

**make
history.**



Practical 4: Computational Complexity

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Find prefixes of s2 in s1

s1:

n elements

4	6	3	4	5	5	4	5	6	7
---	---	---	---	---	---	---	---	---	---

s2:

m elements

4	5	6	8	9
---	---	---	---	---

Prefixes of s2:

4

4 5

4 5 6

4 5 6 8

4 5 6 8 9



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Output (indexes in s1):

0

Find prefixes of s2 in s1

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n elements

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Prefixes of s2:

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4 5
4 5 6
4 5 6 8
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Output (indexes in s1):

0
3

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n elements

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Prefixes of s2:

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4 5 6 8 9

Output (indexes in s1):

0
3
6

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n elements

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---	---	---	---	---	---	---	---	---	---

s2:

m elements

4	5	6	8	9
---	---	---	---	---

Prefixes of s2:

4
4 5
4 5 6
4 5 6 8
4 5 6 8 9

Output (indexes in s1):

0
3
6
-1
-1

Algorithm

```
vector<int> result;
```

$O(m)$ iterations

```
for(size_t i = 1; i <= s2.size(); i++) {
```

$O(i*n)$ the cost of searching prefix of length i in n

```
size_t found = s1.find(s2.substr(0, i));
```

```
if (found != string::npos) {
```

```
    result.push_back(found);
```

```
} else {
```

```
    result.push_back(-1);
```

```
}
```

```
}
```

Overall complexity: $O(n+2n+3n+\dots+i*n+\dots+m*n) = O(m^2n)$

```
return result;
```



Algorithm

Can the algorithm be optimized?

1. Find operations that are performed several times.
2. Try to avoid them. Hint: `s1.find(s2, index)` can find substrings starting from index.
3. If prefix was not found (-1 as an output), the larger prefix will not be found either.
4. What will be the time complexity of the optimized algorithm?



Practical 4

1. Update function :

```
vector<int> Finder::findSubstrings(string s1, string s2)
```

2. Submit Finder.h and Finder.cpp to Practical 4 in Gradescope.

