

III. Physikalisches
Institut A

RWTHAACHEN
UNIVERSITY

Experimental Techniques in Particle Physics (WS 2020/2021)

Gaseous detectors

Date of the written exam

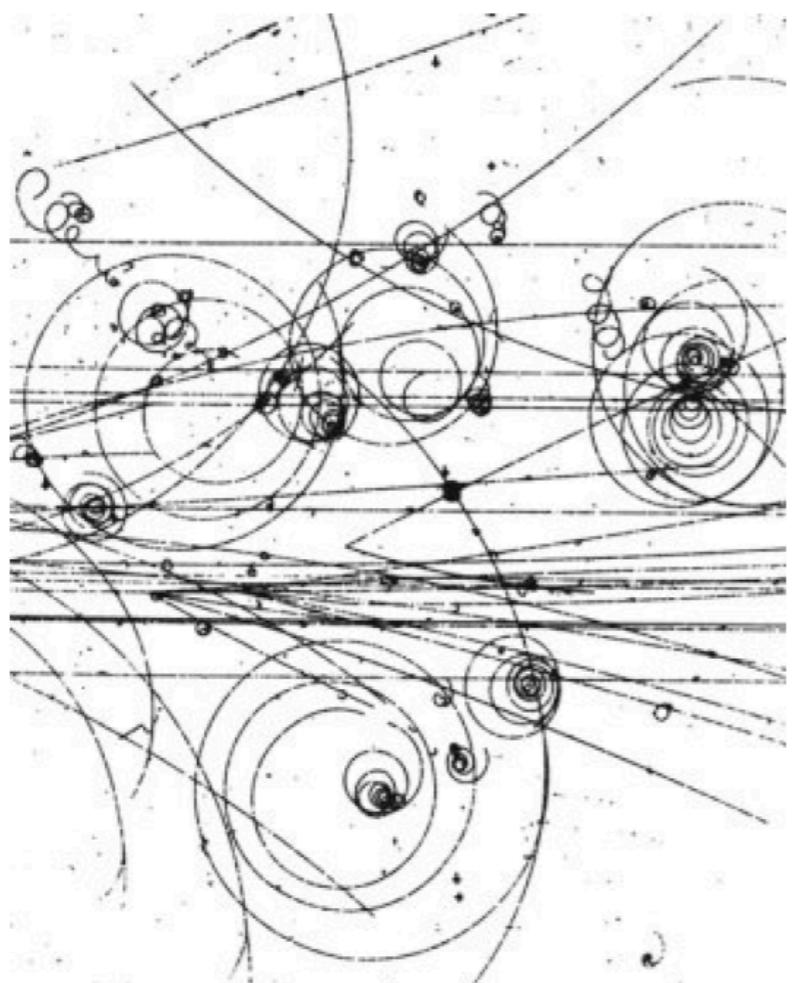
date: 16.03.2021

time: 14:30

location to be announced

History

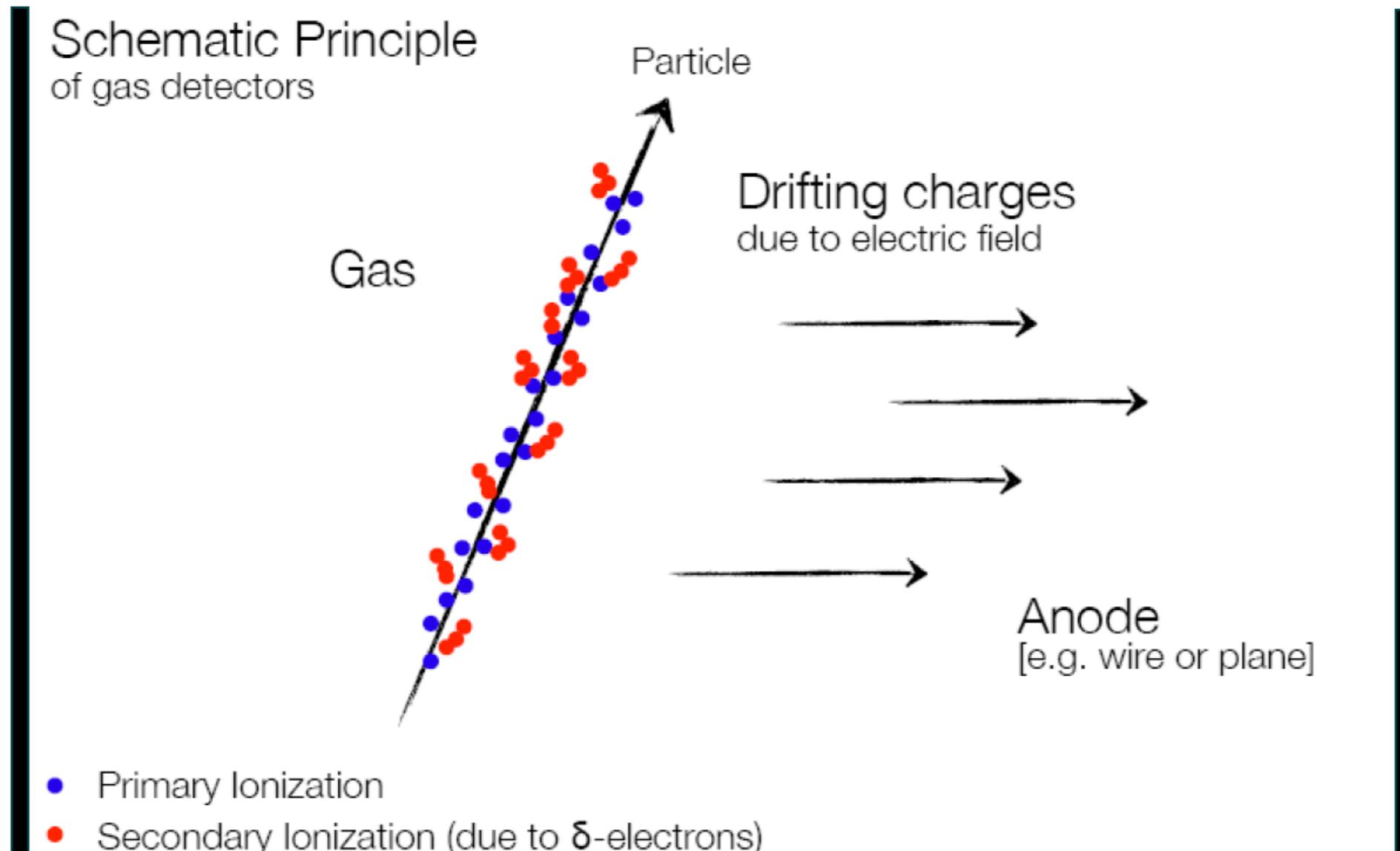
- the first real gas-based detectors were cloud chambers and bubble chambers
- fundamental discoveries until 1980s
- e.g. discovery of weak neutral currents at CERN in the 1970s



- they don't have electronic readout
- they take photographs of ionised gas from different perspectives to reconstruct a 3D picture
- the precision is extremely good
- target and detector are the same material (but not necessary to have a target at all in collider experiments)
- very high precision, but very low rates possible (too slow for modern experiments)

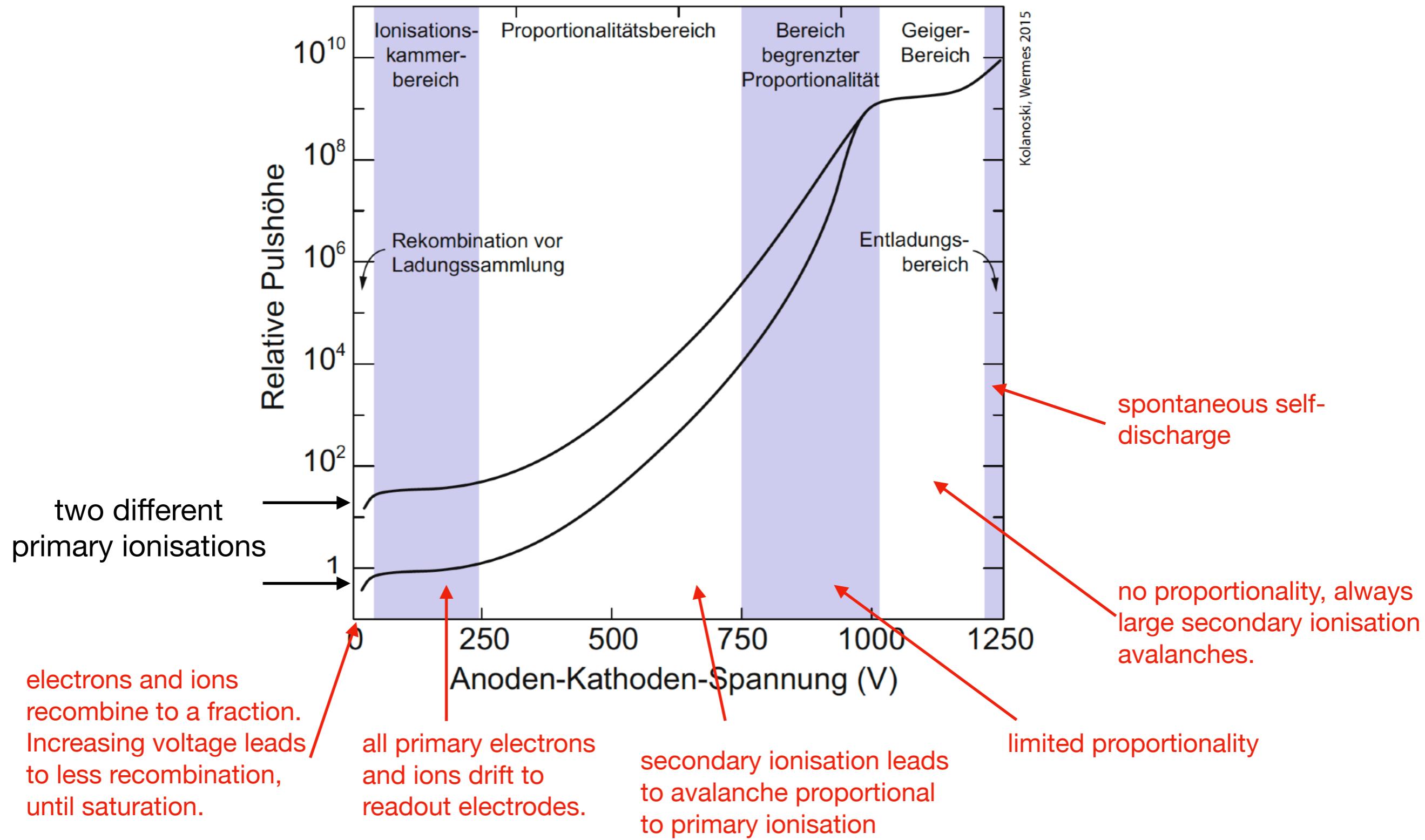
modern operating principle of a gas detector

(synonyms: gas-, gaseous-, gas-filled, gas-ionisation detector)



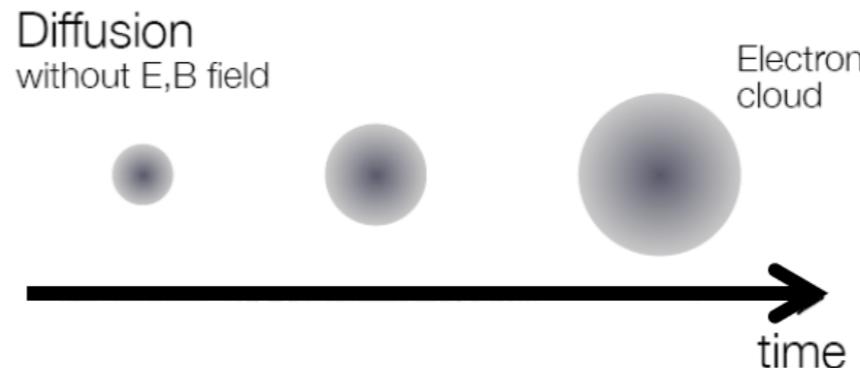
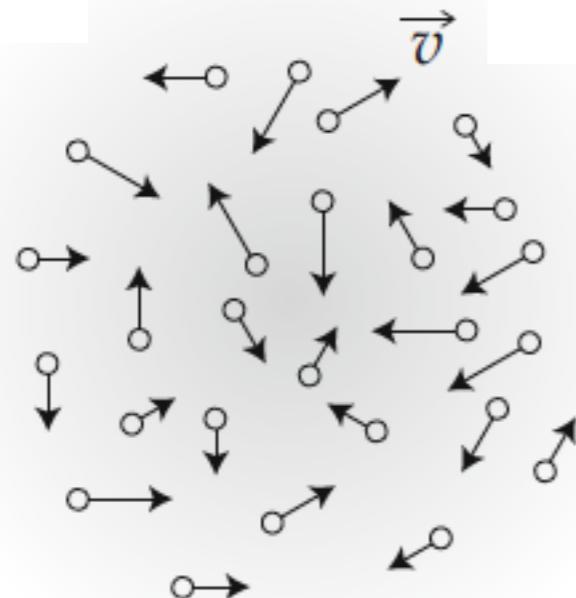
- gas-filled volume between anode and cathode
- voltage between anode and cathode
- collection of electrons and ions which are created by a passing charged particle
- gas has low density, passing particle is mostly undisturbed

The voltage determines the operation mode



Transport of charges through the gas: diffusion

chaotic movements
of charges in gas



classic kinetic theory of gases:

size of cloud $\sigma = \sqrt{6Dt}$

diffusion coefficient D depends on particle type
and gas type (derived from Maxwell distribution)

diffusion coefficient D :

$$D = C_i \frac{1}{p\sigma} \sqrt{\frac{T^3}{m}}$$
$$C_e = \frac{2\sqrt{2}}{3\sqrt{\pi}} = 0.53$$
$$C_I = \frac{2}{3\sqrt{\pi}} = 0.38$$

typical numerical example:

$$D_e \approx 1000 \frac{cm^2}{s} \quad D_I \approx 0.1 \frac{cm^2}{s}$$

Gauß width after drift of 1 μs :

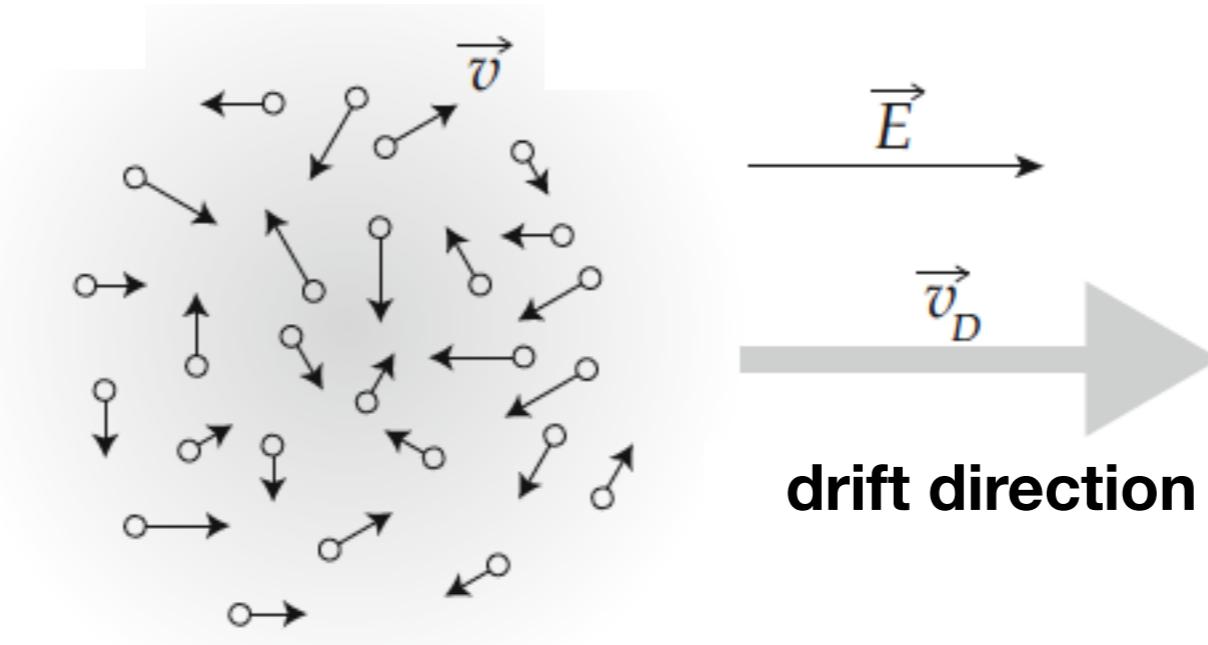
$$\sigma_e \approx 1 mm$$

$$\sigma_I \approx 10 \mu m$$

→ electron cloud expands faster

Transport of charges through the gas: drift velocity

E field applied !



→ net effect: constant drift velocity

$$v_d = \mu |\vec{E}|; \quad \mu: \text{mobility}$$

→ microscopic model:

$$\mu = \frac{e}{m} \tau = \frac{e}{m} \frac{\lambda}{\langle v \rangle} = \frac{e}{T} D$$

→ typical values:

$$v_d(e) \approx 100 \frac{\mu m}{ns}; \quad v_d(I) \approx 0.01 \frac{\mu m}{ns}$$

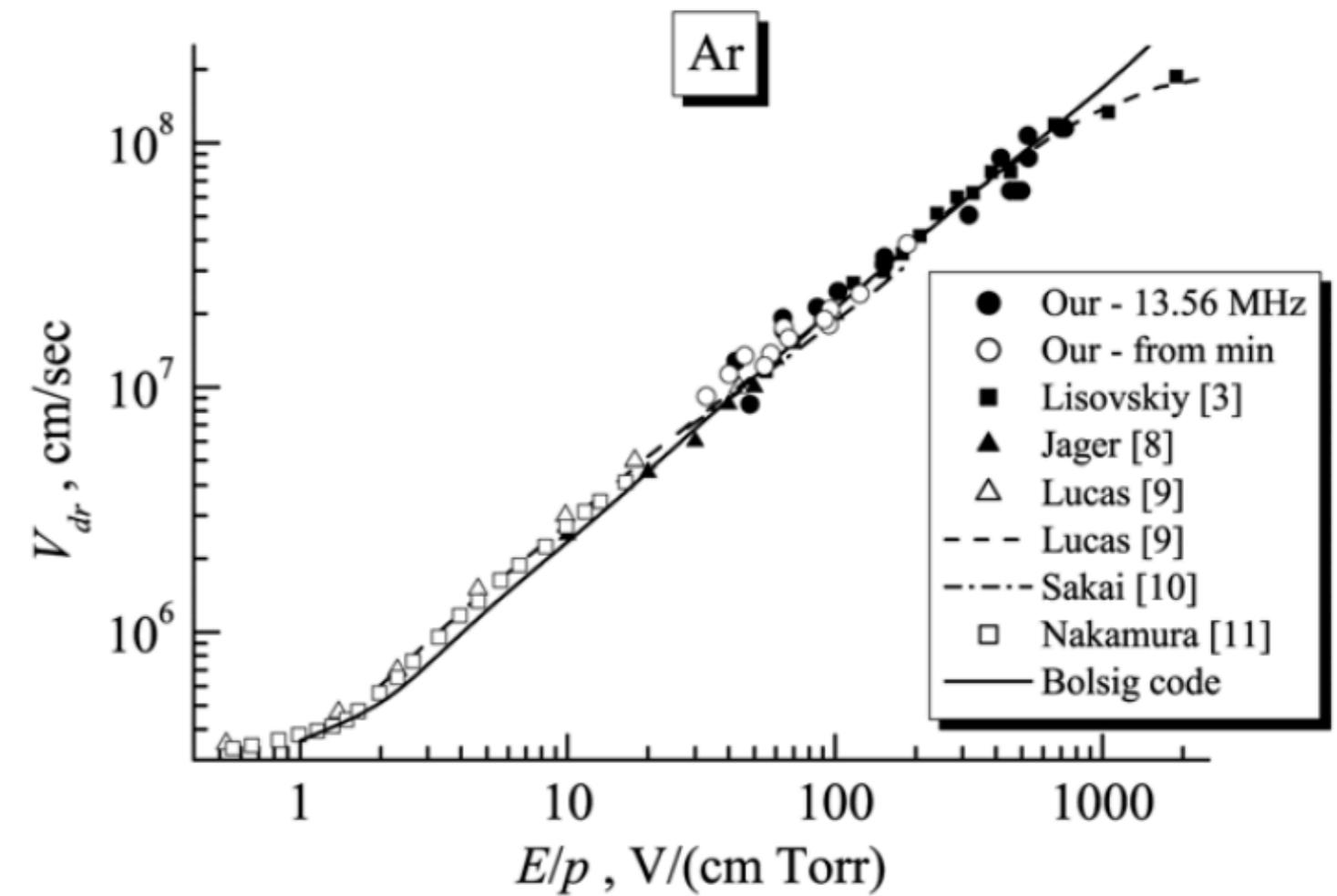
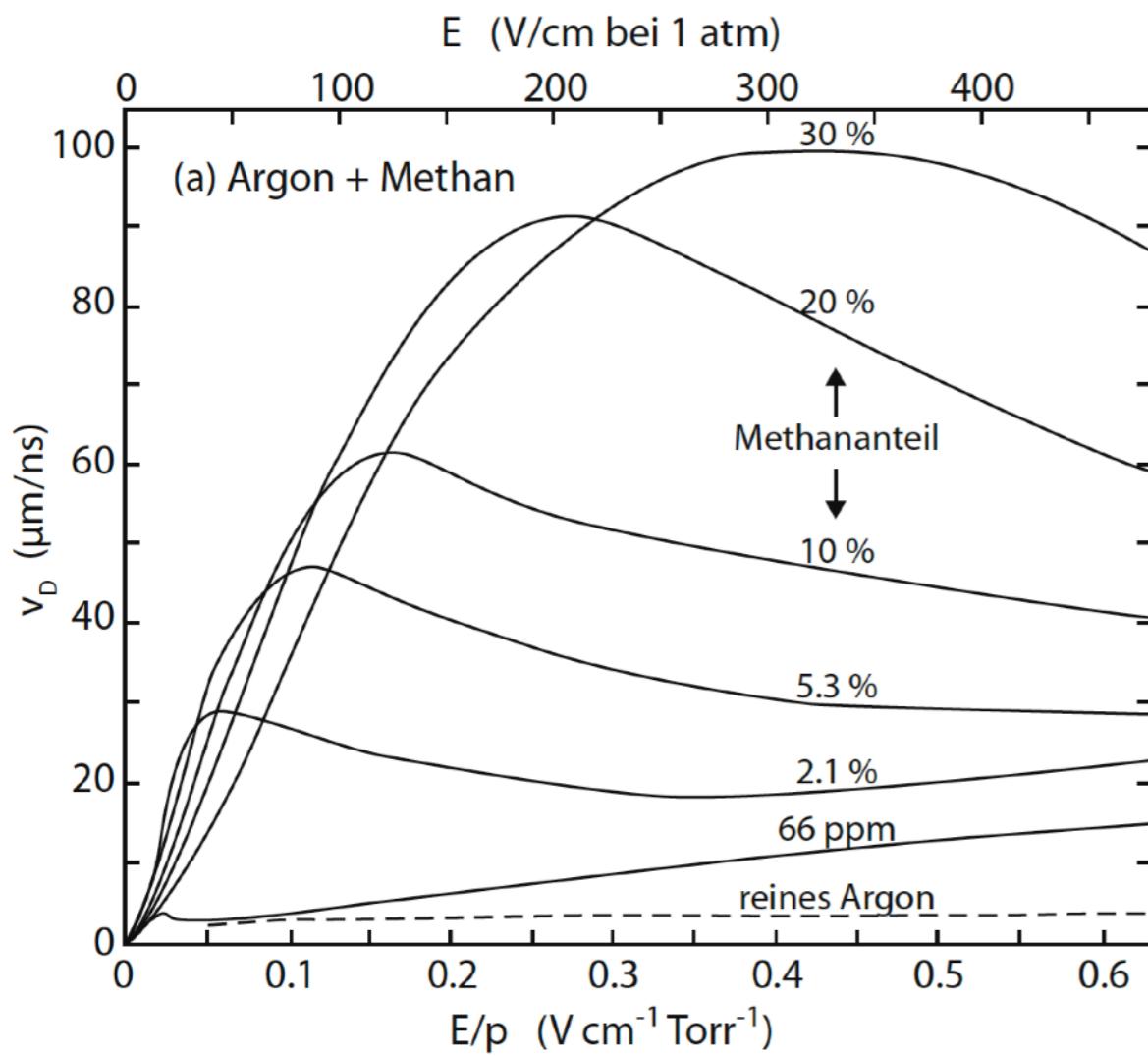
Transport of charges through the gas: ion/electron drift

- ions drift slower than electrons
- mobility is independent of the field (no inelastic scattering etc...)
- examples:

Gas	Ionen	$\mu^+ (\text{cm}^2 \text{ V}^{-1} \text{ s}^{-1})$
H ₂	H ₂ ⁺	13.0
He	He ⁺	10.2
Ar	Ar ⁺	1.7

- electrons can drift very fast and can do inelastic scattering
- scattering cross-sections become energy dependent (excitation of atomic states etc...)
- depends on specific gas mixture
- examples next slide

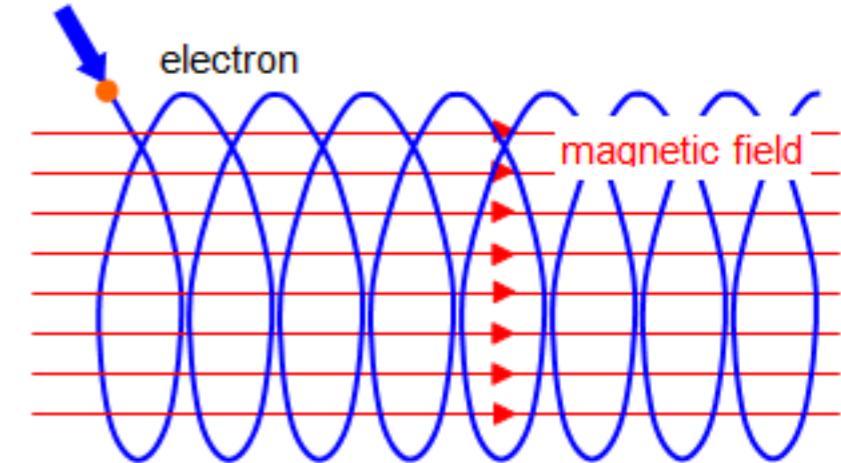
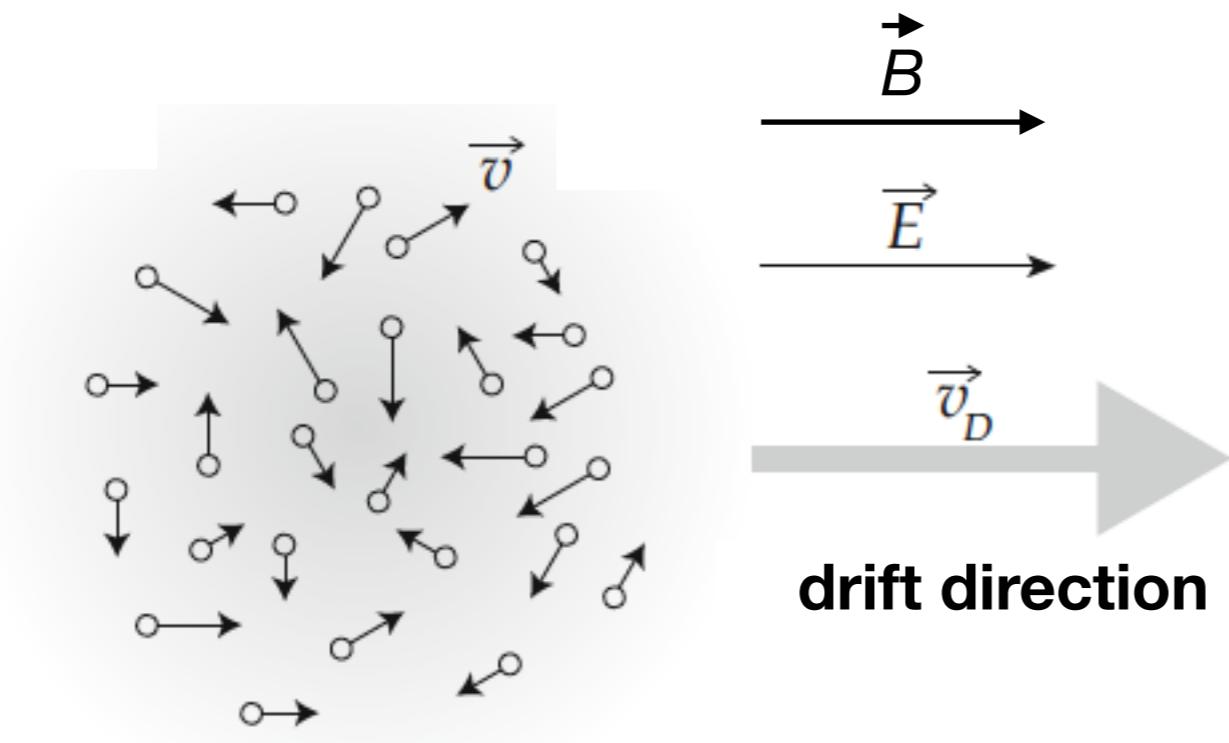
Transport of charges through the gas: electron drift



- energy dependence of (inelastic) scattering cross sections plays important role!
- gas mixture allows to adjust the desired drift behaviour
- quite stable linear behaviour for **pure argon**

Drift with B field

E field and B field applied !



- **longitudinal** drift velocity is the same if B and E field are parallel
- **transverse (!)** diffusion D_T is much reduced (factor 10 or more)

$$D_T = \frac{D}{1 + \omega^2 \tau^2} \quad (\text{where } \omega \text{ is the angular velocity})$$

- long drift distances are facilitated this way (time projection chambers, see later)
- calculation of all effects needs to consider many things:
 - scattering of charge carriers in gas, dependence on pressure, temperature, cross sections, energy, ...
 - statistical treatment of atomic movement, diffusion
 - external fields in arbitrary direction
 - use Boltzmann transport equation, Langevin equation, Diffusion equation, Maxwell equations

Signal formation: general principle

remember last lecture:

- Shockley-Ramo-Theorem etc...
- moving charged particle induces signal in readout electrodes (even before it reaches the electrode)

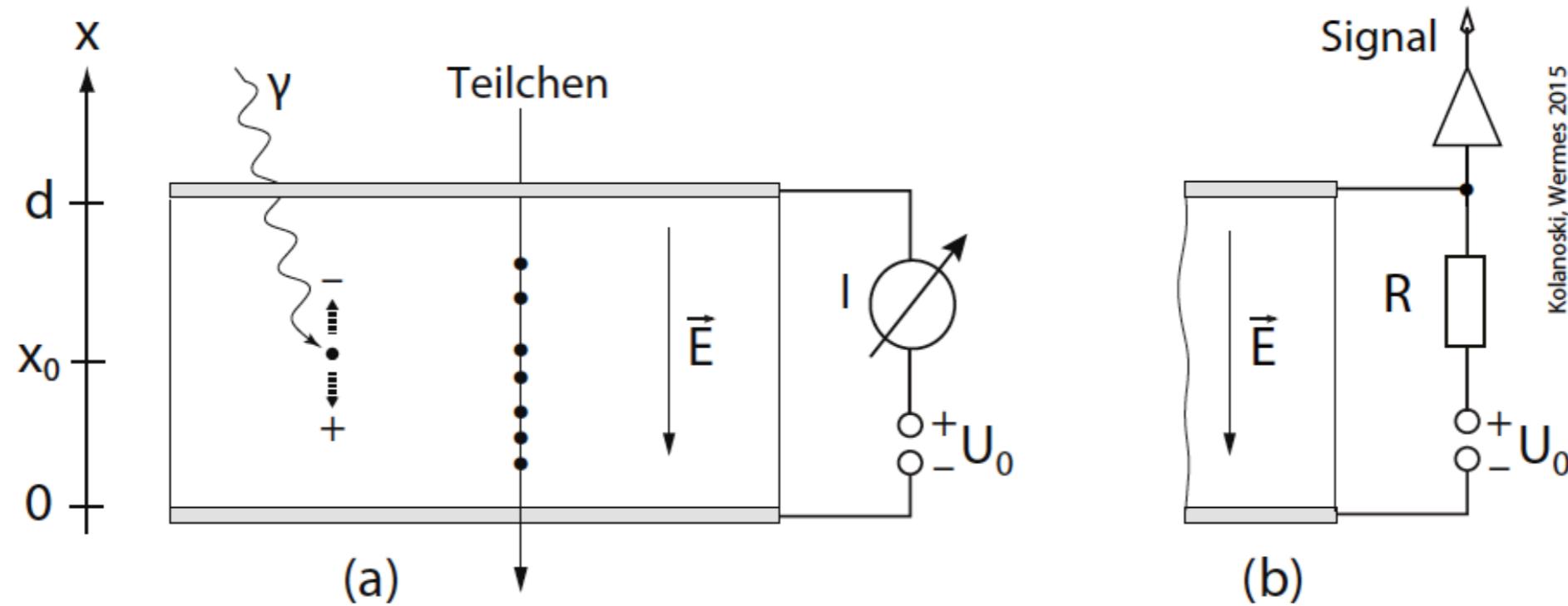
$$i(t) = q \cdot \vec{E}_w \cdot \vec{v}$$

$$Q(t) = \int_0^t i(\tau) d\tau = q \int_{x_1}^{x_2} \vec{E}_w d\vec{x}$$

With q: charge, E_w : weighting field, v: velocity

- How to get the weighting field?
 - Calculate the electrostatic field for each electrode by:
 - removing the signal charge
 - setting the electrode to $U = 1V$ and all others to $0 V$

Signal formation: parallel plates



principle:

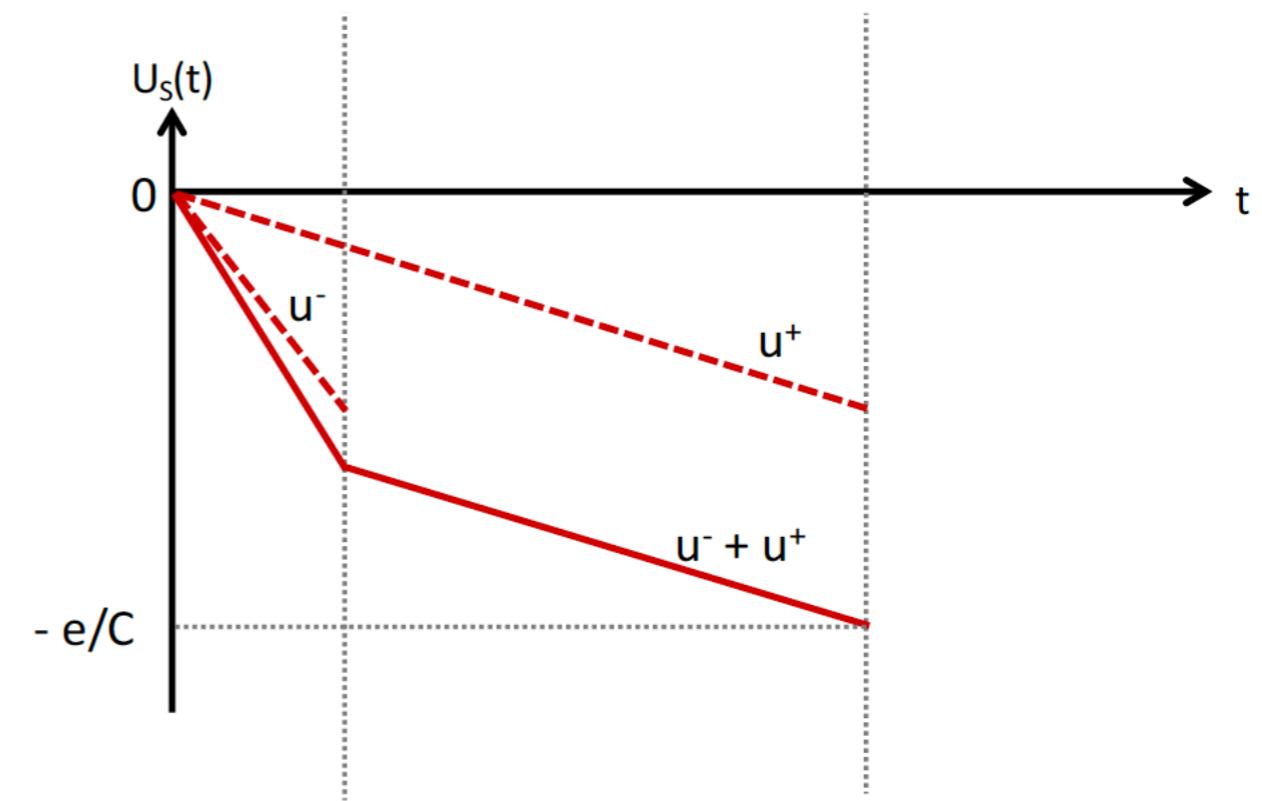
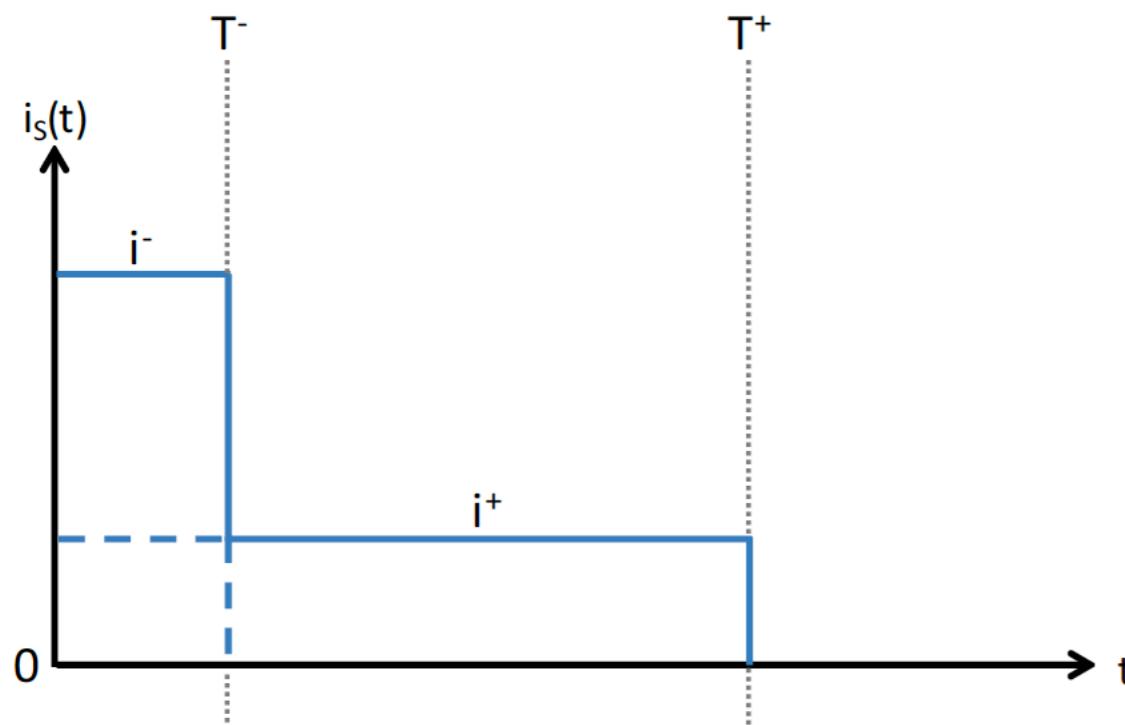
- point-like ionisation from photons **or** extended ionisation track from charged particles
- signal read out as current or as voltage as function of time

Signal formation: parallel plates

- arrival time: $T^- = \frac{d - x_0}{v^-}, \quad T^+ = \frac{x_0}{v^+},$

- current: $i_S^- = \frac{e}{d} v^- \quad i_S^+ = \frac{e}{d} v^+$

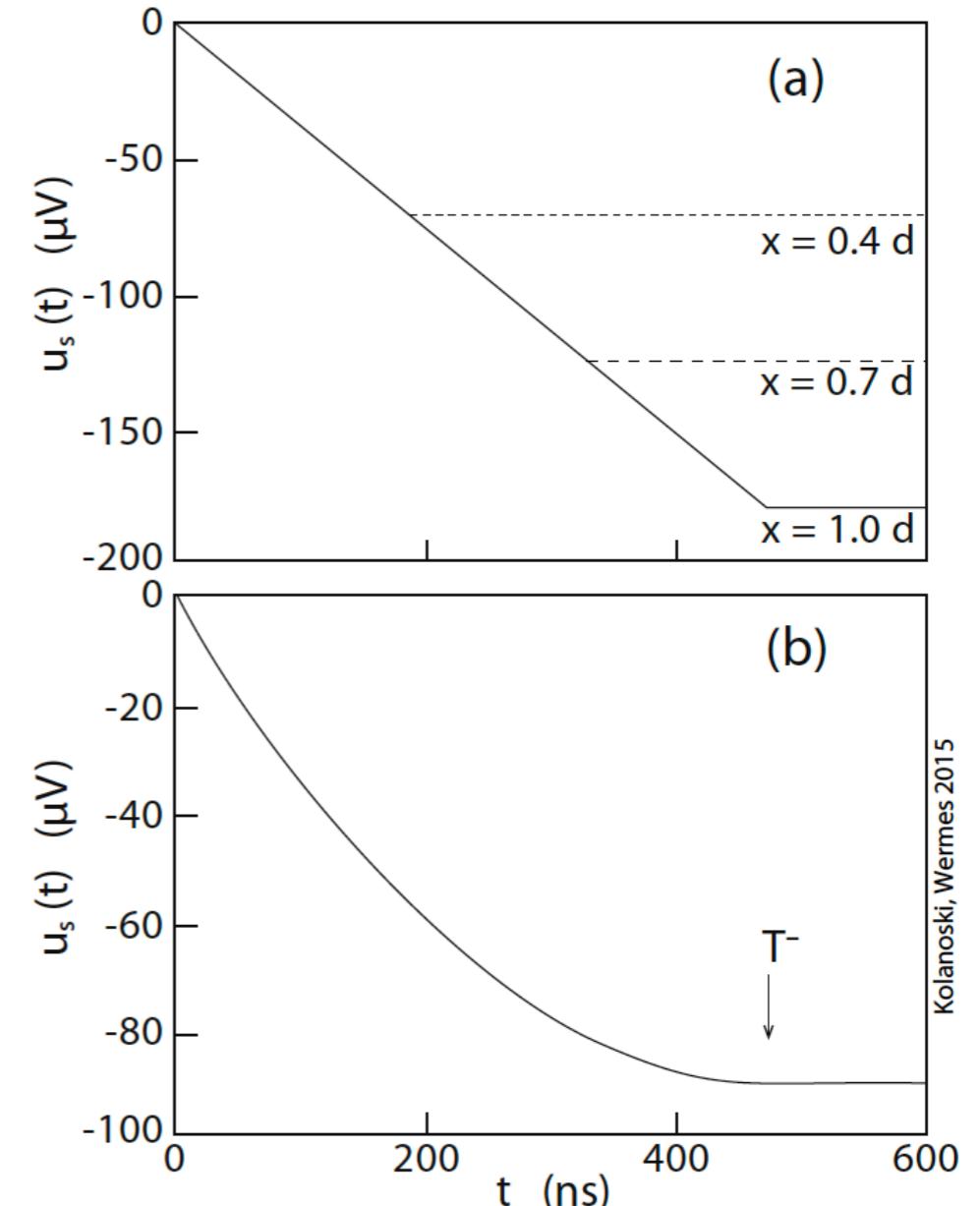
- voltage: $u_S(t) = u_S^-(t) + u_S^+(t) = \begin{cases} -\frac{e}{Cd}(v^- + v^+)t & 0 < t < \min(T^-, T^+) \\ -\frac{e}{Cd}(d - x_0 + v^+t) & \text{für } T^- < t < T^+, \\ -\frac{e}{Cd}(x_0 + v^-t) & T^+ < t < T^- . \end{cases}$



(signal formation in cylindrical geometry, see later...)

Signal formation: parallel plates

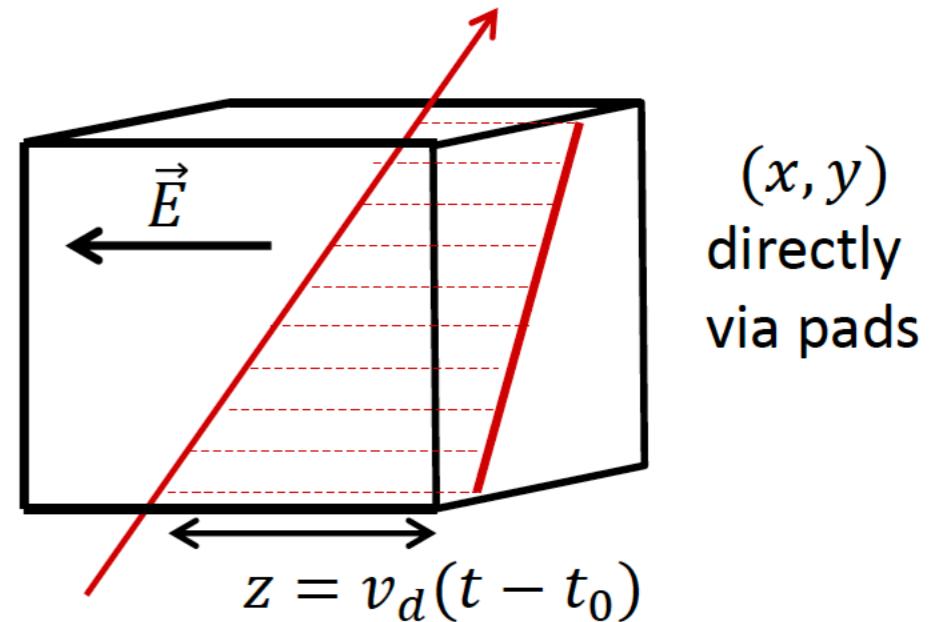
- note that the maximal signal is independent of the position of the initial ionisation
- the maximal signal is therefore the same for an “ionisation track” and a point-like ionisation (see previous slide)
- the time-dependence (shape) of the signal-development is however very different
- the electron-signal is usually extremely fast (microseconds) while the ion-signal is slow (milliseconds)
- the diagram shows the electron-signal only
 - for point-like charges (top), deposited at a distance x from the electrodes
 - and a continuous track (bottom)
- the continuous track can be derived by subdividing the track into many small single charge deposits



Detector type: long drift distance in TPC

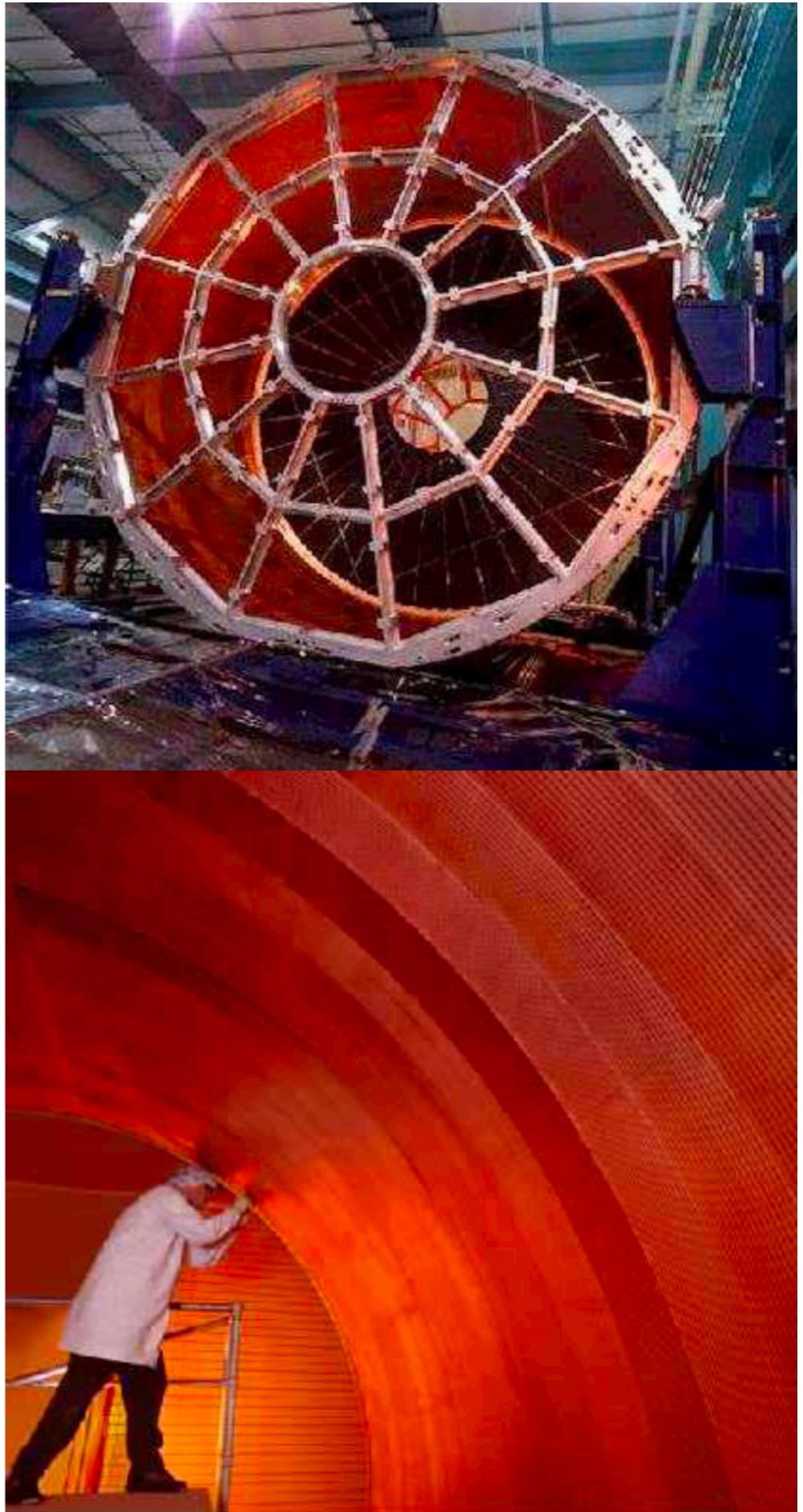
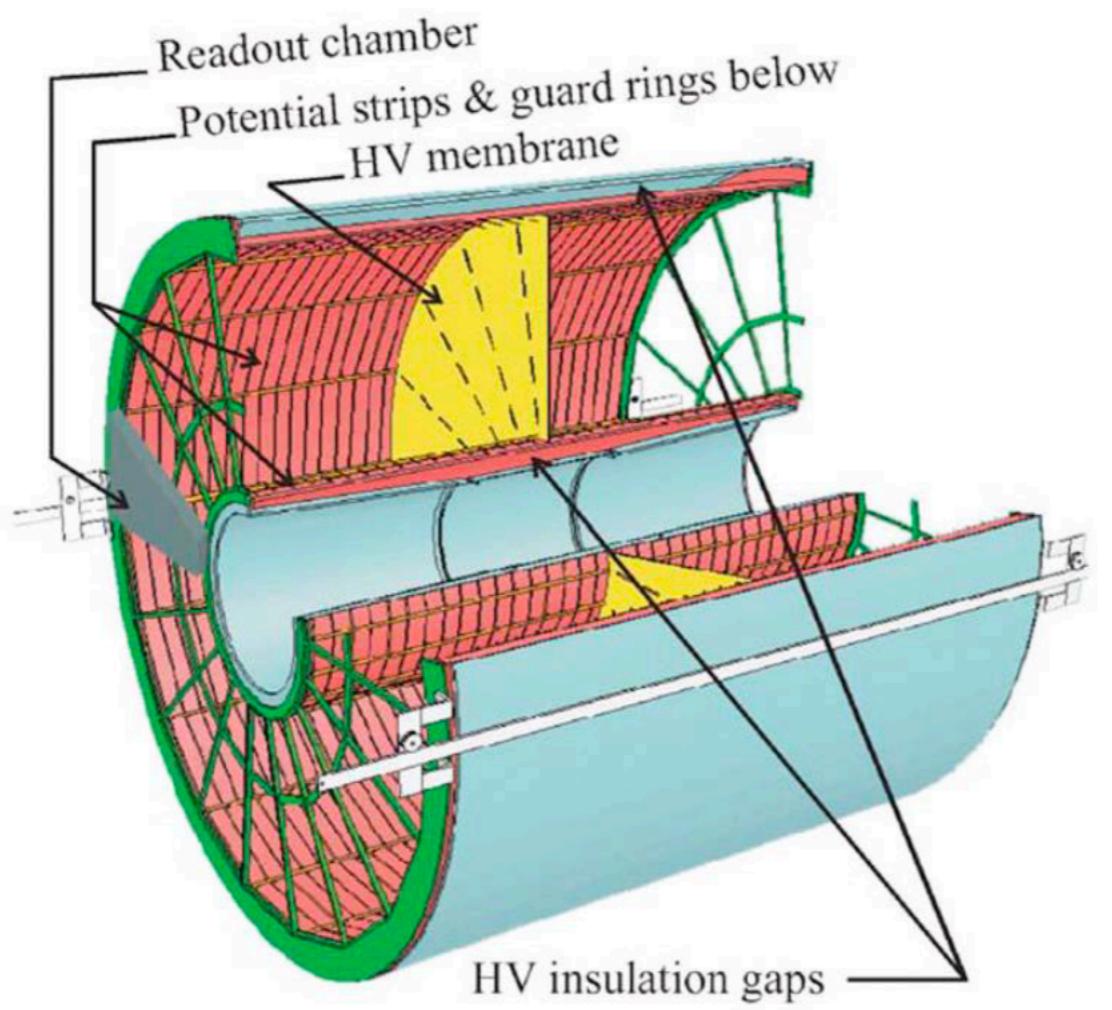
TPC: time projection chamber

- Very little material that particles pass
 - Small multiple scattering
 - Little photon conversion
 - Little bremsstrahlung for electrons/positrons
- Challenges of very long drift distances (several meters)
 - Diffusion must be limited
 - Sufficient fast drift gas at moderate electric field strength
 - High requirements on field homogeneities (\vec{E} and \vec{B})
 - Pure gas to avoid signal loss due to electron attachment
 - Limitation of ion backdrift

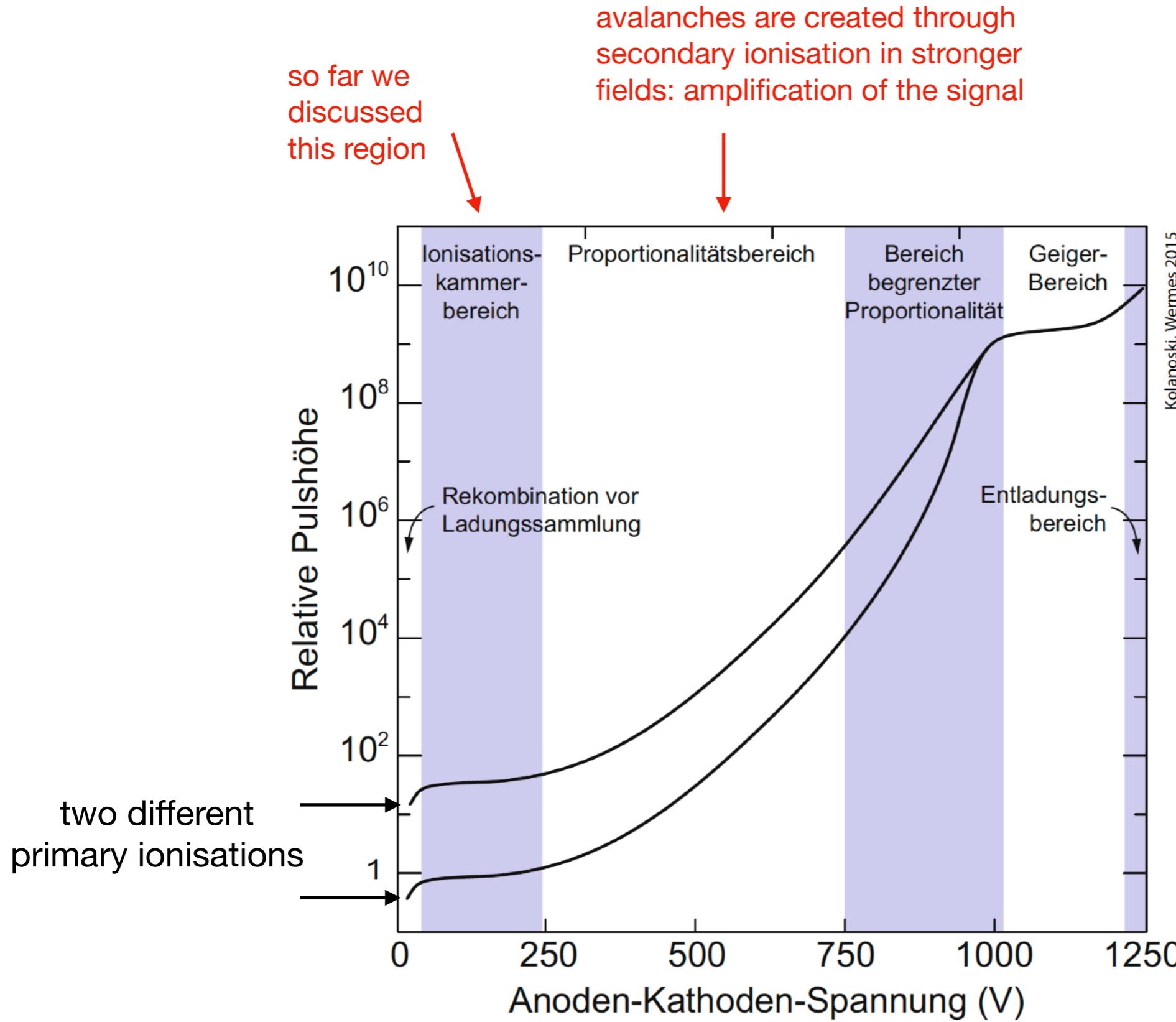


(x, y)
directly
via pads

ALICE-TPC:



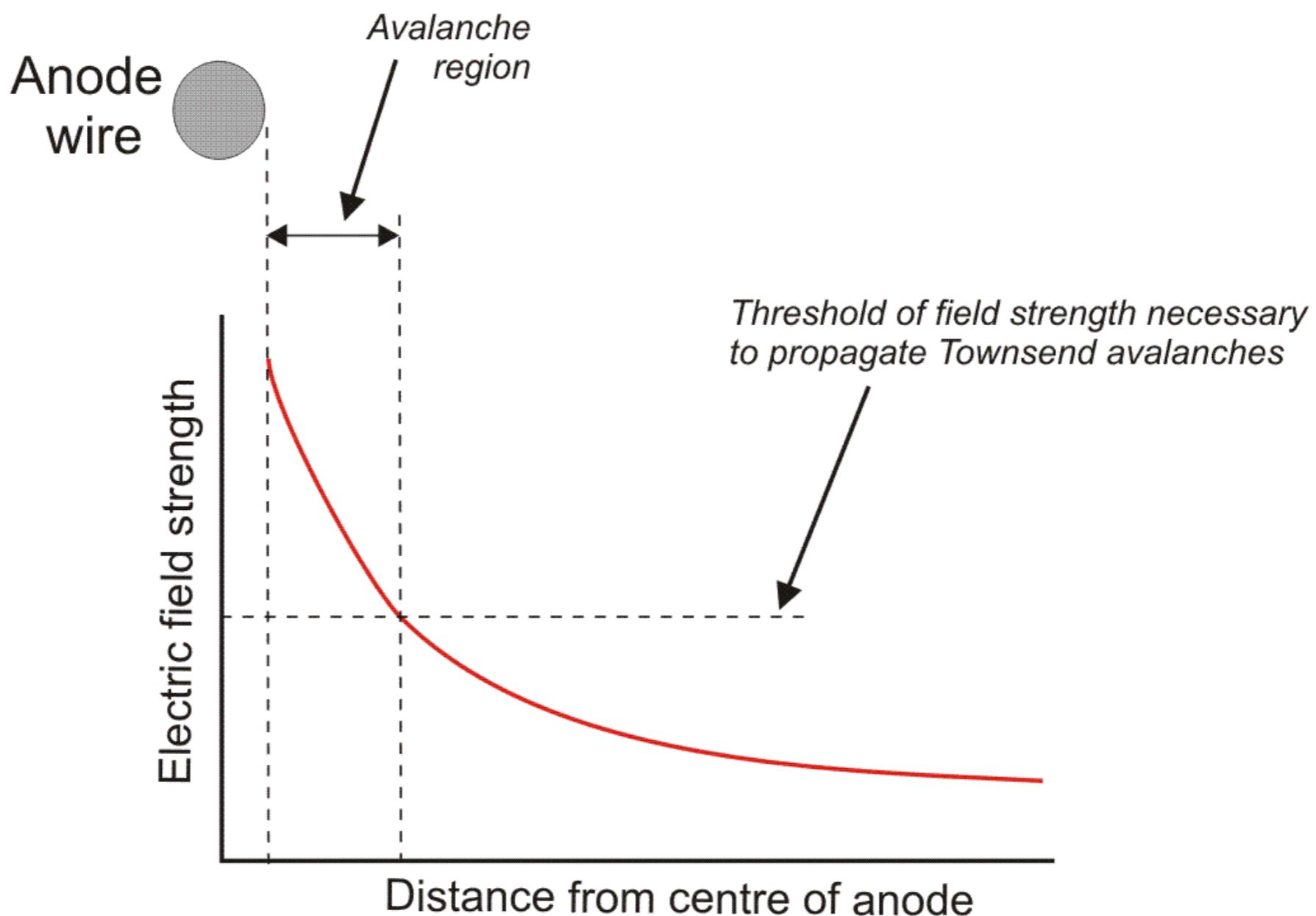
Gas amplification



Gas amplification: field around wires

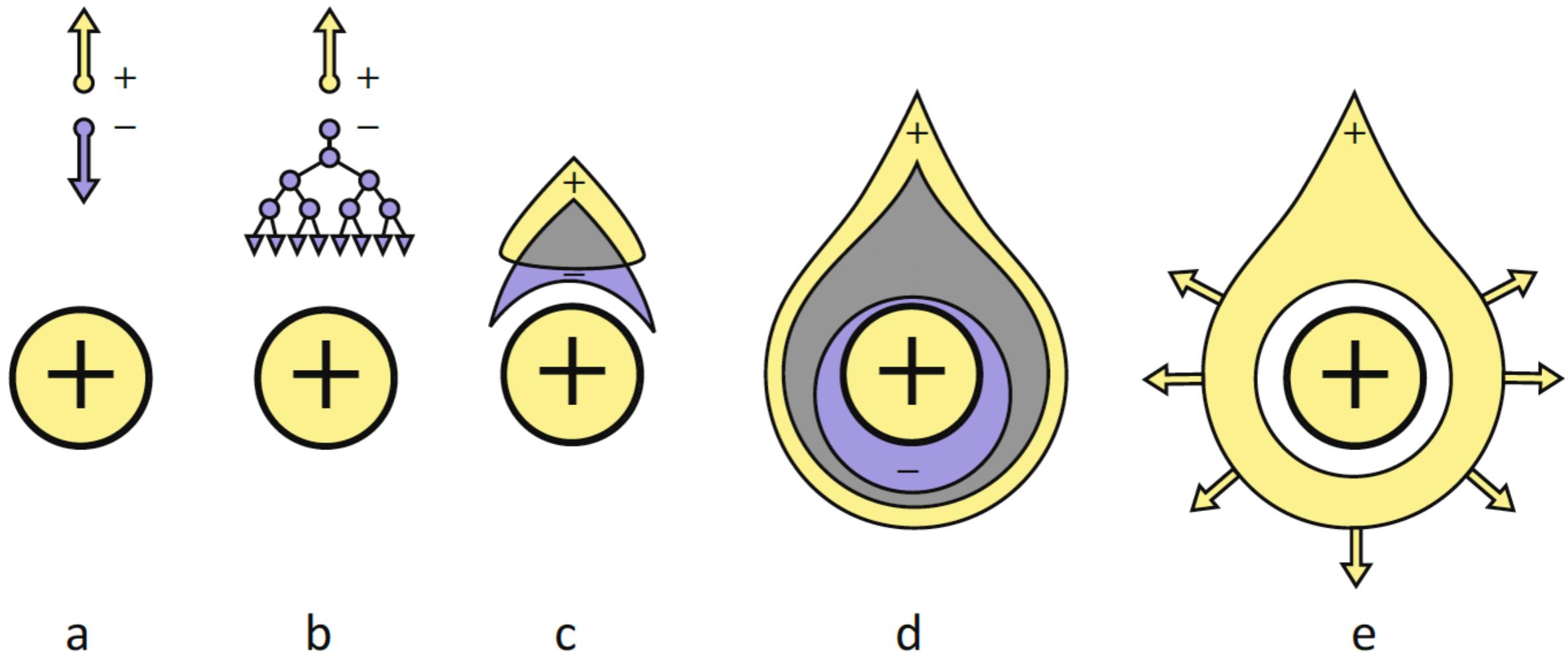
wire in proportional counter:

Electric field strength at a counter anode



Gas amplification: field around wires

development of avalanche in proportional counter



primary
electrons
drift to anode

secondary
ionisation
close to
anode,
avalanche is
created

charges in the
avalanche are
separated by
E field

electrons
diffuse faster
than ions,
avalanche
goes around
the whole wire

positive
charges drift
slowly to
cathode

Gas amplification

- the ratio between number of final electrons N and number of primary electrons N_0 is the gas gain G :
- it can be calculated from the **1st Townsend coefficient** α which is the number of ionisations created by a free electron per distance unit

$$\alpha = \sigma_{ion} \cdot n = \sigma_{ion} \cdot \frac{N_A}{V_{mol}}$$

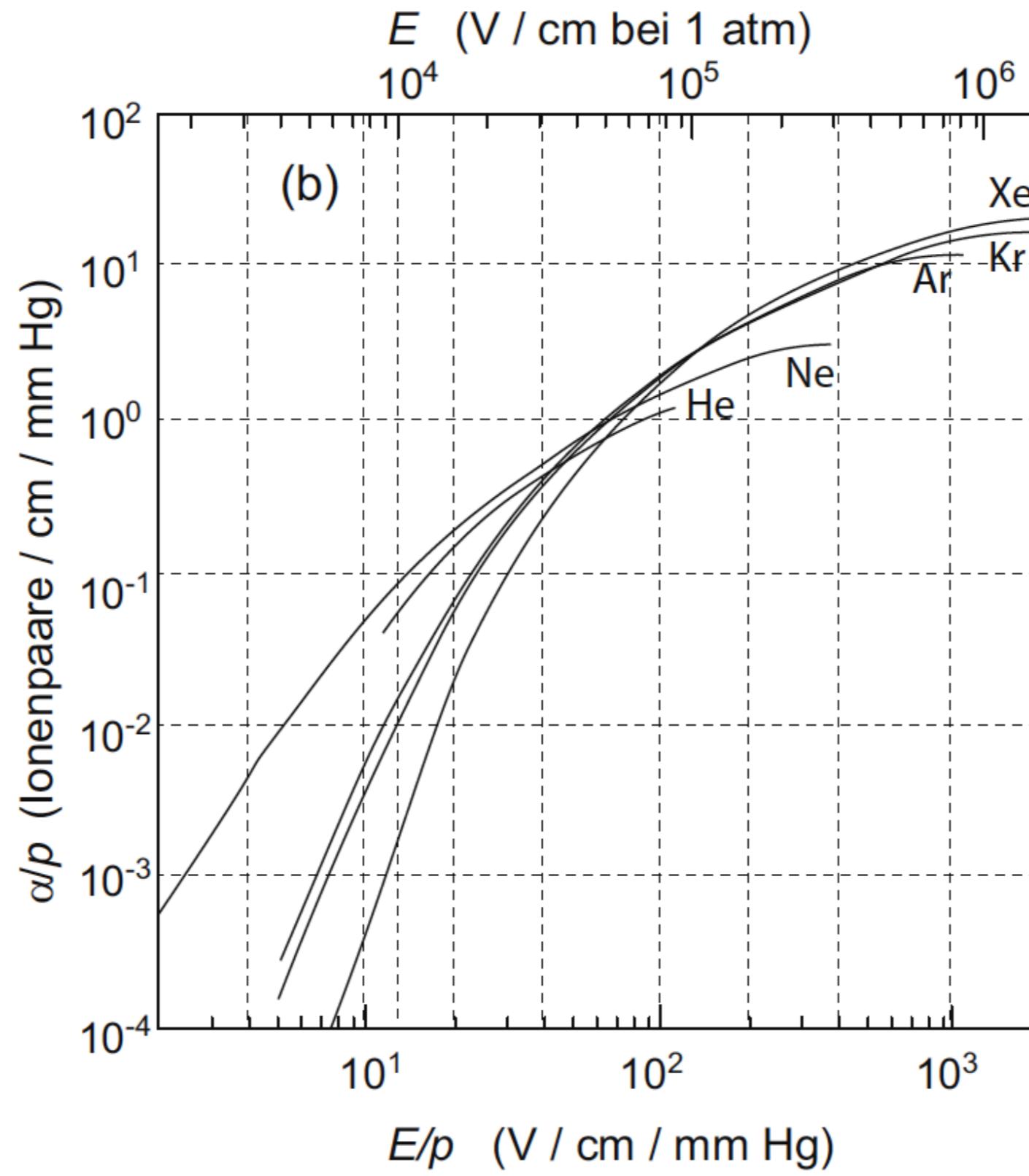
↑
Ionisation cross section

$$\sigma_{ion} = \sigma_{ion}(E) \Rightarrow \alpha = \alpha(|\vec{E}|) = \alpha(\vec{x})$$

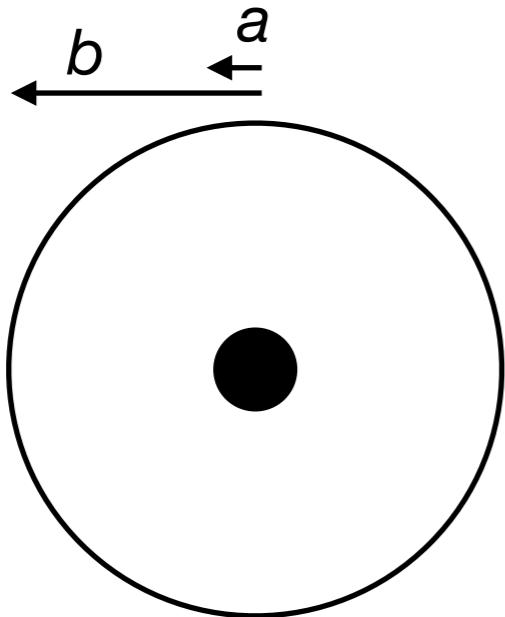
$$dN = \alpha N dx$$
$$N(x) = N_0 \exp \left(\int \alpha(x) dx \right) \equiv N_0 \cdot G$$

↓
Gas gain

Gas amplification: 1st Townsend coefficient



Example: cylindrical “proportional chamber”



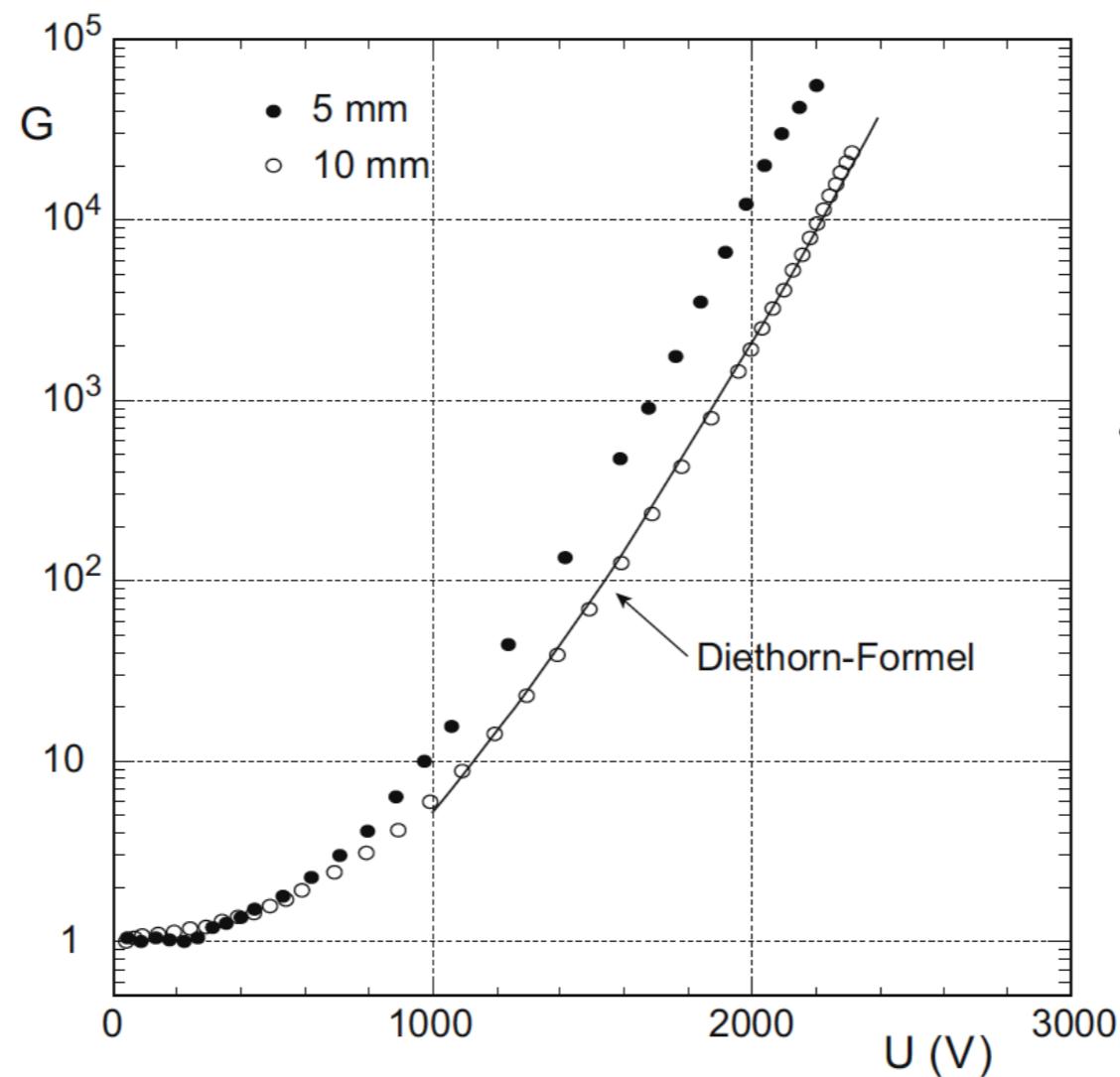
- anode wire diameter: $2a$
- tube diameter: $2b$
- electric field $E(r) = \frac{U}{r \ln \frac{b}{a}}$
- insert into expression for G (previous slides)
- some math and approximations lead to Diethorn formula:

$$\ln G = \frac{\frac{U}{a} \ln 2}{\ln \frac{b}{a} \Delta U} \ln \left(\frac{U}{a \ln \frac{b}{a} E_{min}(p_0) \frac{p}{p_0}} \right)$$

- where the Diethorn parameters ΔU and E_{min} depend on gas type and mixture and are usually measured
- example for CF₄/CH₄ mixture in 80:20 ratio: $\Delta U = 53.8$ V, $E_{min} = 39.2$ kV/cm (see plot next slide)

Example: cylindrical “proportional chamber”

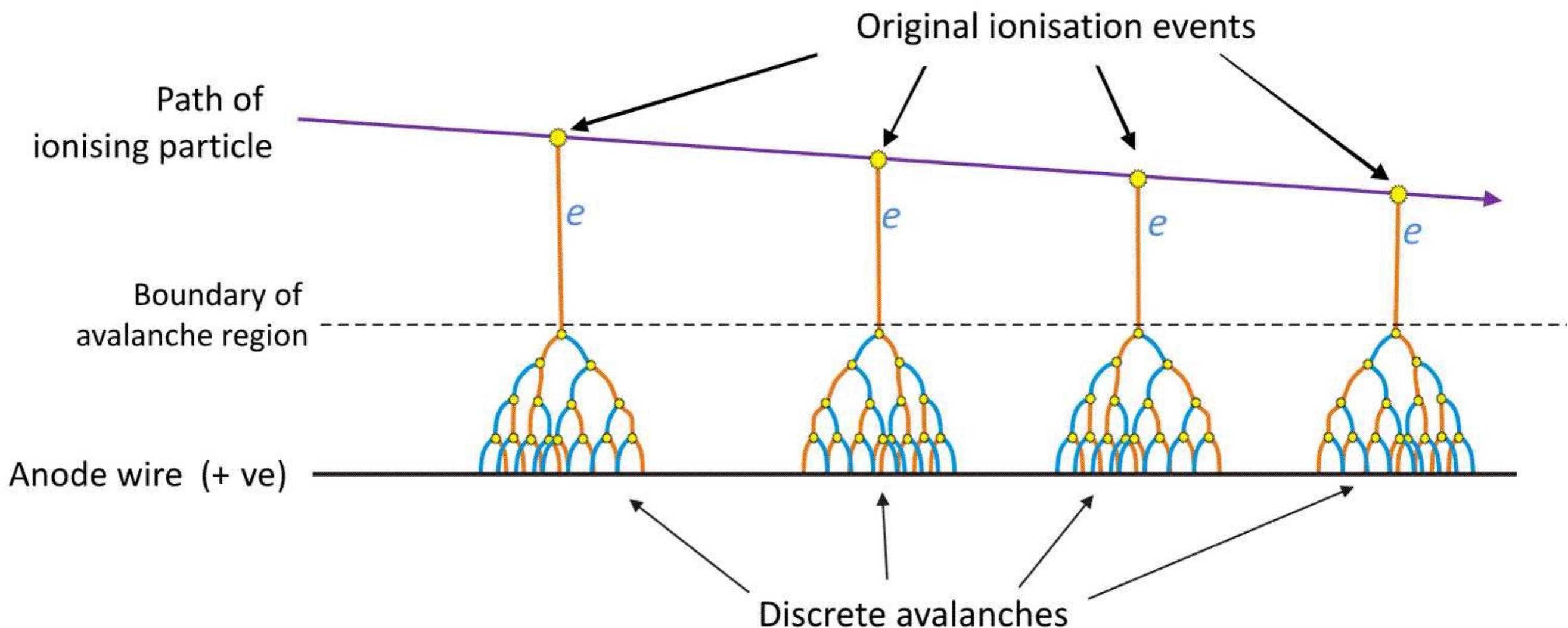
- typical values for G are 10 (at $U=1\text{kV}$) and 10000 (at $U>2\text{kV}$)



- CF4/CH4 mixture
in 80:20 ratio:

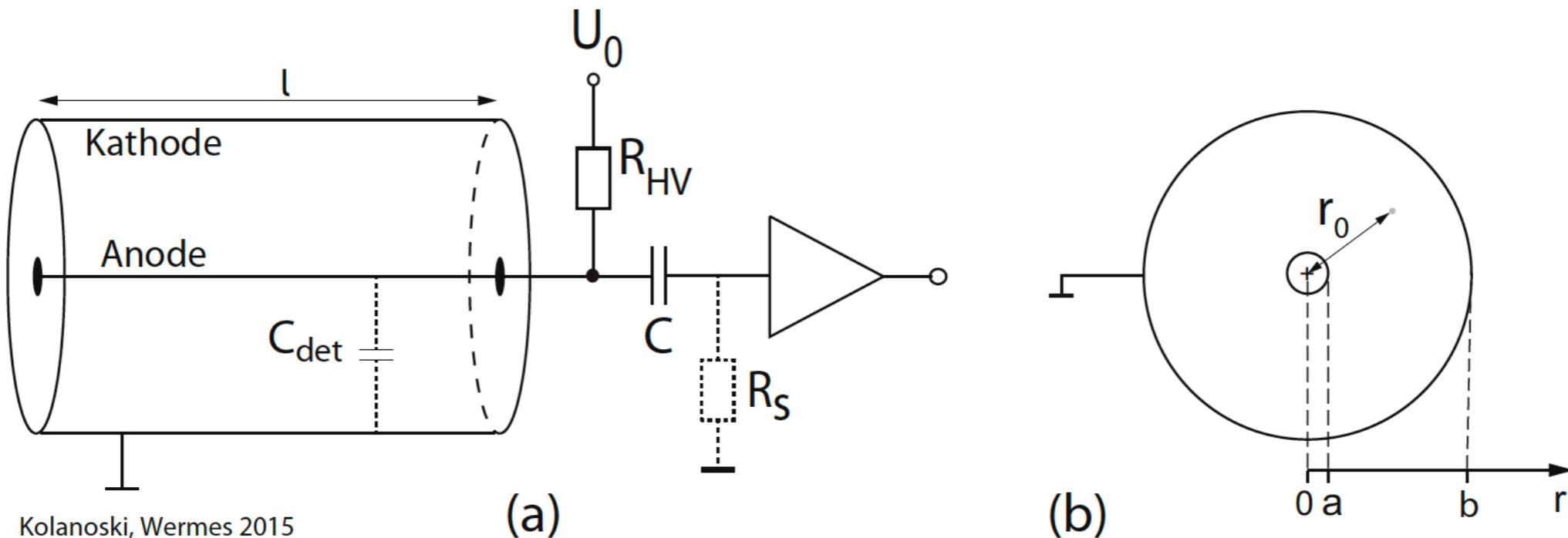
Gas amplification: operating principle

Creation of discrete avalanches in a proportional counter



→ N primary ionisations create N avalanches of GN charges

Signal formation: cylindrical proportional chamber



- fundamentally different from parallel drift chamber signal (see previous slides) because of avalanche close to the wire
- drift or primary ionisation negligible compared to secondary ionisation
- secondary ionisation happens only very close to wire → electrons are immediately absorbed by anode wire (small and short signal, almost negligible)
- the main signal is then created by ions that drift from the anode to the cathode
 - in the beginning the ions drift fast in a strong field
 - at larger distance, the drift gets slower

$$i_S^+(t) = \frac{Ne}{2 \ln b/a} \frac{1}{t + t_0^+} \quad \text{with} \quad t_0^+ = \frac{r_0^2 \ln b/a}{2\mu^+ U_0}$$

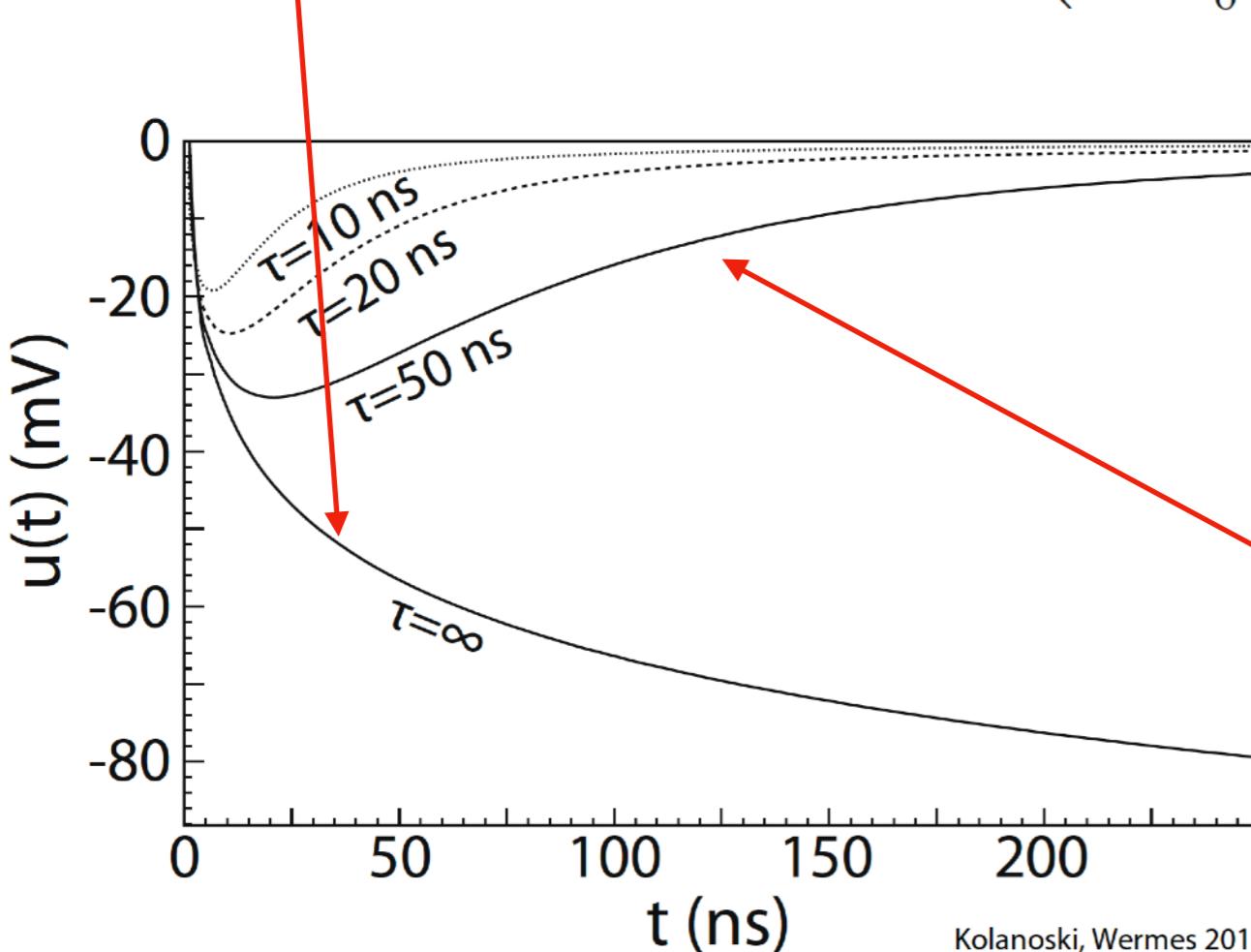
Signal formation: cylindrical proportional chamber

- the charge signal is obtained from integrating i

$$Q_S(t) \approx Q_S^+(t) = -\frac{Ne}{2 \ln b/a} \int_0^t \frac{dt'}{t' + t_0^+} = -\frac{Ne}{2 \ln b/a} \ln \left(1 + \frac{t}{t_0^+} \right)$$

- the voltage is obtained from the capacitance

$$u_s(t) = \frac{Q_S(t)}{C_l l} = -\frac{Ne}{2\pi\epsilon_0 l} \ln \left(1 + \frac{t}{t_0^+} \right) \quad \text{with } C_l = \frac{2\pi\epsilon_0}{\ln b/a}$$

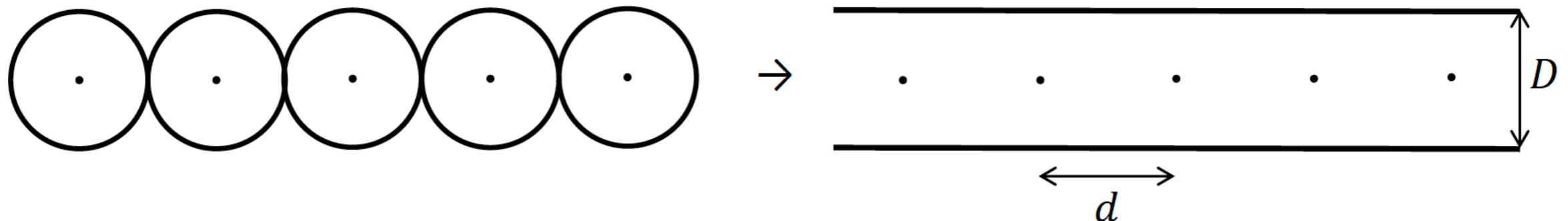


- this is very slow!
- experiments need to separate pulses which are close in time
- use resistance R_S (see picture last slide) to remove the voltage with time constant $\tau = R_S C_{det}$

Detector type: proportional chambers

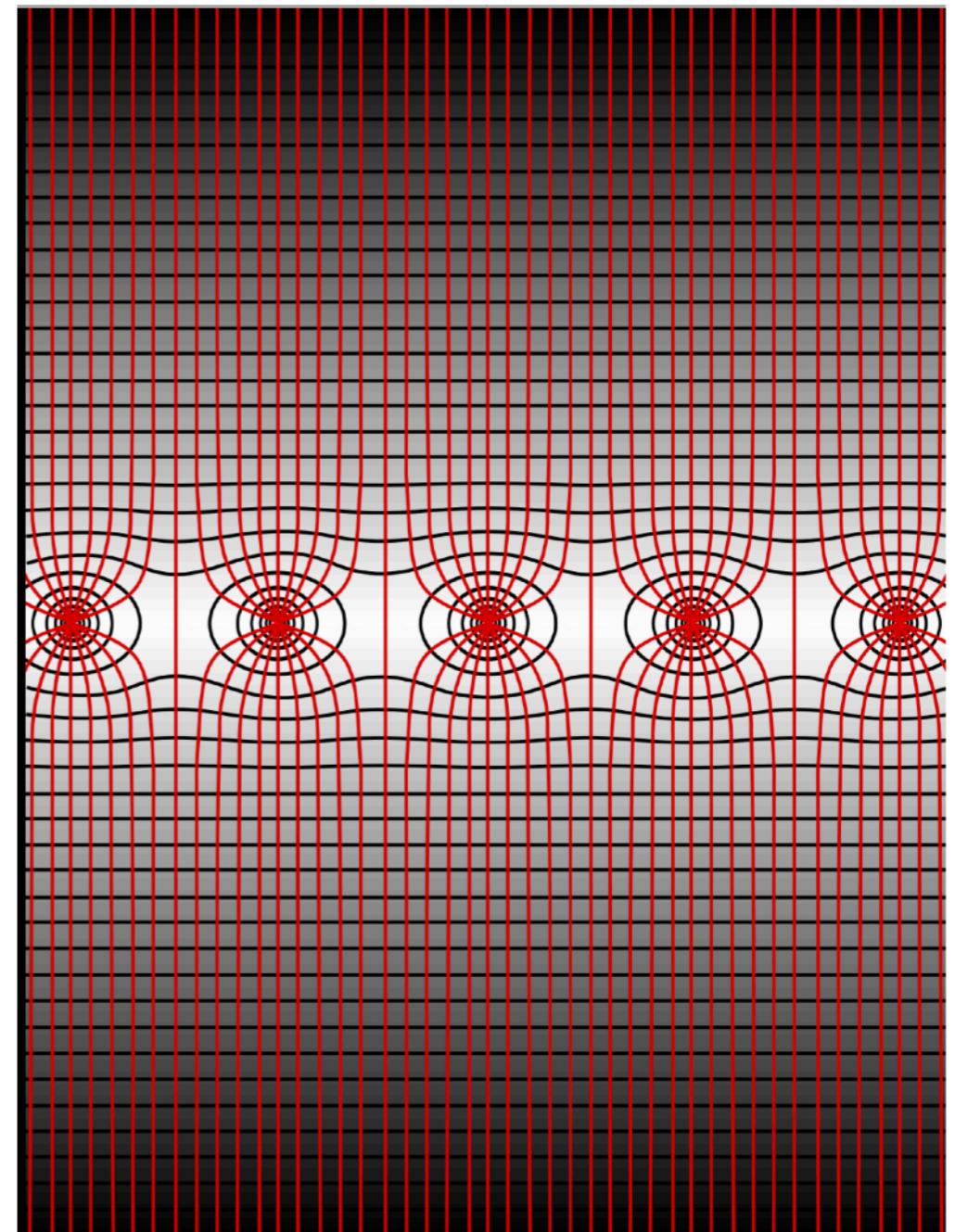
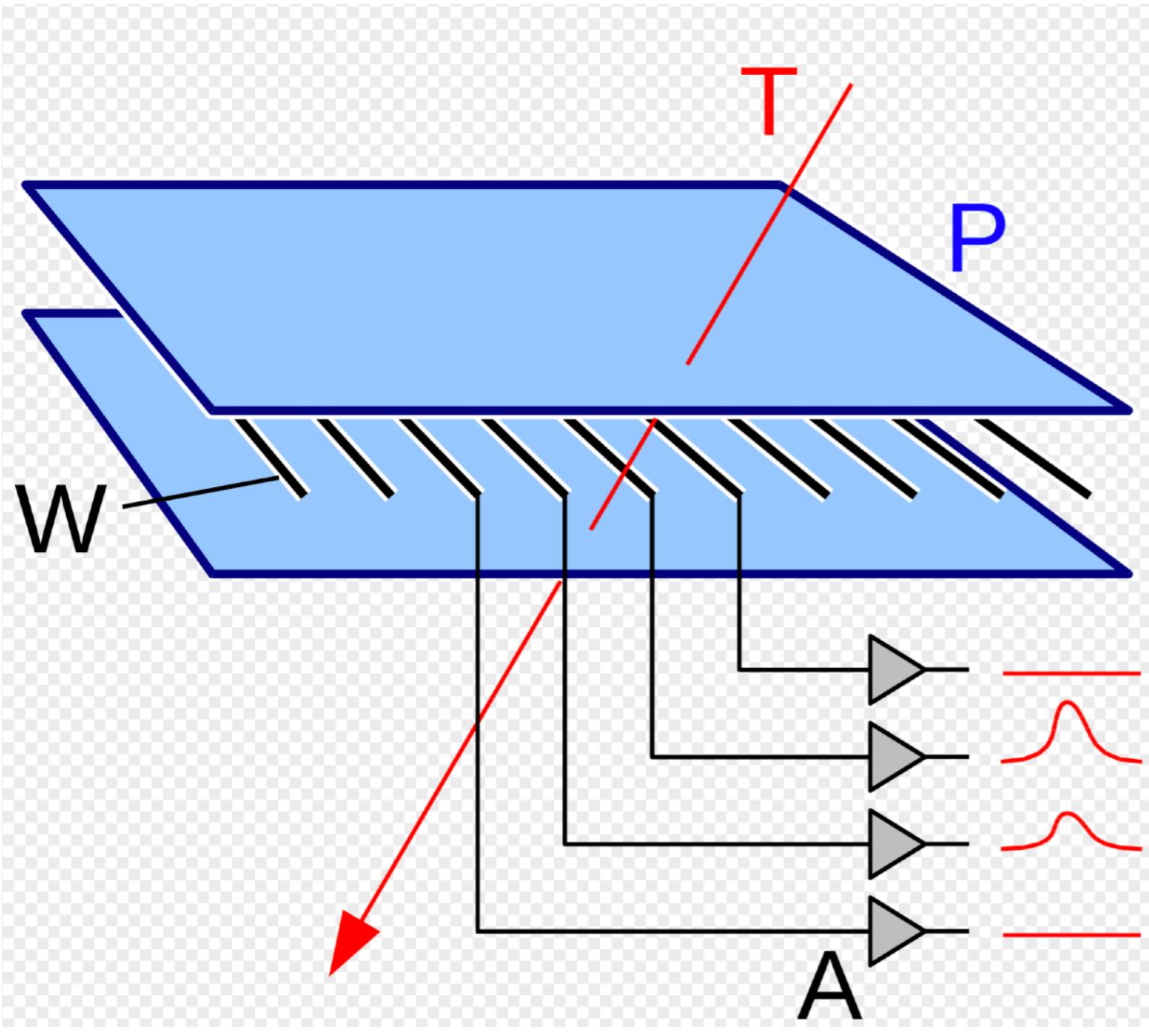
Multi Wire Proportional Chambers (MWPC)

- 1968 developed by Charpak et al. (CERN) → nobel prize 1992
- It is a layer of proportional counters without separating walls

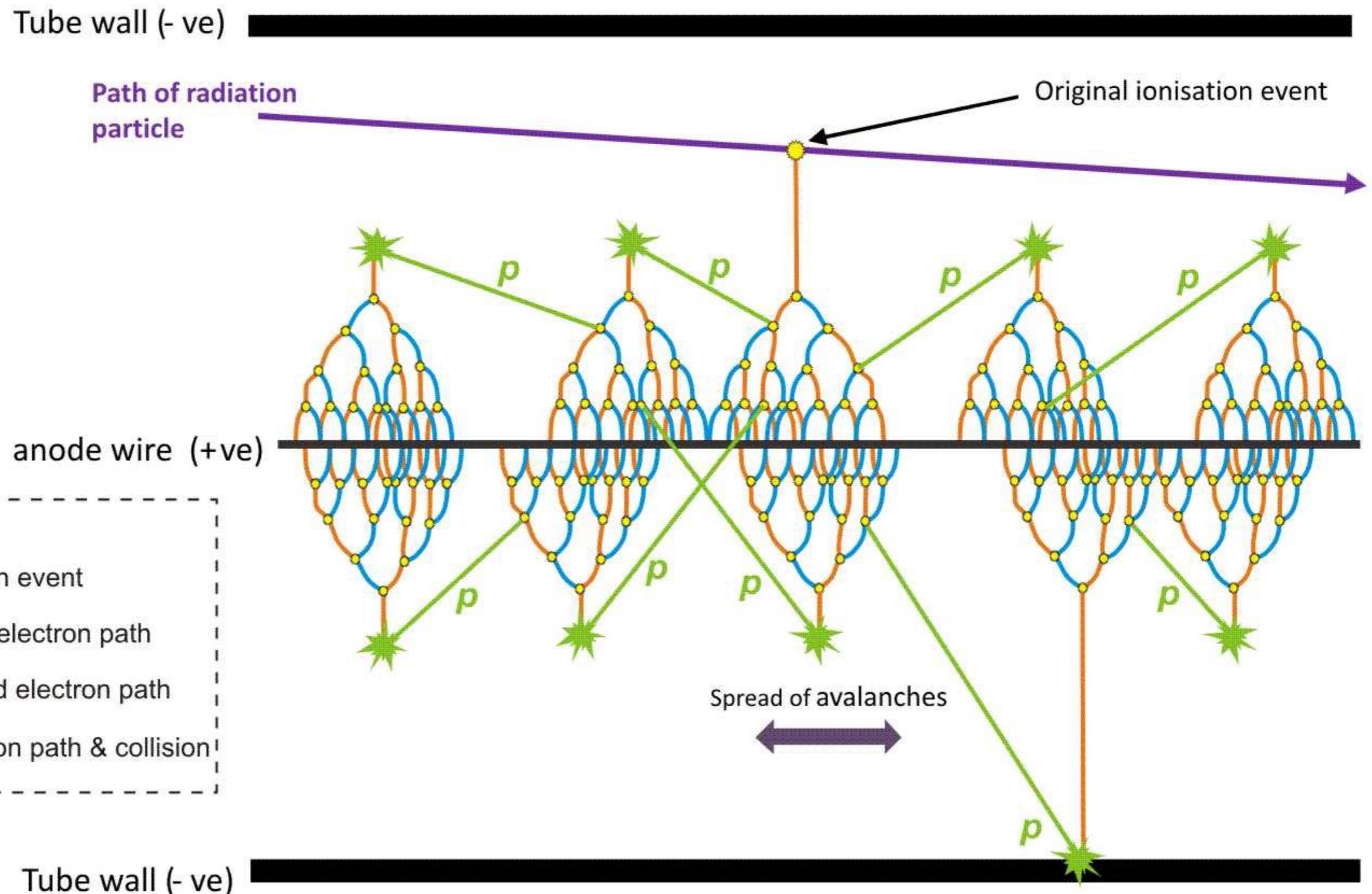


- Typical dimensions: $D \approx 10 \text{ mm}$ $d \approx 1 - 5 \text{ mm}$
- Position resolution: $\frac{1}{\sqrt{12}} d \approx 1 \text{ mm}$
- At each wire electronic circuit → enables electronic data acquisition
→ first purely electronic detectors (advent of semiconductor electronics in 1960's)

Detector type: proportional chambers



Spread of avalanches in a Geiger-Muller tube



Not to scale

→useful only for “counting” of events

GEM: gas electron multiplier

- Voltage of 300 – 500 V between both sides of perforated copper cladded capton foil
- High electric field inside holes yields gas amplification
- Triple GEM: $G \approx 10^5$
- Anode pads below GEM measure pure electron signal, can be kept at ground potential

