


Program transformation is not compositional. Assume program P to be a trivial, terminating program.
Assume that program Q is:

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1. Observe ( $x == 0$ )
2. if ( $x$ ) {
3.     diverge;
4. }
5.  $x := 1$ ;

```



When considering $wp(Q, f)$, as should be done in the case $wp(\widehat{P}; Q, f)$, the wp will consider the diverge-statement on line 3.

However, when considering $wp(\hat{Q}, f)$, the diverge-statement will not be considered, as ~~this~~ the if-statement can safely be ignored. This can be seen when constructing the weakest pre-expectations:

$$\begin{aligned}
 wp(Q, f) &= wp(\text{if } x \text{ then diverge else skip; end, } f) \\
 &= [x] \cdot wp(\text{diverge, } f) + [\neg x] \cdot wp(\text{skip, } f) \\
 &= [x] \cdot 0 + [\neg x] \cdot f = [\neg x] \cdot f.
 \end{aligned}$$

$$\begin{aligned}
 wp(\hat{Q}, f) &= wp(\text{if } x \text{ then diverge else skip; } x := 0; \text{ end, } f) \\
 &= wp(\text{if } x \text{ then diverge else skip; , } f[x := 0]) \\
 &= [x] \cdot wp(\text{diverge, } f[x := 0]) + [\neg x] \cdot wp(\text{skip, } f[x := 0]) \\
 &= 0 \cdot 0 + 1 \cdot f[x := 0] = f[x := 0]
 \end{aligned}$$

Therefore we can conclude that the moment of transformation is significant and not compositional, therefore:

$$wp(\widehat{P}; Q, f) \neq wp(\hat{P}; \hat{Q}, f)$$