Brief Analysis of Norovirus Data

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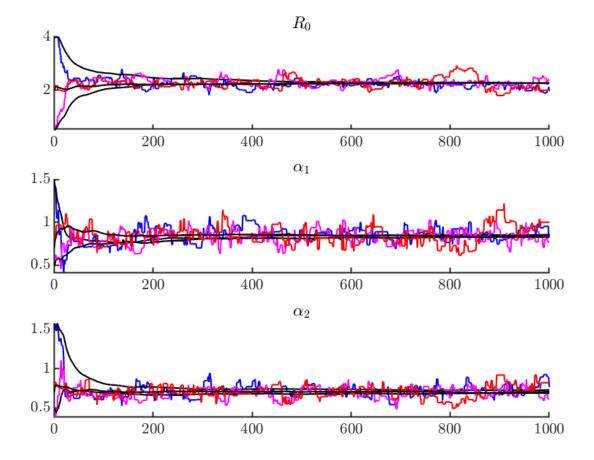


Figure 1: Caption here

Advise the government on effectiveness of interventions, and which should be implemented (if any).

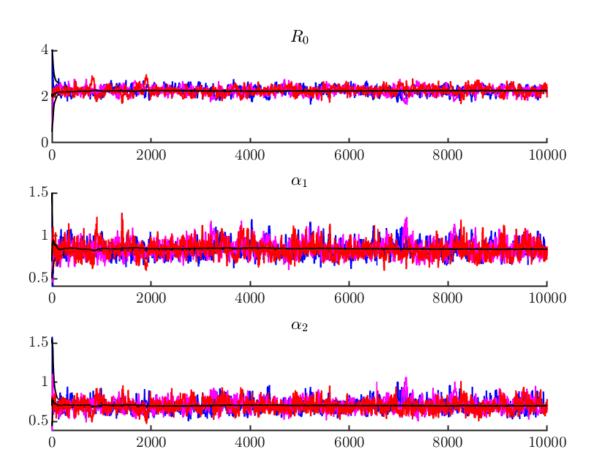


Figure 2: Caption here

.1 Code

.1.1 Main Script (R0Predict.m)

```
%Pretty plots
  set (groot, 'DefaultLineLineWidth', 1, ...
       'DefaultAxesLineWidth', 1, ...
       'DefaultAxesFontSize', 12, ...
       'DefaultTextFontSize', 12, ...
5
       , DefaultTextInterpreter, \\ , illex, \\ , \dots
6
       'DefaultLegendInterpreter', 'latex', ...
       'DefaultColorbarTickLabelInterpreter', 'latex', ...
       'DefaultAxesTickLabelInterpreter', 'latex');
9
10
11
12
  %Speeds up the code for multiple runs
13
      ~exist('dataMat', 'var')
14
       dataMat = readmatrix('NorovirusDataA3.txt');
15
       %print the first few rows
16
       dataMat (1:5,:)
17
  end
18
19
  %Observation of dataset
20
  Thow many of them correspond to the disease effectively dying out?
21
  amountOfData = length(dataMat(:,1))
  propDiedOut = sum(dataMat(:,2) <= 0.1*dataMat(:,1)) / amountOfData
  %dataMat = [#people, #infected, #action]
25
  %consistency
26
  \operatorname{rng}(1)
27
28
29
  %since we are expecting approximately 66%
  %getting the right prior
  %we want the dist to be N'(2.5, sigma)
  %where sigma is the variance to have approx 66\% in (2-3).
  \%\mathrm{N}' since we will drop values below 0 and above 5
  %N' will still be symmetric
  sigma = -(3-2.5)/norminv((1-0.66)/2);
37
  variance = sigma* speye(3);
38
39
  varR0 = 0.01;
40
  distStruct.ProposalDist = @(x) mvnrnd(x, diag([varR0, 0.01, 0.01]));
41
  distStruct.PriorPDF = @(x) normpdf(x, 2.5, sigma);
  distStruct.LogLikelihoodFunc =@(params, data) LogLikelihood(params, data);
  %constrain a<sub>-1</sub>, a<sub>-2</sub> in [0,2]
  distStruct. ProposalConstraints = @(vars) ProposalConstraints(vars, [0,0,0], [5
  %overshoot, undershoot and approximately close
```

```
startVars = [4, 1.5, 1.5;
47
                  0.5, 0.5, 0.5;
48
                  [2,0.7,0.7];
49
50
   vars = zeros(10000,3,3);
51
   for index = 1:3
52
       startPoint = startVars(index,:)
53
       exitflag = 1;
54
       while exitflag~=0
55
            [varsTemp, accrate, exitflag] = MetropolisHastingsPassLikelihood(distStr
56
            if exitflag == -1
57
                %acceptance was too low
58
                %variance is too high
                 varR0 = varR0 *2/3;
60
                 distStruct.ProposalDist = @(x) mvnrnd(x, diag([varR0, 0.01, 0.01]));
61
                 warning ('retrying with decreased variance')
62
            else if exitflag==1
63
                %acceptance was too high
64
                %variance is too low
65
                 varR0 = varR0*2;
66
                 distStruct.ProposalDist = @(x) mvnrnd(x, diag([varR0, 0.01, 0.01]));
67
                 warning ('retrying with decreased variance')
68
                 end
69
            end
70
            vars(:,:,index) = varsTemp;
71
       end
72
74
  end
75
  %%
76
   cumVars = cumsum(vars, 1)./(1:length(vars));
77
   tstr = ["\$R_0\$\$", "\$\alpha_1\$\$", "\$\alpha_2\$\$"];
   for burnin = 0:1
79
       figure
80
       for i=1:3
81
            hold on
82
            subplot (3,1,i)
83
            hold on
84
            plot (vars (:, i, 1), 'b')
            plot (cumVars (:, i, 1), 'k')
            plot (vars (:, i, 2), 'm')
            plot (cumVars (:, i, 2), 'k')
88
            plot (vars (:, i, 3), 'r')
89
            plot (cumVars (:, i, 3), 'k')
90
            title (tstr(i))
91
92
            if burnin
93
                 axis([0,1000,-inf,inf])
94
            end
95
       end
96
```

```
saveas (gcf, "MHplot"+num2str(burnin)+".eps", "epsc")
97
   end
98
        axis([0,1000,-inf,inf])
99
        xlabel ('Iteration')
100
101
   %%
102
103
   %Clean new data
104
   %just take one set since they all converged
105
   %and omit the burnin
106
   varsClean = vars(500:end,:,3);
107
108
   close all
109
   %density plot
110
   %and obtain estimates for R0, a1, a2
111
112
   labs = ["$$R_0$$","$$\alpha_1$$","$$\alpha_2$$"];
113
114
   est = [0, 0, 0];
115
   for i=1:3
116
        figure
117
        [prob, val] = ksdensity(varsClean(:,i));
118
        prob = prob./sum(prob);
119
        plot (val, prob)
120
        xlabel(labs(i))
121
        ylabel("Probability")
122
        title ("Probability density for "+labs(i))
123
        [ \tilde{\ }, ind ] = \max(prob);
124
        %assuming there is no dependence
125
        est(i) = val(ind);
126
        saveas(gcf," Probdensity"+num2str(i)," epsc")
127
   end
128
   est
129
   est(2:3) * est(1)
130
131
   for i=1:2
132
        for j=i+1:3
133
             figure
134
             binscatter (varsClean (:, i), varsClean (:, j), 60, 'Handle Visibility', 'off')
135
             hold on
136
             scatter(est(i),est(j),'xr')
137
             xlabel(labs(i))
138
             ylabel(labs(j))
139
             legend ("Independent approximation")
140
             colormap (gca, 'parula')
141
             saveas (gcf, "BinScatter"+num2str(i)+num2str(j), "epsc")
142
        end
143
   end
```

.1.2 MetropolisHastingsPassLikelihood.m

```
function [vars, accRate, exitflag] = MetropolisHastingsPassLikelihood(distStruct
  %Most generic MetropolisHastings
  %distStruct has fields
  \%-priorDist – the prior to pull from
  %—proposalDist — the proposed distribution
6
  numAccepted = 0;
  PriorPDF = distStruct.PriorPDF;
  ProposalDist = distStruct.ProposalDist;
  BreaksProposalConstraints = distStruct.ProposalConstraints;
  LogLikelihoodFunc = distStruct.LogLikelihoodFunc;
11
  vars = zeros (numIterations, length (startVars));
12
  vars(1,:) = startVars;
13
14
   for i=2:numIterations
15
      proposal = ProposalDist(vars(i-1,:));
16
     %if breaks constraints
17
      if BreaksProposalConstraints(proposal)
18
          vars(i) = vars(i-1);
19
      else
           candidateProbTop = LogLikelihoodFunc(proposal, data) + log(PriorPDF(
21
           candidateProbBottom = LogLikelihoodFunc(vars(i-1,:),data) + log(Prior
22
           candidateProb = candidateProbTop - candidateProbBottom;
23
           acceptProb = log(rand);
24
25
           if acceptProb< candidateProb
26
                vars(i,:) = proposal;
               numAccepted = numAccepted +1;
           else
29
                vars(i,:) = vars(i-1,:);
30
           end
31
      end
32
  end
33
  accRate = numAccepted/numIterations;
34
35
       accRate < 0.2
   i f
36
       warning ("Bad acceptance rate - too low, accRate = "+num2str(accRate));
37
       exitflag = -1;
38
   else if accRate > 0.27
39
       exitflag = 1;
40
       warning ("Bad acceptance rate - too high, accRate = "+num2str(accRate));
41
   else
42
       exitflag = 0;
43
       end
44
  end
45
46
47
  end
```

.1.3 LogLikelihood.m

```
function logLikelihood = LogLikelihood (params, data)
  %Amended SIR finalsize code from Josh
  %Amended by Andrew Martin
  %calculates log likelihood for a given R0, alpha1, alpha2
  logLikelihood = 0;
  % R0
             = params(1);
  % alpha1
             = params(2);
  % alpha2
             = params(3);
  NVec = data(:,1);
  \%[R0, a1R0, a2R0]
  paramsModified = [params(1), params(1)*params(2), params(1)*params(3)];
  %yay matlab uses 1 based indexing
  R0index = data(:,3)+1;
13
14
15
   for iterator=1:length(data)
16
       N = NVec(iterator);
17
       relevantParam = paramsModified(R0index(iterator));
18
       q = zeros(N+1,1);
19
       q(2) = 1;
20
       %Proportions for each number of infection events
21
       %could vectorise, but this is more meaningful
22
       for Z2 = 0:N
23
            for Z1 = Z2+1:N-1
24
                %infection probability (jump prob)
25
                \inf Prob = 1 / (1 + ((N-1)/(relevantParam*(N-Z1))));
26
                q(Z1+2) = q(Z1+2) + q(Z1+1)*infProb;
                q(Z1+1) = q(Z1+1)*(1-\inf Prob);
            end
29
       end
30
       %sum of the log likelihoods (product of likelihoods)
31
       \log \text{Likelihood} = \log \text{Likelihood} + \log (q(\text{data}(\text{iterator}, 2) + 1));
32
  end
33
34
35
  end
36
         ProposalConstraints.m
  .1.4
  function boolean = ProposalConstraints (vals, min, max)
  %
  %OUTPUT:
  %boolean - true if the boundary constraints are broken
  boolean = any(vals < min | vals > max);
6
  % %hardcoded way
  % boolean = \operatorname{vals}(1) < 0 \mid \mid \operatorname{vals}(1) > 5 \dots
```

| | vals(2) < min | | vals(2) > max

| | vals(3) < min | | vals(3) > max;

10

11 12 %

13 end

Assignment III

Worth 15% of course assessment; due by 3pm on Friday 7th June, 2019.

Most-relevant lectures: Lectures 21 - 26.

The total marks for this assignment is 45.

Please provide code where appropriate.

Report to the Government on the effectiveness of interventions. [45 marks]

The CSV file NorovirusDataA3 contains information regarding independent outbreaks in a set of 125 hospital wards of varying sizes. The first column contains the number of occupied beds in the ward, the second column contains the number of those patients which succumbed to norovirus during the outbreak, and the third column indicates the control action implemented; in the last column, 0 corresponds to standard practices, 1 corresponds to a trial intervention strategy, and 2 corresponds to different trial intervention strategy.

You are to analyse this data to advise the Government on the effectiveness of their interventions, and to advise them on which intervention should be adopted (if any).

You may assume that the interventions work to reduce the effective transmission rate parameter. The Chief Medical Officer has said that R_0 for norovirus in typical hospital settings is between 2 and 3 with (approximately) 66% probability; you may use this expert opinion as prior knowledge.

You are to prepare two reports. One is for the Government. The second is to provide detail on how you have performed the statistical analysis, including the model(s) used, any assumptions you have made and providing evidence that your approach/algorithms are working correctly, for example through the use of simulated data of similar form to the 'real' data (e.g., using trace plots from multiple independent chains, and kernel density estimators and box plots). This assignment is deliberately vague – you need to make decisions, but feel free to ask for feedback as you make progress.