

**make  
history.**



# Distribution sorts

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# Bucket sorts

- Setup empty buckets.
- Go over the original list and map the objects into the buckets.
- Sort each bucket.
- Visit the buckets in order and join the results in sequence.





# Counting sort (an example of Bucket sort)

- Counting sort:
  - Bucket size:  $m$  buckets.
  - $O(m+n)$ 
    - $m$  is the number of possible values (number of buckets).
    - $n$  is the size of array to be sorted.
  - Steps:
    - Count the number of each value  $I$  in the input array and store it in an array of size  $m$  called count:  $\text{count}[i]$  stores the number of times  $I$  appears in the input array.
    - Update count to hold a cumulative sum:  
 $\text{count}[i+1] = \text{count}[i+1] + \text{count}[i]$ .
    - Go through input array. Look at value and put value to  $\text{count}[\text{value}]$  index. Subtract 1 from  $\text{count}[\text{value}]$ .



# Example

Input array: 2, 5, 6, 6, 2, 3, 4, 10, 3, 6, 7, 8

Buckets: 1,..., 10

Count = [0, 2, 2, 1, 1, 3, 1, 1, 0, 1]

Cumulative sum = [0, 2, 4, 5, 6, 9, 10, 11, 11, 12]



# Example

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Count = [0, 2, 2, 1, 1, 3, 1, 1, 0, 1]

Cumulative sum = [0, 1, 4, 5, 5, 8, 10, 11, 11, 12]

1	2	3	4	5	6	7	8	9	10	11	12
	2				5			6			



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