



Programming Languages

2nd edition

Tucker and Noonan



Chapter 5



Types



***Types are the leaven of computer programming;
they make it digestible.***


Robin Milner





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- 5.1 Type Errors
 - 5.2 Static and Dynamic Typing
 - 5.3 Basic Types
 - 5.4 NonBasic Types
 - 5.5 Recursive Data Types
 - 5.6 Functions as Types
 - 5.7 Type Equivalence
 - 5.8 Subtypes
 - 5.9 Polymorphism and Generics
 - 5.10 Programmer-Defined Types
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- A *type* is a collection of values and operations on those values.
 - Example: Integer type has values ..., -2, -1, 0, 1, 2, ... and operations $+$, $-$, $*$, $/$, $<$, ...
 - The Boolean type has values true and false and operations \wedge , \vee , \neg .
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- Computer types have a finite number of values due to fixed size allocation; problematic for numeric types.
 - Exceptions:
 - *Smalltalk uses unbounded fractions.*
 - *Haskell type Integer represents unbounded integers.*
 - Floating point problems?
- 


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- Even more problematic is fixed sized floating point numbers:
 - *0.2 is not exact in binary.*
 - *So $0.2 * 5$ is not exactly 1.0*
 - *Floating point is inconsistent with real numbers in mathematics.*



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- In the early languages, Fortran, Algol, Cobol, all of the types were built in.
 - If needed a type color, could use integers; but what does it mean to multiply two colors.
 - Purpose of types in programming languages is to provide ways of effectively modeling a problem solution.
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5.1 Type Errors

- Machine data carries no type information.
- Basically, just a sequence of bits.
- Example: 0100 0000 0101 1000 0000 0000 0000
0000



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- 0100 0000 0101 1000 0000 0000 0000 0000
 - *The floating point number 3.375*
 - *The 32-bit integer 1,079,508,992*
 - *Two 16-bit integers 16472 and 0*
 - *Four ASCII characters: @ X NUL NUL*



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- A *type error* is any error that arises because an operation is attempted on a data type for which it is undefined.
 - Type errors are common in assembly language programming.
 - High level languages reduce the number of type errors.
 - A *type system* provides a basis for detecting type errors.
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5.2 Static and Dynamic Typing

- A type system imposes constraints such as the values used in an addition must be numeric.
 - *Cannot be expressed syntactically in EBNF.*
 - *Some languages perform type checking at compile time (eg, C).*
 - *Other languages (eg, Perl) perform type checking at run time.*
 - *Still others (eg, Java) do both.*

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- A language is *statically typed* if the types of all variables are fixed when they are declared at compile time.
 - A language is *dynamically typed* if the type of a variable can vary at run time depending on the value assigned.
 - Can you give examples of each?
- 



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- A language is *strongly typed* if its type system allows all type errors in a program to be detected either at compile time or at run time.
 - A strongly typed language can be either statically or dynamically typed.
 - *Union* types are a hole in the type system of many languages.
 - Most dynamically typed languages associate a type with each value.
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5.3 Basic Types

- Terminology in use with current 32-bit computers:
 - *Nibble: 4 bits*
 - *Byte: 8 bits*
 - *Half-word: 16 bits*
 - *Word: 32 bits*
 - *Double word: 64 bits*
 - *Quad word: 128 bits*

- In most languages, the numeric types are finite in size.
- So $a + b$ may overflow the finite range.
- Unlike mathematics:
 - $a + (b + c) \neq (a + b) + c$
- Also in C-like languages, the equality and relational operators produce an int, not a Boolean

- 
- An operator or function is *overloaded* when its meaning varies depending on the types of its operands or arguments or result.
 - Java: $a + b$ (ignoring size)
 - *integer add*
 - *floating point add*
 - *string concatenation*
 - Mixed mode: one operand an int, the other floating point
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- A type conversion is a *narrowing* conversion if the result type permits fewer bits, thus potentially losing information.
 - Otherwise it is termed a *widening* conversion.
 - Should languages ban *implicit* narrowing conversions?
 - Why?
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5.4 Nonbasic Types

- Enumeration:

```
enum day {Monday, Tuesday, Wednesday, Thursday, Friday,  
Saturday, Sunday};
```

```
enum day myDay = Wednesday;
```

- In C/C++ the above values of this type are 0, ..., 6.


- More powerful in Java:

```
for (day d : day.values())
```

```
System.out.println(d);
```



Pointers

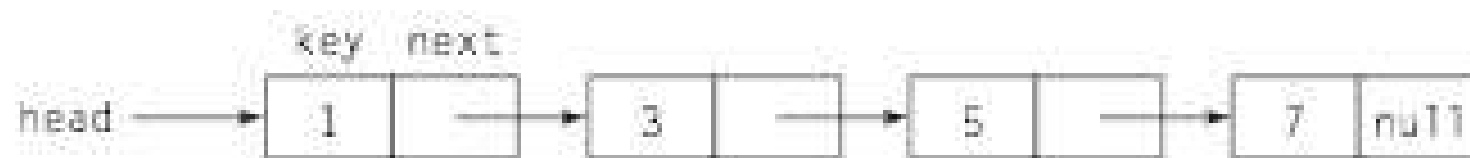
- C, C++, Ada, Pascal
 - Java???
 - Value is a memory address
 - Indirect referencing
 - Operator in C: *
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Example

```
struct Node {  
    int key;  
    struct Node* next;  
};  
  
struct Node* head;
```

- Fig 5.4: A Simple Linked List in C




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- Bane of reliable software development
 - Error-prone
 - Buffer overflow, memory leaks
 - Particularly troublesome in C



```
float sum(float a[ ], int n) {  
    int i;  
    float s = 0.0;  
    for (i = 0; i<n; i++)  
        s += a[i];  
    return s;  
}
```

```
float sum(float *a, int n) {  
    int i;  
    float s = 0.0;  
    for (i = 0; i<n; i++)  
        s += *a++;  
    return s;  
}
```





strcpy

```
void strcpy(char *p, char *q) {  
    while (*p++ = *q++) ;  
}
```

Pointer Operations

- If T is a type and $\text{ref } T$ is a pointer:

$$\& : T \rightarrow \text{ref } T$$

$$* : \text{ref } T \rightarrow T$$

- For an arbitrary variable x :

$$*(\&x) = x$$

Arrays and Lists

- `int a[10];`
- `float x[3][5]; /* odd syntax vs. math */`
- `char s[40];`
- `/* indices: 0 ... n-1 */`

Indexing

- Only operation for many languages

- Type signature

$[] : T[] \times \text{int} \rightarrow T$

- Example

`float x[3][5];`

type of x: `float[][]`

type of `x[1]`: `float[]`

type of `x[1][2]`: `float`

- Equivalence between arrays and pointers

$a = \&a[0]$

- If either $e1$ or $e2$ is type: $\text{ref } T$


$e1[e2] = *((e1) + (e2))$

- Example: a is $\text{float}[]$ and i int

$a[i] = *(a + i)$





Strings

- Now so fundamental, directly supported.
 - In C, a string is a 1D array with the string value terminated by a NUL character (value = 0).
 - In Java, Perl, Python, a string variable can hold an unbounded number of characters.
 - Libraries of string operations and functions.
- 




Structures

- Analogous to a tuple in mathematics
 - Collection of elements of different types
 - Used first in Cobol, PL/I
 - Absent from Fortran, Algol 60
 - Common to Pascal-like, C-like languages
 - Omitted from Java as redundant
- 




```
struct employeeType {  
    int id;  
    char name[25];  
    int age;  
    float salary;  
    char dept;  
};  
struct employeeType employee;  
...  
employee.age = 45;
```





Unions

- C: union
 - Pascal: case-variant record
 - Logically: multiple views of same storage
 - Useful in some systems applications
- 



```
type union =
```

```
  record
```

```
    case b : boolean of
```

```
      true : (i : integer);
```

```
      false : (r : real);
```

```
    end;
```

```
var tagged : union;
```

```
begin tagged := (b => false, r => 3.375);
```

```
  put(tagged.i); -- error
```





```
// simulated union type
```

```
class Value extends Expression {
```

```
    // Value = int intValue | boolean boolValue
```

```
    Type type; int intValue; boolean boolValue;
```

```
    Value(int i) {
```

```
        intValue = i;
```

```
        type = new Type(Type.INTEGER);
```

```
    }
```

```
    Value(boolean b) {
```

```
        boolValue = b;
```

```
        type = new Type(Type.BOOLEAN);
```

```
    }
```

```
    ...
```

```
}
```



5.5 Recursive Data Type

```
data Value = IntValue Integer | FloatValue Float |
```

```
    BoolValue Bool | CharValue Char
```

```
    deriving (Eq, Ord, Show)
```

```
data Expression = Var Variable | Lit Value |
```

```
    Binary Op Expression Expression |
```

```
    Unary Op Expression
```

```
    deriving (Eq, Ord, Show)
```


```
type Variable = String
```

```
type Op = String
```

```
type State = [(Variable, Value)]
```


5.6 Functions as Types

- Pascal example:
 - *function newton(a, b: real; function f: real): real;*
- Know that *f* returns a real value, but the arguments to *f* are unspecified.



```
public interface RootSolvable {  
    double valueAt(double x);  
}
```

```
public double Newton(double a, double b,  
    RootSolvable f);
```




5.7 Type Equivalence


- Pascal Report:

The assignment statement serves to replace the current value of a variable with a new value specified as an expression. ... The variable (or the function) and the expression must be of identical type.

- Nowhere does it define *identical type*.



```
struct complex {  
    float re, im;  
};  
struct polar {  
    float x, y;  
};  
struct {  
    float re, im;  
} a, b;  
struct complex c, d;  
struct polar e;  
int f[5], g[10];  
// which are equivalent types?
```






5.8 Subtypes

- A subtype is a type that has certain constraints placed on its values or operations.
- In Ada subtypes can be directly specified.






```
subtype one_to_ten is Integer range 1 .. 10;

type Day is (Monday, Tuesday, Wednesday, Thursday,
Friday, Saturday, Sunday);

subtype Weekend is Day range Saturday .. Sunday;

type Salary is delta 0.01 digits 9
    range 0.00 .. 9_999_999.99;

subtype Author_Salary is Salary digits 5
    range 0.0 .. 999.99;
```





```
Integer i = new Integer(3);
```

```
...
```

```
Number v = i;
```

```
...
```

```
Integer x = (Integer) v;
```

```
//Integer is a subclass of Number,
```

```
// and therefore a subtype
```





Polymorphism and Generics


- A function or operation is *polymorphic* if it can be applied to any one of several related types and achieve the same result.
- An advantage of polymorphism is that it enables code reuse.

Polymorphism

- Comes from Greek
- Means: having many forms
- Example: overloaded built-in operators and functions

+ - * / == != ...


- Java: + also used for string concatenation
- Ada 83


- 
- Ada, C++: define + - ... for new types
 - Java overloaded methods: number or type of parameters
 - Example: class PrintStream

print, println defined for:

boolean, char, int, long, float, double, char[]

String, Object



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- Java: instance variable, method
 - *name, name()*
 - Ada generics: generic sort
 - *parametric polymorphism*
 - *type binding delayed from code implementation to compile time*
 - *procedure sort is new generic_sort(integer);*



generic

type element is private;

type list is array(natural range <>) of element;


with function ">"(a, b : element) return boolean;

package sort_pck is


procedure sort (in out a : list);

end sort_pck;





```
package sort_pck is
procedure sort (in out a : list) is
begin
  for i in a'first .. a'last - 1 loop
    for j in i+1 .. a'last loop
      if a(i) > a(j) then
        declare t : element;
        begin
          t := a(i);
          a(i) := a(j);
          a(j) := t;
        end;
      end if;
    end loop;
  end loop;
end;
```






Instantiation

package integer_sort is

new generic_sort(Integer, ">");



Programmer-defined Types

- Recall the definition of a type:
 - *A set of values and a set of operations on those values.*
- Structures allow a definition of a representation; problems:
 - *Representation is not hidden*
 - *Type operations cannot be defined*
 - *Defer further until Chapter 12.*