118, 117, 116, 117,
118, 117, 116, 115, 116, 117, 118, 117, 118, 117, 116, 115, 116, 115, 116, 115,
114, 113, 112, 111, 112, 111, 112, 113, 114, 115, 116, 117, 116, 117, 116, 115,
116, 115, 114, 113, 114, 113, 114, 113, 114, 115, 116, 115, 114, 113, 114, 113,
112, 111, 112, 113, 114, 115, 114, 115, 114, 113, 114, 115, 116, 117, 116, 117,
118, 117, 116, 115, 114, 113, 112, 111, 112, 113, 112, 111, 110, 111, 110, 111,
110, 109, 108, 107, 106, 107, 108, 107, 108, 107, 108, 107, 106, 107, 108, 109,
108, 109, 108, 107, 108, 107, 106, 105, 106, 105, 106, 107, 106, 107, 108, 107,
106, 105, 104, 105, 104, 103, 102, 101, 102, 103, 102, 101, 102, 101, 100, 101,
102, 101, 100, 101, 102, 101, 100, 99, 100, 101, 100, 101, 100, 99, 100, 101,
100, 101, 100, 99, 100, 101, 100, 101, 102, 101, 102, 103, 102, 101, 100, 101,
102, 103, 102, 103, 102, 103, 102, 103, 104, 105, 104, 105, 106, 105, 106, 107,
108, 107, 108, 107, 108, 109, 110, 109, 110, 109, 108, 107, 108, 109, 108, 109,
108, 109, 108, 107, 106, 105, 104, 103, 102, 103, 104, 105, 106, 107, 106, 107,
108, 109, 110, 111, 110, 109, 108, 107, 108, 107, 106, 107, 106, 105, 106, 105,
104, 105, 104, 105, 104, 103, 102, 103, 102, 101, 102, 101, 102, 101, 100, 101,
102, 103, 102, 101, 102, 101, 102, 101, 102, 101, 100, 101, 100, 101, 100, 99,
100, 99, 98, 97, 96, 95, 94, 95, 94, 95, 94, 95, 96, 97, 96, 95, 94, 95, 96, 97
98, 99, 100, 99, 98, 97, 96, 97, 96, 97, 96, 97, 96, 97, 96, 97, 96, 97, 96, 97,
98, 97, 96, 97, 96, 95, 94, 95, 96, 97, 98, 99, 100, 101, 100, 101, 100, 101,
100, 99, 100, 99, 98, 97, 98, 97, 98, 99, 100, 99, 100, 99, 100, 99, 98, 99,
100, 101, 102, 101, 102, 103, 102, 101, 100, 101, 100, 99, 98, 99, 98, 99, 98
97, 98, 97, 98, 97, 98, 97, 96, 97, 96, 95, 94, 93, 92, 91, 90, 89, 88, 89, 88,
89, 88, 87, 86, 87, 88, 89, 88, 89, 90, 89, 90, 91, 92, 93, 94, 95, 96, 95, 96
95, 96, 97, 96, 95, 94, 93, 94, 95, 96, 95, 94, 95, 96, 97, 98, 97, 98, 97, 98,
```

97, 96, 95, 96, 97, 98, 97, 98, 99, 98, 97, 96, 95, 96, 97, 96, 97, 98, 99, 100, 99, 100, 101, 102, 103, 102, 103, 102, 103, 104, 105, 106, 105, 104, 105, 104, 105, 106, 107, 106, 105, 104, 105, 104, 105, 104, 103, 104, 103, 102, 103, 104, 105, 104, 105, 104, 103, 102, 103, 104, 105, 104, 103, 102, 101, 102, 103, 102, 101, 100, 101, 100, 99, 100, 99, 98, 97, 98, 97, 96, 95, 96, 97, 96, 97, 98, 97, 96, 97, 96, 97, 98, 97, 98, 99, 98, 99, 100, 99, 98, 99, 98, 97, 98, 97, 98, 99, 98, 99, 100, 101, 100, 101, 100, 99, 100, 101, 102, 103, 102, 101, 102, 101, 100, 99, 98, 97, 98, 99, 98, 99, 100, 99, 98, 97, 96, 95, 96, 95, 96, 97, 96, 95, 96, 97, 98, 97, 96, 95, 96, 97, 98, 99, 98, 97, 96, 97, 96, 95, 94, 93, 92, 91, 92, 93, 92, 93, 92, 93, 94, 93, 94, 93, 92, 93, 94, 93, 94, 95, 96, 97, 98, 97, 98, 97, 96, 97, 96, 95, 96, 97, 98, 99, 100, 101, 100, 99, 98, 97, 98, 99, 98, 97, 98, 97, 98, 97, 98, 99, 100, 101, 102, 103, 104, 103, 102, 101, 102, 103, 104, 105, 106, 107, 108, 107, 108, 107, 108, 109, 110, 111, 110, 109, 108, 107, 108, 107, 108, 109, 110, 109, 110, 111, 112, 111, 110, 109, 110, 111, 110, 109, 110, 111, 112, 113, 112, 111, 112, 111, 112, 111, 112, 111, 110, 109, 108, 109, 108, 109, 110, 109, 108, 109, 108, 107, 108, 109, 108, 109, 108, 107, 108, 109, 108, 109, 110, 111, 112, 113, 112, 113, 112, 113, 114, 115, 114, 115, 116, 115, 114, 115, 114, 113, 112, 111, 112, 111, 110, 109, 110, 109, 108, 109, 108, 109, 110, 109, 110, 109, 108, 109, 110, 111, 110, 109, 108, 109, 108, 107, 106, 107, 106, 105, 106, 107, 108, 107, 106, 107, 106, 107, 106, 107, 108, 107, 106, 107, 106, 107, 106, 105, 104, 105, 106, 107, 106, 105, 104, 105, 104, 105, 106, 107, 106, 105, 104, 103, 102, 101, 100, 101, 100, 101, 100, 99, 100, 101, 100, 101, 100, 101, 102, 101, 102, 101, 102, 101, 102, 101, 102, 101, 102, 103, 104, 105, 106, 105, 104, 103, 102, 101, 102, 103, 104, 103, 104, 103, 104, 103, 102, 101, 100, 99, 98, 99, 100, 101, 100, 99, 100, 101, 100, 101, 102, 101, 100, 101, 102, 103, 102, 101, 102, 103, 102, 101, 102, 101, 102, 103, 104, 103, 102, 103, 102, 103, 102, 101, 102, 101, 100, 101, 102, 101, 102, 103, 102, 101, 102, 103, 104, 105, 104, 105, 106, 105, 104, 103, 104, 105, 104, 103, 104, 103, 104, 105, 106, 105, 104, 103, 102, 103, 104, 105, 104, 103, 102, 101, 102, 101, 102, 103, 104, 105, 104, 103, 102, 101, 102, 101, 100, 101, 102, 103, 104, 105, 106, 107, 108, 107, 106, 107, 106, 105, 104, 105, 104, 103, 102, 101, 100, 99, 98, 99, 100, 101, 100, 101, 102, 101, 102, 101, 100, 99, 98, 99, 100, 101, 100, 101, 102, 103, 104, 103, 104, 105, 106, 107, 106, 107, 108, 109, 108, 107, 106, 107, 108, 107, 106, 107, 108, 109, 110, 111, 110, 109, 108, 107, 108, 107, 106, 105, 106, 105, 104, 105, 106, 105, 106, 105, 104, 105, 106, 107, 106, 107, 106, 105, 106, 107, 108, 109, 110, 109, 110, 109, 110, 109, 108, 109, 110, 109, 110, 109, 110, 109, 108, 109, 108, 109, 108, 107, 108, 107, 106, 107, 108, 109, 108, 109, 108, 109, 108, 107, 108, 107, 106, 107, 108, 109, 110, 109, 108, 107, 106, 105, 106, 105, 104, 105, 106, 105, 104, 103, 102, 101, 100, 99, 98, 99, 100, 99, 100, 101, 100, 101, 102, 101, 102, 103, 104, 105, 104, 103, 102, 101, 102, 103, 102, 101, 100, 99, 98, 99, 100, 99, 98, 97, 98, 99, 98, 97, 96, 97, 96, 95, 94, 95, 96, 95, 94, 95, 94, 93, 92, 93, 92, 93, 94, 93, 94, 95, 94, 93, 94, 93, 94, 95, 96, 95, 96, 97, 98, 97, 96, 97, 98, 97, 98, 99, 100, 101, 102, 103, 102, 101, 100, 101, 102, 101, 102, 103, 104, 103, 102, 101, 100, 99, 100, 99, 100, 99, 100, 101, 102, 101, 100, 99, 98, 99, 98, 99, 98, 97, 96, 95, 96, 97, 96, 97, 96, 97, 98, 97, 96, 97, 98, 97, 98, 99, 98, 97, 98, 99, 98, 99, 98, 97, 96, 97, 98, 99, 98, 97, 98, 97, 96, 97, 96, 97, 96, 95, 96, 95, 94, 95, 94, 95, 94, 93, 94, 93, 94, 95, 96, 97, 98, 97, 98, 99, 100, 101, 102, 103, 102, 101, 100, 101, 102,

103, 104, 103, 104, 103, 102, 101, 102, 101, 102, 103, 102, 101, 100, 101, 100, 101, 102, 101, 100, 99, 98, 99, 100, 99, 98, 99, 100, 101, 100, 99, 98, 99, 100, 101, 100, 99, 98, 99, 98, 99, 98, 99, 100, 99, 98, 97, 96, 95, 96, 95, 96, 95, 94, 93, 92, 91, 92, 91, 90, 89, 88, 87, 88, 89, 90, 91, 90, 89, 90, 91, 92, 91, 92, 93, 94, 93, 92, 93, 92, 93, 94, 95, 96, 95, 94, 93, 94, 93, 94, 93, 94, 93 92, 93, 94, 93, 92, 93, 92, 91, 92, 93, 94, 95, 96, 97, 96, 97, 96, 97, 98, 97, 96, 95, 96, 95, 96, 95, 94, 93, 92, 91, 90, 91, 92, 93, 92, 93, 92, 93, 94, 93, 92, 93, 92, 93, 92, 93, 92, 91, 92, 91, 90, 89, 88, 87, 88, 87, 88, 87, 86, 87, 86, 85, 84, 85, 84, 83, 82, 83, 84, 83, 84, 85, 86, 85, 84, 85, 84, 85, 84, 85, 86, 87, 88, 89, 88, 89, 90, 91, 90, 89, 90, 91, 92, 93, 94, 93, 92, 93, 94, 93, 94, 95, 96, 97, 96, 97, 98, 99, 98, 97, 98, 97, 98, 97, 96, 97, 98, 97, 98, 97, 98, 99, 100, 101, 100, 99, 98, 99, 100, 99, 100, 101, 100, 101, 102, 103, 102, 101, 100, 101, 100, 99, 98, 99, 100, 101, 102, 101, 102, 103, 102, 103, 101, 100, 99, 98, 97, 96, 97, 96, 95, 94, 93, 94, 95, 96, 97, 96, 95, 96, 97, 96, 95, 94, 93, 92, 93, 92, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 101, 102, 103, 102, 101, 100, 99, 100, 101, 100, 99, 100, 101, 100, 99, 98, 99, 98, 99, 98, 97, 98, 99, 98, 97, 96, 97, 98, 99, 98, 97, 96, 97, 96, 95, 96, 95, 94, 93, 92, 93, 94, 95, 94, 93, 94, 95, 94, 95, 96, 95, 96, 95, 94, 93, 94, 93, 94, 95, 96, 95, 96, 97, 96, 97, 98, 99, 98, 99, 100, 99, 100, 101, 102, 101, 100, 99, 98, 99, 100, 99, 100, 99, 98, 97, 96, 95, 94, 95, 94, 95, 96, 95, 94, 93, 92, 93, 92, 91, 92, 91, 90, 89, 90, 91, 92, 93, 94, 93, 94, 95, 96, 97, 96, 95, 94, 93, 94, 93, 92, 91, 90, 91, 92, 91, 92, 93, 92, 93, 94, 93, 94, 95, 94, 95, 94, 95, 94, 93, 94, 95, 96, 97, 98, 99, 98, 99, 98, 99, 100, 99, 100, 99, 100, 101, 102, 103, 104, 103, 104, 105, 104, 105, 106, 105, 106, 107, 106, 107, 108, 107, 106, 107, 108, 107, 106, 105, 106, 105, 106, 107, 108, 109, 110, 111, 110, 109, 110, 111, 110, 109, 108, 109, 110, 111, 110, 111, 110, 109, 108, 109, 108, 107, 108, 107, 108, 109, 108, 107, 106, 105, 104, 105, 104, 105, 106, 107, 106, 105, 106, 107, 108, 107, 108, 107, 106, 107, 108, 107, 108, 107, 106, 105, 106, 107, 106, 107, 108, 109, 110, 109, 108, 109, 110, 111, 112, 111, 112, 113, 114, 113, 112, 111, 110, 109, 110, 109, 108, 107, 106, 107, 108, 107, 106, 107, 106, 105, 104, 105, 106, 107, 106, 107, 106, 107, 106, 105, 106, 107, 108, 109, 108, 107, 106, 107, 106, 107, 106, 105, 104, 105, 104, 103, 104, 103, 102, 101, 102, 103, 104, 105, 104, 103, 102, 103, 104, 103, 102, 101, 100, 101, 100, 99, 100, 99, 100, 101, 100, 101, 102, 101, 102, 103, 102, 103, 102, 101, 102, 101, 100, 99, 100, 101, 102, 103, 104, 103, 102, 101, 102, 101, 102, 101, 102, 103, 102, 101, 102, 103, 104, 103, 102, 103, 102, 103, 104, 105, 104, 105, 104, 105, 104, 103, 104, 103, 102, 103, 102, 101, 100, 99, 98, 99, 98, 99, 100, 99, 98, 99, 100, 101, 100, 101, 102, 101, 100, 101, 102, 101, 102, 101, 100, 101, 100, 99, 98, 97, 98, 99, 100, 101, 100, 101, 100, 101, 102, 101, 102, 103, 104, 105, 104, 105, 106, 107, 106, 105, 104, 103, 102, 101, 102, 103, 104, 103, 102, 103, 102, 101, 100, 101, 100, 99, 100, 99, 98, 99, 98, 99, 100, 99, 100, 99, 100, 101, 102, 101, 102, 101, 102, 103, 104, 105, 104, 103, 104, 105, 106, 107, 106, 105, 106, 105, 106, 105, 106, 105, 104, 105, 104, 105, 104, 103, 102, 101, 100, 101, 100, 101, 100, 101, 100, 101, 102, 101, 100, 99, 98, 97, 96, 97, 96, 97, 98, 99, 100, 101, 100, 99, 100, 101, 100, 101, 102, 103, 102, 101, 100, 99, 98 97, 98, 99, 100, 99, 98, 99, 98, 99, 98, 97, 98, 99, 100, 99, 100, 101, 100, 99, 98, 99, 98, 97, 96, 95, 94, 93, 94, 95, 94, 95, 94, 93, 92, 91, 90, 91, 90, 89 90, 89, 88, 89, 88, 89, 88, 89, 88, 87, 86, 87, 86, 85, 86, 85, 84, 83, 84, 83,

```
84, 83, 82, 83, 84, 83, 82, 81, 82, 83, 84, 85, 86, 85, 84, 85, 84, 85, 84, 83,
82, 83, 82, 81, 80, 81, 82, 83, 82, 83, 84, 85, 86, 87, 86, 85, 86, 87, 88, 87,
86, 87, 88, 87, 86, 87, 88, 89, 90, 89, 88, 87, 88, 89, 90, 91, 92, 91, 92, 93,
92, 91, 90, 89, 90, 89, 90, 89, 88, 87, 88, 89, 90, 91, 90, 91, 90, 91, 90, 91,
90, 91, 90, 91, 92, 91, 92, 93, 94, 95, 94, 95, 96, 97, 98, 99, 100, 101, 102,
103, 104, 105, 106, 105, 106, 105, 106, 105, 106, 107, 106, 107, 108, 109, 108,
109, 110, 111, 112, 113, 112, 111, 112, 113, 112, 111, 112, 111, 112, 111, 110,
109, 108, 107, 106, 105, 104, 105, 104, 105, 106, 105, 104, 103, 104, 103, 102,
101, 100, 101, 102, 101, 100, 99, 100, 101, 102, 101, 100, 101, 100, 99, 98, 99
98, 99, 98, 97, 98, 97, 96, 95, 96, 97, 96, 95, 96, 95, 96, 97, 98, 97, 96, 95,
96, 97, 96, 97, 98, 99, 100, 101, 102, 101, 102, 101, 102, 103, 102, 103, 104,
105, 104, 103, 104, 103, 102, 101, 100, 99, 100, 99, 100, 99, 100, 99, 100, 101
102, 103, 102, 101, 100, 99, 98, 99, 100, 101, 100, 99, 98, 97, 98, 99, 100, 99
98, 97, 98, 97, 96, 97, 96, 95, 94, 95, 96, 97, 96, 97, 96, 95, 94, 95, 96, 95,
94, 95, 94, 95, 96, 95, 94, 95, 96, 95, 96, 97, 96, 97, 98, 97, 96, 95, 94, 95,
96, 95, 94, 95, 96, 97, 98, 97, 98, 99, 100, 99, 100, 99, 100, 99, 98, 97, 96,
97, 98, 97, 98, 97, 98, 97, 96, 95, 96, 97, 96, 95, 94, 93, 92, 91, 92, 91, 92,
93, 92, 91, 92, 93, 94, 95, 96, 95, 96, 97, 96, 95, 94, 93, 94, 93, 92, 93, 92,
93, 92, 93, 94, 93, 92, 93, 92, 91, 90, 89, 88, 87, 88, 89, 90, 89, 90, 91, 90
91, 92, 91, 92, 93, 92, 93, 92, 91, 90, 91, 92, 91, 90, 91, 92, 91, 90, 89, 90,
89, 88, 89, 90, 91, 92, 93, 92, 91, 90, 89, 90, 91, 92, 93, 94, 93, 94, 95, 94
95, 94, 93, 94, 95, 96, 95, 94, 95, 94, 95, 96, 97, 98, 99, 100, 99, 98, 97, 98
97, 96, 97, 96, 95, 96, 97, 96, 97, 96, 95, 96, 95, 96, 97, 98, 99, 98, 97, 98,
97, 98, 97, 96, 97, 96, 97, 96, 95, 94, 93, 92, 93, 92, 93, 94, 95, 96, 97, 96,
97, 96, 97, 96, 97, 98, 97, 98, 97, 96, 97, 96, 95, 96, 95, 96, 97, 96, 95, 96,
95, 94, 93, 92, 91, 90, 91, 92, 93, 92, 91, 92, 93, 94, 93, 92, 91, 92, 93, 94
93, 94, 93, 92, 91, 92, 91, 90, 91, 90, 89, 88, 89, 90, 89, 88, 89, 88, 89, 88,
87, 86, 87, 86, 85, 86, 85, 86, 87, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96
97, 98, 99, 98, 97, 98, 97, 98, 99, 100, 101, 102, 103, 102, 101, 100, 101, 102
103, 104, 105, 106, 105, 106, 105, 106, 107, 106, 107, 106, 105, 106, 107, 106,
105, 106, 105, 104, 103, 102, 101, 100, 101, 100, 101, 102, 103, 104, 103, 104,
105, 106, 107, 108, 109, 110, 111, 110, 111, 112, 111, 110, 111, 110, 111, 110,
111, 112, 113, 114, 113, 114, 115, 114, 113, 114, 113, 112, 113, 114, 115, 116,
115, 116, 115, 116, 117, 116, 117, 118, 117, 116, 115, 114, 113, 112, 113, 112,
113, 114, 115, 114, 115, 114, 115, 114, 113, 114, 115, 114, 115, 114, 115, 116,
117, 116, 117, 118, 117, 118, 117, 118, 119, 120, 121, 120, 121, 122, 123, 122,
121, 122, 123, 122, 123, 122, 123, 124, 123, 122, 121, 120, 119, 120, 121, 120,
121, 122, 123, 124, 123, 124, 123, 122, 123, 124, 125, 126, 127, 126, 127, 128,
127, 126, 125, 126, 127, 126, 125, 126, 125, 124, 123, 124, 123, 122, 121, 122,
121, 122, 123, 124, 125, 124, 123, 122, 121, 120, 121, 122, 123, 122, 123, 122,
123, 124, 125, 126, 125, 126, 125, 124, 125, 124, 125, 124, 123, 122, 123, 124,
123, 122, 123, 122, 121, 122, 121, 120, 119, 118, 119, 118, 117, 118, 119, 118,
117, 116, 115, 116, 117, 116, 117, 116, 117, 118, 119, 118, 119, 120, 121, 120,
121, 122, 123, 124, 125, 124, 125, 126, 125, 124, 123, 124, 125, 124, 125, 124,
125, 124, 123, 124, 125, 126, 125, 126, 127, 126, 127, 126, 125, 124, 125, 124,
123, 122, 123, 122, 121, 122, 121, 122, 123, 124, 123, 124, 125, 126, 127, 128,
129, 128, 129, 130, 129, 130, 129, 130, 131, 132, 131, 132, 131, 130, 129, 128,
127, 126, 127, 126, 125, 124, 125, 124, 125, 124, 123, 122, 121, 120, 119, 120,
```

```
119, 118, 117, 116, 117, 118, 117, 116, 117, 116, 117, 118, 117, 118, 117, 116,
115, 114, 113, 112, 111, 110, 109, 108, 107, 108, 107, 106, 107, 108, 107, 108,
109, 110, 109, 108, 109, 110, 109, 108, 107, 106, 107, 106, 105, 106, 107, 108,
109, 108, 109, 110, 109, 110, 109, 108, 109, 110, 111, 112, 111, 112, 111, 110,
109, 110, 111, 110, 111, 110, 111, 112, 113, 112, 111, 110, 109, 108, 109, 108
109, 108, 107, 106, 107, 108, 107, 108, 107, 106, 107, 106, 105, 104, 105, 104,
105, 104, 103, 102, 103, 102, 103, 102, 101, 102, 101, 102, 101, 100, 99, 100,
101, 100, 99, 98, 97, 96, 95, 96, 95, 96, 97, 96, 97, 98, 99, 100, 99, 100, 101
100, 99, 98, 97, 98, 97, 96, 97, 98, 99, 100, 101, 100, 101, 102, 101, 102, 103
102, 101, 102, 101, 100, 101, 102, 103, 104, 103, 102, 103, 102, 103, 104, 105,
106, 107, 108, 107, 106, 105, 106, 105, 106, 107, 108, 107, 108, 109, 110, 109,
108, 109, 110, 111, 110, 109, 110, 109, 110, 109, 110, 109, 108, 107, 108, 109,
110, 111, 110, 109, 108, 107, 106, 105, 106, 107, 106, 105, 104, 103, 104, 103,
104, 103, 104, 105, 106, 105, 106, 107, 106, 105, 104, 105, 104, 103, 104, 103,
104, 103, 102, 101, 100, 99, 100, 99, 98, 97, 98, 99, 98, 99, 98, 99, 98, 97,
96, 95, 94, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 101, 100, 101, 102, 101,
100, 101, 102, 101, 102, 101, 100, 101, 100, 99, 100, 101, 102, 103, 102, 103,
102, 103, 102, 103, 104, 103, 102, 103, 102, 101, 100, 99, 100, 99, 98, 99, 98,
97, 98, 97, 98, 97, 96, 97, 98, 97, 98, 97, 96, 97, 96, 95, 96, 97, 98, 99, 100
99, 98, 97, 98, 99, 100, 101, 102, 101, 102, 103, 102, 101, 100, 99, 98, 97, 96,
97, 98, 97, 96, 95, 96, 95, 96, 95, 94, 95, 94, 93, 94, 93, 92, 91, 92, 91, 92,
93, 94, 93, 94, 95, 96, 97, 98, 97, 96, 97, 98, 99, 100, 101, 102, 103, 104,
105, 104, 103, 104, 105, 104, 105, 104, 105, 104, 103, 102, 103, 104, 103, 104,
103, 104, 105, 104, 105, 106, 105, 104, 105, 106, 107, 108, 109, 110, 111, 112,
111, 112, 111, 110, 111, 112, 111, 110, 109, 110, 109, 110, 109, 108, 109, 110,
109, 108, 107, 108, 109, 110, 111, 110, 111, 110, 111, 110, 109, 108, 109, 108,
107, 108, 107, 106, 105, 104, 103, 102, 103, 104, 103, 102, 101, 100, 101, 100,
99, 98, 97, 98, 97, 98, 97, 98, 97, 96, 97, 96, 95, 94, 95, 96, 97, 98, 97, 96,
95, 96, 95, 96, 95, 96, 97, 98, 99, 100, 99, 98, 99, 98, 99, 100, 99, 98, 99,
100, 99, 98, 99, 100, 101, 102, 101, 102, 103, 104, 105, 104, 105, 104, 103,
104, 103, 104, 103, 104, 103, 104, 105, 106, 105, 104, 105, 106, 105, 106, 105
104, 103, 104, 103, 104, 105, 104, 105, 106, 105, 104, 103, 102, 103, 102, 101,
102, 103, 102, 103, 102, 101, 100, 99, 100, 101, 102, 103, 104, 105, 106, 105,
106, 107, 108, 109, 110, 109, 108, 109, 108, 109, 110, 111, 110, 111, 112, 111,
110, 109, 108, 109, 108, 107, 108, 109, 110, 111, 110, 111, 112, 113, 114, 115,
116, 117, 118, 117, 116, 115, 114, 115, 116, 117, 118, 117, 116, 117, 116, 117,
116, 115, 114, 113, 112, 111, 112, 111, 112, 111, 110, 111, 112, 113, 112, 111,
112, 111, 112, 111, 110, 111, 112, 111, 110, 109, 108, 109, 108, 109, 110, 111,
112, 113, 114, 115, 116, 115, 116, 115, 116, 117, 116, 117, 116, 117, 118, 119,
118, 117, 118, 119, 120, 119, 118, 119, 120, 119, 118, 117, 118, 117, 118, 117
116, 115, 114, 113, 112, 111, 110, 111, 112, 113, 112, 113, 114, 115, 116, 117,
118, 117, 116, 115, 116, 115, 114, 115, 114, 113, 112, 113, 112, 113, 112, 113,
112, 113, 114, 115, 116, 117, 118, 117, 116, 115, 116, 117, 116, 115, 116, 115
116, 117, 118, 117, 118, 119, 120, 121, 122, 123, 124, 123, 122, 123, 122, 121,
122, 121, 122, 123, 124, 123, 122, 123, 124, 125, 126, 125, 126, 127, 128, 129,
128, 129, 130, 131, 132, 131, 130, 131, 132, 131, 132, 133, 134, 133, 134, 135,
136, 135, 134, 135, 134, 135, 136, 135, 134, 133, 134, 135, 134, 133, 132, 131,
130, 129, 128, 127, 126, 127, 126, 125, 126, 125, 124, 123, 122, 121, 120, 121,
```

```
122, 123, 122, 123, 122, 123, 124, 125, 124, 123, 122, 121, 122, 123, 124, 123,
122, 123, 124, 123, 124, 123, 122, 121, 122, 123, 124, 125, 124, 125, 124, 125,
126, 125, 124, 123, 122, 121, 122, 123, 124, 125, 126, 125, 126, 127, 128, 127,
128, 129, 128, 129, 130, 129, 130, 129, 128, 127, 128, 127, 126, 125, 124, 125,
124, 123, 124, 125, 124, 123, 124, 123, 124, 125, 124, 125, 126, 127, 126, 127
128, 127, 126, 127, 126, 125, 124, 123, 122, 121, 122, 123, 124, 125, 126, 125,
124, 123, 122, 123, 124, 125, 126, 127, 126, 125, 126, 127, 126, 127, 126, 127,
126, 127, 126, 125, 126, 125, 124, 123, 122, 121, 122, 121, 120, 119, 120, 119,
118, 119, 118, 117, 118, 117, 116, 115, 114, 113, 114, 115, 116, 115, 114, 113,
112, 111, 112, 111, 110, 109, 108, 107, 106, 107, 108, 109, 110, 111, 112, 111,
112, 113, 114, 113, 112, 111, 112, 111, 110, 111, 110, 109, 108, 109, 108, 107,
108, 107, 106, 105, 104, 103, 104, 105, 106, 105, 104, 103, 102, 103, 104, 105,
104, 103, 104, 103, 104, 105, 104, 103, 104, 105, 106, 105, 106, 105, 104, 105,
104, 103, 104, 105, 104, 103, 104, 105, 104, 103, 104, 105, 104, 105, 104, 103,
104, 103, 102, 101, 100, 101, 100, 101, 100, 99, 100, 101, 100, 101, 102, 101,
100, 99, 98, 97, 98, 99, 98, 97, 98, 97, 98, 97, 96, 97, 96, 95, 94, 93, 94, 95
96, 97, 96, 95, 94, 93, 92, 93, 92, 93, 94, 93, 94, 95, 96, 97, 96, 95, 96, 97,
98, 99, 100, 101, 100, 101, 102, 103, 104, 105, 106, 105, 104, 103, 104, 105,
106, 107, 106, 105, 104, 105, 106, 105, 104, 103, 102, 103, 104, 103, 102, 101,
100, 101, 100, 99, 100, 99, 100, 99, 100, 99, 98, 99, 100, 101, 102, 103, 102,
101, 102, 103, 104, 105, 106, 107, 106, 107, 106, 107, 108, 107, 108, 107, 108,
107, 108, 107, 106, 107, 108, 109, 108, 109, 108, 107, 106, 107, 106, 105, 104,
103, 102, 101, 100, 99, 100, 99, 100, 99, 98, 97, 96, 95, 96, 95, 96, 97, 98,
97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 110,
109, 110, 109, 110, 111, 110, 109, 108, 107, 108, 107, 108, 107, 106, 105, 104,
105, 104, 105, 104, 105, 106, 107, 108, 109, 110, 109, 108, 109, 110, 109, 110,
111, 112, 111, 110, 111, 110, 109, 110, 111, 112, 113, 114, 115, 114, 113, 112,
113, 112, 113, 112, 113, 114, 115, 116, 117, 116, 115, 114, 115, 114, 113, 112,
113, 112, 111, 112, 113, 112, 113, 112, 111, 110, 111, 110, 109, 110, 111, 112,
113, 112, 111, 110, 111, 110, 111, 112, 113, 112, 113, 112, 111, 110, 109, 108,
107, 108, 109, 108, 107, 106, 107, 106, 107, 106, 105, 106, 105, 106, 105, 106,
107, 108, 109, 108, 107, 106, 107, 108, 109, 108, 107, 106, 105, 106, 105, 106,
107, 108, 107, 108, 107, 108, 109, 110, 109, 110, 111, 110, 111, 110, 111, 110,
111, 112, 113, 112, 111, 110, 109, 110, 111, 112, 111, 112, 111, 110, 109, 110,
109, 108, 107, 108, 107, 106, 107, 106, 105, 104, 105, 104, 103, 104, 103, 104,
105, 106, 105, 106, 107, 106, 105, 106, 107, 108, 107, 108, 109, 110, 109, 108,
107, 106, 107, 108, 109, 108, 107, 106, 107, 106, 107, 108, 109, 108, 107, 106,
105, 104, 105, 104, 105, 104, 103, 102, 101, 100, 99, 98, 97, 96, 95, 94, 95,
94, 95, 94, 95, 96, 95, 94, 93, 92, 93, 94, 95, 96, 97, 96, 97, 98, 97, 96, 97,
96, 97, 96, 97, 96, 97, 98, 97, 96, 97, 98, 99, 98, 97, 96, 95, 96, 95, 94, 95,
96, 95, 94, 95, 94, 95, 96, 97, 96, 95, 96, 95, 94, 93, 94, 95, 96, 97, 98, 99
100, 101, 102, 101, 100, 99, 100, 101, 100, 101, 100, 101, 100, 99, 98, 99, 98
99, 98, 97, 96, 97, 96, 95, 94, 93, 94, 93, 94, 95, 96, 97, 98, 97, 96, 97, 96
97, 96, 95, 94, 95, 96, 95, 94, 95, 96, 95, 96, 97, 96, 95, 96, 95, 96, 95, 94,
93, 92, 93, 92, 93, 94, 93, 94, 93, 92, 93, 94, 93, 92, 93, 94, 95, 96, 97, 96,
97, 96, 95, 96, 95, 96, 95, 96, 97, 98, 99, 100, 99, 100, 99, 100, 101, 100, 99
98, 97, 98, 99, 100, 99, 98, 99, 100, 101, 100, 99, 98, 99, 98, 97, 96, 97, 96
95, 94, 93, 92, 91, 92, 91, 90, 89, 88, 87, 88, 87, 88, 89, 88, 89, 90, 89, 90,
```

```
89, 88, 89, 90, 89, 88, 89, 90, 89, 88, 89, 88, 87, 88, 89, 88, 89, 90, 89, 88,
87, 88, 87, 86, 85, 86, 87, 88, 87, 88, 87, 88, 87, 88, 87, 86, 87, 88, 87, 86,
87, 86, 87, 88, 87, 86, 87, 88, 87, 88, 89, 90, 89, 88, 89, 90, 89, 88, 87, 88,
87, 86, 85, 84, 85, 84, 85, 84, 85, 86, 85, 86, 87, 88, 87, 88, 87, 88, 89, 90,
91, 92, 91, 90, 91, 90, 91, 92, 91, 92, 91, 92, 91, 90, 89, 90, 91, 90, 89, 90
91, 92, 91, 92, 93, 92, 93, 92, 91, 92, 91, 92, 93, 94, 93, 94, 93, 94, 95, 94,
95, 96, 95, 94, 95, 94, 93, 92, 91, 90, 91, 92, 93, 92, 93, 92, 91, 92, 93, 92,
93, 92, 91, 92, 91, 92, 91, 90, 91, 90, 89, 88, 89, 90, 89, 90, 89, 88, 87, 86,
85, 86, 85, 86, 87, 88, 87, 86, 87, 86, 85, 84, 83, 84, 85, 86, 87, 88, 89, 88,
89, 90, 89, 90, 89, 90, 89, 88, 89, 88, 87, 88, 87, 88, 87, 86, 87, 88, 89, 88,
89, 90, 91, 90, 89, 90, 89, 90, 89, 90, 91, 92, 93, 92, 93, 92, 91, 90, 89, 90,
91, 92, 93, 94, 93, 92, 93, 92, 93, 94, 93, 94, 93, 94, 93, 92, 93, 94, 93, 94
93, 94, 95, 96, 95, 94, 95, 94, 95, 96, 95, 96, 95, 96, 97, 98, 99, 100, 101,
100, 101, 100, 101, 102, 101, 102, 103, 102, 101, 102, 103, 102, 103, 102, 103,
104, 103, 104, 103, 104, 105, 106, 105, 104, 105, 104, 103, 102, 103, 102, 103,
102, 101, 102, 101, 100, 99, 98, 99, 98, 99, 98, 99, 100, 99, 100, 101, 100, 99
100, 101, 100, 101, 102, 101, 102, 101, 102, 101, 100, 101, 102, 103, 102, 103,
104, 103, 104, 103, 102, 101, 102, 101, 100, 101, 102, 101, 102, 103, 104, 105,
106, 105, 104, 105, 106, 107, 108, 107, 108, 109, 108, 109, 110, 109, 108, 107,
108, 107, 108, 107, 108, 107, 106, 105, 106, 105, 106, 105, 106, 105, 106, 107,
108, 107, 106, 105, 104, 103, 104, 103, 104, 105, 106, 105, 106, 105, 106, 107,
106, 107, 106, 107, 108, 109, 110, 111, 110, 111, 112, 111, 112, 113, 114, 113,
112, 113, 112, 111, 110, 109, 108, 109, 108, 107, 106, 105, 104, 103, 102, 101,
100, 99, 100, 99, 100, 101, 102, 103, 104, 105, 104, 103, 104, 105, 104, 103,
102, 103, 104, 105, 104, 103, 104, 105, 104, 103, 102, 101, 100, 99, 100, 99,
98, 97, 98, 97, 96, 97, 96, 97, 96, 95, 96, 97, 96, 97, 98, 97, 98, 97, 98, 99,
98, 97, 98, 99, 100, 101, 102, 103, 102, 103, 102, 101, 102, 101, 102, 103, 102,
101, 100, 101, 102, 103, 104, 103, 104, 103, 102, 101, 102, 101, 100, 99, 100,
99, 100, 99, 100, 99, 100, 99, 100, 101, 100, 101, 100, 101, 102, 103, 102, 101,
102, 101, 102, 101, 102, 103, 104, 103, 102, 103, 104, 105, 106, 107, 108, 109,
108, 109, 108, 107, 106, 105, 104, 103, 104, 105, 106, 105, 104, 103, 104, 105,
104, 105, 104, 103, 104, 103, 104, 103, 104, 105, 104, 105, 104, 105, 106, 107,
106, 105, 104, 105, 104, 105, 106, 107, 108, 107, 106, 107, 106, 107, 108, 109,
108, 107, 106, 105, 106, 105, 104, 103, 102, 103, 104, 105, 104, 105, 104, 103,
102, 103, 104, 103, 102, 101, 102, 103, 102, 101, 102, 103, 102, 103, 104, 103,
102, 101, 100, 101, 102, 103, 102, 101, 100, 99, 100, 101, 102, 101, 100, 101,
100, 99, 100, 99, 100, 99, 98, 97, 98, 97, 96, 97, 98, 97, 98, 97, 98, 99, 100,
99, 100, 101, 102, 103, 104, 105, 104, 103, 104, 103, 104, 105, 104, 103, 102,
101, 102, 101, 100, 101, 100, 99, 98, 97, 98, 97, 98, 97, 98, 97, 98, 99, 100,
101, 100, 101, 100, 99, 100, 101, 100, 99, 98, 97, 96, 97, 98, 97, 96, 97, 96,
97, 96, 97, 98, 99, 100, 101, 100, 99, 98, 99, 98, 99, 100, 99, 98, 97, 96, 97,
96, 95, 94, 95, 94, 93, 92, 91, 90, 89, 90, 89, 89, 88, 89, 90, 91, 90, 91,
90, 91, 92, 93, 94, 95, 96, 95, 94, 95, 94, 93, 92, 91, 90, 91, 92, 91, 90, 91,
90, 89, 88, 87, 86, 87, 88, 87, 88, 89, 88, 87, 88, 87, 86, 87, 88, 89, 88, 89,
88, 89, 90, 89, 90, 89, 90, 91, 90, 89, 88, 87, 88, 87, 86, 85, 86, 87, 86, 87,
88, 87, 88, 89, 88, 89, 90, 89, 90, 88, 88, 89, 90, 89, 90, 89, 88, 89, 88, 87,
86, 87, 88, 87, 88, 89, 88, 87, 88, 87, 86, 85, 86, 85, 84, 85, 84, 85, 86, 85
84, 83, 84, 85, 86, 87, 88, 89, 90, 91, 90, 91, 90, 91, 92, 93, 94, 95, 96, 97,
```

96, 97, 96, 97, 96, 95, 94, 95, 96, 95, 96, 95, 96, 95, 94, 93, 92, 91, 92, 93, 92, 93, 94, 93, 92, 91, 92, 93, 92, 93, 92, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 99, 100, 99, 98, 97, 96, 95, 96, 95, 94, 95, 96, 97, 96, 97, 98, 97, 98, 99, 98, 99, 98, 97, 96, 97, 96, 97, 96, 95, 96, 95, 96, 97, 98, 97, 96, 97, 96, 95, 96, 95, 96, 95, 94, 95, 94, 95, 96, 95, 96, 97, 98, 97, 96, 97, 96, 97, 98, 97, 96, 95, 94, 95, 94, 95, 96, 97, 98, 97, 96, 95, 96, 97, 96, 97, 98, 97, 98, 97, 98, 97, 96, 97, 98, 99, 100, 99, 98, 97, 96, 97, 96, 95, 94, 93, 92, 93, 94, 95, 96, 97, 98, 99, 98, 99, 98, 99, 98, 97, 98, 99, 98, 97, 96, 97, 98, 97, 98 97, 96, 95, 94, 95, 94, 95, 96, 95, 96, 97, 96, 97, 96, 95, 96, 95, 94, 93, 92, 93, 94, 95, 94, 95, 94, 95, 94, 95, 94, 95, 96, 97, 96, 95, 96, 95, 94, 93, 92, 91, 90, 91, 90, 91, 92, 91, 90, 89, 88, 89, 90, 89, 88, 89, 88, 89, 88, 87, 88, 87, 86, 87, 86, 85, 84, 85, 86, 85, 86, 87, 86, 87, 88, 89, 90, 91, 92, 93, 94 93, 94, 95, 94, 95, 94, 93, 92, 91, 90, 89, 90, 91, 92, 93, 94, 95, 96, 97, 96, 95, 94, 95, 96, 95, 96, 95, 96, 95, 94, 95, 96, 95, 96, 95, 96, 95, 94, 95, 94, 95, 96, 95, 96, 95, 94, 95, 94, 95, 96, 95, 96, 97, 98, 97, 98, 99, 100, 99, 98, 97, 98, 97, 96, 95, 96, 95, 94, 93, 94, 95, 96, 97, 96, 97, 98, 99, 98, 99, 100, 99, 98, 97, 98, 99, 100, 99, 100, 101, 102, 103, 104, 103, 104, 103, 102, 101, 100, 101, 102, 103, 102, 101, 102, 101, 102, 101, 100, 101, 100, 99, 98, 97, 98, 99, 100, 99, 100, 99, 98, 97, 96, 95, 94, 95, 96, 97, 96, 95, 96, 97, 96, 95, 94, 95, 94, 93, 92, 93, 94, 95, 96, 95, 96, 97, 96, 95, 96, 95, 96, 95, 96, 95, 96, 97, 98, 97, 96, 95, 94, 95, 94, 93, 92, 93, 92, 91, 92, 93, 92, 93, 92, 91, 92, 93, 94, 95, 94, 93, 94, 93, 92, 93, 92, 91, 92, 93, 94, 95, 94, 95, 96, 95, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 102, 103, 102, 101, 102, 101, 100, 99, 98, 97, 98, 97, 96, 97, 96, 97, 98, 99, 98, 99, 98, 99, 98, 97, 98, 97, 96, 97, 98, 99, 100, 101, 100, 101, 102, 101, 102, 101, 102, 103, 104, 105, 106, 107, 108, 107, 106, 105, 104, 105, 104, 105, 106, 107, 106, 105, 104, 103, 102, 101, 100, 101, 102, 103, 104, 105, 106, 105, 104, 103, 102, 103, 104, 105, 106, 105, 104, 103, 104, 103, 102, 101, 100, 101, 102, 101, 102, 103, 104, 103, 102, 103, 102, 103, 102, 103, 104, 105, 106, 105, 106, 105, 104, 105, 104, 103, 102, 103, 104, 103, 102, 103, 104, 103, 102, 101, 102, 101, 100, 101, 100, 99, 98, 99, 98, 97, 96, 95, 94, 95, 94, 95, 96, 95, 96, 97, 98, 97, 96, 95, 96, 97, 96, 95, 94, 95, 96, 97, 98, 97, 96, 97, 96, 95, 96, 95, 94, 93, 94, 95, 94, 95, 94, 95, 94, 95, 94, 93, 92, 91, 92, 91, 90, 89, 90, 91, 90, 91, 92, 93, 92, 93, 92, 91, 92, 93, 94, 95, 96, 97, 98, 99, 98, 99, 98, 99, 100, 101, 100, 101, 102, 101, 100, 99, 98, 97, 98, 97, 96, 97, 96, 95, 96, 97, 96, 97, 98, 97, 96, 95, 94, 95, 96, 95, 94, 95, 94, 95, 94, 93, 94, 95, 96, 95, 96, 97, 98, 99, 100, 99, 98, 99, 98, 97, 96, 97, 98, 97, 98, 99, 98, 99, 100, 99, 98, 97, 96, 97, 98, 99, 100, 101, 102, 101, 100, 99, 100, 99, 98, 99, 98, 99, 100, 101, 100, 99, 100, 99, 100, 101, 102, 101, 102, 101, 102, 101, 102, 101, 100, 101, 100, 99, 98, 97, 98, 99, 98, 99, 98, 97, 96, 97, 98, 99, 100, 101, 100, 101, 100, 101, 102, 103, 104, 103, 102, 103, 102, 101, 100, 99, 98, 99, 98, 97, 96, 97, 96, 97, 98, 97, 98, 99, 98, 99, 98, 99, 98, 97, 98, 97, 98, 99, 98, 97, 98, 97, 96, 95, 96, 97, 96, 95, 94, 93, 92, 91, 90, 89, 88, 89, 88, 89, 90, 89, 90, 91, 90, 91, 92, 93, 92, 91, 92, 93, 94, 93, 92, 93, 94, 93, 92, 93, 92, 91, 92, 91, 92, 91, 92, 91, 90, 89, 88, 87, 86, 87, 88, 87, 88, 89, 90, 91, 90, 89, 88, 87, 86, 87, 88, 89, 88, 89, 88, 87, 86, 87, 86, 85, 84, 85, 84, 85, 86, 85, 84, 83, 82, 81, 80, 81, 80, 81, 80, 81, 82, 81, 82, 83, 82, 81, 82, 83, 82, 83, 84, 85, 86, 87, 86, 87 88, 87, 88, 89, 88, 89, 88, 89, 88, 89, 90, 91, 90, 91, 92, 91, 90, 89, 88, 89,

```
90, 91, 92, 93, 92, 93, 94, 93, 92, 93, 92, 93, 94, 93, 94, 95, 96, 97, 96, 95,
94, 93, 92, 93, 92, 93, 92, 93, 94, 93, 92, 93, 94, 93, 94, 93, 92, 91, 90, 91,
90, 91, 92, 91, 92, 91, 92, 91, 90, 91, 92, 91, 90, 91, 90, 91, 90, 91, 90, 91,
92, 91, 90, 91, 92, 93, 94, 93, 94, 93, 94, 93, 92, 91, 90, 91, 92, 91, 92, 91,
90, 91, 92, 91, 90, 91, 90, 89, 90, 89, 90, 89, 88, 89, 90, 91, 90, 91, 90, 91
92, 93, 92, 91, 90, 91, 92, 91, 92, 93, 92, 91, 92, 91, 90, 89, 90, 91, 92, 91,
92, 91, 92, 93, 94, 93, 92, 93, 94, 93, 94, 93, 92, 93, 94, 93, 92, 91, 92, 91,
92, 93, 94, 93, 94, 95, 94, 93, 94, 93, 92, 93, 94, 93, 94, 93, 92, 91, 90, 91,
90, 91, 90, 89, 90, 89, 88, 87, 86, 87, 86, 87, 88, 89, 88, 89, 90, 89, 88, 89,
88, 89, 88, 89, 88, 87, 88, 89, 90, 89, 90, 91, 92, 93, 92, 91, 90, 91, 90, 91,
90, 91, 90, 89, 88, 89, 90, 89, 88, 89, 90, 91, 90, 91, 92, 93, 94, 95, 96, 95,
96, 95, 94, 93, 92, 93, 94, 95, 94, 93, 92, 93, 94, 93, 92, 91, 92, 93, 94, 93
92, 91, 90, 89, 90, 89, 88, 89, 88, 87, 86, 85, 84, 83, 84, 83, 84, 85, 86, 85
86, 87, 86, 85, 84, 85, 84, 85, 86, 85, 86, 87, 86, 85, 86, 87, 86, 87, 86, 87,
88, 87, 86, 87, 88, 89, 88, 89, 90, 89, 90, 89, 90, 91, 92, 93, 94, 95, 96, 97,
96, 95, 96, 95, 96, 95, 96, 97, 98, 99, 100, 101, 102, 101, 102, 101, 102, 103,
102, 101, 102, 103, 102, 101, 102, 101, 100, 101, 102, 101, 102, 103, 104, 103,
102, 103, 104, 103, 104, 103, 104, 105, 104, 105, 106, 107, 106, 105, 104, 105,
106, 107, 108, 107, 108, 107, 106, 105, 106, 107, 108, 107, 108, 109, 110, 109,
110, 109, 110, 111, 110, 109, 108, 107, 108, 109, 108, 109, 108, 107, 106, 105,
106, 105, 106, 105, 104, 105, 104, 105, 104, 105, 104, 105, 104, 105, 106, 107,
108, 107, 108, 109, 110, 109, 110, 111, 110, 111, 110, 109, 108, 109, 110, 109,
108, 109, 108, 107, 106, 107, 108, 107, 108, 107, 108, 109, 110, 111, 110, 111,
112, 113, 114, 115, 114, 115, 116, 117, 118, 117, 118, 119, 120, 121, 122, 123,
124, 123, 122, 121, 120, 119, 120, 121, 120, 119, 118, 119, 118, 119, 118, 119,
118, 117, 116, 117, 118, 119, 120, 121, 120, 119, 120, 121, 120, 121, 122, 121,
122, 123, 124, 123, 124, 123, 124, 123, 124, 125, 124, 125, 124, 123, 122, 121,
120, 121, 120, 121, 122, 121, 120, 119, 118, 117, 118, 117, 116, 115, 116, 117,
118, 119, 118, 117, 118, 119, 120, 119, 118, 119, 118, 117, 116, 115, 114, 113,
112, 111, 110, 109, 108, 109, 110, 111, 112, 111, 110, 111, 110, 109, 108, 109,
108, 107, 108, 107, 108, 109, 108, 107, 108, 107, 106, 105, 106, 105, 104, 103,
102, 101, 100, 99, 98, 99, 100, 101, 102, 101, 100, 99, 100, 101, 102, 101, 100,
101, 102, 103, 104, 105, 106, 105, 106, 107, 106, 105, 104, 103, 104, 105, 104,
105, 106, 107, 106, 105, 106, 107, 106, 105, 106, 105, 104, 105, 104, 105, 104,
103, 102, 103, 102, 103, 104, 103, 104, 103, 102, 101, 102, 103, 102, 101, 102,
103, 102, 101, 102, 101, 100, 101, 102, 101, 100, 99, 98, 99, 100, 99, 98, 99,
98, 97, 96, 97, 96, 95, 94, 95, 94, 95, 96, 95, 96, 97, 98, 97, 96, 97, 98, 97,
98, 97, 98, 97, 98, 99, 100, 101, 100, 99, 98, 97, 98, 99, 98, 99, 98, 97, 96,
97, 98, 99, 98, 97, 96, 95, 94, 95, 94, 95, 94, 93, 92, 91, 92, 93, 94, 93, 92,
91, 92, 91, 92, 93, 92, 91, 90, 89, 88, 89, 90, 89, 88, 89, 88, 87, 88, 89, 88
87, 88, 87, 88, 89, 90, 89, 88, 89, 90, 91, 90, 91, 92, 93, 92, 93, 92, 93, 92,
93, 92, 93, 94, 95, 96, 97, 98, 99, 98, 97, 96, 95, 94, 95, 94, 93, 92, 93, 94
95, 94, 95, 94, 93, 92, 91, 90, 89, 90, 88, 88, 89, 90, 91, 90, 89, 90, 89, 90,
91, 92, 93, 94, 93, 94, 95, 96, 97, 98, 99, 98, 97, 96, 95, 96, 95, 94, 93, 94
95, 94, 93, 94, 95, 96, 97, 96, 95, 96, 95, 94, 95, 94, 95, 96, 95, 94, 95, 94,
95, 96, 97, 96, 97, 98, 99, 98, 97, 96, 95, 96, 95, 96, 97, 98, 99, 98, 97, 98,
97, 96, 97, 96, 97, 96, 95, 94, 93, 92, 93, 92, 93, 92, 91, 90, 91, 90, 89, 90,
91, 92, 91, 90, 91, 90, 89, 90, 89, 90, 88, 88, 88, 87, 88, 87, 88, 87, 86,
```

```
87, 86, 87, 86, 85, 86, 85, 84, 83, 84, 83, 84, 85, 86, 87, 86, 87, 88, 87, 86,
85, 86, 87, 86, 85, 84, 85, 86, 85, 84, 85, 84, 83, 84, 83, 84, 85, 86, 87, 86,
85, 84, 85, 84, 85, 86, 87, 88, 89, 90, 91, 90, 89, 90, 89, 90, 89, 88, 89, 90,
91, 92, 91, 90, 91, 92, 91, 90, 91, 92, 93, 94, 93, 92, 91, 92, 91, 90, 91, 92,
91, 90, 89, 88, 87, 86, 87, 86, 85, 86, 87, 88, 89, 90, 89, 90, 91, 90, 91, 90
89, 90, 91, 90, 89, 90, 91, 92, 91, 90, 91, 92, 93, 94, 95, 96, 95, 96, 97, 98,
97, 98, 99, 100, 99, 100, 101, 100, 99, 98, 97, 96, 95, 96, 95, 96, 97, 98, 97,
98, 99, 98, 99, 100, 101, 100, 99, 98, 97, 96, 95, 94, 95, 96, 97, 98, 97, 98,
99, 100, 99, 100, 99, 100, 99, 98, 99, 100, 99, 98, 97, 98, 97, 98, 97, 96, 97,
96, 95, 94, 95, 94, 95, 94, 95, 96, 97, 96, 97, 98, 97, 98, 99, 100, 99, 98, 99,
100, 101, 102, 101, 102, 103, 104, 105, 104, 103, 104, 103, 102, 103, 102, 101,
100, 101, 102, 101, 100, 99, 98, 97, 98, 97, 98, 97, 96, 97, 96, 95, 96, 95, 94
95, 94, 95, 96, 95, 96, 97, 96, 95, 94, 93, 92, 93, 92, 91, 92, 93, 94, 95, 96,
95, 96, 95, 94, 93, 94, 93, 92, 93, 94, 93, 94, 93, 94, 95, 96, 95, 94, 95, 94,
93, 94, 93, 92, 91, 90, 89, 88, 89, 88, 89, 90, 89, 90, 91, 92, 93, 94, 95, 94,
93, 94, 95, 96, 95, 94, 95, 94, 95, 96, 95, 96, 97, 98, 97, 98, 97, 96, 97, 98,
97, 98, 99, 98, 97, 96, 95, 94, 93, 94, 93, 94, 93, 92, 91, 90, 91, 92, 93, 94,
93, 94, 95, 94, 95, 94, 93, 92, 91, 92, 93, 92, 91, 92, 93, 92, 91, 92, 91, 92,
91, 92, 93, 94, 95, 96, 97, 98, 99, 98, 97, 96, 97, 96, 95, 94, 93, 94, 93, 92,
93, 92, 91, 92, 91, 90, 89, 90, 91, 92, 91, 92, 93, 92, 91, 90, 89, 90, 89, 90,
89, 90, 89, 90, 91, 90, 91, 90, 91, 90, 91, 90, 89, 90, 91, 92, 93, 94, 95, 96,
97, 98, 97, 96, 95, 96, 95, 94, 93, 92, 93, 94, 95, 96, 97, 98, 99, 98, 97, 98,
97, 96, 95, 94, 93, 94, 93, 94, 93, 94, 93, 94, 93, 94, 95, 96, 95, 96, 95, 94,
93, 92, 93, 92, 91, 92, 93, 94, 95, 96, 97, 98, 99, 98, 97, 98, 97, 98, 99, 100
99, 98, 97, 96, 95, 96, 97, 96, 97, 98, 97, 96, 95, 96, 95, 94, 95, 96, 95, 94,
93, 94, 93, 92, 91, 92, 91, 90, 89, 90, 91, 90, 91, 92, 91, 90, 89, 88, 89, 88
89, 90, 91, 92, 91, 90, 91, 90, 91, 90, 89, 88, 89, 90, 89, 90, 91, 92, 91, 92
91, 92, 91, 90, 91, 90, 89, 90, 91, 90, 91, 92, 93, 92, 93, 94, 95, 94, 95, 96,
97, 98, 99, 98, 99, 98, 99, 100, 101, 102, 101, 100, 101, 100, 99, 100, 99, 98,
99, 100, 99, 100, 99, 98, 97, 96, 97, 98, 99, 100, 99, 98, 97, 98, 99, 98, 99,
100, 99, 98, 99, 98, 99, 100, 101, 100, 99, 100, 99, 98, 99, 98, 99, 98, 99,
100, 101, 100, 99, 98, 99, 98, 97, 98, 97, 96, 95, 96, 97, 98, 99, 98, 97, 98,
99, 98, 97, 98, 99, 98, 97, 98, 99, 100, 99, 100, 101, 102, 103, 102, 103, 104,
103, 104, 103, 102, 101, 102, 101, 102, 103, 104, 103, 104, 103, 104, 105, 104,
105, 106, 105, 104, 105, 104, 105, 104, 105, 104, 103, 102, 101, 102, 101, 102,
101, 100, 99, 100, 101, 100, 99, 98, 99, 100, 101, 102, 101, 100, 99, 98, 97,
96, 97, 96, 95, 96, 95, 94, 93, 92, 93, 94, 95, 94, 93, 94, 95, 96, 95, 96, 95
96, 97, 96, 95, 96, 97, 98, 97, 96, 97, 96, 95, 94, 93, 92, 93, 94, 95, 96, 97,
96, 95, 94, 95, 94, 95, 96, 95, 94, 95, 96, 95, 94, 95, 94, 95, 96, 95, 94, 93,
94, 93, 92, 91, 90, 91, 90, 89, 90, 91, 90, 91, 90, 91, 92, 93, 92, 93, 94, 95,
94, 95, 94, 95, 96, 95, 96, 95, 94, 95, 96, 95, 96, 97, 96, 97, 98, 97, 98, 97,
98, 97, 96, 97, 96, 97, 98, 97, 98, 97, 96, 97, 96, 95, 94, 95, 94, 95, 94, 95,
94, 95, 96, 97, 96, 95, 96, 95, 96, 95, 96, 97, 96, 97, 98, 97, 98, 99, 98, 99,
100, 99, 100, 101, 102, 103, 102, 103, 102, 101, 100, 101, 100, 99, 98, 97, 98,
97, 96, 97, 98, 97, 98, 97, 96, 97, 98, 99, 98, 97, 98, 99, 98, 97, 96, 97, 96,
95, 94, 95, 94, 95, 96, 95, 94, 95, 94, 95, 94, 93, 92, 91, 90, 91, 92, 93, 94,
95, 94, 95, 94, 95, 96, 97, 98, 97, 98, 99, 98, 97, 96, 97, 96, 97, 98, 99, 100
101, 102, 103, 104, 105, 104, 103, 104, 103, 102, 101, 102, 103, 104, 103, 102,
```

```
101, 102, 101, 102, 101, 100, 99, 100, 101, 102, 101, 102, 101, 100, 99, 100,
101, 102, 101, 102, 103, 104, 103, 104, 103, 104, 103, 102, 101, 100, 99, 100,
101, 102, 103, 102, 103, 104, 105, 104, 103, 104, 105, 104, 105, 104, 105, 104,
103, 104, 103, 102, 103, 104, 105, 106, 105, 104, 105, 104, 103, 102, 103, 102,
103, 102, 103, 104, 103, 104, 105, 104, 103, 102, 103, 104, 105, 104, 105, 104,
103, 104, 105, 104, 103, 104, 105, 104, 103, 102, 103, 104, 103, 102, 101, 102,
103, 102, 103, 104, 103, 104, 103, 102, 101, 100, 99, 100, 101, 102, 101, 100,
99, 98, 99, 98, 97, 98, 99, 98, 99, 100, 99, 100, 101, 102, 101, 102, 101, 100,
101, 100, 99, 98, 97, 96, 95, 96, 95, 94, 95, 94, 95, 94, 95, 96, 95, 94, 93,
92, 91, 92, 91, 92, 93, 94, 95, 96, 97, 98, 99, 98, 97, 96, 95, 94, 93, 92, 91,
90, 91, 92, 93, 92, 91, 90, 89, 90, 91, 90, 89, 88, 87, 88, 89, 90, 91, 92, 93,
92, 93, 94, 95, 96, 95, 96, 97, 96, 97, 98, 99, 100, 101, 100, 101, 102, 103,
104, 105, 106, 107, 108, 107, 108, 107, 108, 109, 110, 111, 110, 111, 112, 113,
114, 115, 114, 113, 112, 111, 112, 111, 110, 109, 108, 109, 110, 111, 112, 113,
114, 115, 114, 113, 112, 113, 114, 113, 112, 111, 112, 113, 114, 113, 112, 111,
112, 111, 110, 109, 108, 107, 108, 109, 110, 111, 110, 109, 110, 111, 112, 113,
112, 111, 112, 111, 110, 111, 110, 109, 108, 109, 108, 109, 110, 111, 112, 113,
112, 113, 114, 113, 114, 115, 114, 113, 114, 115, 114, 115, 114, 115, 116, 117,
116, 117, 116, 117, 118, 117, 116, 117, 118, 117, 116, 115, 114, 115, 116, 115,
116, 115, 114, 113, 114, 115, 114, 115, 116, 115, 116, 115, 116, 117, 116, 115,
114, 113, 114, 115, 116, 117, 118, 117, 118, 117, 118, 117, 116, 115, 116, 115,
116, 115, 114, 113, 112, 111, 112, 113, 112, 111, 110, 109, 108, 109, 108, 107,
108, 109, 108, 107, 106, 107, 108, 107, 108, 109, 108, 109, 108, 109, 110, 111,
112, 113, 112, 111, 112, 113, 112, 113, 114, 115, 116, 117, 116, 117, 118, 119,
118, 119, 120, 119, 120, 121, 122, 121, 122, 121, 120, 121, 120, 121, 122, 123,
124, 123, 124, 125, 126, 127, 126, 125, 124, 125, 126, 127, 126, 125, 124, 123,
124, 123, 124, 125, 126, 125, 124, 123, 124, 125, 124, 123, 124, 125, 126, 127,
126, 127, 128, 129, 130, 129, 128, 129, 128, 127, 126, 125, 124, 125, 126, 127,
128, 127, 128, 127, 128, 127, 126, 125, 126, 127, 126, 125, 126, 127, 128, 129,
128, 127, 128, 127, 128, 129, 130, 131, 130, 129, 128, 127, 126, 125, 126, 125,
126, 125, 124, 123, 122, 121, 122, 123, 122, 123, 122, 121, 120, 121, 122, 121,
120, 121, 122, 123, 122, 123, 122, 121, 120, 121, 120, 121, 120, 119, 120, 119,
118, 119, 120, 121, 120, 121, 122, 121, 120, 119, 118, 119, 120, 121, 122, 121,
120, 119, 120, 119, 118, 117, 118, 117, 118, 119, 120, 119, 118, 117, 118, 117,
116, 115, 114, 113, 112, 113, 114, 113, 112, 111, 110, 109, 110, 111, 110, 109,
108, 109, 110, 109, 108, 109, 110, 109, 108, 107, 108, 107, 106, 105, 106, 105,
106, 107, 108, 107, 108, 107, 108, 109, 108, 109, 110, 109, 110, 109, 110, 109,
108, 107, 108, 109, 110, 109, 108, 107, 108, 107, 106, 105, 104, 103, 104, 105,
104, 105, 106, 107, 106, 107, 106, 107, 108, 107, 108, 109, 108, 107, 108, 109,
108, 109, 108, 107, 108, 109, 110, 109, 108, 107, 106, 105, 104, 103, 102, 103,
102, 103, 102, 103, 104, 105, 106, 105, 106, 105, 104, 105, 106, 107, 106, 105,
106, 105, 104, 103, 102, 103, 102, 103, 104, 103, 104, 105, 106, 105, 104, 103,
102, 103, 102, 103, 102, 101, 102, 101, 100, 99, 100, 99, 100, 99, 100, 101,
100, 101, 102, 101, 102, 103, 104, 103, 104, 103, 104, 103, 102, 103, 104, 105,
106, 105, 106, 107, 108, 107, 108, 107, 108, 107, 106, 105, 106, 105, 104, 103,
102, 101, 100, 101, 102, 103, 102, 103, 102, 101, 100, 101, 102, 103, 102, 103,
104, 105, 104, 103, 104, 103, 102, 101, 100, 101, 100, 101, 100, 99, 100, 99,
100, 101, 100, 101, 100, 99, 100, 101, 100, 99, 98, 97, 98, 99, 100, 99, 98, 97,
```

98, 97, 96, 95, 96, 97, 98, 99, 100, 101, 102, 103, 102, 101, 100, 99, 98, 97, 96, 97, 98, 99, 100, 101, 100, 101, 102, 103, 102, 103, 104, 103, 102, 101, 102, 103, 104, 105, 106, 105, 106, 105, 106, 107, 106, 107, 106, 105, 104, 105, 104, 105, 104, 105, 104, 105, 104, 103, 104, 103, 104, 105, 104, 103, 102, 101, 102, 103, 104, 105, 104, 105, 104, 103, 102, 103, 104, 105, 106, 107, 108, 109, 108, 107, 108, 107, 108, 107, 106, 105, 104, 105, 104, 103, 102, 101, 102, 103, 102, 101, 100, 99, 100, 99, 98, 97, 96, 95, 94, 95, 94, 95, 94, 95, 94, 93, 94, 95, 96, 97, 96, 95, 96, 97, 98, 97, 96, 97, 98, 99, 98, 97, 96, 97, 98, 99, 98, 97, 96, 95, 96, 97, 96, 97, 98, 99, 100, 101, 100, 99, 100, 99, 98, 99, 98, 99, 100, 99, 100, 99, 100, 101, 102, 103, 104, 105, 106, 105, 106, 105, 104, 103, 102, 103, 104, 105, 104, 103, 102, 103, 104, 103, 102, 101, 102, 103, 102, 103, 102, 101, 102, 101, 102, 103, 102, 101, 100, 101, 100, 101, 100, 101, 100, 99, 100, 101, 102, 103, 102, 103, 104, 105, 106, 107, 106, 105, 106, 107, 106, 105, 104, 105, 104, 105, 106, 105, 104, 105, 104, 103, 102, 103, 104, 103, 104, 105, 106, 107, 108, 107, 108, 107, 108, 109, 110, 111, 110, 109, 110, 111, 112, 113, 114, 113, 112, 111, 110, 109, 110, 109, 108, 109, 110, 111, 110, 109, 108, 107, 108, 107, 108, 109, 110, 109, 108, 109, 108, 107, 108, 107, 106, 107, 108, 107, 108, 107, 108, 107, 106, 107, 106, 105, 104, 105, 106, 105, 106, 107, 106, 105, 106, 105, 106, 105, 106, 105, 104, 103, 104, 103, 104, 103, 104, 105, 106, 107, 106, 107, 106, 107, 106, 105, 104, 105, 104, 105, 104, 105, 106, 107, 108, 109, 108, 107, 106, 105, 104, 105, 106, 105, 104, 105, 104, 103, 104, 105, 104, 103, 102, 101, 100, 101, 102, 103, 104, 105, 104, 103, 104, 103, 104, 103, 104, 103, 104, 103, 102, 101, 102, 101, 100, 101, 102, 103, 102, 101, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 108, 107, 106, 105, 106, 105, 104, 103, 104, 105, 106, 105, 106, 105, 104, 105, 106, 105, 106, 105, 106, 107, 108, 109, 108, 107, 108, 109, 110, 109, 110, 109, 108, 109, 110, 111, 110, 109, 110, 109, 108, 107, 106, 105, 106, 105, 104, 105, 104, 105, 104, 103, 104, 105, 104, 103, 102, 103, 104, 103, 104, 103, 102, 103, 104, 103, 104, 103, 102, 103, 104, 105, 106, 107, 106, 107, 108, 107, 108, 109, 108, 107, 106, 107, 106, 107, 108, 109, 110, 109, 108, 107, 108, 109, 108, 109, 108, 107, 108, 109, 110, 109, 108, 107, 108, 109, 108, 107, 106, 105, 106, 107, 106, 105, 106, 105, 106, 105, 104, 105, 104, 103, 104, 103, 102, 103, 102, 103, 104, 103, 104, 105, 106, 107, 106, 105, 104, 105, 104, 105, 104, 105, 104, 103, 102, 103, 104, 105, 104, 105, 104, 105, 104, 103, 104, 105, 104, 103, 102, 103, 102, 101, 102, 103, 102, 101, 100, 101, 100, 101, 102, 103, 104, 103, 104, 103, 104, 105, 104, 103, 102, 103, 104, 105, 106, 105, 106 105, 104, 105, 106, 107, 106, 107, 106, 107, 106, 105, 106, 107, 108, 109, 110, 111, 112, 111, 112, 113, 112, 111, 110, 111, 112, 113, 112, 111, 112, 111, 112, 113, 114, 115, 114, 115, 116, 117, 116, 115, 116, 115, 116, 115, 114, 113, 112, 113, 114, 113, 114, 113, 114, 113, 114, 115, 116, 117, 116, 117, 118, 119, 120, 119, 118, 117, 118, 119, 118, 117, 116, 117, 116, 117, 116, 115, 116, 117, 118, 119, 118, 119, 118, 117, 116, 115, 114, 113, 112, 113, 112, 111, 110, 109, 108, 107, 108, 107, 108, 109, 108, 109, 108, 109, 110, 111, 112, 113, 112, 111, 110, 111, 110, 109, 108, 107, 106, 107, 106, 105, 106, 107, 108, 107, 106, 107, 106, 107, 108, 107, 106, 107, 108, 109, 108, 109, 110, 111, 112, 111, 110, 111, 112, 111, 110, 111, 112, 113, 112, 111, 112, 113, 114, 113, 114, 113, 114, 113, 114, 113, 114, 113, 112, 111, 110, 111, 110, 111, 112, 113, 112, 111, 110, 111, 112, 111, 110, 109, 108, 107, 106, 105, 104, 105, 106, 105, 104, 105, 104, 105, 106, 105, 104, 103, 102, 101, 102, 101, 100, 99, 100, 99, 98, 99, 98, 97, 98, 99, 98,

```
99, 98, 97, 96, 97, 98, 97, 98, 99, 100, 101, 100, 99, 100, 99, 98, 99, 98, 99,
100, 101, 100, 101, 100, 101, 100, 99, 100, 99, 100, 99, 98, 97, 98, 97, 98, 97
96, 97, 98, 97, 96, 97, 96, 95, 94, 93, 94, 93, 94, 93, 92, 93, 92, 93, 94, 95,
94, 93, 92, 91, 92, 91, 90, 91, 90, 91, 90, 91, 92, 91, 92, 93, 92, 91, 92, 93,
94, 95, 96, 97, 98, 99, 100, 101, 102, 101, 100, 101, 100, 101, 102, 103, 102,
103, 104, 105, 106, 107, 108, 107, 108, 107, 108, 109, 110, 109, 110, 111, 112,
111, 110, 109, 108, 107, 108, 109, 108, 109, 110, 111, 110, 109, 110, 109, 108,
107, 108, 107, 106, 107, 106, 107, 108, 109, 108, 109, 110, 109, 110, 111, 112,
111, 110, 109, 110, 111, 112, 111, 112, 111, 110, 109, 108, 109, 108, 107, 108,
107, 106, 107, 108, 109, 110, 109, 108, 109, 110, 109, 110, 111, 110, 111, 110,
109, 110, 111, 112, 113, 114, 113, 112, 111, 112, 111, 110, 111, 112, 111, 110,
109, 108, 109, 108, 107, 106, 105, 104, 103, 104, 103, 104, 105, 104, 103, 102,
103, 102, 103, 104, 105, 106, 105, 104, 105, 106, 105, 106, 105, 106, 105, 106,
105, 106, 107, 106, 107, 106, 107, 108, 107, 106, 105, 106, 107, 106, 107, 108,
109, 110, 109, 110, 111, 110, 109, 110, 109, 110, 111, 112, 113, 112, 113, 114,
115, 114, 115, 116, 115, 116, 115, 114, 113, 114, 113, 112, 111, 112, 111, 112,
111, 112, 111, 110, 109, 110, 109, 110, 111, 112, 113, 114, 115, 116, 115, 116
115, 116, 115, 114, 113, 114, 115, 114, 115, 114, 115, 114, 113, 112, 111, 110,
111, 110, 111, 112, 113, 114, 113, 112, 113, 114, 113, 112, 111, 112, 111, 110,
111, 110, 111, 112, 111, 110, 111, 112, 113, 114, 113, 114, 115, 116, 115, 114,
115, 114, 113, 112, 113, 112, 111, 110, 111, 110, 111, 112, 111, 112, 113, 114,
115, 114, 115, 116, 115, 114, 115, 114, 115, 114, 115, 114, 115, 114, 115, 114,
115, 114, 113, 112, 111, 112, 113, 112, 111, 112, 111, 110, 109, 108, 109, 110,
111, 112, 113, 114, 113, 112, 113, 114, 113, 114, 113, 112, 111, 110, 109, 108,
107, 108, 109, 110, 109, 110, 111, 110, 109, 110, 109, 110, 111, 112, 113, 114,
113, 114, 115, 116, 117, 118, 117, 116, 117, 118, 119, 118, 117, 118, 119, 118,
117, 116, 115, 114, 115, 114, 113, 112, 113, 112, 111, 110, 109, 108, 109, 110,
111, 110, 109, 110, 111, 112, 113, 112, 111, 112, 113, 112, 111, 112, 113, 114,
113, 112, 111, 112, 113, 112, 113, 112, 113, 114, 115, 116, 115, 116, 115, 114,
113, 114, 113, 114, 113, 112, 111, 112, 113, 112, 113, 114, 113, 114, 115, 116,
117, 116, 115, 116, 117, 116, 115, 114, 115, 116, 117, 116, 115, 116, 115, 114,
113, 114, 113, 114, 115, 114, 115, 114, 115, 114, 115, 116, 117, 116, 117, 116,
117, 118, 117, 116, 115, 114, 115, 114, 113, 112, 113, 112, 111, 110, 111, 112,
113, 114, 113, 112, 113, 112, 113, 112, 113, 112, 113, 114, 115, 114, 113, 112,
111, 110, 111, 112, 113, 114, 115, 116, 115, 116, 115, 116, 115, 116, 115, 116,
117, 116, 117, 118, 117, 116, 115, 116, 115, 114, 113, 114, 113, 112, 111, 112,
111, 110, 109, 110, 111, 112, 111, 110, 109, 110, 109, 108, 109, 110, 111, 112,
113, 112, 113, 112, 111, 112, 111, 110, 109, 110, 111, 112, 113, 114, 115, 116,
115, 116, 115, 114, 113, 112, 111, 112, 111, 112, 113, 112, 111, 110, 111, 110,
109, 108, 109, 110, 109, 110, 109, 110, 109, 110, 109, 108, 107, 108, 109, 110,
111, 112, 111, 110, 111, 112, 113, 114, 113, 112, 113, 112, 111, 112, 111, 112,
113, 114, 113, 112, 113, 114, 113, 112, 111, 110, 111, 110, 111, 110, 109, 108,
107, 106, 105, 106, 107, 108, 109, 108, 107, 108, 109, 108, 109, 108, 109, 110,
111, 112, 113, 112, 113, 114, 113, 112, 111, 110, 109, 110, 111, 112, 111, 110,
111, 112, 111, 110, 111, 110, 109, 110, 109, 108, 109, 108, 109, 108, 109, 108,
109, 108, 107, 106, 107, 108, 109, 108, 107, 106, 105, 104, 105, 106, 105, 106,
105, 106, 107, 106, 107, 106, 105, 104, 103, 104, 103, 104, 103, 104, 103, 102,
103, 102, 101, 102, 103, 102, 101, 102, 101, 100, 101, 102, 103, 102, 103, 102,
```

101, 100, 99, 100, 101, 102, 101, 102, 103, 104, 105, 104, 103, 104, 105, 106, 107, 106, 107, 108, 107, 108, 107, 106, 107, 108, 109, 110, 109, 110, 111, 110, 111, 110, 111, 110, 109, 108, 107, 106, 107, 108, 107, 108, 107, 108, 109, 110, 109, 108, 107, 106, 105, 106, 107, 106, 105, 106, 105, 104, 103, 104, 103, 102, 101, 102, 101, 102, 101, 102, 103, 104, 105, 104, 103, 104, 103, 102, 103, 104, 103, 104, 103, 102, 101, 100, 99, 98, 97, 98, 99, 100, 99, 100, 99, 98, 99, 98, 97, 96, 97, 98, 99, 98, 99, 98, 97, 96, 95, 94, 93, 92, 91, 90, 91, 90, 91, 90, 91, 90, 91, 92, 93, 92, 93, 92, 93, 92, 93, 92, 93, 92, 91, 90, 91, 90, 91, 92, 93, 94, 95, 96, 97, 96, 95, 96, 95, 96, 95, 96, 95, 96, 95, 96, 95, 96, 95, 96, 95, 96, 95, 96, 97, 96, 95, 94, 93, 92, 91, 90, 91, 90, 91, 90, 91, 92, 91, 92, 91, 92, 93, 92, 93, 94, 95, 94, 95, 94, 95, 96, 97, 98, 97, 96, 97, 98, 99, 100, 99, 100, 99, 100, 99, 100, 101, 100, 101, 100, 99, 100, 101, 102, 103, 102, 103, 104, 103, 102, 101, 100, 99, 98, 97, 96, 97, 98, 99, 100, 101, 102, 101, 102, 101, 100, 99, 98, 99, 98, 99, 100, 101, 100, 99, 98, 97, 96, 97, 98, 97, 96, 95, 96, 97, 98, 99, 98, 99, 100, 99, 98, 97, 98, 97, 98, 99, 98, 99, 100, 101, 100, 99, 98, 99, 98, 97, 98, 99, 98, 97, 98, 99, 100, 101, 102, 101, 100, 99, 98, 99, 100, 99, 100, 99, 100, 99, 98, 97, 98, 99, 100, 101, 100, 101, 102, 101, 100, 101, 102, 101, 100, 99, 100, 99, 100, 101, 102, 103, 104, 105, 106, 105, 104, 103, 104, 105, 106, 107, 106, 105, 104, 103, 104, 105, 104, 103, 102, 103, 102, 103, 104, 105, 106, 105, 106, 107, 108, 109, 110, 111, 110, 111, 110, 111, 112, 111, 112, 113, 114, 115, 114, 113, 114, 115, 116, 115, 116, 115, 114, 115, 114, 115, 116, 117, 118, 117, 118, 119, 120, 121, 120, 121, 122, 123, 124, 123, 124, 123, 122, 123, 122, 121, 120, 119, 120, 119, 120, 121, 120, 121, 120, 121, 120, 121, 122, 123, 122, 121, 120, 119, 120, 121, 120, 121, 120, 119, 118, 119, 118, 117, 116, 115, 116, 115, 116, 115, 114, 113, 112, 113, 114, 113, 114, 113, 114, 113, 114, 113, 114, 113, 114, 115, 114, 115, 114, 115, 116, 115, 114, 115, 114, 113, 112, 113, 114, 115, 114, 113, 112, 111, 112, 111, 110, 111, 110, 109, 108, 107, 106, 105, 106, 107, 108, 107, 106, 107, 106, 107, 108, 107, 106, 105, 106, 105, 106, 107, 108, 107, 106, 105, 106, 105, 104, 105, 104, 103, 102, 103, 104, 103, 104, 103, 104, 103, 102, 103, 104, 105, 104, 103, 104, 103, 104, 103, 102, 103, 102, 103, 102, 101, 100, 99, 98, 97, 98, 97, 96, 97, 96, 97, 98, 97, 96, 97, 96, 97, 96, 95, 96, 95, 96, 95, 96, 95, 96, 97, 96, 95, 96, 97, 98, 97, 98, 97, 96, 97, 96, 95, 94, 95, 96, 95, 94, 93, 92, 91, 92, 91, 90, 89, 88, 89, 88 87, 86, 85, 86, 87, 88, 87, 88, 89, 90, 89, 88, 87, 86, 87, 86, 85, 84, 83, 82, 81, 82, 83, 82, 81, 80, 79, 78, 77, 76, 75, 76, 77, 76, 75, 74, 75, 76, 75, 76 77, 78, 77, 76, 75, 76, 75, 74, 73, 74, 73, 72, 71, 70, 71, 72, 73, 74, 73, 72, 73, 74, 73, 74, 73, 72, 71, 70, 69, 70, 69, 68, 69, 70, 71, 72, 73, 74, 73, 74, 75, 74, 73, 74, 73, 72, 71, 72, 71, 72, 73, 72, 73, 74, 73, 72, 71, 72, 73, 74, 75, 74, 73, 74, 75, 76, 77, 76, 77, 78, 79, 78, 77, 76, 77, 76, 77, 76, 77, 76, 77, 78, 79, 80, 79, 80, 79, 80, 79, 78, 77, 78, 79, 80, 81, 80, 81, 82, 81, 80, 81, 82, 83, 84, 85, 84, 85, 84, 83, 82, 81, 82, 81, 80, 79, 78, 77, 78, 77, 76, 77, 76, 77, 76, 77, 78, 77, 76, 75, 76, 77, 76, 77, 76, 77, 78, 77, 76, 77, 78, 79, 78, 77, 76, 75, 76, 77, 76, 77, 78, 77, 78, 77, 78, 79, 78, 77, 76, 77, 78 77, 78, 79, 80, 81, 82, 81, 82, 83, 82, 83, 82, 83, 82, 83, 84, 85, 86, 87, 86, 87, 86, 87, 86, 85, 86, 85, 86, 87, 86, 87, 86, 85, 84, 83, 84, 83, 82, 83, 84, 85, 86, 87, 88, 89, 88, 89, 90, 89, 88, 89, 90, 89, 90, 91, 90, 89, 90, 89, 90, 91, 92, 93, 94, 93, 92, 93, 92, 93, 94, 95, 96, 95, 96, 97, 98, 97, 98, 97, 98 99, 100, 99, 98, 97, 96, 97, 98, 97, 96, 95, 94, 93, 94, 95, 94, 95, 94, 93, 94,

```
95, 94, 95, 96, 95, 96, 97, 98, 99, 100, 101, 100, 99, 100, 101, 102, 103, 102,
103, 104, 103, 102, 101, 100, 101, 100, 101, 100, 101, 100, 101, 102, 103, 104,
103, 104, 103, 104, 105, 106, 107, 108, 107, 106, 107, 108, 109, 108, 109, 108,
107, 106, 107, 108, 109, 110, 111, 110, 109, 108, 109, 110, 109, 108, 109, 110,
111, 110, 111, 112, 113, 114, 115, 114, 113, 112, 113, 112, 111, 110, 109, 108,
109, 108, 107, 106, 107, 106, 105, 104, 105, 104, 105, 106, 107, 106, 105, 104,
105, 106, 107, 106, 105, 104, 105, 106, 105, 104, 103, 104, 105, 106, 107, 108,
109, 108, 109, 110, 109, 108, 107, 106, 107, 106, 105, 106, 105, 104, 103, 102,
101, 100, 99, 98, 99, 98, 99, 100, 101, 100, 101, 100, 99, 100, 101, 102, 103,
102, 103, 104, 103, 102, 101, 100, 101, 100, 99, 100, 99, 98, 99, 98, 97, 96,
97, 98, 97, 96, 95, 96, 97, 98, 97, 96, 95, 94, 93, 94, 93, 94, 95, 96, 95, 94,
95, 96, 97, 96, 95, 94, 95, 94, 95, 94, 93, 94, 95, 94, 95, 96, 97, 96, 97, 98
99, 100, 99, 98, 99, 98, 97, 98, 99, 98, 97, 96, 95, 94, 93, 92, 93, 94, 93, 92
93, 94, 93, 94, 95, 96, 95, 94, 93, 94, 93, 92, 93, 92, 93, 92, 91, 90, 89, 90,
89, 88, 87, 88, 87, 88, 89, 88, 87, 86, 85, 84, 83, 84, 85, 84, 83, 82, 81, 80,
79, 78, 77, 78, 77, 76, 75, 76, 77, 78, 79, 80, 79, 78, 79, 80, 81, 80, 81, 80,
79, 80, 81, 80, 81, 82, 81, 80, 81, 82, 83, 82, 83, 84, 85, 84, 83, 82, 83, 84,
85, 84, 83, 82, 81, 82, 83, 84, 83, 84, 85, 86, 85, 86, 87, 88, 89, 90, 89, 88,
89, 88, 89, 88, 89, 88, 89, 88, 87, 86, 87, 88, 87, 86, 85, 84, 85, 86, 85, 86,
87, 88, 87, 88, 87, 88, 87, 88, 89, 90, 89, 90, 89, 88, 87, 88, 87, 88, 89, 90,
91, 92, 93, 94, 93, 92, 93, 94, 93, 92, 93, 94, 95, 96, 95, 96, 95, 96, 95, 94,
93, 94, 93, 92, 91, 92, 93, 92, 91, 90, 89, 90, 91, 90, 91, 92, 91, 90, 91, 90,
91, 92, 93, 92, 93, 94, 93, 92, 93, 94, 95, 96, 97, 98, 97, 98, 99, 98, 99, 100
101, 100, 101, 102, 103, 102, 101, 102, 101, 102, 103, 102, 101, 102, 103, 102,
103, 102, 103, 104, 105, 104, 103, 102, 103, 104, 105, 104, 103, 104, 103, 102,
101, 102, 101, 100, 99, 100, 101, 100, 101, 100, 99, 98, 97, 96, 97, 96, 97, 96,
95, 96, 97, 98, 97, 98, 97, 98, 99, 100, 99, 100, 99, 98, 97, 98, 99, 98, 99,
98, 97, 98, 97, 98, 99, 98, 99, 98, 99, 100, 99, 100, 101, 100, 101, 100, 99,
100, 101, 100, 99, 100, 101, 100, 99, 98, 97, 98, 97, 98, 99, 100, 101, 100,
101, 100, 101, 100, 101, 100, 101, 100, 101, 102, 101, 100, 101, 100, 101, 100,
99, 100, 99, 100, 101, 100, 101, 102, 103, 102, 101, 102, 103, 104, 105, 106,
105, 104, 105, 104, 105, 104, 103, 102, 101, 100, 99, 100, 101, 100, 99, 100,
101, 102, 101, 100, 99, 98, 97, 96, 95, 94, 93, 94, 95, 96, 95, 96, 95, 94, 95
96, 97, 96, 97, 98, 97, 96, 95, 96, 97, 98, 97, 98, 97, 98, 99, 100, 101, 102,
101, 102, 103, 104, 105, 104, 103, 104, 103, 102, 103, 104, 105, 104, 105, 106,
107, 106, 107, 106, 107, 106, 105, 104, 105, 106, 107, 106, 107, 106, 107, 108,
107, 108, 107, 108, 109, 110, 111, 110, 109, 110, 109, 110, 111, 112, 113, 112,
111, 110, 109, 108, 109, 110, 111, 110, 111, 112, 111, 110, 111, 110, 111, 112,
111, 112, 113, 112, 113, 114, 113, 112, 113, 112, 111, 112, 111, 110, 111, 112,
111, 112, 111, 110, 111, 112, 111, 110, 111, 112, 113, 114, 115, 114, 113, 114,
113, 114, 113, 112, 111, 110, 111, 110, 109, 110, 109, 108, 107, 106, 105, 106,
107, 108, 109, 108, 107, 106, 107, 108, 107, 106, 107, 108, 109, 110, 109, 110,
109, 108, 107, 106, 105, 104, 103, 104, 103, 104, 105, 106, 107, 106, 107, 106,
107, 106, 105, 106, 105, 106, 107, 106, 107, 106, 105, 106, 105, 104, 103, 104,
105, 106, 105, 106, 105, 106, 107, 108, 107, 108, 107, 106, 107, 108, 107, 106,
107, 106, 105, 106, 105, 106, 107, 106, 105, 106, 105, 104, 103, 102, 101, 100,
101, 100, 99, 98, 97, 98, 99, 100, 101, 100, 99, 98, 99, 100, 99, 98, 97, 98,
97, 98, 97, 96, 97, 98, 99, 98, 97, 98, 99, 100, 101, 102, 101, 102, 103, 102,
```

```
101, 100, 101, 102, 103, 102, 103, 104, 103, 104, 103, 102, 101, 102, 101, 102,
101, 102, 103, 104, 103, 104, 105, 106, 105, 104, 105, 104, 105, 106, 107, 108,
107, 106, 107, 106, 107, 106, 107, 106, 105, 104, 103, 104, 103, 102, 103, 104,
103, 104, 103, 104, 105, 104, 103, 104, 103, 104, 103, 104, 103, 104, 105, 104,
103, 102, 101, 102, 101, 100, 99, 100, 99, 98, 99, 100, 99, 98, 97, 96, 95, 96
97, 98, 99, 98, 99, 100, 99, 98, 97, 96, 95, 96, 95, 94, 93, 94, 93, 94, 95, 96
97, 96, 97, 98, 97, 98, 97, 98, 99, 98, 97, 96, 97, 96, 95, 94, 95, 94, 95, 96,
95, 94, 95, 94, 93, 92, 93, 92, 91, 90, 89, 90, 89, 90, 88, 88, 89, 90,
89, 90, 91, 92, 93, 94, 93, 94, 93, 92, 91, 92, 93, 94, 93, 92, 91, 92, 93, 92,
93, 94, 95, 96, 95, 94, 95, 96, 97, 96, 97, 96, 95, 96, 97, 98, 97, 96, 95, 94,
93, 94, 95, 94, 95, 94, 93, 92, 93, 94, 93, 92, 91, 92, 93, 92, 93, 94, 93, 94,
93, 92, 93, 94, 95, 96, 97, 96, 95, 94, 93, 92, 93, 92, 91, 92, 91, 92, 91, 90
91, 92, 93, 92, 91, 92, 91, 90, 91, 92, 91, 90, 91, 90, 89, 90, 91, 90, 89, 90
89, 90, 91, 92, 93, 92, 91, 92, 93, 92, 91, 92, 93, 94, 95, 94, 93, 94, 93, 92,
91, 90, 91, 92, 91, 92, 91, 92, 91, 92, 93, 92, 93, 92, 93, 94, 95, 94, 93, 94,
93, 92, 91, 90, 91, 90, 91, 92, 91, 92, 91, 92, 93, 92, 91, 92, 93, 94, 93, 92,
91, 92, 93, 92, 93, 92, 93, 94, 93, 92, 93, 94, 93, 92, 91, 92, 93, 92, 91, 90,
91, 90, 91, 90, 91, 92, 93, 92, 93, 92, 91, 90, 91, 92, 91, 90, 89, 88, 87, 88,
87, 88, 87, 86, 85, 84, 83, 84, 85, 84, 83, 84, 85, 86, 85, 84, 85, 86, 87, 88
89, 90, 91, 90, 91, 92, 91, 92, 93, 94, 93, 92, 93, 92, 91, 90, 91, 92, 93, 94
95, 96, 95, 96, 95, 96, 97, 96, 95, 94, 93, 94, 95, 96, 97, 98, 99, 100, 99, 98
97, 98, 99, 98, 97, 98, 97, 96, 95, 96, 95, 94, 95, 96, 95, 96, 95, 94, 95, 96,
97, 98, 99, 100, 99, 100, 101, 100, 101, 102, 103, 102, 101, 100, 99, 98, 99,
98, 97, 96, 97, 98, 99, 98, 97, 96, 95, 96, 95, 94, 95, 94, 93, 92, 91, 90, 91,
90, 91, 90, 89, 88, 89, 90, 91, 90, 89, 90, 89, 90, 91, 90, 89, 90, 89, 88, 89,
88, 89, 90, 91, 92, 91, 90, 91, 92, 91, 90, 89, 90, 89, 88, 89, 88, 89, 90, 89
90, 91, 92, 91, 92, 91, 92, 91, 92, 91, 92, 91, 90, 91, 90, 89, 89, 88, 89
88, 89, 90, 91, 90, 91, 90, 91, 92, 93, 94, 95, 94, 95, 94, 93, 92, 91, 90, 91
92, 93, 92, 93, 92, 93, 92, 93, 94, 95, 94, 95, 96, 97, 96, 95, 94, 93, 94, 93
94, 93, 92, 93, 92, 91, 92, 93, 92, 93, 92, 91, 92, 93, 94, 93, 92, 93, 94, 95,
96, 95, 94, 95, 96, 97, 98, 99, 100, 101, 100, 101, 102, 101, 102, 103, 104,
105, 106, 105, 104, 105, 104, 105, 104, 103, 104, 105, 104, 105, 104, 105, 106,
107, 106, 105, 106, 107, 108, 107, 108, 109, 108, 109, 108, 109, 110, 109, 108,
107, 106, 105, 106, 107, 106, 105, 104, 105, 104, 105, 104, 105, 106, 105, 104,
105, 106, 107, 108, 109, 110, 111, 110, 111, 112, 113, 112, 113, 112, 113, 114
115, 114, 115, 116, 115, 116, 115, 114, 115, 116, 115, 116, 117, 116, 117, 116,
115, 114, 115, 114, 113, 112, 113, 114, 115, 114, 115, 116, 115, 114, 113, 114,
113, 112, 113, 112, 113, 114, 115, 114, 115, 114, 113, 114, 115, 116, 115, 116,
117, 118, 119, 118, 119, 120, 119, 118, 117, 116, 117, 116, 117, 118, 117, 118,
117, 118, 117, 118, 117, 116, 117, 116, 115, 114, 115, 114, 113, 114, 115, 114,
113, 114, 113, 112, 113, 114, 115, 116, 115, 116, 117, 118, 117, 116, 117, 118,
117, 116, 117, 118, 117, 118, 119, 120, 121, 120, 121, 120, 119, 120, 121, 120,
119, 120, 119, 118, 117, 116, 117, 116, 115, 116, 117, 118, 119, 118, 119, 120,
121, 120, 121, 120, 121, 122, 123, 122, 123, 122, 123, 122, 123, 122, 121, 122,
121, 120, 119, 120, 121, 122, 121, 120, 119, 120, 119, 118, 117, 116, 117, 116,
117, 116, 117, 118, 119, 120, 119, 120, 119, 120, 119, 118, 117, 118, 117, 116,
115, 116, 117, 118, 119, 118, 117, 116, 115, 114, 113, 112, 111, 112, 113, 114,
113, 112, 113, 114, 115, 114, 113, 112, 111, 112, 113, 112, 111, 112, 113, 112,
```

```
111, 110, 109, 110, 109, 108, 107, 108, 107, 108, 109, 110, 109, 108, 107, 106,
105, 104, 105, 106, 105, 106, 105, 104, 105, 106, 107, 108, 109, 108, 109, 110,
111, 112, 113, 114, 115, 116, 115, 114, 113, 114, 115, 114, 113, 112, 111, 110,
109, 110, 111, 112, 113, 114, 113, 114, 115, 116, 115, 116, 115, 114, 115, 114,
113, 112, 111, 112, 111, 110, 111, 110, 111, 112, 113, 114, 113, 112, 113, 112,
111, 110, 109, 110, 111, 112, 111, 110, 109, 108, 107, 108, 107, 106, 105, 106,
107, 108, 107, 108, 109, 108, 107, 106, 107, 106, 105, 104, 103, 102, 103, 102,
101, 100, 101, 100, 101, 102, 101, 100, 99, 98, 97, 96, 97, 96, 95, 94, 93, 94,
93, 94, 95, 94, 93, 94, 93, 94, 95, 94, 93, 94, 95, 94, 95, 94, 95, 94, 95, 94,
95, 94, 95, 94, 93, 94, 93, 94, 93, 92, 93, 92, 93, 94, 95, 96, 97, 96, 95, 96
97, 98, 99, 100, 101, 100, 101, 100, 101, 100, 101, 102, 103, 102, 103, 104,
103, 104, 105, 106, 107, 108, 107, 106, 107, 108, 107, 106, 107, 108, 107, 106,
105, 104, 105, 104, 105, 106, 107, 106, 105, 104, 105, 106, 105, 106, 107, 106,
107, 106, 105, 106, 107, 106, 105, 104, 103, 104, 103, 102, 101, 100, 99, 98,
99, 100, 99, 98, 99, 100, 101, 100, 99, 100, 101, 102, 103, 104, 103, 104, 103,
104, 105, 106, 105, 104, 105, 104, 105, 104, 103, 102, 101, 102, 101, 100, 99,
98, 99, 98, 97, 98, 99, 98, 99, 100, 99, 98, 97, 98, 99, 100, 99, 100, 101, 100,
99, 98, 97, 98, 99, 100, 99, 100, 99, 98, 97, 98, 97, 98, 97, 96, 95, 96, 95,
96, 95, 94, 95, 96, 95, 96, 95, 96, 97, 96, 97, 98, 97, 98, 97, 96, 97, 96, 97,
96, 95, 96, 95, 96, 95, 94, 93, 92, 93, 94, 93, 92, 93, 92, 91, 92, 91, 92, 93
92, 91, 92, 91, 92, 93, 94, 95, 94, 93, 94, 93, 92, 93, 94, 95, 96, 97, 96, 95,
96, 95, 96, 97, 98, 97, 98, 97, 96, 97, 98, 99, 100, 101, 102, 101, 100, 99,
100, 99, 98, 99, 100, 99, 98, 99, 100, 99, 98, 97, 96, 95, 96, 97, 98, 97, 98,
97, 98, 99, 98, 97, 96, 97, 98, 97, 98, 99, 98, 99, 100, 99, 100, 101, 102, 101,
100, 99, 100, 101, 100, 101, 102, 103, 102, 101, 100, 101, 100, 99, 98, 97, 98,
99, 98, 99, 100, 99, 100, 99, 98, 99, 100, 101, 100, 101, 102, 103, 104, 105,
106, 105, 104, 105, 106, 107, 106, 107, 106, 107, 106, 105, 104, 105, 104, 105
106, 107, 106, 107, 108, 109, 108, 107, 108, 109, 110, 111, 112, 111, 110, 109,
108, 107, 108, 107, 108, 107, 108, 109, 108, 109, 108, 109, 108, 107, 106, 105,
104, 105, 106, 107, 108, 109, 108, 107, 106, 107, 108, 109, 110, 109, 108, 107,
108, 107, 108, 109, 108, 107, 108, 107, 106, 107, 106, 105, 104, 103, 102, 103,
104, 103, 104, 103, 102, 101, 100, 99, 100, 99, 98, 97, 98, 97, 98, 99, 100, 99,
100, 101, 102, 103, 102, 101, 100, 101, 102, 103, 104, 103, 102, 103, 102, 101,
102, 103, 104, 105, 104, 105, 106, 107, 108, 107, 106, 105, 106, 105, 106, 107,
108, 109, 110, 111, 110, 109, 110, 109, 110, 111, 110, 111, 110, 111, 110, 111,
112, 113, 112, 111, 110, 111, 110, 109, 108, 109, 108, 107, 106, 105, 106, 105
104, 103, 104, 105, 106, 105, 106, 105, 106, 107, 108, 107, 108, 109, 110, 111,
110, 111, 112, 111, 110, 109, 108, 109, 108, 107, 106, 107, 108, 107, 106, 105,
104, 105, 104, 105, 106, 107, 108, 107, 108, 107, 106, 107, 108, 107, 106, 105,
104, 103, 104, 103, 104, 103, 104, 103, 104, 103, 102, 103, 102, 101, 102, 101,
100, 101, 100, 101, 102, 103, 102, 103, 102, 103, 102, 103, 104, 105, 106, 107,
108, 109, 110, 109, 108, 107, 108, 109, 108, 107, 108, 109, 110, 111, 110, 109,
110, 109, 110, 111, 112, 113, 114, 115, 116, 117, 116, 115, 114, 115, 114, 115
114, 113, 114, 115, 114, 115, 116, 117, 118, 119, 120, 121, 120, 121, 122, 121,
122, 121, 122, 121, 122, 121, 120, 121, 122, 123, 122, 121, 122, 121, 120, 119,
120, 121, 120, 121, 120, 121, 122, 121, 122, 121, 120, 121, 122, 123, 122, 121,
122, 123, 122, 121, 122, 121, 122, 123, 122, 121, 122, 123, 122, 123, 122, 121,
120, 119, 118, 119, 118, 119, 118, 117, 116, 117, 116, 117, 118, 119, 118, 119,
```

```
120, 121, 120, 121, 120, 121, 122, 121, 120, 119, 120, 121, 122, 121, 120, 121,
122, 123, 122, 123, 122, 121, 122, 121, 120, 121, 122, 123, 122, 121, 120, 121,
122, 121, 120, 119, 118, 119, 118, 119, 120, 119, 118, 117, 118, 117, 118, 117
118, 117, 118, 119, 118, 117, 116, 117, 116, 115, 116, 117, 118, 119, 118, 117,
118, 117, 118, 119, 118, 119, 120, 121, 122, 123, 122, 123, 124, 123, 122, 123
122, 123, 124, 125, 124, 125, 126, 125, 126, 125, 124, 125, 124, 123, 122, 121,
120, 119, 120, 119, 120, 121, 122, 123, 124, 125, 124, 125, 124, 123, 122, 121,
122, 123, 122, 123, 124, 125, 124, 123, 124, 125, 124, 123, 122, 123, 124, 123,
124, 123, 124, 123, 122, 121, 120, 121, 120, 119, 120, 119, 118, 117, 116, 117,
116, 117, 118, 117, 116, 117, 116, 117, 118, 117, 116, 115, 114, 115, 114, 113,
114, 113, 114, 115, 116, 117, 116, 117, 116, 117, 118, 117, 118, 119, 118, 117,
118, 119, 118, 117, 118, 117, 116, 115, 114, 113, 114, 115, 114, 115, 114, 115,
114, 115, 116, 117, 118, 117, 116, 117, 116, 117, 118, 117, 118, 117, 116, 117,
116, 115, 114, 113, 114, 115, 114, 113, 114, 115, 116, 117, 116, 117, 116, 117,
116, 117, 118, 119, 118, 117, 116, 117, 116, 115, 116, 117, 118, 117, 118, 117
116, 115, 114, 113, 114, 115, 114, 113, 114, 115, 116, 115, 116, 115, 116, 117,
116, 115, 114, 115, 116, 115, 114, 115, 116, 115, 114, 115, 116, 117, 118, 119,
118, 119, 120, 121, 122, 121, 120, 121, 122, 123, 124, 125, 126, 125, 126, 127,
128, 127, 126, 127, 128, 127, 128, 127, 126, 125, 124, 125, 126, 127, 126, 127,
128, 127, 126, 127, 128, 127, 128, 129, 130, 131, 130, 129, 128, 129, 130, 131,
132, 133, 132, 131, 132, 131, 132, 133, 132, 131, 130, 129, 128, 129, 128, 127,
126, 127, 128, 129, 130, 129, 130, 131, 130, 129, 130, 129, 130, 129, 130, 131,
132, 131, 130, 129, 130, 131, 130, 129, 130, 131, 130, 129, 130, 129, 130, 129,
128, 129, 128, 129, 128, 127, 126, 127, 126, 127, 128, 127, 128, 127, 126, 127,
126, 125, 124, 125, 126, 125, 124, 123, 124, 123, 122, 123, 122, 121, 122, 121,
120, 119, 118, 117, 118, 119, 118, 119, 120, 121, 120, 121, 122, 123, 124, 123,
122, 123, 122, 123, 122, 123, 124, 123, 122, 121, 120, 119, 118, 117, 116, 115,
114, 115, 114, 113, 114, 113, 112, 111, 112, 113, 112, 111, 110, 109, 108, 107,
108, 109, 108, 107, 108, 109, 108, 107, 106, 107, 106, 105, 106, 107, 108, 107,
108, 109, 110, 109, 108, 107, 108, 109, 108, 107, 106, 105, 104, 105, 106, 107,
108, 107, 108, 109, 108, 109, 110, 109, 110, 109, 108, 109, 110, 111, 110, 111,
112, 111, 112, 111, 112, 113, 114, 113, 114, 113, 112, 111, 110, 111, 110, 109,
110, 109, 110, 111, 110, 109, 108, 109, 110, 109, 110, 109, 110, 109, 110, 111,
112, 113, 112, 113, 114, 113, 112, 111, 112, 113, 114, 113, 112, 113, 112, 111,
110, 111, 110, 111, 110, 109, 110, 111, 112, 113, 114, 113, 112, 111, 110, 111,
110, 111, 110, 111, 110, 109, 108, 107, 106, 105, 106, 105, 106, 107, 106, 105,
106, 107, 106, 107, 108, 109, 110, 109, 108, 109, 108, 107, 108, 107, 106, 105,
104, 103, 102, 103, 102, 103, 102, 101, 102, 101, 100, 99, 100, 99, 100, 99,
100, 101, 102, 101, 100, 101, 102, 101, 102, 101, 102, 101, 100, 99, 98, 99, 98,
99, 100, 101, 102, 101, 102, 101, 102, 101, 102, 103, 104, 103, 104, 103, 104,
105, 104, 103, 104, 105, 104, 105, 106, 105, 106, 105, 106, 107, 108, 107, 108,
107, 108, 107, 106, 105, 106, 105, 104, 103, 102, 101, 100, 99, 98, 97, 98, 97
96, 97, 98, 97, 96, 95, 94, 93, 92, 91, 92, 93, 94, 95, 96, 95, 96, 97, 96, 97
98, 97, 96, 95, 96, 95, 96, 95, 96, 95, 96, 95, 94, 93, 92, 91, 90, 89, 90, 91,
90, 89, 90, 91, 92, 91, 92, 91, 92, 93, 92, 93, 92, 93, 92, 91, 92, 91, 90, 89
90, 91, 90, 91, 90, 89, 88, 89, 90, 91, 92, 93, 94, 95, 94, 93, 92, 91, 90, 89,
90, 91, 92, 93, 92, 93, 94, 95, 96, 95, 94, 93, 92, 91, 90, 91, 90, 91, 92, 91,
90, 89, 88, 89, 88, 89, 88, 87, 88, 89, 90, 91, 92, 93, 94, 93, 94, 93, 94, 95,
```

```
96, 95, 94, 93, 92, 91, 92, 93, 94, 93, 94, 93, 92, 91, 92, 91, 92, 93, 92, 93,
92, 91, 90, 89, 90, 91, 92, 91, 92, 91, 92, 93, 92, 91, 90, 91, 92, 93, 94, 93,
92, 91, 90, 89, 90, 89, 88, 89, 90, 91, 92, 93, 94, 93, 92, 93, 92, 91, 92, 93,
94, 93, 94, 95, 96, 95, 94, 93, 92, 93, 92, 91, 90, 91, 92, 91, 90, 89, 88, 87,
88, 89, 88, 89, 88, 89, 90, 89, 90, 89, 88, 89, 90, 89, 88, 87, 88, 89, 90, 89
90, 91, 92, 93, 92, 93, 92, 91, 90, 91, 92, 93, 92, 93, 94, 93, 92, 93, 92, 91,
92, 93, 92, 91, 92, 93, 94, 93, 94, 93, 94, 93, 94, 93, 92, 91, 92, 93, 94, 93,
92, 91, 92, 93, 94, 93, 94, 93, 92, 93, 94, 95, 96, 95, 96, 95, 94, 93, 92, 91,
92, 91, 92, 91, 92, 91, 90, 89, 90, 91, 92, 91, 90, 91, 92, 93, 92, 93, 92, 91,
90, 89, 90, 91, 90, 89, 90, 91, 92, 93, 92, 91, 92, 93, 92, 91, 90, 91, 92, 93,
94, 93, 94, 93, 94, 95, 96, 95, 94, 93, 94, 93, 92, 91, 90, 91, 92, 93, 94, 95,
94, 93, 92, 93, 92, 93, 94, 95, 96, 95, 94, 93, 92, 91, 90, 91, 90, 91, 90, 91,
92, 93, 94, 95, 94, 95, 94, 93, 94, 95, 96, 97, 98, 99, 100, 99, 98, 99, 100,
101, 100, 99, 98, 99, 98, 99, 98, 99, 100, 99, 98, 97, 98, 99, 100, 99, 100, 99
98, 99, 98, 97, 96, 97, 98, 99, 100, 99, 98, 99, 98, 99, 98, 99, 98, 97, 98, 99,
100, 99, 98, 97, 96, 95, 96, 95, 94, 95, 96, 95, 96, 95, 94, 95, 94, 95, 94, 93,
92, 93, 92, 93, 94, 95, 96, 97, 96, 95, 96, 95, 96, 95, 94, 95, 96, 97, 96, 95,
96, 97, 96, 97, 98, 97, 96, 97, 98, 97, 96, 95, 94, 95, 94, 93, 92, 93, 94, 93,
92, 93, 92, 93, 92, 93, 92, 91, 90, 89, 88, 89, 88, 87, 86, 87, 86, 85, 86, 87
86, 87, 86, 85, 84, 85, 84, 85, 84, 85, 84, 83, 84, 85, 86, 87, 86, 85, 84, 83
84, 85, 86, 87, 86, 85, 84, 85, 86, 87, 86, 87, 86, 85, 84, 85, 86, 87, 88, 89,
88, 87, 88, 89, 90, 89, 88, 89, 90, 89, 90, 91, 90, 91, 90, 91, 90, 91, 92, 91,
90, 91, 92, 93, 92, 93, 92, 91, 90, 91, 92, 91, 90, 91, 90, 91, 90, 91, 92, 91,
92, 93, 92, 91, 92, 91, 92, 91, 92, 93, 92, 93, 92, 93, 94, 93, 92, 93, 92, 93
94, 95, 94, 93, 94, 93, 94, 93, 92, 93, 92, 93, 94, 95, 94, 93, 92, 93, 94, 93,
92, 91, 92, 93, 94, 93, 92, 91, 92, 93, 94, 95, 94, 95, 96, 95, 96, 95, 96, 95
96, 97, 98, 97, 96, 95, 94, 95, 96, 95, 96, 95, 96, 95, 96, 95, 94, 95, 94, 95
94, 93, 94, 93, 92, 93, 92, 93, 94, 93, 92, 91, 92, 93, 94, 95, 94, 95, 94, 95
94, 95, 94, 93, 94, 93, 94, 95, 96, 95, 96, 95, 94, 95, 96, 95, 96, 95, 94, 95
96, 95, 94, 93, 92, 91, 90, 91, 92, 93, 92, 93, 94, 95, 94, 93, 92, 91, 92, 93,
92, 91, 90, 91, 90, 91, 92, 93, 92, 93, 92, 93, 92, 91, 90, 89, 88, 87, 88, 89,
88, 87, 88, 87, 88, 89, 90, 91, 90, 91, 92, 93, 94, 93, 94, 95, 94, 95, 94, 95,
96, 97, 98, 97, 96, 97, 96, 95, 94, 93, 92, 91, 90, 91, 90, 89, 88, 89, 90, 91,
90, 91, 90, 89, 88, 87, 86, 87, 86, 87, 86, 85, 84, 85, 84, 85, 84, 83, 84, 85,
86, 85, 84, 85, 86, 87, 88, 89, 90, 89, 88, 87, 88, 89, 88, 87, 88, 89, 90, 91
92, 93, 94, 93, 92, 93, 92, 93, 92, 91, 92, 93, 92, 93, 92, 91, 92, 93, 92, 93,
94, 95, 96, 95, 94, 93, 92, 93, 94, 93, 92, 91, 92, 91, 90, 89, 90, 89, 88, 87,
88, 87, 86, 85, 86, 85, 86, 85, 86, 87, 86, 85, 84, 83, 84, 85, 86, 85, 84, 83,
84, 85, 84, 85, 84, 83, 84, 83, 84, 85, 84, 85, 86, 85, 86, 87, 88, 89, 88, 89,
88, 87, 86, 87, 86, 87, 88, 87, 86, 85, 86, 85, 84, 85, 84, 83, 84, 83, 82, 83,
82, 81, 80, 79, 78, 77, 78, 79, 78, 79, 80, 79, 80, 81, 82, 83, 82, 81, 80, 81,
82, 83, 84, 85, 86, 87, 88, 89, 88, 89, 88, 87, 88, 89, 88, 87, 86, 87, 88, 89,
88, 89, 88, 89, 88, 89, 90, 89, 88, 87, 86, 85, 86, 87, 86, 87, 86, 87, 86, 87,
88, 89, 90, 91, 90, 91, 90, 89, 88, 87, 88, 89, 90, 91, 92, 91, 92, 93, 94, 93,
94, 93, 92, 93, 92, 91, 92, 93, 92, 93, 92, 93, 94, 93, 92, 91, 90, 91, 92, 93,
94, 95, 94, 95, 94, 95, 96, 97, 98, 99, 100, 99, 98, 97, 96, 95, 96, 95, 96, 95,
94, 95, 94, 93, 92, 93, 94, 95, 96, 95, 96, 97, 96, 97, 98, 99, 98, 99, 100,
101, 102, 103, 104, 105, 106, 105, 104, 105, 104, 103, 104, 105, 106, 107, 106,
```

```
105, 106, 107, 106, 105, 104, 105, 104, 103, 102, 103, 104, 103, 102, 101, 100,
99, 100, 101, 102, 103, 102, 103, 104, 105, 106, 107, 108, 109, 108, 107, 106,
107, 108, 107, 106, 105, 106, 107, 108, 107, 108, 107, 106, 105, 106, 107, 106
107, 108, 109, 108, 107, 106, 105, 106, 107, 106, 105, 104, 105, 104, 105, 104,
103, 102, 103, 104, 103, 102, 103, 102, 103, 104, 105, 106, 105, 104, 105, 104
103, 104, 105, 106, 107, 108, 109, 110, 111, 110, 111, 112, 113, 114, 115, 116,
115, 114, 113, 114, 115, 114, 115, 114, 115, 116, 115, 116, 117, 118, 117, 116,
117, 118, 117, 116, 115, 114, 115, 116, 117, 116, 115, 114, 115, 114, 115, 114,
113, 114, 115, 114, 115, 116, 117, 118, 119, 118, 117, 118, 119, 120, 121, 122,
123, 124, 123, 122, 123, 122, 121, 122, 121, 122, 123, 124, 123, 124, 123, 122,
123, 124, 125, 126, 125, 124, 125, 124, 123, 122, 121, 122, 121, 122, 121, 122,
123, 124, 123, 122, 123, 122, 123, 122, 123, 124, 123, 122, 121, 120, 119, 120,
119, 120, 119, 120, 121, 120, 121, 120, 121, 120, 119, 120, 119, 120, 121, 120,
121, 120, 119, 118, 117, 118, 117, 118, 117, 118, 119, 118, 117, 118, 119, 120,
119, 120, 119, 120, 119, 118, 119, 118, 117, 118, 119, 118, 117, 118, 119, 118,
119, 118, 117, 118, 117, 116, 117, 118, 119, 118, 117, 118, 117, 116, 115, 114,
113, 114, 115, 114, 113, 114, 115, 114, 115, 116, 117, 116, 115, 114, 113, 114,
115, 116, 115, 114, 113, 112, 113, 114, 113, 112, 113, 112, 111, 112, 113, 112,
113, 114, 115, 116, 115, 114, 115, 114, 113, 114, 113, 112, 111, 112, 111, 112,
113, 112, 113, 114, 113, 112, 113, 112, 111, 110, 109, 108, 107, 108, 109, 110,
111, 112, 113, 112, 113, 112, 111, 112, 111, 112, 113, 112, 111, 112, 111, 112
113, 114, 113, 114, 113, 112, 113, 114, 115, 116, 117, 118, 119, 118, 119, 118,
117, 116, 117, 118, 117, 116, 115, 116, 115, 114, 115, 114, 115, 114, 113, 112,
113, 112, 113, 112, 111, 112, 111, 110, 109, 108, 109, 108, 109, 110, 111, 110,
111, 110, 111, 112, 113, 112, 113, 114, 115, 114, 113, 112, 113, 114, 115, 114,
113, 112, 111, 110, 111, 110, 111, 112, 113, 112, 113, 112, 113, 114, 115, 114,
115, 114, 115, 114, 115, 114, 113, 114, 115, 116, 115, 114, 115, 114, 113, 112,
113, 112, 113, 112, 111, 112, 111, 110, 111, 112, 111, 112, 111, 112, 113, 112,
111, 110, 109, 110, 111, 112, 113, 114, 115, 116, 115, 114, 115, 116, 117, 116,
115, 114, 115, 116, 117, 116, 117, 116, 117, 118, 117, 118, 119, 120, 119, 120,
119, 118, 119, 118, 117, 116, 115, 116, 117, 118, 117, 118, 119, 120, 119, 118,
119, 120, 119, 120, 121, 122, 121, 122, 121, 120, 121, 122, 121, 122, 121, 120,
119, 120, 121, 122, 123, 124, 123, 122, 123, 122, 121, 122, 123, 122, 121, 120,
121, 122, 123, 122, 121, 122, 123, 122, 121, 120, 121, 120, 119, 120, 121, 122,
121, 120, 121, 120, 119, 120, 119, 120, 121, 120, 119, 118, 117, 116, 117, 118
119, 118, 117, 116, 115, 116, 117, 116, 117, 116, 117, 118, 117, 116, 115, 114,
115, 116, 117, 118, 117, 116, 117, 118, 119, 118, 119, 118, 117, 116, 117, 116,
117, 116, 115, 116, 115, 114, 115, 116, 115, 114, 115, 114, 113, 112, 113, 114,
115, 116, 117, 118, 117, 118, 117, 116, 117, 116, 115, 116, 117, 116, 115, 114,
115, 114, 115, 114, 113, 114, 113, 112, 111, 112, 111, 112, 111, 112, 113, 112,
113, 114, 115, 116, 117, 118, 117, 116, 115, 116, 115, 116, 115, 114, 115, 114,
113, 112, 111, 112, 113, 112, 111, 112, 111, 110, 111, 112, 113, 112, 111, 112,
111, 110, 109, 108, 107, 106, 105, 106, 107, 108, 107, 106, 105, 106, 107, 106,
105, 106, 107, 106, 105, 104, 103, 104, 105, 106, 105, 104, 103, 104, 105, 106,
107, 108, 107, 108, 107, 106, 105, 106, 107, 108, 107, 108, 109, 108, 109, 108,
109, 110, 111, 110, 111, 110, 111, 110, 111, 110, 109, 110, 109, 108, 109, 108,
107, 108, 107, 108, 109, 108, 107, 106, 107, 108, 107, 108, 109, 108, 107, 108,
109, 108, 107, 106, 105, 104, 105, 106, 105, 106, 107, 106, 105, 104, 103, 102,
```

101, 102, 103, 102, 103, 102, 101, 102, 103, 102, 101, 102, 103, 104, 103, 102, 103, 102, 103, 104, 103, 102, 103, 104, 105, 104, 105, 104, 103, 102, 103, 104, 105, 106, 107, 106, 105, 106, 105, 104, 103, 104, 105, 104, 103, 102, 101, 100, 101, 100, 101, 100, 101, 100, 101, 102, 103, 104, 103, 102, 101, 102, 101, 100, 101, 100, 101, 102, 101, 100, 99, 100, 99, 98, 97, 98, 97, 98, 99, 98, 99, 98, 97, 98, 97, 98, 99, 98, 99, 100, 99, 98, 97, 96, 97, 96, 95, 96, 95, 96, 95, 96, 97, 96, 97, 98, 99, 100, 101, 100, 101, 102, 103, 104, 105, 104, 105, 106, 107, 106, 107, 108, 107, 108, 107, 106, 107, 106, 105, 104, 105, 104, 105, 104, 103, 102, 103, 104, 103, 104, 103, 102, 101, 100, 99, 98, 97, 96, 97, 98, 99, 98, 99, 98, 97, 96, 95, 96, 95, 96, 97, 96, 97, 98, 97, 98, 99, 100, 99, 98, 97, 96, 97, 98, 99, 98, 97, 96, 97, 96, 95, 96, 97, 96, 95, 96, 97, 98, 97, 98, 97, 98, 99, 100, 99, 100, 99, 98, 99, 100, 101, 100, 99, 100, 101, 100, 99, 100, 101, 102, 101, 100, 99, 100, 101, 102, 101, 100, 101, 100, 101, 102, 101, 102, 103, 104, 105, 106, 107, 108, 107, 106, 107, 106, 107, 106, 107, 106, 105, 104, 103, 104, 103, 102, 103, 104, 105, 106, 105, 104, 103, 104, 105, 104, 105, 106, 105, 106, 107, 106, 105, 104, 103, 104, 103, 104, 103, 104, 105, 106, 105, 106, 105, 106, 107, 106, 105, 106, 107, 106, 107, 106, 107, 106, 105, 106, 105, 106, 105, 106, 107, 106, 107, 106, 105, 106, 107, 106, 105, 104, 105, 106, 107, 108, 109, 110, 109, 108, 109, 108, 109, 108, 109, 108, 109, 108, 109, 110, 109, 108, 107, 106, 107, 108, 109, 108, 107, 106, 107, 108, 107, 108, 107, 108, 107, 106, 105, 104, 105, 106, 105, 106, 105, 106, 107, 108, 107, 108, 109, 108, 107, 108, 107, 106, 107, 108, 107, 108, 107, 106, 105, 104, 105, 104, 105, 104, 103, 102, 101, 102, 101, 100, 99, 100, 99, 98, 99, 98, 97, 98, 97, 96, 97, 96, 97, 98, 97, 98, 99, 98, 99, 100, 101, 100, 99, 98, 97, 96, 95, 96, 97, 96, 97, 98, 97, 96, 95, 94, 95, 94, 93, 94, 95, 96, 97, 96, 95, 96, 97, 98, 99, 100, 101, 100, 101, 100, 99, 98, 97, 96, 95, 94, 93, 92, 93, 92, 91, 90, 89, 88, 89, 90, 91, 92, 91, 92, 91, 90, 91, 92, 91, 90, 91, 92, 91, 92, 93, 94, 93, 94, 93, 94, 95, 94, 95, 94, 93, 94, 93, 92, 91, 92, 93, 94, 95, 94, 93, 92, 93, 92, 93, 94, 95, 96, 95, 94, 93, 92, 93, 92, 93, 92, 93, 92, 91, 90, 91, 92, 93, 94, 93, 92, 91, 92, 91, 92, 93, 92, 91, 92, 91, 90, 91, 90, 91, 90, 89, 88, 89, 90, 89, 88, 87, 88, 89, 88, 89, 88, 89, 88, 87, 86, 87, 88, 89, 88, 87, 86, 85, 86, 85, 86, 87, 86, 87, 86, 87, 88, 87, 88, 89, 90, 89, 90, 91, 92, 91, 92, 93, 92, 93, 92, 93, 94, 93, 94, 93, 94, 95, 96, 97, 96, 95, 96, 95, 96, 97, 98, 97, 96, 95, 94, 93, 94, 95, 96, 97, 98, 97, 98, 97, 98, 99, 100, 101, 100, 99, 98, 99, 98, 97, 98, 97, 98, 97, 98, 97, 96, 95, 94, 93, 92, 91, 90, 89, 90, 91, 92, 93, 94, 95, 96, 95, 96, 95, 96 97, 98, 99, 98, 97, 96, 95, 96, 95, 94, 95, 96, 97, 98, 97, 96, 97, 96, 95, 96 97, 96, 97, 96, 95, 94, 95, 96, 97, 98, 99, 100, 101, 100, 99, 100, 99, 98, 99, 100, 99, 100, 99, 100, 101, 102, 101, 100, 99, 98, 99, 100, 101, 102, 101, 102, 101, 102, 101, 100, 99, 100, 101, 102, 103, 102, 101, 100, 101, 102, 101, 102, 101, 102, 101, 102, 101, 100, 99, 98, 99, 100, 101, 100, 99, 98, 97, 96, 95, 96 97, 98, 99, 98, 99, 98, 99, 100, 99, 98, 97, 96, 97, 98, 97, 96, 97, 96, 97, 96, 97, 96, 97, 96, 97, 96, 95, 94, 95, 94, 95, 96, 95, 96, 97, 96, 95, 94, 95, 94, 95, 94, 93, 94, 95, 94, 93, 94, 93, 92, 91, 92, 91, 92, 91, 90, 89, 88, 89, 90, 91, 90, 91, 90, 89, 90, 91, 92, 91, 92, 93, 94, 95, 94, 93, 94, 93, 92, 93, 92, 91, 90, 89, 90, 89, 90, 91, 92, 91, 92, 93, 94, 93, 92, 93, 92, 91, 92, 93, 94, 93, 92, 91, 92, 91, 90, 91, 90, 91, 90, 91, 92, 91, 92, 93, 94, 95, 96, 97, 98, 99, 98, 99, 98, 97, 98, 97, 98, 99, 98, 99, 100, 101, 100, 101, 100, 99, 98, 99 98, 99, 100, 101, 100, 101, 102, 101, 100, 101, 100, 101, 100, 99, 100, 99, 98,

97, 98, 99, 100, 99, 98, 99, 100, 99, 100, 99, 100, 99, 98, 97, 98, 99, 100, 99, 100, 101, 100, 101, 100, 99, 98, 97, 96, 97, 96, 95, 96, 95, 96, 95, 94, 93, 94, 95, 96, 95, 94, 93, 94, 93, 92, 93, 94, 93, 92, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 99, 98, 99, 100, 101, 100, 101, 102, 101, 102, 101, 100, 99, 98, 97, 96, 95, 96, 95, 96, 97, 98, 97, 98, 97, 98, 99, 100, 99, 100, 99, 98, 97, 98, 99, 100, 99, 100, 101, 100, 101, 102, 103, 104, 103, 102, 103, 102, 103, 104, 105, 104, 103, 102, 101, 100, 99, 100, 99, 100, 101, 102, 101, 102, 103, 102, 101, 100, 101, 102, 101, 100, 101, 102, 101, 100, 99, 98, 99, 98, 99, 100, 101, 100, 101, 102, 103, 104, 105, 106, 105, 106, 105, 104, 103, 104, 105, 106, 107, 106, 107, 108, 109, 108, 109, 110, 111, 110, 111, 112, 113, 112, 111, 110, 111, 110, 111, 110, 111, 110, 111, 110, 109, 110, 109, 110, 111, 112, 113, 114, 115, 114, 113, 112, 111, 110, 111, 112, 113, 112, 113, 114, 115, 114, 113, 112, 111, 112, 111, 112, 113, 112, 113, 112, 113, 114, 113, 114, 115, 116, 117, 118, 117, 116, 115, 114, 115, 116, 117, 116, 117, 118, 117, 118, 117, 116, 117, 116, 115, 116, 117, 118, 117, 118, 117, 118, 119, 120, 121, 122, 121, 122, 123, 122, 121, 122, 123, 124, 125, 124, 123, 124, 123, 122, 121, 120, 121, 120, 121, 120, 121, 122, 121, 122, 121, 122, 123, 124, 123, 122, 121, 122, 123, 124, 125, 124, 125 124, 125, 124, 123, 124, 125, 126, 125, 124, 123, 122, 123, 122, 121, 120, 121, 122, 121, 120, 119, 120, 119, 118, 117, 118, 119, 120, 119, 120, 119, 118, 117, 118, 117, 118, 119, 120, 121, 120, 121, 122, 121, 120, 121, 120, 119, 118, 117, 116, 117, 116, 115, 114, 113, 112, 111, 112, 113, 114, 113, 112, 113, 112, 111, 112, 113, 112, 113, 114, 115, 116, 117, 116, 115, 116, 115, 114, 113, 114, 113, 112, 113, 112, 111, 112, 111, 110, 111, 112, 111, 112, 113, 112, 111, 110, 109, 110, 109, 110, 111, 112, 111, 110, 111, 110, 111, 112, 113, 114, 115, 116, 117, 118, 117, 118, 119, 120, 121, 120, 121, 120, 119, 120, 119, 120, 121, 120, 121, 122, 121, 122, 123, 122, 123, 122, 121, 120, 121, 120, 119, 118, 119, 120, 121, 120, 121, 122, 123, 122, 121, 122, 121, 120, 121, 122, 123, 124, 125, 124, 125 126, 125, 126, 127, 126, 125, 126, 125, 126, 127, 128, 129, 128, 129, 130, 129, 128, 129, 128, 127, 128, 127, 126, 127, 126, 127, 126, 125, 124, 123, 124, 125, 126, 125, 124, 123, 122, 121, 120, 121, 120, 121, 120, 119, 120, 119, 120, 121, 120, 121, 120, 119, 120, 119, 120, 121, 120, 121, 120, 121, 122, 123, 124, 123, 122, 123, 122, 121, 120, 121, 120, 119, 120, 119, 118, 117, 116, 115, 116, 117, 116, 115, 114, 115, 114, 113, 112, 111, 110, 111, 112, 111, 110, 111, 110, 111, 112, 111, 110, 109, 110, 109, 108, 107, 106, 107, 108, 107, 108, 109, 108, 109, 108, 107, 106, 107, 108, 107, 106, 107, 108, 109, 110, 109, 110, 109, 110, 109, 110, 111, 110, 109, 108, 107, 108, 107, 108, 109, 110, 109, 110, 111, 110, 111, 112, 111, 110, 109, 110, 111, 110, 111, 112, 111, 110, 109, 108, 109, 108, 107, 106, 107, 108, 107, 106, 107, 106, 107, 106, 105, 104, 103, 102, 103, 102, 103, 102, 101, 102, 101, 102, 103, 104, 103, 104, 105, 106, 105, 106, 105, 104, 105, 106, 105, 106, 105, 106, 107, 108, 109, 108, 109, 110, 111, 110, 111, 110, 111, 110, 111, 112, 111, 112, 111, 110, 111, 110, 111, 112, 113, 114, 113, 114, 115, 114, 113, 114, 115, 116, 117, 118, 117, 116, 115, 114, 115, 114, 113, 112, 111, 110, 109, 108, 109, 110, 111, 112, 113, 112, 113, 114, 115, 114, 113, 112, 113, 112, 111, 112, 111, 110, 111, 110, 109, 110, 109, 108, 107, 106, 107, 106, 107, 106, 107, 108, 107, 106, 107, 106, 105, 104, 103, 102, 103, 104, 105, 106, 105, 104, 105, 104, 105, 106, 107, 106, 105, 104, 105, 104, 105, 106, 105, 104, 103, 104, 103, 102, 101, 102, 103, 104, 103, 102, 103, 102, 103, 104, 103, 104, 105, 106, 107, 108, 107, 106, 107, 106, 105, 104, 105, 104, 103, 102, 103, 104, 105,

```
106, 105, 106, 107, 106, 105, 106, 107, 106, 105, 104, 103, 102, 101, 100, 101,
102, 103, 104, 103, 102, 103, 104, 103, 102, 101, 102, 101, 102, 101, 100, 101,
100, 99, 98, 99, 98, 97, 96, 95, 94, 93, 92, 91, 90, 91, 90, 91, 90, 91, 90, 91
90, 89, 90, 91, 90, 89, 90, 91, 92, 93, 92, 91, 90, 89, 88, 89, 90, 91, 90, 91,
90, 91, 92, 93, 94, 95, 94, 93, 94, 93, 92, 91, 92, 91, 92, 91, 92, 91, 90, 91
90, 89, 88, 87, 88, 87, 88, 89, 88, 89, 88, 89, 88, 87, 88, 87, 86, 87, 88, 89,
88, 89, 88, 87, 86, 85, 84, 83, 84, 85, 86, 87, 88, 87, 86, 85, 86, 85, 86, 85,
84, 85, 84, 85, 86, 87, 88, 89, 88, 87, 88, 87, 88, 87, 86, 85, 84, 85, 86, 87,
88, 89, 90, 89, 88, 89, 88, 87, 88, 87, 86, 87, 86, 87, 88, 89, 88, 89, 88, 89,
90, 91, 92, 91, 90, 89, 88, 89, 90, 89, 88, 87, 86, 87, 88, 89, 88, 89, 88, 87,
88, 89, 88, 89, 88, 87, 88, 89, 88, 89, 90, 89, 88, 87, 86, 85, 84, 83, 84, 85,
86, 85, 84, 85, 86, 87, 88, 89, 90, 91, 92, 91, 90, 89, 90, 91, 92, 93, 92, 93
94, 95, 96, 97, 96, 97, 98, 99, 100, 101, 102, 103, 104, 103, 104, 103, 102,
103, 104, 105, 104, 105, 106, 105, 104, 103, 102, 103, 104, 105, 106, 105, 106,
107, 106, 107, 106, 105, 104, 103, 104, 103, 104, 105, 104, 103, 102, 103, 102,
103, 102, 103, 102, 101, 100, 101, 102, 103, 102, 101, 102, 103, 104, 105, 106,
107, 106, 105, 104, 105, 106, 105, 106, 105, 106, 107, 106, 105, 106, 105, 106,
107, 106, 107, 106, 107, 108, 109, 108, 109, 108, 109, 108, 109, 108, 109, 110,
109, 110, 111, 110, 111, 112, 111, 112, 113, 114, 113, 112, 111, 112, 113, 114,
113, 114, 113, 112, 111, 112, 113, 114, 113, 112, 111, 110, 109, 110, 109, 108,
109, 108, 107, 106, 107, 108, 107, 108, 109, 110, 109, 110, 109, 108, 109, 108,
107, 106, 107, 106, 105, 106, 107, 106, 107, 106, 107, 106, 105, 106, 107, 108,
109, 110, 109, 108, 107, 106, 105, 104, 103, 102, 101, 100, 101, 100, 99, 98,
97, 96, 97, 98, 97, 96, 95, 96, 97, 98, 99, 98, 99, 98, 99, 100, 101, 102, 103,
102, 101, 102, 101, 100, 99, 98, 99, 100, 101, 102, 103, 102, 103, 104, 103,
104, 105, 106, 105, 104, 105, 104, 105, 104, 103, 102, 103, 104, 105, 104, 103,
102, 101, 100, 101, 100, 99, 100, 99, 100, 101, 102, 103, 104, 105, 106, 105,
104, 103, 104, 103, 102, 101, 102, 101, 100, 101, 100, 99, 98, 97, 98, 99, 98,
99, 98, 97, 98, 97, 96, 97, 98, 97, 98, 99, 98, 97, 96, 97, 96, 97, 96, 97, 96,
97, 98, 97, 96, 97, 96, 97, 96, 97, 96, 97, 96, 95, 94, 93, 94, 95, 96, 97, 98,
99, 100, 99, 98, 97, 98, 99, 100, 99, 100, 101, 102, 101, 102, 103, 104, 105,
104, 103, 102, 101, 102, 103, 104, 105, 106, 105, 106, 107, 108, 107, 108, 107,
108, 107, 106, 107, 106, 107, 106, 107, 106, 105, 104, 105, 104, 105, 106, 107,
108, 107, 108, 107, 108, 109, 110, 109, 110, 109, 110, 109, 110, 109, 108, 107,
108, 109, 108, 107, 108, 107, 106, 107, 108, 109, 108, 109, 110, 111, 110, 109,
108, 107, 106, 107, 106, 107, 108, 109, 108, 109, 110, 109, 110, 111, 110, 109,
108, 107, 108, 109, 110, 109, 110, 109, 108, 107, 108, 109, 108, 107, 108, 107,
106, 107, 106, 107, 108, 109, 110, 109, 110, 111, 110, 111, 110, 109, 110, 111,
110, 111, 112, 111, 112, 111, 110, 109, 108, 109, 108, 107, 106, 105, 104, 103,
102, 101, 100, 101, 102, 101, 102, 103, 102, 101, 100, 101, 102, 103, 104, 103,
104, 103, 102, 101, 102, 101, 100, 101, 102, 103, 104, 103, 104, 105, 104, 105,
106, 107, 106, 105, 104, 105, 104, 103, 104, 103, 104, 103, 104, 105, 104, 105
106, 105, 106, 105, 106, 107, 106, 107, 106, 105, 104, 103, 102, 103, 102, 103,
102, 101, 102, 101, 100, 101, 102, 101, 102, 101, 102, 103, 102, 103, 104, 105,
106, 105, 106, 105, 104, 103, 104, 105, 106, 105, 106, 107, 108, 107, 106, 105,
106, 105, 106, 107, 106, 107, 106, 107, 106, 107, 108, 107, 108, 107, 106, 107,
106, 105, 106, 105, 104, 105, 104, 105, 106, 107, 106, 105, 106, 107, 108, 107,
108, 107, 106, 107, 106, 105, 106, 105, 106, 105, 106, 105, 106, 105, 106, 107,
```

106, 105, 106, 105, 104, 103, 102, 103, 104, 105, 106, 105, 104, 105, 106, 105, 106, 105, 106, 105, 106, 105, 106, 105, 104, 103, 104, 103, 102, 103, 102, 103, 102, 103, 102, 103, 104, 103, 102, 101, 100, 99, 98, 97, 96, 95, 94, 95, 96, 97, 98, 99, 98, 99, 100, 99, 98, 97, 98, 99, 98, 99, 100, 99, 100, 99, 100, 101, 100, 99, 98, 99, 100, 99, 100, 99, 98, 97, 98, 97, 96, 95, 94, 95, 94, 93, 94, 95, 96, 95, 96, 95, 94, 95, 96, 97, 96, 97, 98, 99, 100, 99, 98, 99, 100, 101, 102, 103, 102, 101, 100, 101, 102, 101, 102, 103, 102, 101, 102, 101, 102, 101, 100, 101, 102, 103, 104, 103, 102, 103, 104, 103, 104, 105, 104, 103, 104, 103 102, 103, 102, 101, 102, 101, 102, 103, 102, 103, 104, 103, 104, 105, 104, 103, 102, 103, 102, 103, 102, 101, 100, 99, 98, 99, 98, 99, 98, 99, 100, 101, 100, 101, 102, 101, 100, 99, 98, 97, 96, 95, 94, 93, 92, 93, 92, 93, 94, 93, 94, 95, 96, 97, 96, 95, 94, 95, 96, 95, 96, 95, 96, 97, 98, 97, 98, 99, 100, 101, 100, 99, 100, 101, 102, 103, 102, 103, 102, 103, 102, 103, 102, 101, 102, 101, 102, 103, 102, 103, 102, 103, 104, 105, 104, 105, 104, 105, 104, 103, 102, 103, 104, 103, 102, 103, 102, 101, 102, 101, 100, 99, 98, 97, 98, 99, 100, 101, 100, 101, 102, 103, 104, 103, 104, 105, 106, 105, 104, 103, 102, 103, 102, 101, 100, 101, 102, 103, 104, 105, 104, 105, 106, 105, 104, 105, 106, 105, 104, 105, 104, 103, 102, 101, 100, 99, 98, 99, 100, 101, 102, 101, 100, 101, 102, 103, 102, 103, 102, 101, 100, 101, 102, 103, 102, 101, 100, 99, 100, 99, 98, 99, 100, 99, 98, 97, 98, 99, 100, 99, 100, 99, 98, 99, 98, 99, 98, 99, 100, 101, 100, 99, 98, 97 98, 99, 98, 99, 100, 101, 102, 103, 102, 101, 100, 101, 100, 101, 102, 103, 102, 101, 102, 101, 100, 99, 100, 101, 102, 103, 102, 103, 102, 101, 100, 99, 100, 99, 98, 97, 96, 97, 96, 95, 94, 93, 94, 95, 96, 95, 96, 97, 96, 95, 96, 97, 98, 97, 98, 99, 98, 99, 100, 101, 100, 99, 100, 101, 100, 99, 98, 97, 96, 97, 96, 95, 96, 95, 96, 95, 96, 95, 94, 95, 94, 95, 96, 95, 96, 97, 98, 99, 98, 97, 96, 97, 96, 97, 96, 97, 96, 95, 96, 95, 96, 95, 94, 93, 94, 93, 94, 93, 92, 91, 90, 89, 90, 89, 90, 89, 90, 89, 90, 89, 90, 89, 88, 87, 88, 89, 90, 89, 88, 87, 88 89, 88, 87, 86, 87, 88, 89, 90, 89, 88, 87, 86, 85, 84, 83, 84, 85, 86, 85, 86 87, 88, 89, 90, 91, 90, 89, 90, 91, 92, 93, 94, 95, 96, 95, 94, 95, 94, 93, 92, 91, 90, 89, 88, 89, 88, 89, 90, 91, 90, 91, 92, 93, 92, 93, 94, 95, 96, 97, 98, 97, 98, 99, 98, 99, 100, 101, 100, 101, 100, 101, 102, 103, 104, 105, 104, 103, 104, 103, 102, 101, 102, 103, 104, 103, 102, 103, 104, 105, 106, 107, 108, 109, 108, 109, 108, 107, 108, 109, 108, 109, 110, 111, 110, 109, 110, 109, 108, 107, 106, 107, 106, 107, 106, 105, 104, 103, 102, 103, 104, 103, 104, 103, 102, 101, 102, 103, 102, 103, 104, 103, 104, 103, 102, 101, 102, 101, 100, 101, 100, 101, 102, 101, 102, 103, 104, 105, 104, 103, 104, 105, 106, 107, 106, 107, 106, 107, 106, 107, 108, 107, 108, 109, 108, 107, 106, 105, 106, 107, 106, 105, 106, 105, 106, 107, 108, 107, 108, 107, 106, 107, 108, 107, 108, 107, 106, 107, 108, 109, 108, 109, 108, 109, 108, 107, 108, 109, 108, 107, 108, 107, 108, 109, 108, 107, 106, 107, 108, 107, 108, 107, 106, 105, 104, 105, 106, 107, 106, 107, 108, 109, 110, 109, 108, 107, 106, 105, 106, 105, 106, 107, 108, 109, 110, 109, 108, 107, 106, 107, 108, 109, 108, 107, 108, 109, 110, 111, 112, 111, 112, 113, 112, 113, 114, 113, 114, 115, 114, 115, 114, 113, 114, 113, 112, 113, 114, 115, 116, 115, 114, 113, 112, 113, 114, 115, 114, 113, 114, 115, 116, 117, 116, 115, 116, 115, 116, 117, 118, 119, 120, 119, 118, 117, 116, 115, 114, 113, 112, 111, 112, 113, 112, 111, 112, 113, 114, 113, 114, 115, 116, 117, 118, 117, 118, 117, 118, 117, 118, 117, 116, 117, 118, 117, 116, 117, 118, 117, 118, 119, 120, 119, 118, 117, 118, 117, 116, 115, 116, 115, 116, 115, 116, 115, 116, 115, 116, 115, 114, 113,

```
114, 113, 112, 111, 112, 111, 110, 109, 108, 107, 108, 107, 106, 107, 106, 107,
106, 107, 106, 107, 106, 107, 106, 105, 106, 105, 106, 107, 108, 109, 108, 109,
108, 109, 110, 111, 112, 113, 112, 111, 112, 113, 114, 113, 114, 113, 112, 111,
112, 113, 114, 113, 112, 111, 112, 113, 114, 115, 114, 115, 114, 113, 114, 115,
114, 113, 112, 113, 114, 115, 116, 117, 118, 119, 120, 119, 120, 119, 120, 121,
122, 123, 122, 123, 122, 121, 122, 121, 120, 119, 118, 119, 120, 119, 120, 121,
122, 121, 120, 119, 120, 121, 122, 123, 124, 123, 122, 121, 122, 121, 120, 119,
120, 121, 122, 121, 120, 121, 120, 119, 118, 119, 118, 117, 116, 115, 116, 117,
116, 117, 118, 117, 116, 115, 114, 115, 114, 113, 114, 113, 112, 111, 112, 113,
112, 113, 112, 111, 112, 111, 110, 109, 108, 109, 108, 109, 110, 109, 110, 111,
110, 109, 110, 111, 110, 111, 110, 111, 112, 113, 114, 115, 114, 115, 116, 117,
118, 119, 118, 119, 118, 119, 120, 121, 120, 121, 122, 123, 124, 123, 122, 121,
120, 119, 118, 119, 118, 117, 118, 119, 120, 121, 120, 119, 120, 121, 120, 119,
120, 121, 122, 123, 122, 123, 124, 123, 122, 121, 120, 121, 120, 119, 118, 117,
116, 117, 116, 117, 118, 119, 118, 117, 118, 119, 120, 121, 122, 123, 124, 123,
122, 121, 122, 123, 124, 123, 122, 123, 124, 123, 122, 121, 120, 119, 120, 119,
120, 121, 122, 123, 122, 121, 122, 121, 120, 119, 118, 119, 120, 119, 120, 121,
122, 123, 124, 123, 122, 121, 120, 121, 122, 123, 122, 123, 122, 123, 122, 123,
122, 123, 124, 125, 126, 125, 124, 123, 122, 123, 124, 123, 124, 123, 124, 125,
124, 123, 122, 123, 122, 123, 122, 123, 124, 123, 122, 121, 120, 119, 120, 119
120, 121, 120, 119, 120, 119, 118, 119, 118, 117, 116, 115, 116, 115, 114, 115,
116, 117, 116, 115, 114, 113, 112, 111, 110, 109, 110, 111, 112, 113, 114, 113,
114, 115, 114, 113, 112, 111, 112, 113, 114, 115, 114, 113, 112, 111, 110, 111,
112, 111, 110, 111, 112, 113, 114, 115, 116, 117, 116, 117, 118, 117, 118, 117,
116, 115, 114, 113, 114, 113, 114, 113, 112, 113, 112, 113, 112, 113, 112, 113,
112, 113, 112, 111, 112, 111, 110, 109, 110, 109, 108, 107, 106, 107, 106, 105,
106, 107, 108, 109, 108, 107, 106, 107, 106, 105, 104, 103, 104, 105, 106, 105,
104, 103, 102, 103, 104, 103, 104, 105, 104, 103, 104, 105, 106, 107, 108, 109,
108, 107, 108, 109, 108, 107, 108, 107, 108, 107, 106, 107, 106, 105, 104, 105,
106, 105, 106, 105, 106, 107, 108, 109, 108, 107, 108, 109, 110, 109, 110, 109,
108, 107, 106, 107, 106, 105, 104, 105, 106, 105, 104, 103, 102, 103, 104, 103,
104, 103, 104, 103, 104, 105, 104, 103, 102, 103, 102, 101, 100, 99, 100, 99,
100, 101, 100, 99, 100, 101, 102, 103, 104, 105, 106, 105, 104, 105, 106, 105,
106, 105, 104, 103, 104, 103, 104, 103, 104, 103, 104, 103, 104, 103, 104, 105,
106, 105, 106, 107, 106, 107, 106, 107, 106, 105, 104, 105, 106, 107, 108, 109,
108, 109, 110, 109, 110, 109, 110, 109, 110, 109, 108, 109, 108, 107, 108, 109,
108, 107, 106, 105, 104, 103, 104, 105, 106, 107, 106, 107, 108, 107, 106, 107,
106, 107, 106, 105, 106, 107, 106, 107, 106, 105, 104, 103, 104, 103, 102, 101,
100, 101, 100, 101, 100, 101, 102, 101, 100, 101, 100, 99, 98, 99, 100, 101,
100, 101, 100, 99, 100, 99, 100, 99, 98, 97, 98, 97, 96, 97, 98, 97, 96, 97, 96
95, 94, 93, 92, 91, 90, 89, 90, 89, 88, 89, 90, 89, 90, 89, 88, 87, 88, 89, 90,
91, 90, 89, 88, 87, 86, 87, 86, 85, 84, 83, 82, 83, 84, 85, 86, 85, 86, 87, 86,
85, 84, 85, 86, 85, 86, 85, 84, 83, 84, 83, 82, 81, 82, 83, 82, 83, 84, 83, 82,
83, 84, 85, 86, 85, 84, 83, 82, 83, 82, 81, 80, 79, 80, 81, 80, 79, 78, 77, 78
79, 80, 81, 82, 83, 82, 81, 82, 81, 80, 81, 82, 81, 80, 79, 78, 79, 80, 81, 80,
81, 82, 81, 80, 81, 82, 81, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 90,
91, 92, 91, 90, 91, 92, 93, 94, 95, 94, 95, 96, 97, 96, 97, 96, 95, 96, 97, 96
95, 94, 93, 94, 95, 94, 93, 92, 93, 92, 93, 94, 93, 92, 93, 92, 91, 92, 93, 94,
```

```
93, 92, 91, 90, 89, 90, 89, 88, 87, 88, 87, 88, 87, 86, 85, 86, 85, 84, 83, 84,
85, 84, 85, 86, 87, 86, 87, 86, 87, 88, 87, 86, 87, 86, 87, 88, 87, 88, 89, 88,
89, 90, 89, 90, 89, 88, 89, 88, 87, 88, 87, 88, 87, 86, 87, 88, 87, 86, 85, 86,
87, 86, 87, 88, 87, 88, 87, 88, 87, 88, 87, 88, 89, 88, 87, 86, 87, 88, 87, 88,
89, 88, 89, 88, 89, 88, 87, 86, 85, 86, 85, 86, 87, 86, 87, 88, 89, 90, 91, 90,
89, 88, 89, 88, 87, 86, 85, 86, 87, 86, 87, 86, 87, 88, 87, 86, 87, 88, 89, 90,
89, 88, 87, 86, 85, 86, 87, 88, 87, 88, 87, 86, 87, 86, 85, 86, 85, 84, 85, 86,
85, 84, 85, 84, 85, 86, 85, 86, 87, 86, 85, 84, 85, 86, 85, 84, 85, 84, 85, 86,
87, 88, 89, 90, 91, 92, 91, 92, 93, 92, 91, 92, 93, 92, 91, 90, 89, 88, 89, 90,
89, 90, 91, 92, 91, 90, 91, 92, 91, 90, 89, 88, 89, 88, 89, 90, 91, 90, 91, 92,
93, 94, 93, 94, 95, 94, 95, 94, 93, 94, 95, 94, 95, 96, 97, 98, 97, 98, 99, 100,
101, 102, 101, 100, 99, 98, 97, 96, 95, 96, 95, 96, 95, 94, 95, 96, 95, 96, 95,
94, 95, 94, 93, 94, 95, 96, 97, 98, 97, 98, 99, 100, 101, 100, 101, 102, 101,
100, 99, 100, 99, 98, 97, 98, 97, 98, 99, 100, 99, 100, 101, 100, 99, 98, 99,
98, 99, 100, 99, 100, 101, 100, 99, 98, 97, 96, 97, 96, 97, 96, 97, 98, 99, 98,
97, 98, 97, 96, 97, 98, 97, 98, 97, 98, 97, 96, 97, 96, 97, 96, 95, 96, 97, 98,
97, 98, 99, 98, 99, 100, 101, 102, 103, 104, 105, 104, 105, 104, 103, 104, 103,
104, 103, 102, 103, 104, 105, 104, 105, 106, 105, 106, 105, 104, 105, 106, 105,
104, 105, 106, 105, 104, 103, 102, 101, 100, 99, 100, 99, 98, 99, 98, 97, 98,
97, 96, 97, 96, 95, 94, 93, 94, 93, 94, 93, 92, 93, 94, 95, 94, 93, 94, 95, 94
93, 92, 93, 92, 91, 92, 93, 94, 95, 94, 93, 92, 93, 94, 93, 92, 91, 90, 89, 90,
89, 90, 89, 90, 91, 92, 93, 94, 95, 94, 95, 96, 95, 94, 93, 94, 93, 92, 93, 94,
95, 96, 95, 94, 95, 96, 95, 96, 97, 96, 97, 96, 95, 94, 93, 92, 93, 92, 91, 92,
93, 92, 91, 92, 91, 92, 93, 92, 93, 92, 91, 92, 93, 94, 95, 96, 97, 96, 97, 96,
95, 94, 93, 92, 91, 92, 93, 94, 93, 92, 93, 94, 95, 94, 93, 94, 95, 96, 95, 96,
95, 94, 95, 96, 97, 98, 99, 100, 101, 100, 99, 100, 99, 98, 97, 96, 95, 94, 93,
92, 91, 90, 91, 92, 93, 94, 93, 94, 93, 92, 93, 94, 95, 96, 97, 96, 97, 96, 97,
98, 99, 98, 99, 98, 99, 98, 97, 98, 99, 100, 101, 102, 103, 102, 101, 102, 101,
102, 103, 102, 103, 102, 103, 102, 101, 100, 99, 98, 99, 100, 101, 100, 99, 100,
99, 100, 101, 102, 103, 102, 103, 102, 103, 102, 103, 104, 105, 104, 103, 104,
103, 104, 105, 106, 105, 104, 105, 104, 103, 102, 101, 102, 103, 104, 105, 106,
105, 104, 103, 104, 103, 102, 101, 100, 101, 100, 99, 100, 99, 98, 97, 96, 95,
96, 95, 94, 95, 96, 95, 96, 97, 96, 95, 94, 95, 94, 95, 96, 97, 98, 99, 100,
101, 102, 101, 102, 101, 100, 101, 102, 101, 102, 103, 102, 101, 102, 101, 100,
99, 98, 99, 98, 99, 100, 99, 100, 101, 102, 103, 104, 103, 104, 103, 104, 105,
104, 103, 104, 105, 104, 105, 104, 103, 102, 101, 100, 99, 100, 101, 102, 103,
104, 103, 104, 105, 104, 103, 104, 103, 102, 103, 102, 101, 100, 101, 102, 103,
104, 103, 102, 103, 104, 103, 102, 101, 100, 99, 98, 99, 98, 99, 100, 101, 102,
101, 100, 99, 98, 97, 96, 97, 98, 99, 98, 99, 98, 97, 98, 97, 96, 95, 96, 97,
96, 95, 96, 97, 96, 97, 96, 97, 96, 97, 96, 97, 98, 99, 100, 99, 100, 99, 100,
101, 100, 99, 98, 97, 96, 97, 96, 97, 98, 97, 98, 97, 96, 97, 96, 97, 96, 97,
96, 95, 96, 95, 96, 95, 96, 95, 94, 95, 94, 93, 94, 95, 94, 93, 94, 95, 96, 97,
98, 97, 96, 97, 96, 95, 96, 97, 96, 95, 96, 97, 96, 95, 96, 95, 96, 97, 96, 97,
96, 97, 98, 99, 100, 99, 98, 97, 98, 97, 96, 97, 98, 97, 96, 95, 96, 97, 96, 95
94, 93, 94, 95, 96, 97, 96, 95, 94, 95, 96, 95, 96, 95, 96, 95, 96, 95, 96, 95,
94, 95, 96, 95, 94, 93, 94, 93, 94, 95, 96, 97, 98, 97, 96, 95, 94, 93, 92, 91,
92, 91, 90, 89, 88, 89, 90, 91, 90, 89, 90, 91, 90, 89, 90, 91, 92, 93, 94, 93,
94, 95, 94, 95, 94, 95, 94, 93, 94, 95, 96, 95, 96, 97, 96, 97, 98, 99, 100, 99,
```

98, 97, 98, 97, 96, 97, 98, 97, 96, 97, 96, 97, 98, 99, 100, 99, 100, 101, 100, 101, 102, 101, 100, 101, 102, 103, 102, 101, 100, 101, 100, 101, 100, 99, 100, 99, 98, 97, 98, 99, 98, 99, 100, 99, 100, 101, 102, 103, 102, 101, 100, 99, 98, 97, 98, 97, 96, 97, 98, 99, 100, 99, 98, 99, 98, 97, 98, 97, 98, 99, 100, 99, 100, 101, 100, 101, 102, 101, 102, 101, 102, 103, 104, 105, 104, 103, 104, 103 104, 105, 104, 105, 104, 105, 104, 105, 106, 107, 108, 107, 108, 109, 110, 109, 110, 111, 112, 113, 114, 115, 114, 115, 114, 113, 112, 113, 112, 113, 112, 111, 112, 111, 112, 111, 110, 109, 110, 109, 108, 109, 108, 109, 108, 109, 110, 111, 112, 113, 112, 113, 114, 115, 114, 113, 112, 113, 114, 113, 112, 111, 112, 113, 112, 113, 114, 115, 116, 115, 116, 117, 118, 117, 116, 117, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 128, 129, 130, 131, 132, 131, 132, 131, 130, 129, 128, 129, 128, 129, 128, 127, 128, 129, 128, 127, 126, 125 124, 123, 124, 125, 124, 125, 126, 125, 126, 125, 126, 125, 124, 125, 124, 125, 124, 125, 126, 125, 126, 125, 126, 127, 128, 127, 128, 127, 128, 127, 126, 125, 126, 125, 124, 125, 126, 125, 126, 125, 126, 125, 124, 125, 124, 123, 122, 121, 122, 121, 120, 121, 120, 121, 122, 121, 120, 119, 118, 119, 120, 121, 122, 121, 122, 123, 122, 121, 122, 123, 122, 121, 120, 121, 122, 121, 122, 121, 122, 123, 122, 123, 122, 121, 120, 119, 120, 121, 120, 121, 120, 119, 120, 119, 118, 119, 118, 117, 118, 119, 120, 119, 120, 121, 120, 119, 120, 119, 120, 121, 120, 121, 122, 121, 122, 121, 122, 123, 122, 121, 122, 121, 122, 123, 124, 123, 122, 121, 122, 121, 120, 119, 118, 119, 118, 117, 116, 117, 116, 115, 116, 115, 114, 113, 112, 113, 112, 111, 112, 111, 112, 111, 112, 113, 112, 113, 112, 111, 112, 111, 112, 111, 112, 111, 110, 109, 110, 111, 112, 111, 110, 109, 110, 109, 108, 109, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 117, 118, 119, 118, 119, 120, 119, 120, 121, 120, 121, 120, 119, 120, 119, 118, 117, 116, 115, 114, 115, 116, 117, 116, 117, 116, 117, 118, 117, 118, 119, 120, 121, 122, 121, 122, 123, 122, 123, 122, 123, 122, 123, 122, 121, 122, 121, 120, 121, 120, 119, 118, 119, 118, 119, 120, 119, 118, 119, 120, 119, 118, 119, 118, 117, 116, 115, 114, 115, 116, 117, 116, 117, 118, 117, 118, 119, 118, 117, 118, 119, 118, 117, 116, 117, 116, 115, 116, 117, 118, 119, 118, 119, 118, 117, 116, 117, 116, 117, 118, 119, 120, 121, 120, 121, 120, 121, 122, 123, 122, 123, 122, 121, 120, 121, 122, 121, 122, 121, 120, 121, 122, 123, 124, 123, 124, 125, 124, 123, 122, 123, 124, 123, 124, 125, 126, 127, 126, 127, 128, 129, 128, 129, 130, 129, 128, 127, 128, 129, 128, 129, 128, 129, 128, 129, 128, 127, 128, 127, 126, 125, 126, 125, 126, 127, 126, 127, 126, 125, 126, 127, 128, 127, 128, 129, 130, 129, 130, 131, 132, 133, 134, 133, 132, 133, 134, 135, 134, 133, 132, 131, 132, 133, 132, 131, 130, 129, 130, 129, 130, 129, 128, 127, 126, 125, 124, 123, 122, 123, 124, 125, 124, 123, 122, 123, 124, 125, 124, 125, 124, 125, 126, 125, 124, 125, 124, 125, 124, 125 124, 123, 122, 121, 120, 119, 120, 119, 118, 117, 118, 119, 120, 121, 122, 121, 120, 119, 120, 121, 120, 121, 120, 121, 120, 119, 120, 119, 120, 119, 120, 119, 118, 117, 116, 117, 116, 117, 116, 117, 116, 115, 116, 117, 118, 119, 118, 119, 120, 121, 120, 121, 120, 121, 122, 121, 120, 121, 122, 121, 122, 121, 120, 121, 122, 121, 120, 121, 122, 121, 120, 121, 122, 121, 120, 119, 120, 119, 120, 121, 122, 121, 122, 121, 122, 121, 120, 119, 118, 119, 120, 121, 122, 121, 122, 121, 122, 121, 120, 121, 120, 121, 122, 123, 124, 123, 122, 123, 124, 123, 122, 121, 120, 119, 118, 117, 116, 115, 116, 115, 116, 115, 114, 113, 114, 113, 114, 113, 112, 111, 112, 113, 114, 115, 114, 113, 112, 113, 112, 113, 114, 115, 114, 115 114, 113, 114, 113, 112, 113, 112, 113, 112, 113, 112, 113, 112, 111, 112, 111,

```
110, 109, 110, 109, 110, 111, 110, 111, 112, 113, 114, 113, 112, 111, 110, 109,
108, 107, 108, 109, 110, 111, 112, 111, 110, 111, 110, 109, 110, 111, 110, 109,
110, 109, 108, 109, 108, 109, 110, 109, 110, 109, 108, 109, 110, 109, 110, 109,
110, 109, 110, 109, 108, 107, 106, 105, 104, 105, 104, 105, 104, 105, 106, 105,
106, 105, 104, 103, 102, 103, 102, 101, 102, 101, 102, 103, 104, 105, 104, 105
104, 105, 104, 105, 106, 105, 106, 105, 106, 107, 106, 107, 106, 107, 106, 105,
104, 105, 106, 107, 106, 107, 108, 107, 106, 107, 108, 107, 108, 107, 106, 105,
106, 107, 106, 105, 106, 105, 104, 105, 104, 105, 104, 103, 102, 103, 102, 103,
102, 101, 100, 101, 102, 103, 102, 101, 100, 101, 102, 103, 104, 103, 102, 101,
102, 101, 102, 103, 102, 103, 102, 103, 102, 101, 102, 103, 104, 105, 106, 107,
106, 107, 108, 107, 108, 107, 106, 105, 106, 105, 106, 107, 106, 107, 108, 109,
110, 111, 112, 113, 112, 111, 110, 109, 108, 107, 106, 107, 106, 107, 106, 105,
106, 107, 108, 109, 110, 111, 110, 109, 108, 109, 110, 109, 108, 107, 108, 107,
106, 105, 106, 107, 106, 105, 106, 105, 106, 105, 106, 107, 108, 109, 110, 109,
108, 109, 108, 109, 110, 111, 112, 111, 112, 111, 110, 109, 110, 109, 108, 109,
108, 109, 110, 111, 110, 109, 108, 109, 110, 111, 110, 109, 110, 111, 112, 113,
112, 111, 110, 109, 110, 111, 110, 109, 108, 109, 108, 107, 108, 107, 108, 109,
108, 109, 110, 109, 110, 111, 110, 109, 108, 109, 108, 109, 108, 109, 110, 111,
110, 109, 108, 109, 110, 109, 110, 111, 110, 111, 110, 109, 110, 111, 110, 111,
110, 109, 110, 109, 110, 111, 110, 111, 110, 109, 110, 109, 108, 107, 106, 105,
104, 105, 106, 105, 104, 105, 104, 103, 102, 101, 102, 101, 102, 103, 104, 105,
104, 103, 104, 103, 102, 101, 100, 101, 102, 101, 100, 101, 100, 99, 100, 101,
102, 101, 100, 101, 100, 101, 100, 101, 100, 101, 102, 101, 102, 101, 102, 103,
104, 105, 104, 105, 106, 107, 106, 105, 106, 105, 106, 107, 108, 107, 106, 107,
106, 107, 106, 107, 108, 109, 108, 107, 106, 107, 106, 107, 108, 109, 110, 111,
110, 111, 110, 109, 108, 109, 108, 107, 108, 107, 108, 107, 108, 107, 106, 107,
108, 107, 108, 107, 106, 105, 106, 105, 104, 103, 102, 101, 102, 103, 104, 105
104, 105, 104, 103, 102, 101, 102, 101, 100, 99, 98, 97, 98, 97, 98, 99, 98, 99,
98, 97, 98, 99, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 108,
107, 108, 107, 108, 107, 106, 105, 104, 103, 104, 105, 104, 103, 102, 101, 100,
99, 100, 101, 102, 101, 100, 99, 100, 99, 98, 97, 98, 99, 100, 99, 98, 97, 98,
97, 96, 97, 98, 97, 98, 97, 96, 95, 96, 95, 96, 95, 94, 93, 94, 95, 94, 93, 92,
91, 92, 93, 94, 95, 96, 97, 98, 97, 96, 97, 96, 97, 98, 99, 98, 99, 98, 99, 98
97, 98, 97, 98, 97, 96, 97, 98, 99, 100, 99, 98, 97, 96, 95, 94, 93, 94, 95, 96
95, 96, 95, 94, 95, 96, 95, 94, 93, 94, 95, 96, 95, 94, 93, 94, 95, 96, 95, 94
93, 94, 95, 96, 97, 96, 95, 94, 93, 92, 93, 94, 93, 94, 93, 92, 91, 92, 93, 94,
95, 96, 95, 96, 97, 96, 95, 96, 95, 94, 93, 92, 93, 94, 93, 94, 95, 94, 93, 92
93, 94, 95, 94, 93, 92, 93, 94, 93, 94, 95, 96, 97, 98, 97, 96, 95, 96, 95, 96,
97, 98, 99, 98, 97, 98, 99, 98, 99, 100, 99, 100, 99, 98, 99, 98, 99, 98, 99,
100, 101, 102, 103, 104, 105, 106, 105, 106, 105, 104, 103, 104, 105, 106, 107,
106, 107, 108, 109, 110, 111, 112, 113, 112, 113, 114, 113, 112, 113, 112, 113,
114, 113, 112, 113, 114, 115, 114, 115, 114, 113, 112, 111, 110, 109, 110, 109,
108, 107, 108, 109, 110, 109, 110, 111, 112, 111, 110, 109, 108, 107, 106, 105,
104, 105, 104, 105, 104, 105, 106, 105, 106, 107, 106, 105, 106, 107, 106, 105,
106, 107, 106, 105, 106, 107, 108, 109, 108, 107, 108, 107, 106, 107, 108, 109,
110, 109, 110, 109, 108, 109, 110, 111, 112, 113, 114, 115, 114, 113, 114, 113,
112, 111, 112, 111, 110, 109, 108, 107, 108, 109, 108, 109, 110, 111, 110, 111,
110, 111, 112, 111, 112, 113, 114, 115, 114, 115, 114, 113, 112, 113, 112, 111,
```

```
112, 111, 112, 113, 112, 113, 112, 111, 110, 111, 112, 111, 112, 111, 112, 113,
114, 113, 114, 115, 114, 113, 114, 113, 112, 111, 110, 111, 110, 109, 108, 107,
108, 107, 108, 107, 106, 107, 108, 107, 106, 105, 104, 103, 102, 103, 104, 105,
106, 105, 104, 105, 104, 105, 104, 105, 106, 107, 108, 109, 110, 109, 108, 107,
108, 109, 108, 109, 110, 109, 110, 109, 110, 109, 108, 107, 106, 107, 106, 107,
108, 109, 110, 109, 108, 109, 110, 109, 110, 109, 108, 107, 108, 109, 110, 109,
108, 107, 108, 109, 108, 107, 106, 105, 104, 105, 106, 107, 106, 105, 104, 105,
104, 105, 104, 103, 102, 103, 104, 105, 104, 105, 106, 107, 108, 107, 106, 107,
108, 109, 110, 111, 110, 109, 110, 111, 110, 111, 112, 111, 110, 111, 110, 109,
110, 109, 108, 107, 106, 107, 108, 109, 110, 109, 110, 109, 110, 109, 108, 107,
106, 105, 104, 105, 106, 105, 106, 107, 108, 107, 106, 105, 106, 105, 104, 105,
106, 107, 106, 107, 106, 105, 106, 107, 106, 107, 108, 107, 108, 107, 106, 105
104, 103, 102, 101, 100, 99, 98, 99, 100, 99, 98, 99, 100, 101, 102, 101, 102,
103, 104, 105, 104, 103, 102, 101, 100, 101, 102, 103, 104, 103, 104, 105, 104,
105, 104, 105, 106, 107, 106, 105, 106, 105, 106, 105, 106, 107, 108, 109, 110,
111, 110, 111, 112, 113, 112, 111, 110, 111, 110, 111, 112, 113, 114, 113, 114,
115, 116, 117, 116, 117, 118, 117, 118, 119, 118, 119, 118, 117, 118, 117, 116,
117, 116, 117, 118, 119, 120, 121, 120, 121, 120, 119, 118, 117, 116, 117, 116,
117, 116, 115, 116, 115, 116, 115, 116, 115, 114, 115, 114, 113, 112, 113, 112,
111, 112, 111, 110, 111, 110, 109, 108, 109, 110, 109, 110, 111, 112, 113, 114,
113, 114, 113, 114, 113, 114, 115, 116, 117, 116, 115, 114, 113, 112, 113, 114,
113, 112, 111, 112, 113, 114, 113, 112, 111, 110, 109, 108, 107, 108, 109, 108,
109, 110, 111, 110, 111, 110, 111, 112, 111, 110, 111, 110, 111, 112, 113, 114,
113, 114, 113, 114, 115, 114, 115, 116, 115, 114, 113, 112, 113, 112, 113, 114,
113, 112, 113, 112, 113, 114, 115, 116, 117, 118, 119, 120, 119, 120, 121, 120,
121, 120, 121, 122, 121, 122, 123, 124, 123, 124, 123, 124, 123, 124, 125, 124,
125, 126, 125, 126, 125, 126, 127, 126, 125, 126, 125, 124, 123, 124, 123, 124,
123, 124, 123, 122, 123, 124, 125, 124, 125, 126, 125, 126, 125, 126, 127, 128,
127, 126, 125, 124, 123, 124, 125, 126, 127, 126, 127, 126, 125, 124, 125, 126,
125, 124, 125, 126, 127, 126, 125, 124, 123, 122, 123, 122, 121, 122, 123, 122,
123, 122, 121, 122, 123, 122, 123, 122, 123, 122, 121, 120, 121, 120, 121, 120,
119, 118, 117, 116, 117, 118, 119, 120, 121, 120, 119, 120, 121, 122, 121, 120,
121, 122, 121, 122, 121, 122, 121, 122, 121, 120, 121, 120, 119, 118, 117, 118,
117, 116, 115, 114, 115, 116, 117, 116, 115, 114, 113, 112, 111, 110, 111, 112,
113, 112, 113, 112, 113, 112, 111, 112, 111, 112, 111, 110, 111, 110, 109, 110,
109, 108, 109, 110, 109, 110, 111, 112, 113, 112, 113, 114, 113, 114, 113, 112,
111, 110, 111, 112, 111, 110, 111, 110, 109, 108, 109, 110, 111, 112, 113, 114,
115, 114, 113, 112, 113, 112, 113, 114, 113, 114, 115, 114, 113, 114, 113, 114,
113, 112, 113, 112, 111, 110, 109, 108, 107, 108, 109, 108, 109, 110, 109, 110,
109, 108, 109, 108, 107, 106, 105, 106, 105, 104, 105, 106, 105, 106, 105, 104,
103, 102, 103, 104, 103, 104, 103, 104, 105, 104, 105, 104, 105, 104, 105, 104,
105, 104, 103, 102, 103, 102, 103, 104, 103, 102, 103, 102, 101, 100, 99, 98,
99, 98, 97, 98, 99, 100, 99, 100, 99, 98, 97, 96, 97, 98, 99, 98, 97, 98, 97,
96, 95, 96, 95, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 102, 101, 100, 99
100, 101, 100, 99, 100, 101, 102, 101, 102, 101, 102, 101, 100, 101, 100, 99,
98, 97, 96, 95, 94, 95, 94, 95, 96, 97, 98, 99, 98, 99, 100, 101, 100, 101, 102,
101, 102, 101, 102, 101, 102, 101, 100, 101, 100, 101, 100, 101, 102, 101, 102,
103, 102, 101, 100, 101, 100, 101, 102, 103, 104, 105, 106, 105, 106, 107, 106,
```

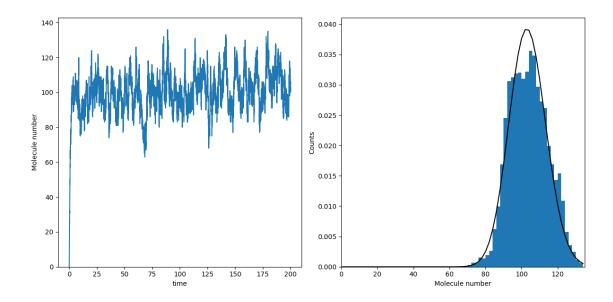
```
105, 106, 107, 108, 109, 110, 111, 112, 113, 112, 111, 112, 113, 112, 111, 110,
111, 112, 111, 110, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 117, 116,
115, 114, 113, 112, 113, 112, 111, 112, 113, 114, 115, 114, 113, 112, 111, 110,
111, 112, 113, 114, 115, 114, 113, 114, 113, 112, 113, 114, 115, 116, 115, 116
115, 116, 117, 116, 115, 116, 117, 116, 117, 118, 117, 116, 117, 118, 119, 118
117, 116, 117, 118, 119, 118, 119, 120, 119, 120, 121, 120, 121, 122, 123, 122,
123, 122, 121, 120, 119, 118, 117, 118, 117, 116, 115, 114, 115, 114, 115, 116,
115, 116, 115, 114, 115, 116, 115, 116, 117, 116, 117, 116, 117, 116, 117, 116,
117, 116, 115, 116, 115, 116, 115, 116, 117, 118, 117, 118, 119, 118, 119, 118,
117, 118, 119, 120, 121, 122, 123, 122, 123, 124, 125, 124, 123, 122, 121, 120,
121, 120, 119, 118, 117, 118, 119, 118, 119, 120, 119, 118, 119, 120, 119, 118,
119, 118, 119, 120, 119, 120, 119, 118, 117, 118, 117, 118, 117, 118, 119, 120,
121, 120, 119, 120, 121, 122, 121, 120, 121, 120, 119, 120, 121, 120, 119, 118,
117, 118, 119, 120, 121, 120, 121, 122, 121, 122, 121, 120, 119, 120, 119, 118,
119, 120, 121, 120, 121, 120, 121, 120, 119, 118, 119, 118, 117, 116, 117, 118,
119, 118, 117, 118, 117, 116, 115, 114, 113, 112, 113, 112, 113, 112, 111, 112,
111, 110, 109, 108, 109, 110, 111, 112, 111, 112, 113, 112, 111, 112, 113, 112,
113, 112, 111, 112, 111, 112, 113, 112, 113, 112, 111, 110, 111, 110, 109, 110,
111, 112, 111, 112, 111, 112, 111, 112, 111, 110, 109, 108, 107, 108, 109, 108,
107, 106, 105, 106, 107, 108, 107, 108, 107, 108, 107, 106, 107, 108, 109, 110,
111, 110, 109, 110, 111, 110, 111, 110, 111, 112, 111, 112, 113, 112, 113, 114,
115, 114, 113, 112, 113, 112, 111, 112, 113, 114, 113, 114, 113, 114, 113, 112,
111, 110, 111, 110, 111, 112, 113, 112, 111, 112, 111, 110, 111, 110, 111, 112,
111, 112, 111, 112, 111, 112, 113, 114, 113, 114, 113, 112, 113, 112, 113, 112,
111, 112, 113, 112, 111, 110, 111, 110, 111, 112, 113, 112, 113, 112, 113, 112,
113, 114, 115, 114, 113, 114, 115, 116, 115, 114, 113, 114, 113, 114, 113, 114
113, 112, 113, 114, 113, 114, 113, 112, 111, 112, 113, 114, 113, 112, 113, 112,
111, 110, 109, 110, 111, 112, 111, 112, 111, 112, 113, 114, 113, 114, 113, 112,
113, 112, 111, 110, 111, 110, 111, 112, 111, 112, 111, 112, 113, 114, 113, 112,
113, 114, 115, 114, 113, 114, 113, 112, 113, 114, 115, 114, 115, 116, 117, 116,
115, 114, 113, 114, 115, 114, 113, 112, 113, 112, 111, 112, 113, 114, 115, 116,
117, 116, 115, 114, 115, 116, 117, 116, 117, 118, 117, 118, 119, 120, 119, 118,
119, 120, 121, 120, 119, 118, 117, 118, 119, 120, 121, 120, 119, 118, 119, 118,
117, 118, 117, 116, 115, 116, 117, 116, 117, 118, 117, 116, 117, 116, 115, 114,
113, 114, 113, 112, 113, 112, 111, 112, 113, 112, 111, 112, 113, 114, 115, 116,
115, 114, 115, 116, 117, 116, 117, 118, 119, 118, 119, 118, 117, 116, 117, 118,
119, 118, 117, 118, 117, 118, 117, 118, 119, 118, 117, 118, 117, 116, 115, 116,
117, 118, 117, 116, 117, 116, 115, 116, 115, 116, 117, 118, 119, 120, 121, 122,
123, 122, 121, 120, 121, 120, 121, 120, 119, 120, 121, 120, 119, 118, 119, 120,
119, 118, 117, 116, 117, 116, 115, 114, 113, 112, 113, 112, 111, 110, 111, 110,
111, 112, 111, 112, 113, 112, 113, 114, 115, 116, 117, 116, 115, 116, 115, 114,
113, 112, 111, 110, 109, 110, 111, 110, 111, 112, 113, 112, 113, 112, 111, 110,
109, 108, 109, 108, 109, 108, 109, 110, 109, 110, 109, 108, 107, 106, 105, 106,
105, 104, 105, 104, 105, 106, 105, 104, 103, 104, 103, 102, 101, 102, 101, 102,
103, 102, 101, 100, 101, 100, 99, 100, 99, 100, 101, 100, 101, 102, 101, 100,
99, 98, 97, 96, 97, 98, 99, 100, 101, 102, 103, 102, 103, 102, 103, 102, 101,
102, 103, 102, 101, 100, 99, 98, 99, 100, 101, 102, 103, 104, 105, 104, 105,
106, 105, 104, 105, 106, 107, 106, 105, 104, 103, 102, 103, 102, 103, 104, 103,
```

```
104, 105, 104, 103, 102, 103, 104, 105, 106, 105, 106, 105, 106, 105, 104, 105,
106, 107, 108, 109, 108, 109, 110, 111, 112, 111, 110, 109, 110, 109, 108, 109,
110, 109, 110, 109, 108, 107, 106, 107, 108, 107, 108, 107, 106, 105, 104, 105,
106, 105, 106, 105, 104, 103, 104, 105, 106, 105, 104, 103, 102, 103, 104, 105,
104, 103, 102, 103, 102, 101, 102, 103, 104, 103, 104, 105, 104, 105, 106, 105,
106, 105, 104, 103, 102, 101, 102, 103, 104, 105, 104, 103, 102, 103, 104, 105,
106, 107, 106, 107, 108, 109, 110, 111, 110, 109, 110, 111, 110, 109, 108, 109,
110, 111, 110, 111, 112, 111, 112, 113, 112, 113, 112, 111, 110, 109, 108, 107,
106, 105, 106, 107, 106, 105, 104, 103, 104, 103, 102, 101, 102, 103, 102, 101,
102, 101, 100, 99, 100, 99, 98, 97, 96, 97, 98, 99, 98, 97, 98, 97, 98, 97, 98,
99, 98, 99, 100, 101, 102, 103, 102, 103, 104, 103, 102, 103, 104, 105, 106,
107, 106, 107, 106, 105, 106, 105, 104, 105, 106, 105, 106, 107, 106, 107, 108,
109, 108, 107, 106, 105, 104, 103, 102, 103, 104, 105, 104, 105, 106, 107, 108,
107, 108, 109, 108, 109, 108, 107, 108, 109, 110, 109, 108, 107, 106, 105, 104,
103, 104, 103, 104, 105, 106, 105, 104, 105, 104, 103, 102, 103, 104, 103, 102,
101, 100, 101, 102, 101, 100, 99, 98, 97, 98, 99, 98, 97, 96, 95, 96, 95, 94,
95, 94, 95, 94, 95, 94, 95, 94, 93, 94, 93, 92, 91, 92, 93, 94, 93, 92, 91, 90,
89, 88, 89, 88, 89, 90, 89, 90, 89, 90, 89, 90, 89, 88, 89, 90, 89, 90, 89, 88,
87, 86, 87, 88, 87, 88, 89, 90, 91, 92, 93, 94, 95, 94, 93, 94, 93, 94, 95, 94,
93, 94, 93, 92, 91, 92, 91, 90, 89, 90, 91, 92, 93, 94, 93, 94, 93, 94, 93, 92,
91, 92, 91, 92, 91, 90, 89, 88, 89, 90, 91, 92, 91, 90, 89, 88, 87, 88, 87, 86,
85, 86, 85, 86, 85, 86, 87, 88, 87, 88, 89, 90, 91, 92, 93, 92, 93, 92, 91, 92
93, 92, 91, 92, 93, 92, 91, 90, 89, 90, 89, 88, 89, 88, 87, 86, 87, 88, 89, 90,
91, 90, 91, 90, 91, 92, 93, 94, 93, 94, 93, 94, 93, 92, 91, 90, 91, 90, 91, 92,
91, 92, 91, 92, 93, 94, 95, 94, 95, 96, 95, 96, 97, 96, 97, 96, 97, 98, 99, 98,
97, 98, 99, 98, 97, 96, 95, 94, 93, 94, 95, 96, 95, 94, 93, 94, 93, 92, 93, 94
93, 94, 93, 94, 93, 94, 93, 94, 93, 94, 93, 92, 93, 92, 93, 94, 95, 96, 97, 96
95, 96, 95, 96, 97, 98, 99, 100, 101, 102, 103, 102, 103, 102, 101, 102, 103,
102, 101, 102, 103, 104, 103, 104, 103, 104, 105, 104, 103, 104, 105, 106, 107
106, 107, 108, 109, 110, 109, 108, 107, 106, 107, 108, 109, 110, 109, 110, 109,
108, 107, 108, 109, 108, 107, 106, 105, 104, 105, 104, 105, 106, 107, 108, 107,
106, 105, 104, 105, 106, 105, 104, 105, 106, 107, 108, 109, 110, 111, 112, 111,
110, 111, 112, 113, 112, 111, 112, 111, 110, 109, 108, 109, 110, 109, 108, 109,
110, 109, 108, 109, 108, 109, 108, 109, 108, 107, 108, 107, 108, 107, 106, 107,
108, 107, 108, 107, 106, 107, 106, 107, 108, 109, 108, 109, 110, 111, 110, 111,
110, 111, 110, 111, 110, 109, 108, 107, 108, 109, 108, 109, 108, 107, 106, 105,
104, 103, 102, 103, 104, 103, 102, 101, 102, 103, 104, 105, 106, 105, 106, 107,
106, 105, 106, 105, 106, 105, 104, 103, 102, 101, 102, 101, 102, 101, 100, 101,
100, 99, 98, 99, 100, 99, 100, 101, 102, 101, 100, 99, 98, 99, 100, 99, 100, 99,
98, 97, 96, 95, 96, 97, 96, 95, 96, 95, 96, 97, 98, 99, 100, 99, 100, 99, 100,
101, 102, 103, 102, 101, 102, 101, 100, 99, 98, 97, 98, 97, 98, 99, 100, 101,
100, 99, 98, 97, 96, 95, 96, 95, 94, 95, 94, 95, 94, 93, 94, 95, 94, 93, 92, 91,
90, 89, 90, 89, 88, 89, 90, 89, 90, 89, 90, 89, 88, 89, 90, 89, 90, 91, 92, 91,
90, 89, 88, 89, 88, 89, 90, 89, 88, 89, 90, 91, 92, 91, 92, 93, 94, 95, 96, 97,
96, 95, 96, 95, 96, 95, 94, 93, 94, 93, 92, 91, 90, 91, 92, 91, 92, 91, 92, 93,
92, 93, 94, 95, 94, 95, 96, 95, 94, 95, 94, 95, 96, 95, 94, 95, 96, 95, 96, 97,
96, 97, 98, 97, 98, 99, 100, 101, 100, 99, 100, 99, 100, 101, 102, 101, 102,
101, 100, 99, 100, 99, 98, 97, 98, 97, 98, 99, 98, 99, 100, 101, 102, 101, 100,
```

```
99, 98, 97, 98, 99, 98, 97, 96, 95, 94, 95, 96, 97, 98, 99, 100, 99, 100, 101,
102, 101, 100, 101, 100, 99, 100, 99, 100, 99, 98, 99, 98, 97, 98, 99, 98, 99,
98, 97, 96, 95, 94, 95, 96, 95, 94, 93, 92, 91, 92, 93, 94, 95, 94, 95, 94, 95,
94, 93, 92, 91, 90, 91, 92, 91, 90, 91, 90, 89, 88, 89, 90, 91, 90, 89, 90, 89,
88, 89, 90, 89, 90, 89, 88, 87, 86, 87, 86, 85, 86, 85, 86, 85, 86, 87, 88, 87
86, 85, 84, 85, 84, 85, 84, 85, 86, 85, 84, 85, 84, 85, 84, 85, 86, 87, 88, 89
90, 89, 88, 89, 88, 89, 88, 87, 88, 89, 88, 89, 90, 91, 92, 91, 92, 91, 92, 93,
92, 93, 94, 93, 94, 95, 94, 93, 92, 91, 90, 91, 92, 93, 92, 91, 90, 89, 88, 89,
90, 91, 92, 93, 92, 93, 92, 91, 92, 93, 92, 93, 94, 93, 92, 91, 90, 91, 90, 91,
92, 93, 92, 91, 92, 93, 94, 93, 92, 93, 92, 93, 94, 93, 94, 95, 94, 93, 94, 95,
94, 93, 92, 93, 94, 95, 96, 97, 96, 95, 94, 93, 92, 91, 92, 93, 92, 93, 92, 93,
94, 95, 96, 95, 96, 97, 96, 97, 96, 95, 96, 97, 96, 97, 96, 95, 96, 95, 96, 95,
96, 97, 98, 97, 98, 99, 98, 97, 96, 95, 94, 95, 94, 95, 96, 95, 94, 95, 96, 97,
96, 97, 96, 95, 94, 93, 94, 95, 94, 95, 96, 95, 94, 93, 94, 93, 92, 91, 92, 91,
92, 91, 90, 89, 88, 89, 90, 91, 92, 91, 92, 93, 94, 95, 96, 97, 98, 97, 96, 97,
96, 95, 94, 93, 92, 91, 90, 91, 92, 91, 90, 89, 90, 91, 90, 89, 88, 89, 90, 91,
90, 91, 90, 91, 92, 91, 90, 89, 88, 89, 88, 87, 88, 87, 88, 89, 88, 89, 90, 89,
90, 91, 90, 91, 90, 91, 90, 89, 88, 89, 88, 87, 86, 87, 88, 87, 86, 87, 88, 87,
88, 89, 90, 89, 90, 89, 90, 89, 88, 89, 90, 91, 90, 91, 90, 89, 88, 87, 88, 89,
88, 89, 90, 89, 88, 89, 90, 91, 90, 89, 90, 89, 90, 89, 90, 89, 90, 89, 90, 89,
88, 87, 88, 87, 86, 87, 88, 87, 88, 87, 88, 87, 88, 87, 88, 87, 88, 89, 90, 89,
90, 91, 90, 91, 92, 93, 92, 91, 90, 89, 90, 91, 92, 91, 92, 91, 92, 91, 92, 93,
94, 93, 94, 93, 94, 93, 92, 93, 92, 91, 92, 93, 92, 91, 92, 93, 94, 95, 94, 95,
96, 97, 96, 95, 94, 95, 96, 97, 98, 99, 98, 99, 100, 101, 102, 103, 104, 103,
104, 105, 104, 103, 104, 103, 104, 103, 104, 103, 102, 101, 102, 101, 102, 101,
100, 101, 102, 103, 104, 103, 104, 105, 106, 107, 108, 109, 110, 109, 108, 107,
108, 109, 108, 107, 106, 105, 104, 105, 106, 105, 104, 103, 104, 103, 102, 101,
100, 101, 102, 103, 104, 105, 104, 105, 104, 103, 104, 103, 104, 105, 104, 105,
106, 107, 108, 109, 108, 107, 108, 109, 110, 111, 112, 113, 112, 113, 112, 111,
110, 109, 110, 109, 108, 107, 108, 107, 106, 105, 106, 105, 106, 107, 106, 107,
106, 107, 106, 107, 108, 109, 108, 109, 110, 111, 110, 111, 112, 113, 112, 111,
112, 111, 110, 109, 110, 111, 110, 111, 112, 113, 112, 113, 112, 113, 114, 113,
114, 115, 116, 117, 116, 117, 118, 117, 116, 115, 114, 113, 112, 111, 110, 109,
108, 107, 106, 105, 104, 103, 102, 103, 102, 101, 100, 101, 100, 101, 100, 99,
100, 99, 98, 99, 100, 101, 100, 101, 102, 103, 104, 105, 104, 105, 104, 103,
104, 105, 106, 105, 104, 105, 104, 105, 106, 107, 106, 107, 106, 105, 106, 107,
108, 107, 106, 105, 104, 105, 106, 107, 108, 107, 108, 107, 106, 107, 108, 109,
108, 107, 108, 107, 106, 107, 106, 105, 106, 105, 104, 103, 102, 103, 102, 103,
104, 105, 106, 107, 108, 109, 110, 109, 110, 109, 110, 111, 110, 109, 110, 111,
112, 113, 114, 113, 114, 113, 112, 111, 110, 111, 110, 109, 108, 109, 108, 107,
106, 105, 106, 107, 106, 107, 106, 107, 106, 105, 106, 107, 106, 105, 104, 103,
102, 103, 102, 101, 100, 101, 100, 101, 102, 103, 102, 103, 102, 101, 102, 103,
104, 103, 102, 101, 102, 103, 104, 105, 106]
```

Now we plot the time series of molecule numbers, and the histogram of molecule number of all data during the second half of the simulation (stationary state). Normalize this histogram so that it has unit area, and compare it with the expression of the Poisson distribution derived in class.

```
[26]: plt.figure(figsize=(12, 6))
      plt.subplot(1, 2, 1)
      #Plot molecule number
      plt.plot(timeList, n_molec)
      plt.ylim(0)
      plt.xlabel("time")
      plt.ylabel("Molecule number")
      #Histogram parameters
      half_sim=len(timeList)//2 #divide by half and get an integer to find 2nd half of
      \rightarrow the simulation (2n time period)
      h2_molecList=n_molec[half_sim:] #2nd half of the molec list
      #Bin sizes for histogram
      binxStart=min(h2_molecList)
      binxEnd=max(h2_molecList)+1
      bin_Xvalues=np.arange(0, binxEnd, 2)
      plt.subplot(1, 2, 2)
      #Poisson distribution
      poisson_pmf=poisson.pmf(bin_Xvalues, np.mean(h2_molecList))
      plt.plot(bin_Xvalues, poisson_pmf, color="black")
      #Histogram plot
      plt.hist(h2_molecList, bins=bin_Xvalues, density=True) #density=True normalizes_
      \rightarrow the data
      plt.xlim(0, max(h2_molecList))
      plt.xlabel("Molecule number")
      plt.ylabel("Counts")
      plt.tight_layout()
      plt.show()
```



We can see that the number of molecules is a bit varied but always around 100. This shows a robust model that is able to conserve and go back to the 100 molecules state. This is further confirmed when looking at the boxplot right underneath, the biggest counts are around the number 100 (+-20) We can therefore see a great balance between death and creation of molecules as the molecules remain more or less the same.

Next, we separate the expression into transcription and translation. We thus have four reactions (transcription, translation, mRNA degradation and protein degradation) and two species (mRNA and protein). Integrate the system of reactions and plot the resulting time series and normalized histograms for the two species. Consider a transcription rate $k_{tx} = 10$, a translation rate $k_{tl} = 100$, and $k_{deg} = 1$.

Set parameters

```
[27]: #Set reaction rates, parameters and result lists

k_tx = 10 #Transcription rate(mRNA synthesis)
k_tl = 100 #Translation rate(protein synthesis)
k_deg_mRNA = 1 #mRNA degradation rate
k_deg_protein = 1 #protein degradation rate

#Parameters
c_time = 0 #reset c_time
#use prev tmax
mRNA_count = 0 #initial mRNA
protein_count = 0 #initial protein
```

```
# Lists to store simulation results
time_list = []
mRNA_list = []
protein_list = []
```

Define functions

```
[28]: #Steps 2 to 5
      #Step2: Define function to calculate propensities for each reaction
      def calculate_propensities(mRNA, protein, k_tx, k_tl, k_deg_mRNA, k_deg_protein):
          a_tx = k_tx
          a_tl = k_tl * mRNA
                                            #Translation (protein synthesis)
          a_mRNA_deg = k_deg_mRNA * mRNA  #mRNA degradation
          a_protein_deg = k_deg_protein * protein #protein degradation
          return a_tx, a_tl, a_mRNA_deg, a_protein_deg
      #Step3: Calculate time to next reaction
      #Use existing next_Rtime
      #Step4: Decide which reaction to perform based on propensities
      def choose_reaction(propensities, a_total):
          z2 = np.random.uniform(0, 1) * a_total
          cumulative_sum = 0
          for i, propensity in enumerate(propensities):
              cumulative_sum += propensity
              if cumulative_sum > z2:
                  return i # Reaction index
      #Step5: Update molecule counts based on selected reaction
      def update_counts(reaction, mRNA_count, protein_count):
          if reaction == 0:
                                    #transcription
              mRNA count += 1
          elif reaction == 1:
                                  #translation
              protein_count += 1
          elif reaction == 2 and mRNA_count > 0: #mRNA degradation
              mRNA_count -= 1
          elif reaction == 3 and protein_count > 0: #protein degradation
              protein_count -= 1
          return mRNA_count, protein_count
```

Run the simulation

```
[29]: #Simulate
      while c_time < tmax:</pre>
          #record the current state
          time_list.append(c_time)
          mRNA_list.append(mRNA_count)
          protein_list.append(protein_count)
          #calculate propensities+total
          propensities = calculate_propensities(mRNA_count, protein_count, k_tx, k_tl,
       →k_deg_mRNA, k_deg_protein)
          a_total = sum(propensities)
          #stop simulation if no reactions can occur
          if a_total == 0:
              break
          #determine the time to next reaction and update the time
          reaction_time = next_Rtime(a_total)
          c_time += reaction_time
          #determine which reaction occurs
          reaction = choose_reaction(propensities, a_total)
          mRNA_count, protein_count = update_counts(reaction, mRNA_count,_
       →protein_count)
```

Plot the simulation

```
[30]: #Plotting

plt.subplot(2, 2, 1)

# Time series for mRNA

plt.plot(time_list, mRNA_list, color="darkred")

plt.title("mRNA")

plt.xlabel("Time")

plt.ylabel("mRNA molecule number")

plt.subplot(2, 2, 2)

#Time series for protein

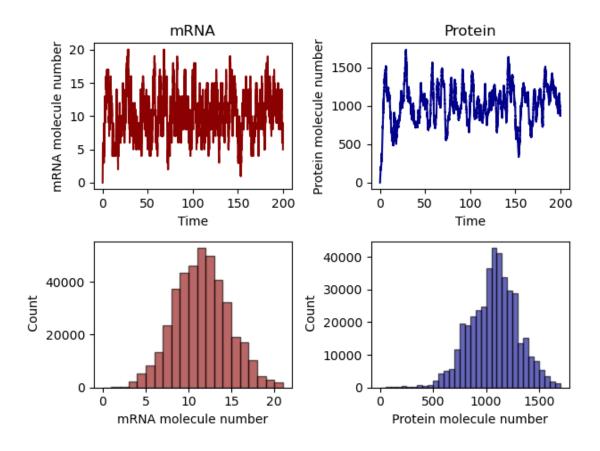
plt.plot(time_list, protein_list, color="darkblue")

plt.title("Protein")

plt.xlabel("Time")

plt.ylabel("Protein molecule number")
```

```
#Steady-state histograms for the second half of the simulation data
half_simulation = len(time_list) // 2
mRNA_steady_state = mRNA_list#[half_simulation:]
protein_steady_state = protein_list#[half_simulation:]
#Define bins for histograms
mRNA_bins = np.arange(0, max(mRNA_steady_state) + 2, 1)
protein_bins = np.arange(0, max(protein_steady_state) + 2, 50)
plt.subplot(2, 2, 3)
#Histogram for mRNA
plt.hist(mRNA_steady_state, bins=mRNA_bins, alpha=0.6, color='darkred',_
→edgecolor='black')
plt.xlabel("mRNA molecule number")
plt.ylabel(" Count")
plt.subplot(2, 2, 4)
#Histogram for protein
plt.hist(protein_steady_state, bins=protein_bins, alpha=0.6, color='darkblue', u
→edgecolor='black')
plt.xlabel("Protein molecule number")
plt.ylabel(" Count")
plt.tight_layout()
plt.show()
```



What we observe in this new model, is also balance. We observe in the mRNA there are a peaks but we still have a number of molecules of aroun 10 (+- 5). As for the counts we once again see more counts of molecules around 10. The same can be said about the protein. Although it may seem as though there is more noise in translation, we still have a regulate number of protein molecules. This makes sense as these plots show the expected variability in mRNA and protein levels in cells under constant conditions. The variability reflects gene expression noise, which is biologically significant because it contributes to differences between cells (even genetically identical ones). In conclusion, this shows a balance between synthesis and degradation again that maintains steady state levels, showing a bit of noise as well

Finally, scale the transcription and translation rates by the same factor, multiplying one of the rates and dividing the other, in such a way that the product remains constant, and discuss what happens with the mean and standard deviation of the distribution of protein numbers for different values of this factor (smaller and larger than 1).

```
[]: scaling_factor=1
k_tx = 10 #Transcription rate(mRNA synthesis)
```

```
k_tl = 100 #Translation rate(protein synthesis)
k_deg_mRNA = 1 #mRNA degradation rate
k_deg_protein = 1 #protein degradation rate
def scaled_sim(k_tx, k_tl, k_deg_mRNA, k_deg_protein, scaling_factor):
    k_tx_scaled = k_tx * scaling_factor
   k_tl_scaled = k_tl / scaling_factor
    #Parameters
    c_time = 0 #reset c_time
    #use prev tmax
   mRNA_count = 0 #initial mRNA
   protein_count = 0 #initial protein
    # Lists to store simulation results
    time_list = []
    mRNA_list = []
    protein_list = []
    #Simulate
    while c_time < tmax:</pre>
        #record the current state
        time_list.append(c_time)
        mRNA_list.append(mRNA_count)
       protein_list.append(protein_count)
        #calculate propensities+total
        propensities = calculate_propensities(mRNA_count, protein_count,_
 →k_tx_scaled, k_tl_scaled, k_deg_mRNA, k_deg_protein)
        a_total = sum(propensities)
        #stop simulation if no reactions can occur
        if a_total == 0:
            break
        #determine the time to next reaction and update the time
        reaction_time = next_Rtime(a_total)
        c_time += reaction_time
        #determine which reaction occurs
        reaction = choose_reaction(propensities, a_total)
        mRNA_count, protein_count = update_counts(reaction, mRNA_count,__
 →protein_count)
```

```
return time_list, mRNA_list, protein_list
```

Run the simulation for various scaling factors

```
[]: for scaling_factor in range(1, 52, 10):
         time_list, mRNA_list, protein_list=scaled_sim(k_tx, k_tl, k_deg_mRNA,
      →k_deg_protein, scaling_factor)
         #Plotting
        plt.subplot(2, 2, 1)
         # Time series for mRNA
         plt.plot(time_list, mRNA_list, color="darkred")
         plt.title("mRNA")
         plt.xlabel("Time")
         plt.ylabel("mRNA molecule number")
         plt.subplot(2, 2, 2)
         #Time series for protein
         plt.plot(time_list, protein_list, color="darkblue")
         plt.title("Protein")
         plt.xlabel("Time")
         plt.ylabel("Protein molecule number")
         #Steady-state histograms for the second half of the simulation data
         half_simulation = len(time_list) // 2
         mRNA_steady_state = mRNA_list#[half_simulation:]
         protein_steady_state = protein_list#[half_simulation:]
         #Define bins for histograms
         mRNA_bins = np.arange(0, max(mRNA_steady_state) + 2, 1)
         protein_bins = np.arange(0, max(protein_steady_state) + 2, 50)
         plt.subplot(2, 2, 3)
         #Histogram for mRNA
         plt.hist(mRNA_steady_state, bins=mRNA_bins, alpha=0.6, color='darkred',_

    dedecolor='black')

         plt.xlabel("mRNA molecule number")
         plt.ylabel(" Count")
```

```
plt.subplot(2, 2, 4)

#Histogram for protein

plt.hist(protein_steady_state, bins=protein_bins, alpha=0.6, 
color='darkblue', edgecolor='black')

plt.xlabel("Protein molecule number")

plt.ylabel(" Count")

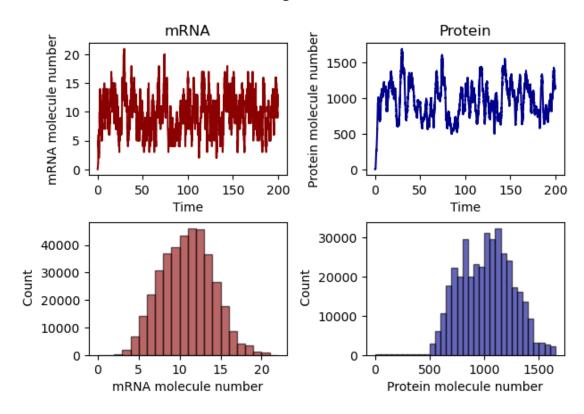
plt.tight_layout()

plt.suptitle(f"Scaling factor {scaling_factor}")

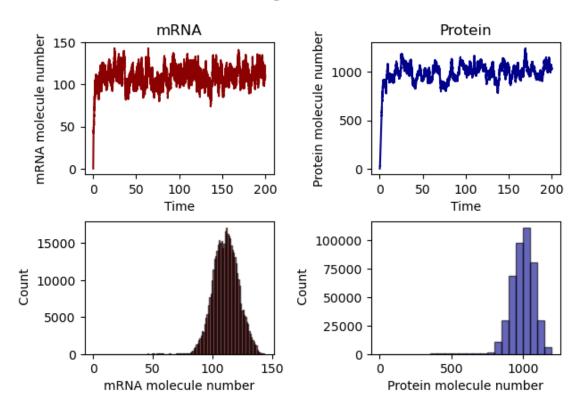
plt.subplots_adjust(top=0.85)

plt.show()
```

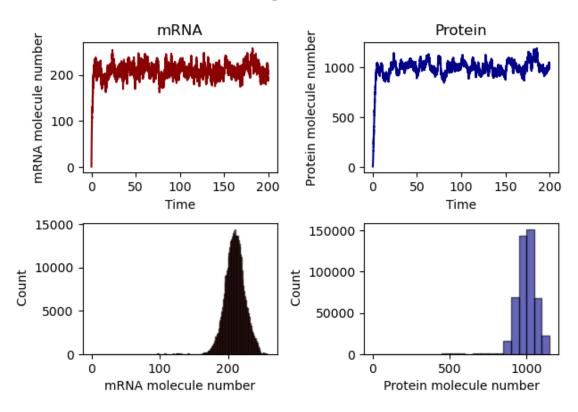
Scaling factor 1



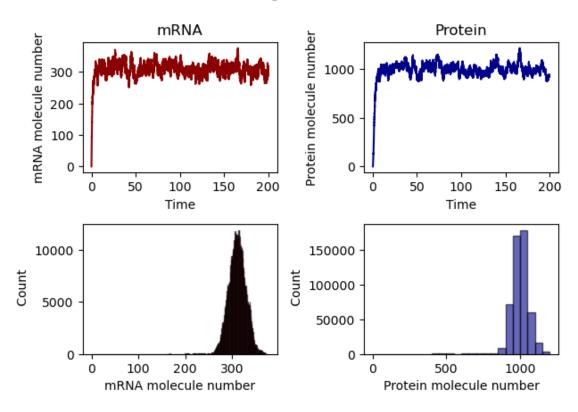
Scaling factor 11



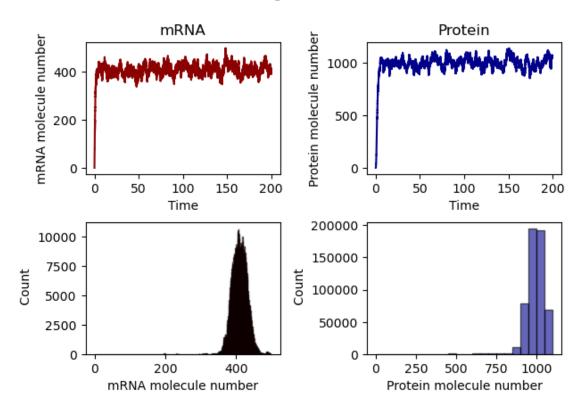
Scaling factor 21



Scaling factor 31



Scaling factor 41



We've run the simulation multiple times with different scaling factors. Our main take-out is the fact that the bigger the scaling factor, the more stable the number of molecules, in both protein and mRNA. This makes sense because cells want consistency across changes for a stable functionning throughout its life.