

# Learning general mixtures of Gaussian

$$P(X = x|Y = i) = \frac{1}{\sqrt{(2\pi)^m |\Sigma_i|}} \exp \left( -\frac{1}{2} (x - \mu_i)^T \Sigma_i^{-1} (x - \mu_i) \right)$$

- Marginal likelihood, for data  $\{x^j \mid j = 1..n\}$ :

$$\begin{aligned} \prod_{j=1}^n P(x^j) &= \prod_{j=1}^n \sum_i P(X = x^j, Y = i) = \prod_{j=1}^n \sum_i P(X = x^j | Y = i) P(Y = i) \\ &= \prod_{j=1}^n \sum_i \frac{1}{\sqrt{(2\pi)^m |\Sigma_i|}} \exp \left( -\frac{1}{2} (x^j - \mu_i)^T \Sigma_i^{-1} (x^j - \mu_i) \right) P(Y = i) \end{aligned}$$

- Need to differentiate and solve for  $\mu_i$ ,  $\Sigma_i$ , and  $P(Y=i)$  for  $i=1..k$
- There will be no closed for solution, gradient is complex, lots of local optimum
- Wouldn't it be nice if there was a better way!