

Pick K random cluster centers, $c^1 \dots c^k$

For $t=1..T$:

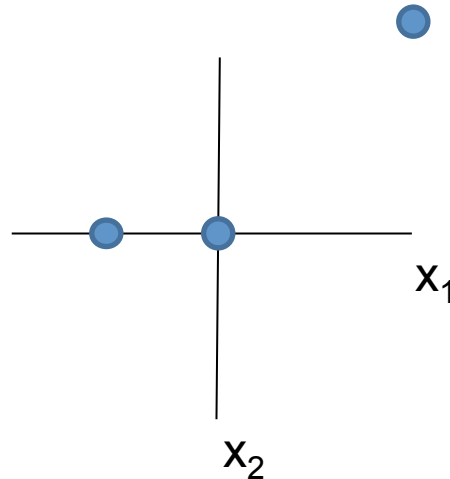
- for $j = 1..n$: [recompute assignments]

$$a^j = \arg \min_i \text{dist}(x^j, c^i)$$

- for $j= 1...k$: [recompute cluster centers]

$$c^j = \frac{1}{|\{i|a^i = j\}|} \sum_{\{i|a^i=j\}} x^i$$

| x_1 | x_2 |
|-------|-------|
| -1 | 0 |
| 0 | 0 |
| 2 | 2 |



$$\text{dist}(x, x') = \sum_i (x_i - x'_i)^2$$

Random cluster means:

- $c^1 = [-1, 0]$, $c^2 = [0, 0]$

t=0:

| $d(x^j, c^i)$ | x^1 | x^2 | x^3 |
|---------------|-------|-------|-------|
| c^1 | 0 | 1 | 13 |
| c^2 | 1 | 0 | 8 |

- $a^1 = \arg \min_i \text{dist}(x^1, c^i) = 1$
- $a^2 = \arg \min_i \text{dist}(x^2, c^i) = 2$
- $a^3 = \arg \min_i \text{dist}(x^3, c^i) = 2$
- $c^1 = (1/1) * [-1, 0] = [-1, 0]$
- $c^2 = (1/2) * ([0, 0] + [2, 2]) = [1, 1]$

t=1:

| $d(x^j, c^i)$ | x^1 | x^2 | x^3 |
|---------------|-------|-------|-------|
| c^1 | 0 | 1 | 13 |
| c^2 | 4 | 4 | 18 |

- $a^1 = \arg \min_i \text{dist}(x^1, c^i) = 1$
- $a^2 = \arg \min_i \text{dist}(x^2, c^i) = 1$
- $a^3 = \arg \min_i \text{dist}(x^3, c^i) = 2$
- $c^1 = (1/2) * ([-1, 0] + [0, 0]) = [-0.5, 0]$
- $c^2 = (1/1) * ([2, 2]) = [2, 1]$

t=2:

- Stop!! (cluster assignments a^i won't change in next round; you can verify!)