

# **CS915/435 Advanced Computer Security**

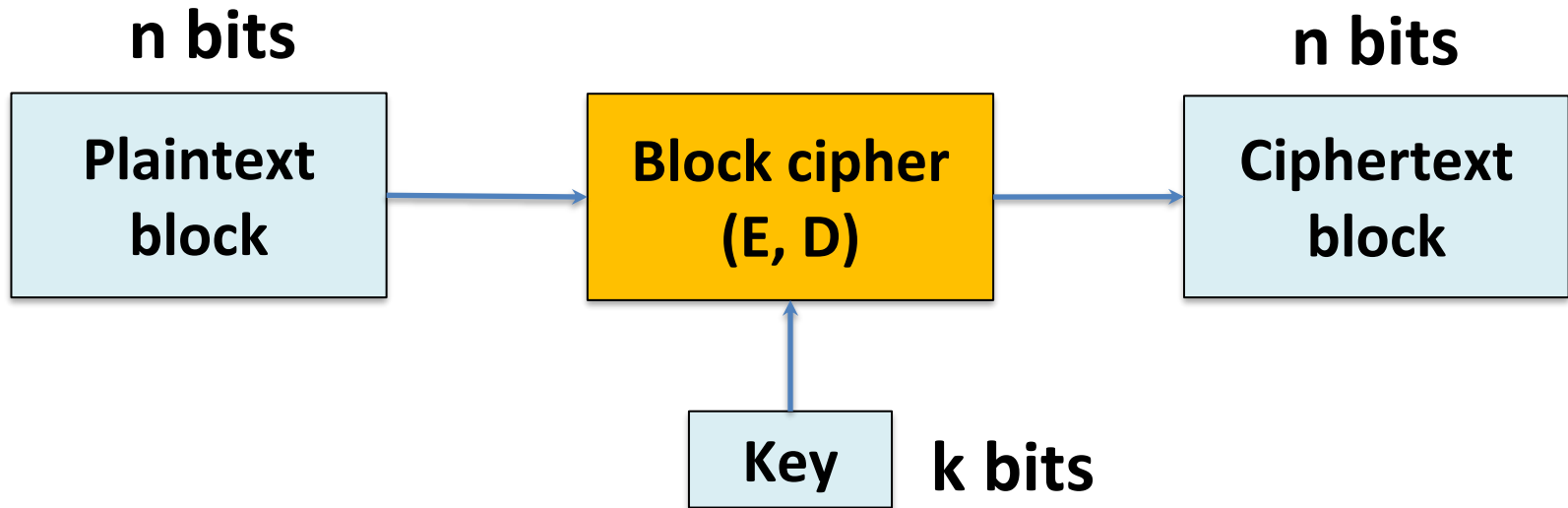
## **- Elementary Cryptography**

Block Cipher I

# Roadmap

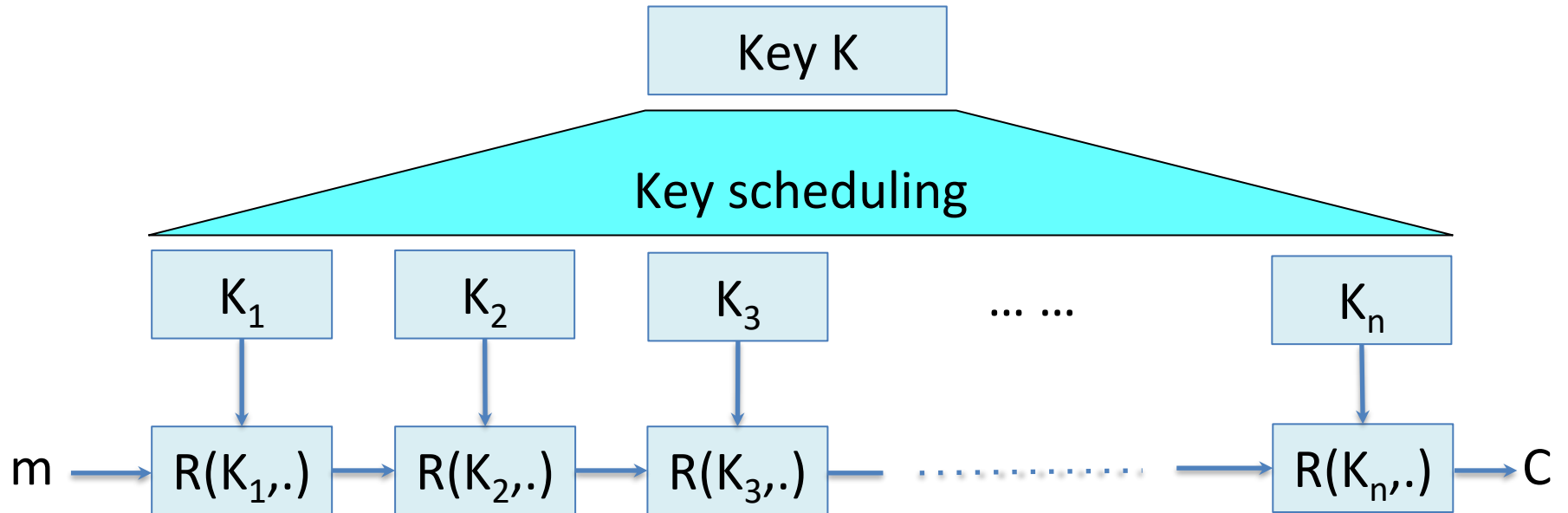
- Symmetric cryptography
  - Classical cryptographic
  - Stream cipher
  - **Block cipher I, II**
  - Hash
  - MAC
- Asymmetric cryptography
  - Key agreement
  - Public key encryption
  - Digital signature

# Block cipher: overview



- Canonical examples:
  - DES:  $n=64$  bits  $k=56$  bits
  - 3DES:  $n=64$  bits  $k=168$  bits
  - AES:  $n=128$  bits  $k=128, 192, 256$  bits

# Iterated construction



- $R(K, .)$  is called a round function
- DES 16 rounds, 3DES 48 round, AES-128 10 rounds

# Performance

- AMD Opteron, 2,2 GHz, Linux, Crypto++ 5.6.0 (Wei Dai)

|        | <u>Cipher</u> | <u>Block/key size</u> | <u>Speed (MB/sec)</u> |
|--------|---------------|-----------------------|-----------------------|
| stream | RC4           |                       | 126                   |
|        | Salsa20/12    |                       | 643                   |
|        | Sosemanuk     |                       | 727                   |
| block  | 3DES          | 64/168                | 13                    |
|        | AES-128       | 128/128               | 109                   |

# Abstractly: PRF and PRP

- Pseudo Random Function (PRF) defined over  $(K, X, Y)$

$$F: K \times X \rightarrow Y$$

Such that:

1. Exists “efficient” algorithm to evaluate  $F(k, x)$

- Pseudo Random Permutation (PRP) defined over  $(K, X)$

$$E: K \times X \rightarrow X$$

Such that:

1. Exists “efficient” deterministic algorithm to evaluate  $E(k, x)$
2. The function  $E(k, \cdot)$  is one-to-one
3. Exists “efficient” inversion algorithm  $D(k, \cdot)$

# Running example

- Example PRPs: 3DES, AES, ...

AES:  $K \times X \rightarrow X$  where  $K = X = \{0,1\}^{128}$

3DES:  $K \times X \rightarrow X$  where  $X = \{0,1\}^{64}$ ,  $K = \{0,1\}^{168}$

- A PRP is a PRF where

1)  $X = Y$

2) It is invertible

# Data Encryption Standard

- Early 1970s: Horst Feistel designed Lucifer at IBM
- 1973: NBS asked for block cipher proposals
  - IBM submitted a variant of Lucifer (128-bit key and 128-bit block size)
- 1977: NBS adopted DES as a federal standard
  - But reduced key to 56 bits and block size to 64 bits
- 1997: DES broken by exhaustive search
  - 56-bit key is too small
- 2000: NIST adopted AES to replace DES



# Historical importance of DES (I)

- Before 1970s, crypto was a *forbidden* science
  - Almost no research papers published
  - National Security Agency had considerable knowledge crypto, but they didn't admit existence
  - But financial transactions must be protected
  - A secure encryption standard was badly needed.

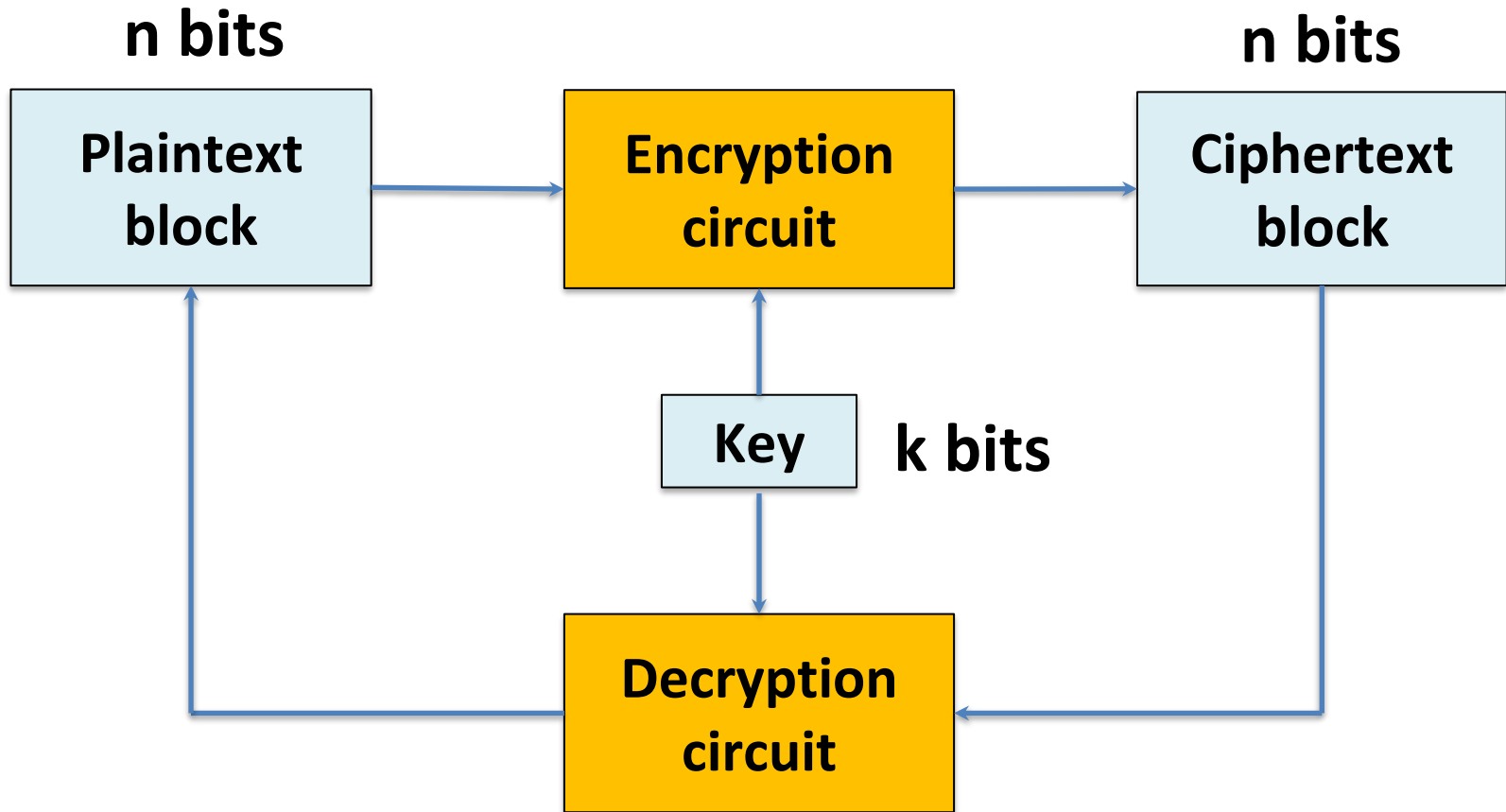
# Historical importance of DES (II)

- In 1972, National Bureau of Standards (NBS) initiated to develop a standard cipher
  - Must provide a high level of security
  - Must be completely specified and easy to understand
  - The security must reside in the key not the algorithm
  - Must be available to all users.
  - Must be adaptable for use in diverse applications
  - Must be economically implementable in electronic devices
  - Must be efficient to use
  - Must be able to be validated
  - Must be exportable
- Public interest was high, but public expertise was lacking
- None of the submissions came close to the requirements

# Historical importance of DES (III)

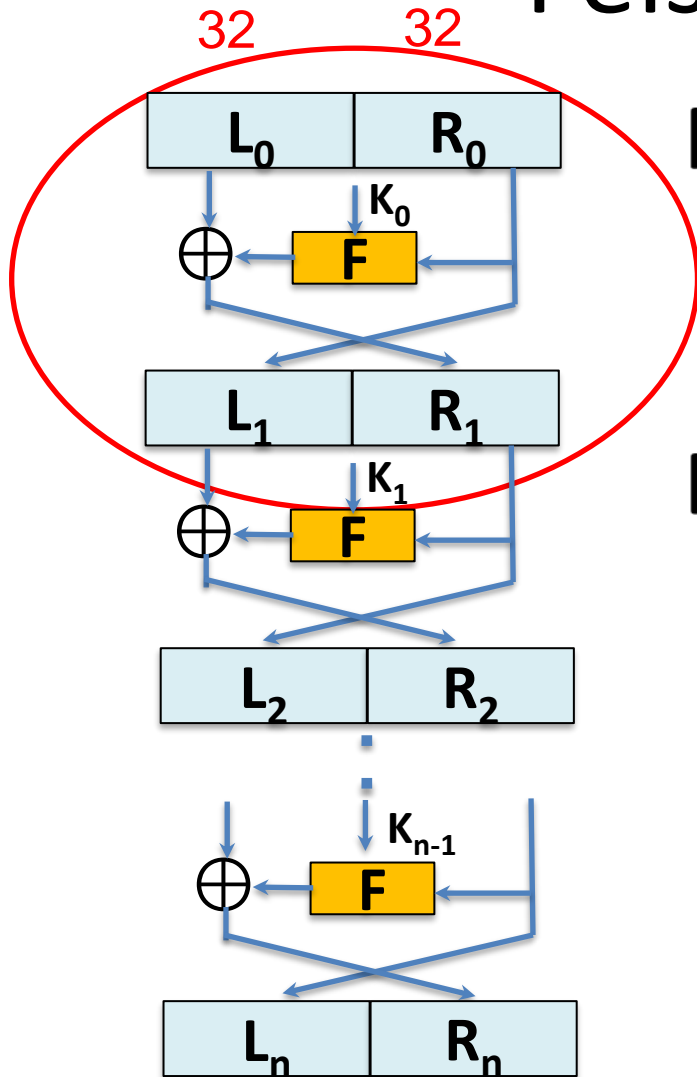
- In 1974, NBS issued a second request
  - IBM submitted Lucifer
- NBS requested NSA to help evaluation
  - NSA reduced the key size from 128 to 56 bits
  - But this received widespread criticisms
- 1976, the modified Lucifer adopted as standard
- After 1976, public research on crypto became unstoppable
- “DES did more to galvanize the field of cryptanalysis than anything else.” (Bruce Schneier)

# A challenge in efficiency



Can we use the same circuit for both Enc/Dec?

# Feistel Network



For  $i = 0, 1, \dots, n-1$

$$L_{i+1} = R_i$$

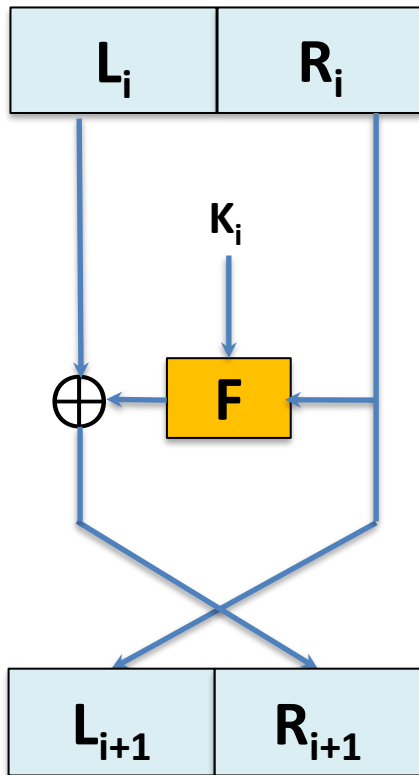
$$R_{i+1} = L_i \oplus F(K_i, R_i)$$

End

$$L_1 = R_0$$

$$R_1 = L_0 \text{ XOR } F(K_0, R_0)$$

# Invertible design

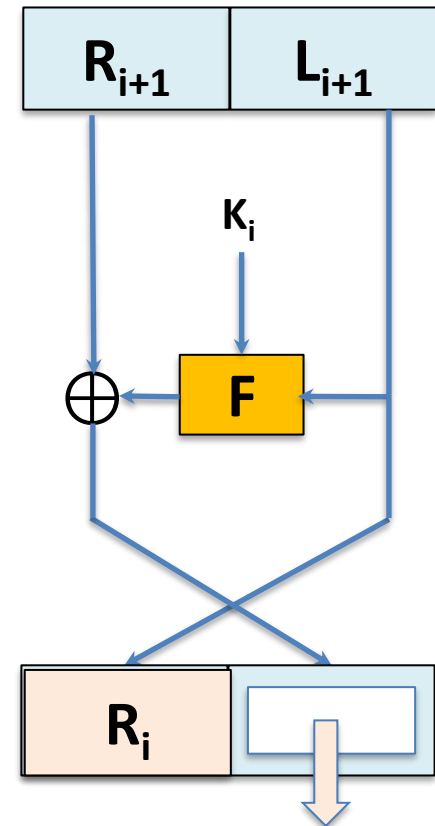


$$\begin{aligned} L_{i+1} &= R_i \\ R_{i+1} &= L_i \oplus F(K_i, R_i) \end{aligned}$$



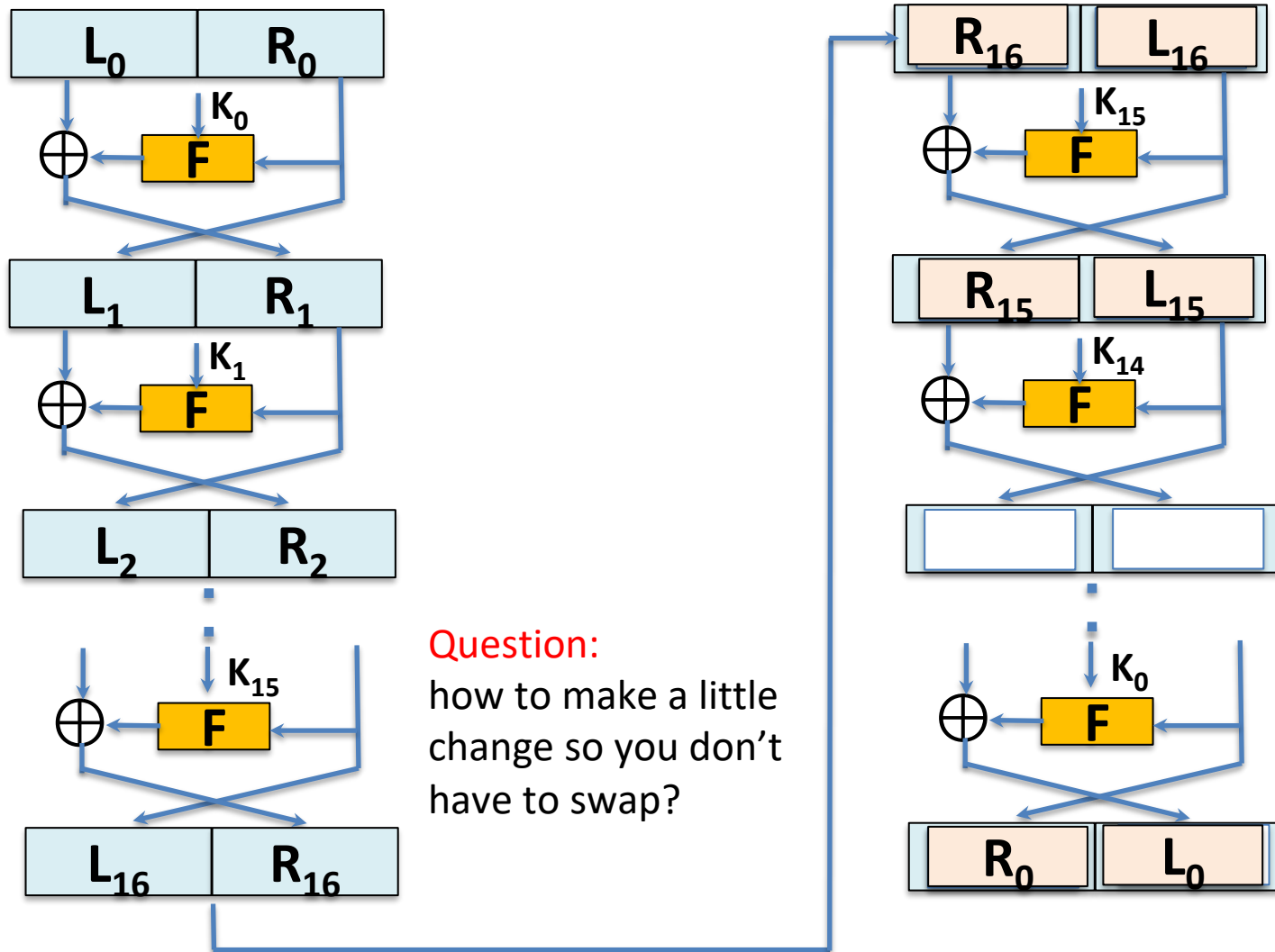
Inverse

$$\begin{aligned} R_i &= L_{i+1} \\ L_i &= \end{aligned}$$

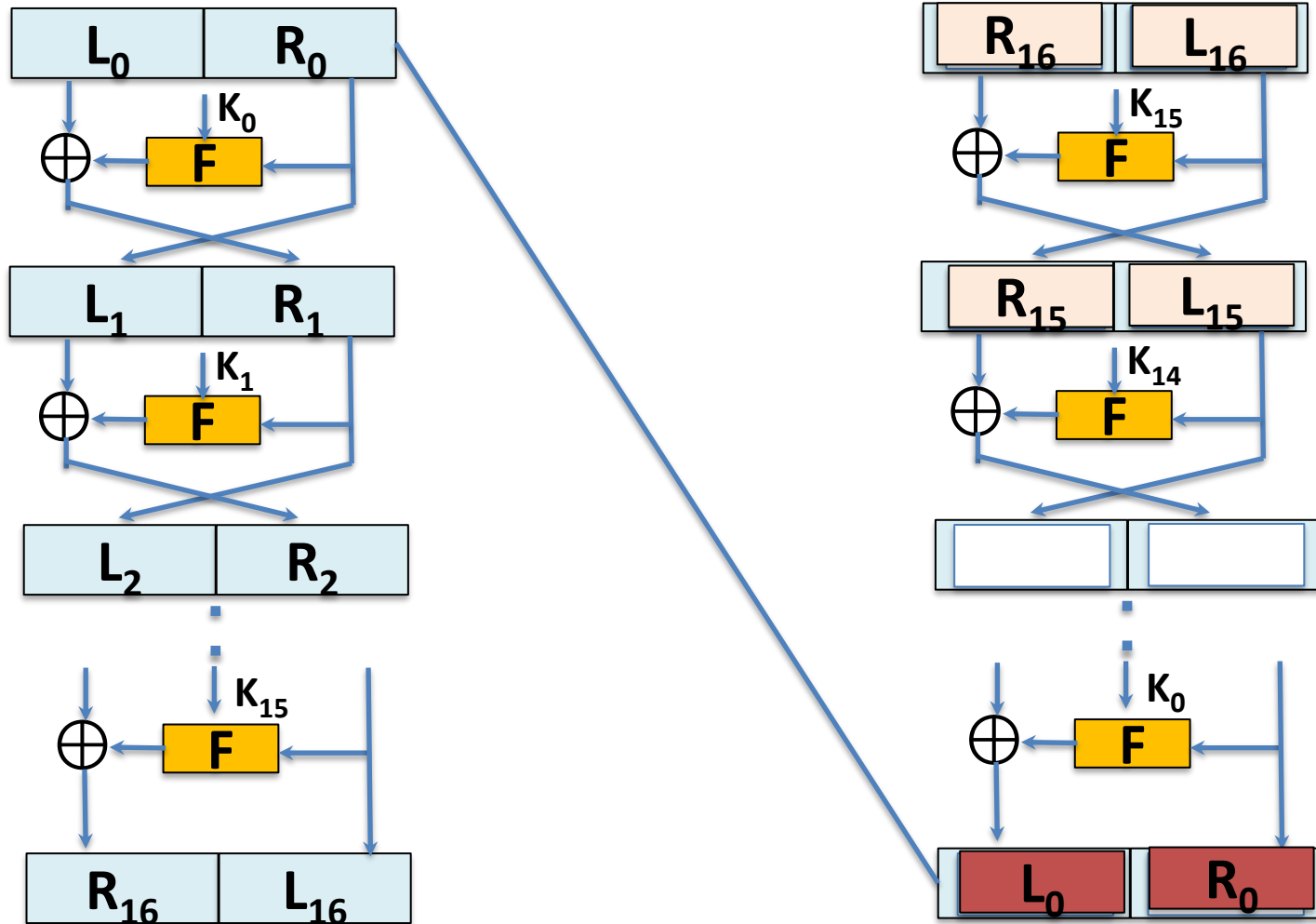


$$L_i = R_{i+1} \text{ XOR } F(K_i, L_{i+1})$$

# DES Decryption

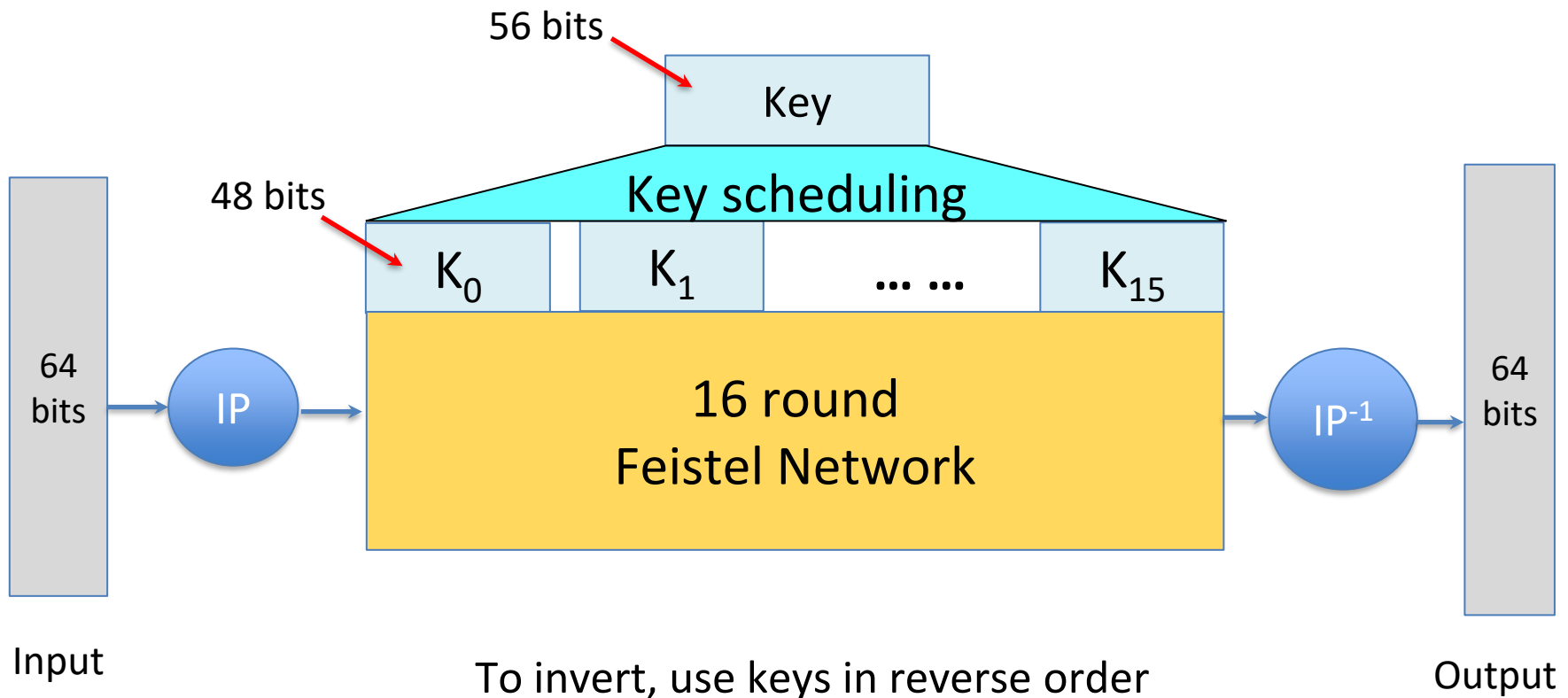


# DES Decryption

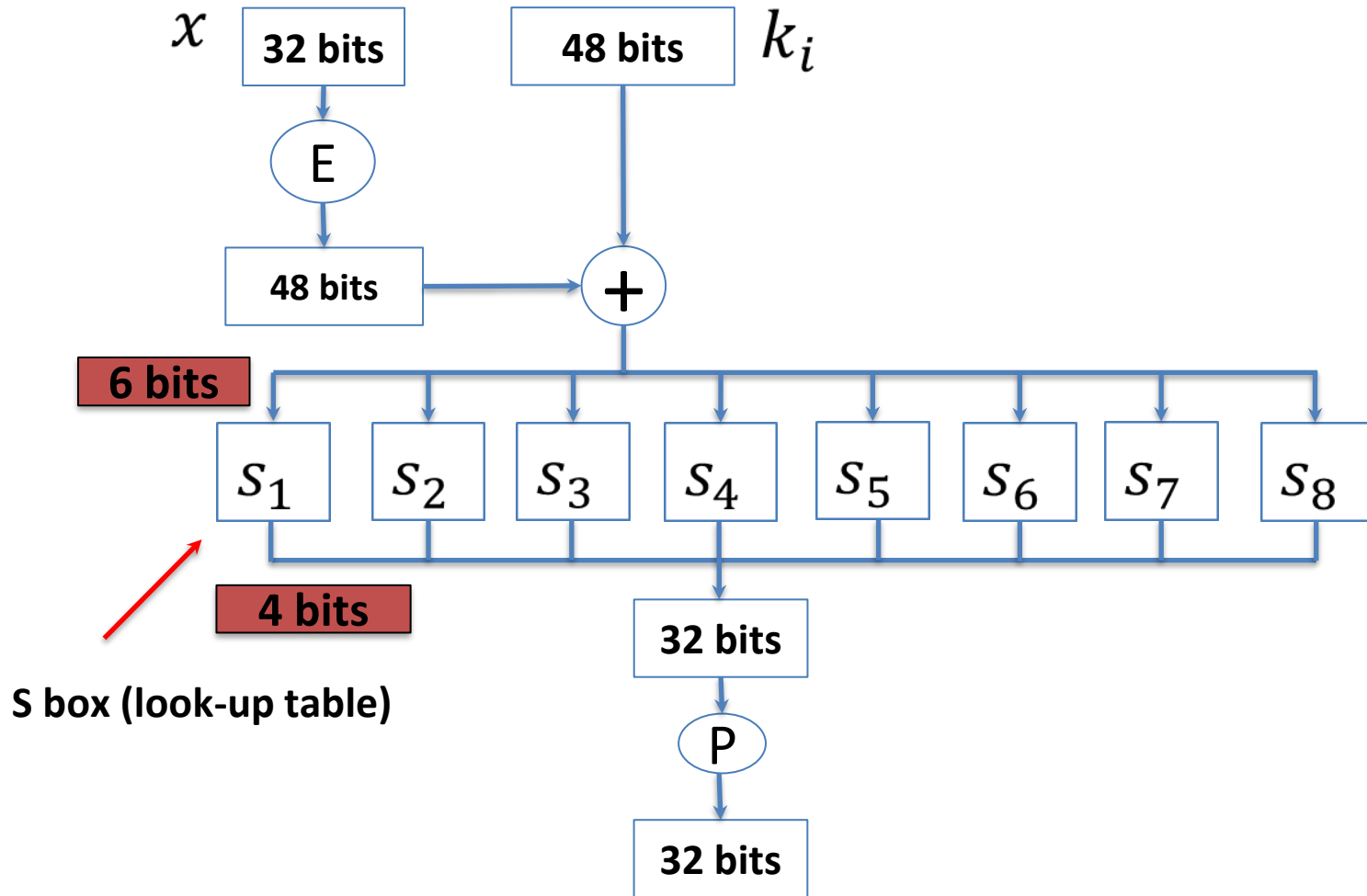




# DES: 16 round Feistel network



# The F function: $F(k_i, x)$



# The S-boxes

- $$S_i: \{0,1\}^6 \rightarrow \{0,1\}^4$$

|            | Middle 4 bits of input |    |    |    |    |    |    |    |    |    |    |    |    |   |    |    |
|------------|------------------------|----|----|----|----|----|----|----|----|----|----|----|----|---|----|----|
| Outer bits | 2                      | 12 | 4  | 1  | 7  | 10 | 11 | 6  | 8  | 5  | 3  | 15 | 13 | 0 | 14 | 9  |
|            | 14                     | 11 | 2  | 12 | 4  | 7  | 13 | 1  | 5  | 0  | 15 | 10 | 3  | 9 | 8  | 6  |
|            | 4                      | 2  | 1  | 11 | 10 | 13 | 7  | 8  | 15 | 9  | 12 | 5  | 6  | 3 | 0  | 14 |
|            | 11                     | 8  | 12 | 7  | 1  | 14 | 2  | 13 | 6  | 15 | 0  | 9  | 10 | 4 | 5  | 3  |

For example:

- Input = 011011      Outer bits: 01      Middle bits: 1101
- Output = 1001

# The P-boxes

- $P: \{0,1\}^{32} \rightarrow \{0,1\}^{32}$

|    |    |    |    |
|----|----|----|----|
| 16 | 7  | 20 | 21 |
| 29 | 12 | 28 | 17 |
| 1  | 15 | 23 | 26 |
| 5  | 18 | 31 | 10 |
| 2  | 8  | 24 | 14 |
| 32 | 27 | 3  | 9  |
| 19 | 13 | 30 | 6  |
| 22 | 11 | 4  | 25 |

Suppose  $C = (c_1, c_2, c_3, c_4, c_5, \dots, c_{31}, c_{32})$

Then  $P(C) = (c_{16}, c_7, c_{20}, c_{21}, c_{29}, \dots, c_4, c_{25})$


# Choosing the S-boxes and P-box

- S-boxes and P-box must be a careful choice
- Choosing at random would result in an insecure block cipher
- Several rules used in choice of S and P boxes
  - No output bit should be close to a linear function of the inputs bits
  - S-boxes are 4-to-1 mapping

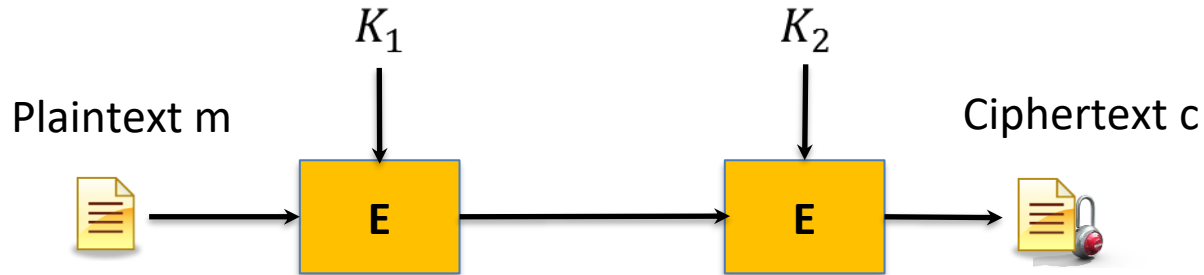
# Brute-force attack on DES

- DES challenge by RSA company
  - Given plaintext/ciphertext pairs, find the key
- 1997:
  - Internet search, 96 days
- 1998
  - DES search machine (EFF), 56 hours
  - Cost: US\$250K
  - The prize: US\$10K
- 1999
  - Combined internet search and DES machine: **22 hours**
- Conclusion: 56-bit is too weak (128-bit key is the standard)

  
1 sec

  
 $2^{(128-56)/3600/24/365} = 100 \text{ millions millions years}$

# Strengthen DES by double encryption

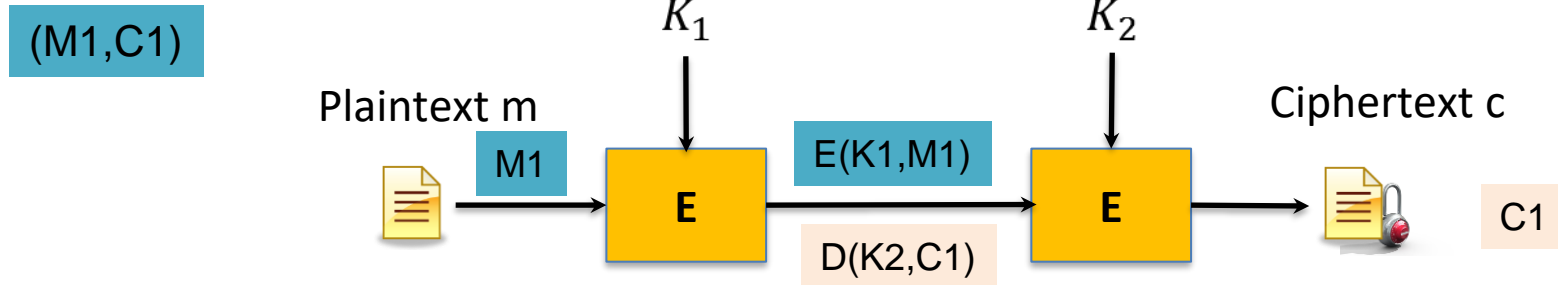


- Use double key 112-bits and encrypt twice

$$c = E(k_2, E(k_1, m))$$

Is this secure?

# Breaking double encryptions



**Meet in the middle attack:** knowing a few  $(m, c)$  pairs

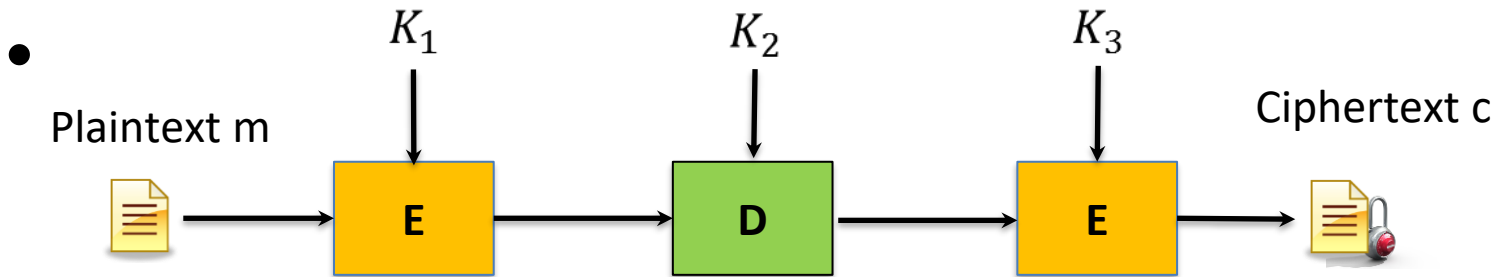
| $k_1$ (56 bits) | $E(k_1, m_1)$ | $D(k_2, c_1)$ | $k_2$ (56 bits) |
|-----------------|---------------|---------------|-----------------|
| 00...000        | ... ..        | ... ..        | 00...000        |
| 00...001        | ...           | ... ..        | 00...001        |
| ... ..          | ... ..        | ...           | ... ..          |
| 11...111        | ... ..        | ... ..        | 11...111        |

A red double-headed arrow connects the circled cell in the first table (00...001) to the circled cell in the second table (the row corresponding to 00...001).

Time:  $2^{56} \times 2 = 2^{57}$  encryptions, Space:  $2^{56} \times 2 \times 15$  bytes



# A more secure combination: Triple DES



- Variants

- $k_1 \neq k_2 \neq k_3$ : key size 168 bits, security 112 bits
- $k_1 = k_3$ : key size 112 bits, security 80 bits
- $k_1 = k_2 = k_3$ : key size 56 bits, security 56 bits