### GARCG Model GBPJPY

Jane

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# Forcasting Exchange Rate Using GARCH Model for Bristish Pound And Japanese Yen

Reading GBP and JPY Currency into r

```
library(readr)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
       filter, lag
##
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
GBPJPYGARCH <- read.csv ("GBPJPY_Candlestick_1_D_BID_01.01.2000-31.12.2020.csv")%>%
  select('GMT.TIME', CLOSE)%>%
  rename(Date = ('GMT.TIME'), RateGBPJPY = ("CLOSE"))
head(GBPJPYGARCH)
          Date RateGBPJPY
## 1 2000-01-03 166.01
## 2 2000-01-04 168.81
                 171.34
173.37
## 3 2000-01-05
## 4 2000-01-06
## 5 2000-01-07
                   172.56
```

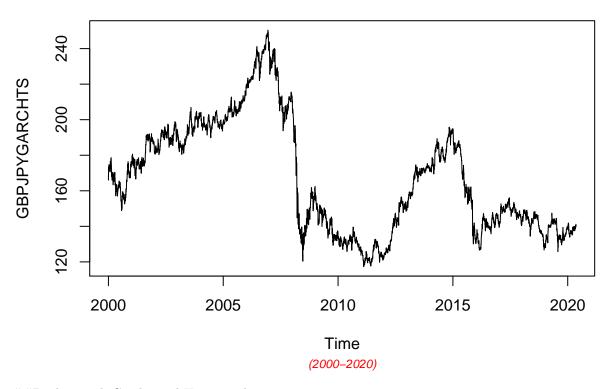
Conversion of Gmt time to date format

171.98

## 6 2000-01-10

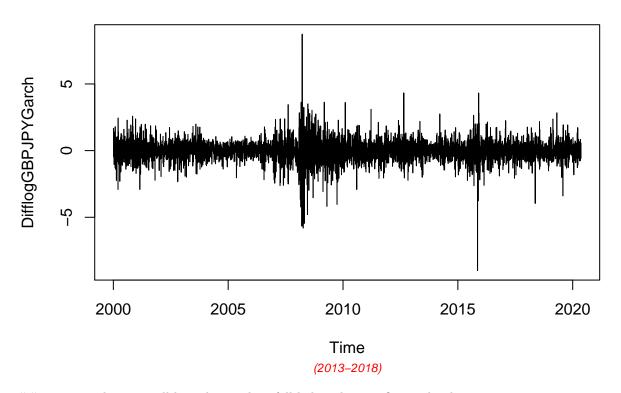
```
library(dplyr)
library(lubridate)
##
## Attaching package: 'lubridate'
## The following objects are masked from 'package:base':
##
##
       date, intersect, setdiff, union
GBPJPYGARCH$Date <- lubridate::ymd(GBPJPYGARCH$Date)</pre>
head(GBPJPYGARCH)
           Date RateGBPJPY
## 1 2000-01-03 166.01
## 2 2000-01-04
                    168.81
## 3 2000-01-05 171.34
## 4 2000-01-06
                  173.37
## 5 2000-01-07
                    172.56
## 6 2000-01-10
                    171.98
##Checking for obvious errors or missingg value
#Checking for obvious errors
which(is.na(GBPJPYGARCH))
## integer(0)
##Converting the data set into time series object
#Converting the data set into time series object
GBPJPYGARCHTS<- ts(as.vector(GBPJPYGARCH$Rate), frequency = 314, start= c(2000,01,03))
plot.ts(GBPJPYGARCHTS)
title("Time Series plot of GBPJPYTimeseries ", sub = "(2000-2020)",
      cex.main = 1.5, font.main= 4, col.main= "blue",
      cex.sub = 0.75, font.sub = 3, col.sub = "red")
```

# Time Series plot of GBPJPYTimeseries



##Dealing with Conditional Heteroscedaticity:

# Plot of returns of GBPJPY



## nature as almost at all lags the p-values fall below the significance levels.

```
library(TSA)
```

```
## Warning: package 'TSA' was built under R version 4.0.5

## ## Attaching package: 'TSA'

## The following object is masked from 'package:readr':

## spec

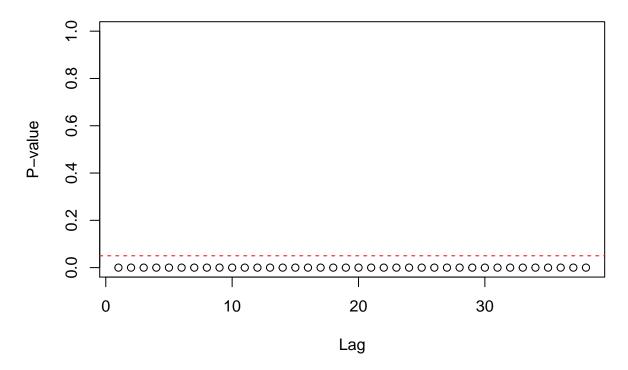
## The following objects are masked from 'package:stats':

## acf, arima

## The following object is masked from 'package:utils':

## ## tar
```

# McLeod-Li test statistics for Daily return series



In order to get an order of GARCH , we further transform the return series into absolute values and squared return values.

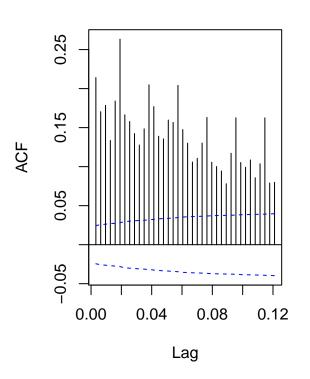
```
abs = abs(DifflogGBPJPYGarch)
sqr = DifflogGBPJPYGarch^2
```

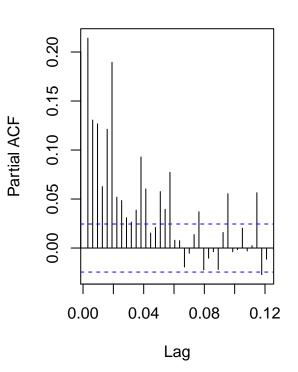
## GARCH Model specification:

```
par(mfrow=c(1,2))
acf(abs, ci.type="ma",main=" ACF for abs. returns")
pacf(abs, main=" PACF plot for abs.returns")
```

#### ACF for abs. returns

## PACF plot for abs.returns





##From ACF and PACF we see many lags are significant. Hence, we plot EACF to get the candidate models

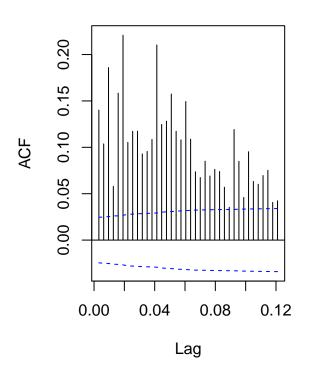
```
eacf(abs)
```

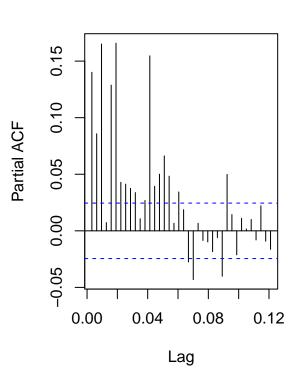
##From the squared returns ACF and PACF plot, it is not that clear to derive the order of p and q. Hence, I approach EACF and the order of ARMA are ARMA (2,3), ARMA (3,3), ARMA (2,4). Thus, GARCH candidate models would be GARCH (3,2) GARCH (3,3) GARCH (4,2)

```
par(mfrow=c(1,2))
acf(sqr, ci.type="ma",main="ACF for sqr. return")
pacf(sqr, main="PACF for sqr. return")
```

# ACF for sqr. return

### PACF for sqr. return





```
eacf(sqr)
```

With reference to the Dickey-Fuller Test, p-value is less than the 0.02 and we can reject the null hypothesis stating the non-stationarity. Hence, we can proceed further for model selection.

#MODEL ESTIMATION: ##GARCH (2,1): for GBP and JPY Curruency Pair

```
# GARCH(2,1)
library(tseries)
```

```
## Registered S3 method overwritten by 'quantmod':
##
    method
                       from
##
     as.zoo.data.frame zoo
GBPJPYGARCHFit.21 = garch(DifflogGBPJPYGarch, order=c(2,1), trace = FALSE)
summary(GBPJPYGARCHFit.21)
##
## Call:
## garch(x = DifflogGBPJPYGarch, order = c(2, 1), trace = FALSE)
## Model:
## GARCH(2,1)
##
## Residuals:
##
       Min
                  1Q
                     Median
                                    3Q
                                            Max
## -9.54664 -0.51722 0.02074 0.54171 6.65772
##
## Coefficient(s):
      Estimate Std. Error t value Pr(>|t|)
##
## a0 0.007075
                  0.000929
                              7.616 2.62e-14 ***
## a1 0.080166
                  0.004060
                              19.746 < 2e-16 ***
## b1 0.281123
                  0.056798
                              4.949 7.44e-07 ***
## b2 0.625927
                  0.054423
                              11.501 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Diagnostic Tests:
## Jarque Bera Test
## data: Residuals
## X-squared = 4956.7, df = 2, p-value < 2.2e-16
##
##
##
   Box-Ljung test
##
## data: Squared.Residuals
## X-squared = 0.55835, df = 1, p-value = 0.4549
```

#### GARCH (2,2):

## Model:

##This model can be interpreted as an overfit model of GARCH(2,1) and p values from residual tests confirms that residuals are highly correlated. Thus this model is not consider to be a good fit.

```
GBPJPYGARCHFit.22 = garch(DifflogGBPJPYGarch, order =c(2,2),trace =FALSE)
summary(GBPJPYGARCHFit.22)
##
## Call:
```

## garch(x = DifflogGBPJPYGarch, order = c(2, 2), trace = FALSE)

```
## GARCH(2,2)
##
## Residuals:
##
                      Median
                                    3Q
       Min
                  1Q
                                            Max
## -9.63377 -0.51689 0.02092 0.53844 6.70066
##
## Coefficient(s):
       Estimate Std. Error t value Pr(>|t|)
##
## a0 7.321e-03
                  1.247e-03
                               5.872 4.31e-09 ***
## a1 7.931e-02
                  9.207e-03
                               8.614 < 2e-16 ***
                               0.000 1.000000
## a2 1.411e-14
                  1.621e-02
## b1 3.527e-01
                  1.624e-01
                               2.172 0.029889 *
## b2 5.547e-01
                               3.646 0.000267 ***
                 1.521e-01
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Diagnostic Tests:
   Jarque Bera Test
##
## data: Residuals
## X-squared = 5124, df = 2, p-value < 2.2e-16
##
##
##
  Box-Ljung test
##
## data: Squared.Residuals
## X-squared = 0.59085, df = 1, p-value = 0.4421
##GARCH (3,1): ##This model can be interpreted as an overfit model of GARCH(2,1) and GARCH (2,2).
This model may not be consider to be a good fit.
GBPJPYGARCHFit.31 = garch(DifflogGBPJPYGarch,order=c(3,1),trace =FALSE)
summary(GBPJPYGARCHFit.31)
##
## Call:
## garch(x = DifflogGBPJPYGarch, order = c(3, 1), trace = FALSE)
##
## Model:
## GARCH(3,1)
## Residuals:
                1Q Median
                                3Q
                                       Max
## -9.5534 -0.5168 0.0207 0.5406 6.6654
##
## Coefficient(s):
       Estimate Std. Error t value Pr(>|t|)
## a0 0.007172
                   0.001162
                               6.170 6.82e-10 ***
## a1 0.081406
                   0.008621
                               9.443 < 2e-16 ***
## b1 0.270620
                   0.088069
                               3.073 0.00212 **
## b2 0.613316
                   0.072433
                               8.467 < 2e-16 ***
## b3 0.021708
                               0.208 0.83507
                   0.104267
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Diagnostic Tests:
## Jarque Bera Test
##
## data: Residuals
## X-squared = 4965.8, df = 2, p-value < 2.2e-16
##
##
## Box-Ljung test
##
## data: Squared.Residuals
## X-squared = 0.49673, df = 1, p-value = 0.4809</pre>
```

##GARCH (3,2): ##This model can be interpreted as an overfitting model and p values from residual tests confirms that residuals are highly correlated. Thus this model is not consider to be a good fit.

## GARCH(3,2)

```
GBPJPYGARCHFit.32 = garch(DifflogGBPJPYGarch,order=c(3,2),trace =FALSE)
summary(GBPJPYGARCHFit.32)
```

```
##
## Call:
## garch(x = DifflogGBPJPYGarch, order = c(3, 2), trace = FALSE)
##
## Model:
## GARCH(3,2)
## Residuals:
                  1Q
                      Median
## -9.67047 -0.51514 0.02096 0.53768 6.78868
##
## Coefficient(s):
      Estimate Std. Error t value Pr(>|t|)
## a0 8.036e-03
                 3.049e-03
                               2.636 0.00839 **
## a1 9.126e-02
                 9.413e-03
                               9.695 < 2e-16 ***
## a2 3.998e-15
                 3.762e-02
                               0.000 1.00000
## b1 3.610e-01
                  4.297e-01
                               0.840 0.40085
## b2 3.322e-01
                  2.068e-01
                               1.606 0.10817
## b3 2.018e-01
                 2.351e-01
                               0.858 0.39071
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Diagnostic Tests:
   Jarque Bera Test
##
## data: Residuals
## X-squared = 5317.1, df = 2, p-value < 2.2e-16
##
##
```

```
## Box-Ljung test
##
## data: Squared.Residuals
## X-squared = 0.12248, df = 1, p-value = 0.7264
```

#### GARCH (3,3):

This model can be interpreted as an overfitting model and p values from residual tests confirms that residuals are highly correlated. Thus, this model is not consider to be a good fit.

### GARCH(3,3)

```
GBPJPYGARCHFit.33 = garch(DifflogGBPJPYGarch,order=c(3,3),trace =FALSE)
summary(GBPJPYGARCHFit.33)
```

```
##
## Call:
## garch(x = DifflogGBPJPYGarch, order = c(3, 3), trace = FALSE)
##
## Model:
## GARCH(3,3)
## Residuals:
       Min
                 10
                      Median
                                   30
                                           Max
## -9.71580 -0.51581 0.02086 0.53810 6.77201
##
## Coefficient(s):
##
      Estimate Std. Error t value Pr(>|t|)
## a0 8.673e-03 4.430e-03
                              1.957
                                      0.0503 .
## a1 8.975e-02
                1.022e-02
                              8.779
                                      <2e-16 ***
## a2 7.855e-03 7.642e-02
                              0.103
                                      0.9181
## a3 1.042e-14
                 3.370e-02
                              0.000
                                      1.0000
## b1 2.177e-01
                 8.282e-01
                              0.263
                                      0.7927
## b2 4.237e-01 6.187e-01
                              0.685
                                      0.4935
## b3 2.457e-01 2.265e-01
                              1.085
                                      0.2781
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Diagnostic Tests:
   Jarque Bera Test
## data: Residuals
## X-squared = 5301, df = 2, p-value < 2.2e-16
##
##
##
   Box-Ljung test
##
## data: Squared.Residuals
## X-squared = 0.16504, df = 1, p-value = 0.6846
```

##GARCH (4,2): ##This model can be interpreted as an overfitting model and p values from residual tests confirms that residuals are highly correlated. Thus, this model is not considered to be a good fit.

```
GBPJPYGARCHFit.42 = garch(DifflogGBPJPYGarch,order=c(4,2),trace =FALSE)
summary(GBPJPYGARCHFit.42)
```

```
##
## Call:
## garch(x = DifflogGBPJPYGarch, order = c(4, 2), trace = FALSE)
##
## Model:
## GARCH(4,2)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   30
                                            Max
## -9.32418 -0.51109 0.02176 0.54211 6.82509
##
## Coefficient(s):
##
      Estimate Std. Error t value Pr(>|t|)
## a0 9.602e-03 1.980e-03
                              4.850 1.24e-06 ***
## a1 1.023e-01 9.541e-03
                             10.718 < 2e-16 ***
## a2 6.383e-03 2.347e-02
                              0.272
                                      0.7857
## b1 3.731e-01 1.875e-01
                              1.990
                                      0.0466 *
## b2 1.184e-01
                              1.037
                                      0.2997
                 1.141e-01
## b3 5.157e-16
                 9.570e-02
                              0.000
                                      1.0000
## b4 3.822e-01
                8.858e-02
                              4.315 1.60e-05 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Diagnostic Tests:
   Jarque Bera Test
##
##
## data: Residuals
## X-squared = 4722, df = 2, p-value < 2.2e-16
##
##
   Box-Ljung test
##
##
## data: Squared.Residuals
## X-squared = 0.00066967, df = 1, p-value = 0.9794
```

#### Model Selection:

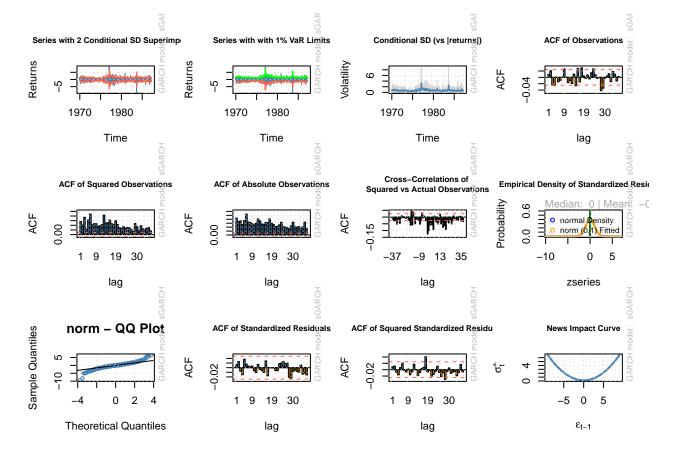
##Best possible model is selected by AIC scores of the models. From the below sort function, GARCH(3,1) would be the best model for the return series. From the p-value, 3.1 also has the lowest correlation

```
library(dLagM)
```

```
## Warning: package 'dLagM' was built under R version 4.0.5
## Loading required package: nardl
```

```
## Warning: package 'nardl' was built under R version 4.0.5
## Loading required package: dynlm
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
GARCHModelSelectionGBPJPY = AIC(GBPJPYGARCHFit.21,GBPJPYGARCHFit.22 ,GBPJPYGARCHFit.31,GBPJPYGARCHFit.3
sortScore(GARCHModelSelectionGBPJPY, score ="aic")
##
                     df
                             AIC
## GBPJPYGARCHFit.42 7 12480.94
## GBPJPYGARCHFit.31 5 12496.58
## GBPJPYGARCHFit.21 4 12497.92
## GBPJPYGARCHFit.22 5 12500.54
## GBPJPYGARCHFit.32 6 12502.07
## GBPJPYGARCHFit.33 7 12504.32
```

#### Model Fitting:



#### ##Model Diagnostics

#### GBPJPYgarchMODEL4.2

```
##
              GARCH Model Fit
##
  Conditional Variance Dynamics
  GARCH Model : sGARCH(4,2)
## Mean Model
               : ARFIMA(1,0,1)
## Distribution : norm
##
  Optimal Parameters
##
##
           Estimate
                     Std. Error
                                  t value Pr(>|t|)
##
           0.009953
                       0.007544
                                 1.319218 0.187096
  mu
##
           0.338255
                       0.392711
                                 0.861333 0.389055
  ar1
          -0.322162
                       0.395069 -0.815459 0.414810
  ma1
           0.006888
## omega
                       0.001663
                                4.141388 0.000035
## alpha1
           0.080713
                       0.013121
                                 6.151562 0.000000
## alpha2
           0.000000
                       0.011010
                                 0.000029 0.999977
## alpha3
           0.000000
                       0.015454
                                 0.000001 0.999999
           0.000000
                       0.013550 0.000001 0.999999
## alpha4
```

```
0.040195 6.852302 0.000000
## beta1 0.275429
## beta2  0.631659  0.037299 16.935169 0.000000
## Robust Standard Errors:
        Estimate Std. Error t value Pr(>|t|)
## mu
        0.009953 0.007726 1.288258 0.197656
## ar1 0.338255 0.213924 1.581191 0.113834
## ma1 -0.322162 0.215716 -1.493457 0.135318
## omega 0.006888 0.003687 1.868006 0.061761
## alpha1 0.080713 0.016792 4.806538 0.000002
## alpha2 0.000000 0.012472 0.000025 0.999980
## alpha3 0.000000 0.022680 0.000001 0.999999 ## alpha4 0.000000 0.022413 0.000000 1.000000
## beta1 0.275429 0.020521 13.422143 0.000000
## beta2 0.631659 0.014112 44.760794 0.000000
##
## LogLikelihood : -6167.916
##
## Information Criteria
## -----
##
## Akaike
             1.9634
## Bayes
             1.9741
            1.9634
## Shibata
## Hannan-Quinn 1.9671
## Weighted Ljung-Box Test on Standardized Residuals
## -----
##
                         statistic p-value
## Lag[1]
                            0.3013 0.5831
                            2.4498 0.8046
## Lag[2*(p+q)+(p+q)-1][5]
## Lag[4*(p+q)+(p+q)-1][9]
                          3.9828 0.6950
## d.o.f=2
## HO : No serial correlation
## Weighted Ljung-Box Test on Standardized Squared Residuals
## -----
##
                          statistic p-value
## Lag[1]
                             0.5323 0.4656
## Lag[2*(p+q)+(p+q)-1][17] 7.6935 0.6023
## Lag[4*(p+q)+(p+q)-1][29] 17.2591 0.2820
## d.o.f=6
## Weighted ARCH LM Tests
##
              Statistic Shape Scale P-Value
## ARCH Lag[7] 0.02393 0.500 2.000 0.8771
## ARCH Lag[9] 0.36343 1.485 1.796 0.9371
## ARCH Lag[11] 1.77820 2.440 1.677 0.8203
## Nyblom stability test
## Joint Statistic: 2.4099
## Individual Statistics:
```

```
## mu
       0.09370
## ar1 0.06582
## ma1 0.06554
## omega 0.26862
## alpha1 0.10312
## alpha2 0.12405
## alpha3 0.12105
## alpha4 0.12097
## beta1 0.11150
## beta2 0.11123
## Asymptotic Critical Values (10% 5% 1%)
## Joint Statistic: 2.29 2.54 3.05
## Individual Statistic: 0.35 0.47 0.75
##
## Sign Bias Test
## -----
## t-value prob sig
## Sign Bias 0.246 0.80566
## Negative Sign Bias 1.970 0.04891 **
## Positive Sign Bias 1.213 0.22500
## Joint Effect 10.962 0.01193 **
##
## Adjusted Pearson Goodness-of-Fit Test:
## -----
## group statistic p-value(g-1)
## 1 20 344.1 1.681e-61
## 2 30 364.0 1.389e-59
## 3 40 402.6 6.119e-62
## 4 50 397.9 3.803e-56
##
##
## Elapsed time : 0.8677609
```

#### Forecasting

```
forcgarchGBPJPY= ugarchforecast(GBPJPYgarchMODEL4.2, data = DiffGBPJPYLogTran, n.ahead = 100, n.roll =1
print(forcgarchGBPJPY)
```

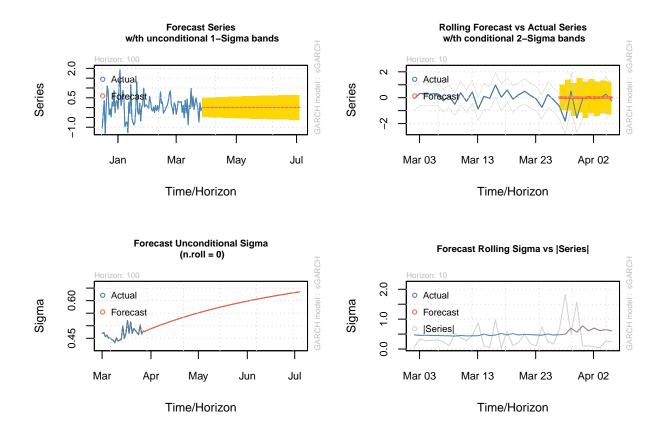
```
## ## *------*
## * GARCH Model Forecast *
## *-----*
## Model: sGARCH
## Horizon: 100
## Roll Steps: 10
## Out of Sample: 100
##
## 0-roll forecast [T0=1987-03-26 02:00:00]:
## Series Sigma
## T+1 0.007108 0.4792
```

```
## T+2
         0.008990 0.4758
## T+3
         0.009627 0.4822
## T+4
         0.009843 0.4824
         0.009916 0.4865
## T+5
## T+6
         0.009940 0.4880
## T+7
         0.009949 0.4911
## T+8
         0.009951 0.4932
         0.009952 0.4958
## T+9
## T+10
         0.009953 0.4981
         0.009953 0.5005
## T+11
## T+12
         0.009953 0.5028
## T+13
         0.009953 0.5052
        0.009953 0.5074
## T+14
        0.009953 0.5097
## T+15
## T+16
        0.009953 0.5119
## T+17
         0.009953 0.5141
## T+18
         0.009953 0.5163
## T+19
         0.009953 0.5184
## T+20
        0.009953 0.5205
## T+21
        0.009953 0.5226
## T+22
        0.009953 0.5247
## T+23
        0.009953 0.5268
## T+24
        0.009953 0.5288
## T+25
         0.009953 0.5308
## T+26
        0.009953 0.5328
## T+27
        0.009953 0.5347
## T+28
        0.009953 0.5367
         0.009953 0.5386
## T+29
## T+30
        0.009953 0.5405
## T+31
         0.009953 0.5424
## T+32
         0.009953 0.5442
## T+33
         0.009953 0.5461
## T+34
        0.009953 0.5479
## T+35
        0.009953 0.5497
## T+36
         0.009953 0.5514
## T+37
         0.009953 0.5532
## T+38
        0.009953 0.5549
## T+39
         0.009953 0.5567
## T+40
         0.009953 0.5584
## T+41
        0.009953 0.5601
## T+42
        0.009953 0.5617
## T+43
        0.009953 0.5634
        0.009953 0.5650
## T+44
        0.009953 0.5666
## T+45
        0.009953 0.5682
## T+46
## T+47
         0.009953 0.5698
## T+48
         0.009953 0.5714
## T+49
         0.009953 0.5729
## T+50
        0.009953 0.5745
## T+51
         0.009953 0.5760
        0.009953 0.5775
## T+52
## T+53
        0.009953 0.5790
## T+54 0.009953 0.5804
## T+55 0.009953 0.5819
```

```
## T+56 0.009953 0.5834
## T+57
        0.009953 0.5848
## T+58
        0.009953 0.5862
## T+59
         0.009953 0.5876
## T+60
         0.009953 0.5890
## T+61
        0.009953 0.5904
## T+62
        0.009953 0.5917
         0.009953 0.5931
## T+63
## T+64
         0.009953 0.5944
## T+65
        0.009953 0.5957
## T+66
        0.009953 0.5971
         0.009953 0.5984
## T+67
        0.009953 0.5996
## T+68
## T+69
        0.009953 0.6009
## T+70
        0.009953 0.6022
## T+71
         0.009953 0.6034
## T+72
         0.009953 0.6047
         0.009953 0.6059
## T+73
## T+74
        0.009953 0.6071
         0.009953 0.6083
## T+75
## T+76
        0.009953 0.6095
## T+77
         0.009953 0.6107
         0.009953 0.6118
## T+78
## T+79
         0.009953 0.6130
## T+80
        0.009953 0.6141
## T+81
         0.009953 0.6153
## T+82
         0.009953 0.6164
## T+83
        0.009953 0.6175
        0.009953 0.6186
## T+84
## T+85
        0.009953 0.6197
## T+86
         0.009953 0.6208
## T+87
         0.009953 0.6219
## T+88
         0.009953 0.6230
## T+89
         0.009953 0.6240
## T+90
        0.009953 0.6251
## T+91
        0.009953 0.6261
## T+92
        0.009953 0.6271
## T+93
        0.009953 0.6281
## T+94
         0.009953 0.6291
        0.009953 0.6301
## T+95
## T+96
        0.009953 0.6311
## T+97
         0.009953 0.6321
## T+98
        0.009953 0.6331
## T+99
        0.009953 0.6340
## T+100 0.009953 0.6350
```

#### plotting

```
plot(forcgarchGBPJPY, which= "all")
```



#### Forecasting the rate

```
RateUSCanadaGarch = 1.27219
  RUSCanadaGARCH <-c(-0.0260997,0.0157132, -0.0133859, 0.0068652, -0.0072283, 0.0025799, -0.0042460, 0.
-0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -0.0014450, -
```

```
## [1] 1.271858

## [1] 1.27239

## [1] 1.27202

## [1] 1.272277

## [1] 1.272098

## [1] 1.272136

## [1] 1.272196

## [1] 1.272154
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- ## [1] 1.272184
- ## [1] 1.272163
- ## [1] 1.272177
- ## [1] 1.272168
- ## [1] 1.272174
- ## [1] 1.27217
- ## [1] 1.272173
- ## [1] 1.272171
- ## [1] 1.272172
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