

# **CS915/435 Advanced Computer Security**

## **- Emerging topics**

BitCoin and Blockchain

# Overview

- Bitcoin address
- Bitcoin transactions
- Locking and unlocking script
- Blocks and Bitcoin mining
- Blockchain

# History

- Research on digital currency dates back to early 80's.
- 1983, David Chaum proposed e-cash using blind signatures. He set up a company called DigitCash (later went bankrupt)
- 1997, Adam Back proposed proof-of-work called Hashcash to limit email spam
- 1998, Wei Dai proposed b-money: proof-of-work, broadcasting, signing, decentralized ledger, incentivisation of mining
- 1998, Nick Szabo proposed Bit Gold, commonly seen as precursor to BitCoin. But Bit Gold has a **double-spending** problem.
- 31 October 2008, Satoshi Nakamoto proposed BitCoin.
- 3 Jan, 2009, Bitcoin network came to existence. BitCoin was born!



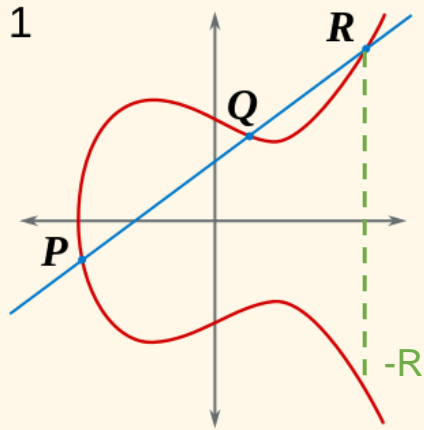
For latest price, see <https://coinmarketcap.com/currencies/bitcoin/>

# Background on Elliptic Curve Cryptography

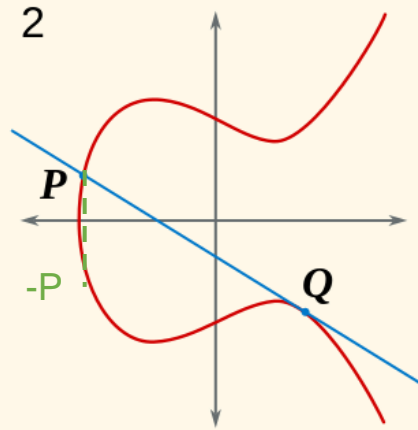
$$y^2 = x^3 + ax + b$$

FF:  $X = g^x \bmod p$

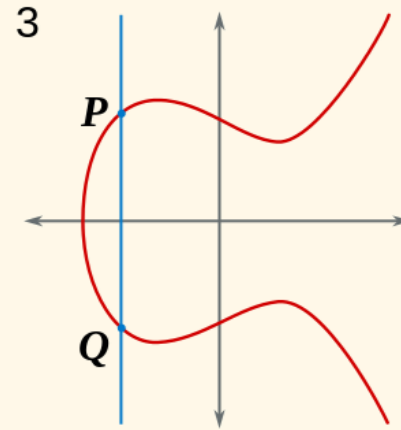
ECC:  $X = x.G$



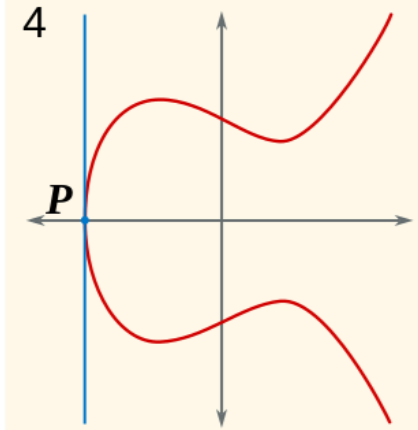
$$P + Q + R = 0$$



$$P + Q + Q = 0$$



$$P + Q + 0 = 0$$



$$P + P + 0 = 0$$

# Bitcoin uses Elliptic Curve Cryptography

Bitcoin uses a NIST curve secp256k1

$$y^2 = x^3 + 7$$

## Generating Public and Private Keys

```
Private-Key: (256 bit)
priv:
  01:68:d2:65:bf:f8:66:88:e0:b0:64:d5:76:cc:7d:
  51:ae:1d:5b:62:64:fd:2e:1e:24:ec:53:eb:5d:9d:
  0c:20
pub:
  04:73:e3:c6:ce:48:da:81:fd:c1:04:86:74:83:4f:
  06:27:85:88:c4:af:59:7b:bf:bc:a6:ef:5a:57:52:
  07:16:bc:b7:15:f8:a4:f5:16:f0:a7:20:2a:1a:59:
  e4:8b:0d:41:f7:ab:ae:ba:86:3c:37:4a:79:7c:02:
  75:3b:34:27:d7
ASN1 OID: secp256k1
```

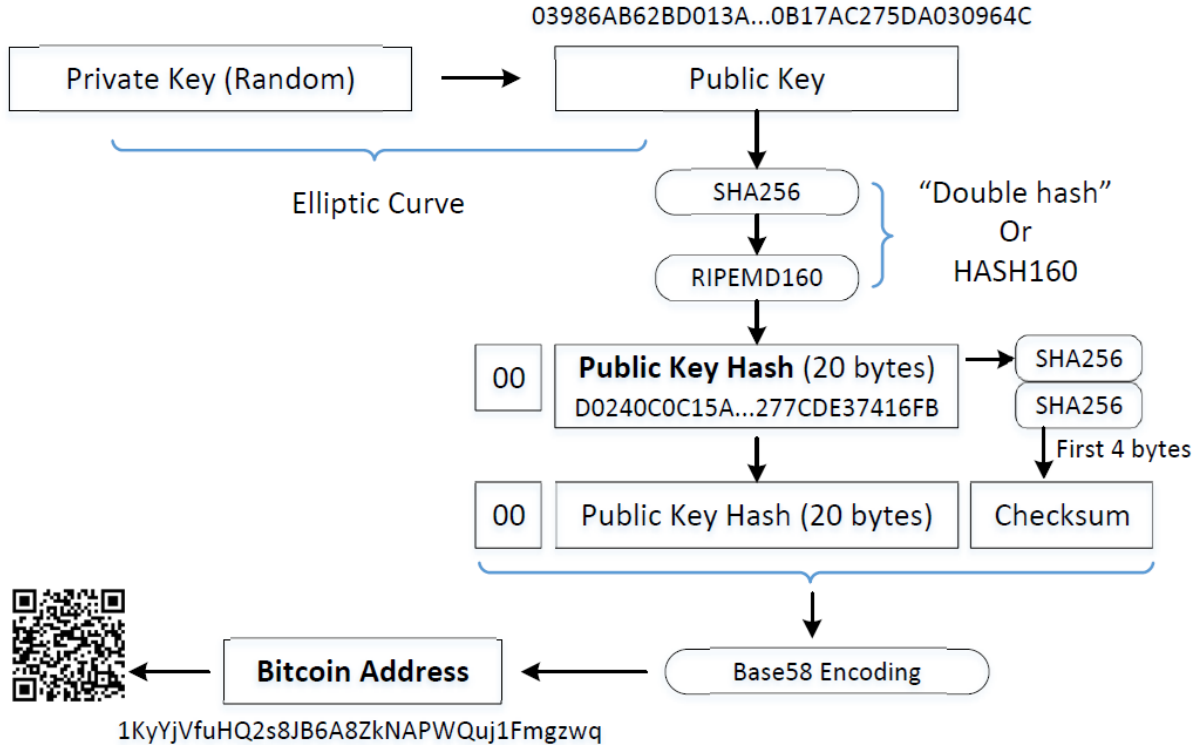
## Compressing Public Key

```
pub:
  03:73:e3:c6:ce:48:da:81:fd:c1:04:86:74:83:4f:
  06:27:85:88:c4:af:59:7b:bf:bc:a6:ef:5a:57:52:
  07:16:bc
ASN1 OID: secp256k1
```

## Generating Public-Key Hash

```
$ echo 0373e3c6c...5a57520716bc | xxd -r -p \
    | openssl dgst -sha256 -binary \
    | openssl dgst -ripemd160
(stdin)= 9390b28a0280cde7eac94e410a74f652aed6e937
```

# Turning Public-Key Hash into Bitcoin Address



# Base58 Encoding

Integer	Division	Quotient	Remainder	Base58 Symbol
2,864,386,338	div 58	49,385,971	20	M
49,385,971	div 58	851,482	15	G
851,482	div 58	14,680	42	j
14,680	div 58	253	6	7
253	div 58	4	21	N
4	div 58	0	4	5

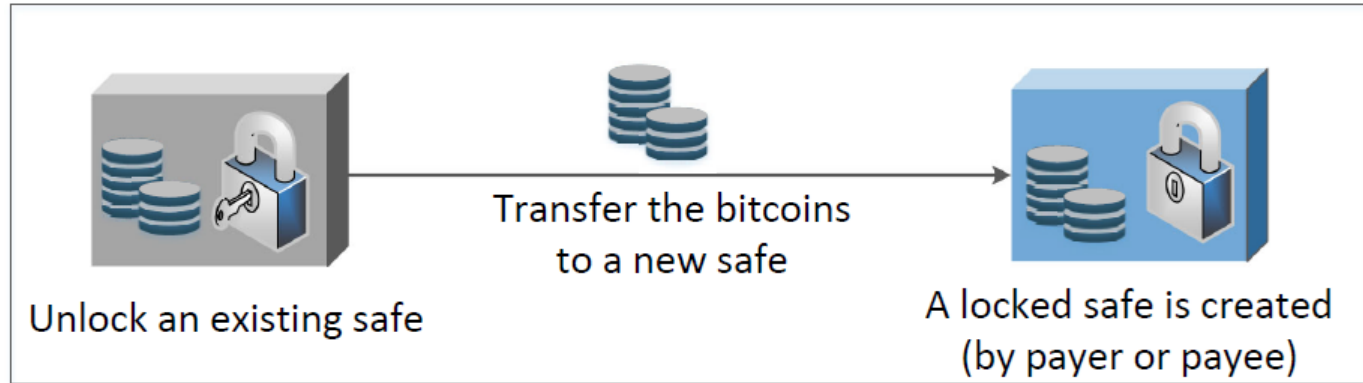
Final Base58 encoding: **5N7jGM**

```
$ echo aabb1122 | xxd -r -p | python base58.py && echo
5N7jGM
$ echo 009390b28a0280cde7eac94e410a74f652aed6e937b2b07b3f \
    | xxd -r -p | python base58.py && echo
1ETffxDNaF8rWsuorMKhdHruxSuT9BDUGE
```

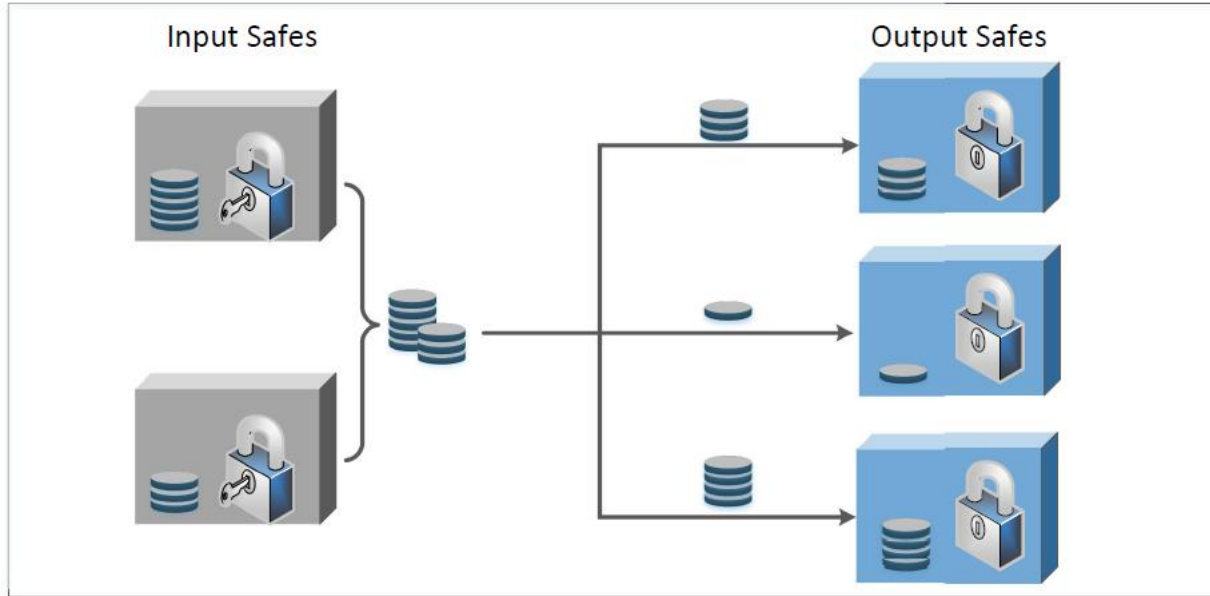




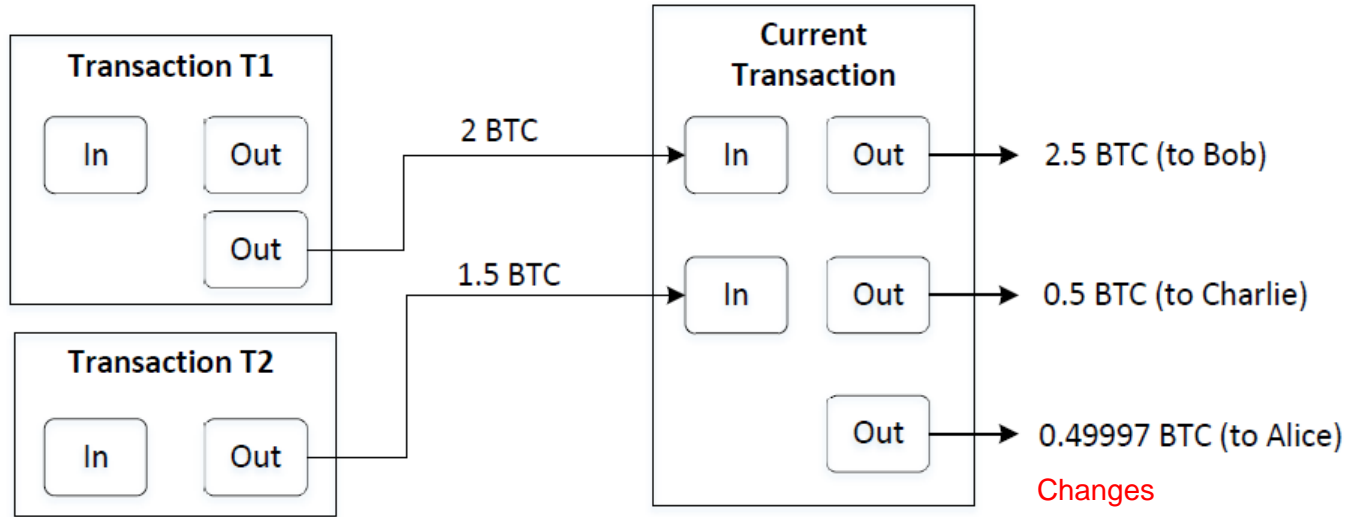
# Transactions: Intuition



# Components of Transactions & Examples



# An Example



**Transaction fee** =  $(2 + 1.5) - (2.5 + 0.5 + 0.49997) = 0.00003 \text{ BTC}$

# Input

The input to the current transaction specifies the source of the money

Input 0:

Transaction ID: T1

Output Index: 1

ScriptSig (Unlocking Script): ... omitted ...

Input 1:

Transaction ID: T2

Output Index: 0

ScriptSig (Unlocking Script): ... omitted ...

# Output

The output of a transaction specifies where the money goes.

Output 0:

Value: 2.5 BTC

ScriptPubKey: (a lock that can only be unlocked by Bob)

Output 1:

Value: 0.5 BTC


ScriptPubKey: (a lock that can only be unlocked by Charlie)]

Output 2:

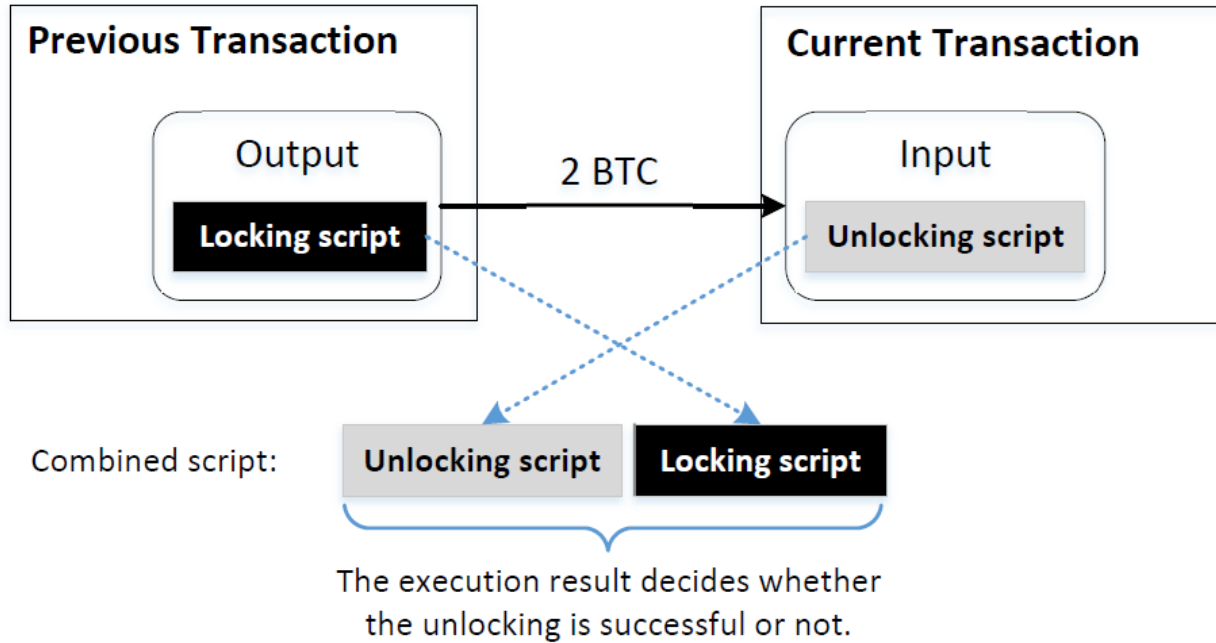
Value: 0.49997 BTC

ScriptPubKey: (a lock that can only be unlocked by Alice)

Alice pays  
herself (change)



# Locking and Unlocking Script



# Unlocking the output of a transaction

- Two types of locking scripts
  - Pay-to-Pubkey-Hash
  - Pay-to-Script-Hash
- Locking/unlocking is done by script
- In BitCoin, script is a basic programming language: no loops (not Turing-complete).

# Script Examples

```
scriptPubKey: OP_RETURN  
scriptSig: ... (does not matter)
```

```
Combined script: ... (does not matter) ... OP_RETURN
```


No one can spend



```
scriptPubKey: OP_ADD <100> OP_EQUAL  
scriptSig:    <5> <95>
```

```
Combined script: <5> <95> OP_ADD <100> OP_EQUAL
```


Any one who can find  
two numbers that add  
to 100 can unlock



```
scriptPubKey: OP_SHA256 <6fe2...3ffe> OP_EQUAL  
scriptSig:    <f343...f0f5>
```

```
Combined script:  
    <f343...f0f5> OP_SHA256 <6fe2...3ffe> OP_EQUAL
```

Anyone who can find  
preimage of a hash can  
unlock

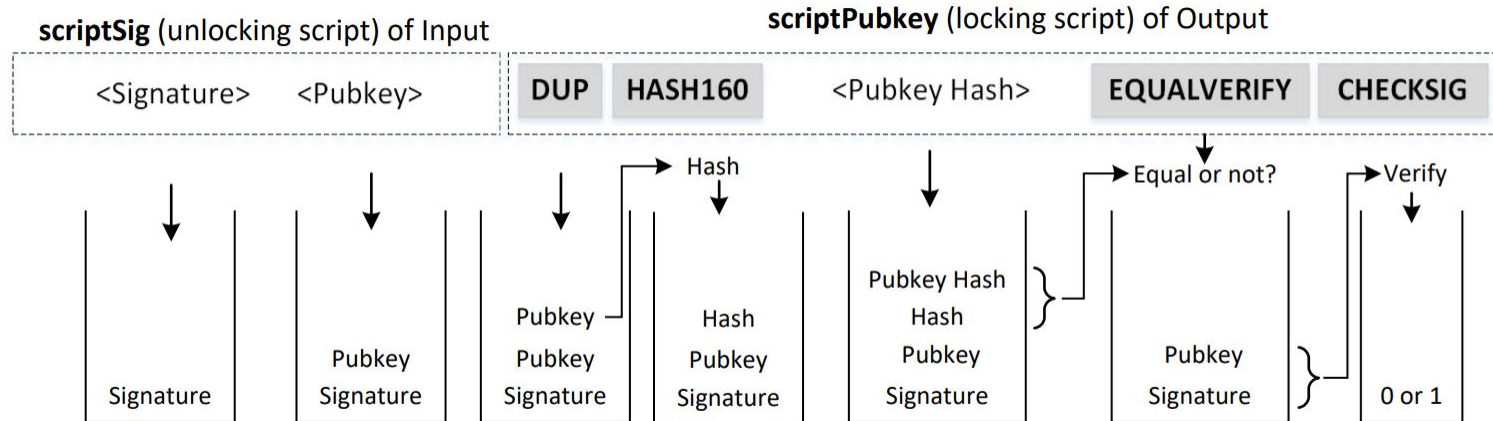




# Pay-to-PubKey-Hash (P2PH)

```
scriptPubKey: OP_DUP OP_HASH160 <Public KeyHash> OP_EQUAL OP_CHECKSIG  
scriptSig:    <Signature> <Public Key>
```

```
Combined script: <Signature> <Public Key> OP_DUP OP_HASH160  
                  <Public KeyHash> OP_EQUAL OP_CHECKSIG
```



# Pay-to-MultiSig (P2MS)

```
scriptPubKey: <2> <PubKey 1> <PubKey 2> <PubKey 3> <3>  
              OP_CHECKMULTISIG  
scriptSig: <Signature 1> <Signature 2>  
  
Combined script:  
  <Signature 1> <Signature 2>  
  <2> <PubKey 1> <PubKey 2> <PubKey 3> <3> OP_CHECKMULTISIG
```

- As long as two out of three approve (with a digital signature), they can spend the money.
- However, it's being replaced by P2SH

# Pay-to-Script-Hash (P2SH)

scriptPubKey: OP\_HASH160 <Script Hash> OP\_EQUAL

scriptSig: <Unlocking Script> <Serialized Redeem Script>

Redeem Script:

<Pubkey>

CHECKSIG

Unlocking Script (scriptSig)

<Signature>

<Serialized redeem script>

Locking Script (scriptPubKey)

HASH160

<Script Hash>

EQUAL

Deserialization



<Serialized redeem script>

HASH160

<Script Hash>

EQUAL

Standard execution

Redeem script execution

<Signature>

<Pubkey>

CHECKSIG

Essentially, this does the same as Pay-to-PubKey-Hash

# Use P2SH for MultiSig

## Pay-to-MultiSig (P2MS)

```
scriptPubKey: <2> <PubKey 1> <PubKey 2> <PubKey 3> <3>  
              OP_CHECKMULTISIG  
scriptSig: <Signature 1> <Signature 2>  
  
Combined script:  
  <Signature 1> <Signature 2>  
  <2> <PubKey 1> <PubKey 2> <PubKey 3> <3> OP_CHECKMULTISIG
```

## Pay-to-Script-Hash (P2SH)

```
Redeem Script:  
  <2> <PubKey 1> <PubKey 2> <PubKey 3> <3> OP_CHECKMULTISIG  
  
scriptPubKey: OP_HASH160 <Hash of Redeem Script> OP_EQUAL  
scriptSig:    <Sig 1> <Sig 2> <Serialized Redeem Script>
```

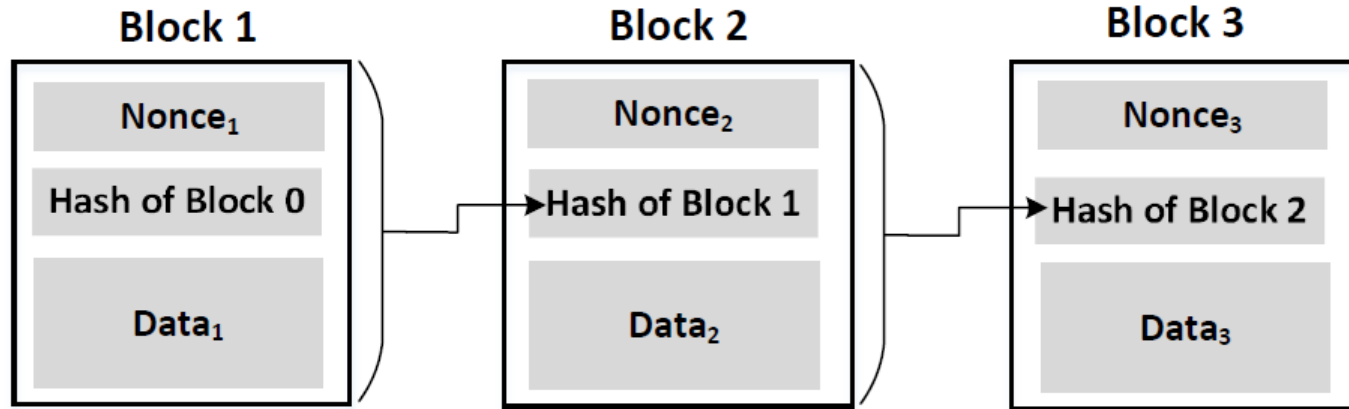
In P2SH, the receiver needs to include the original redeem script. Bigger size -> higher transaction fee. Hence, P2SH moves the cost to the receiver of the payment.

# Sending Transaction

- After a node has generated a transaction, it sends the transaction to its peers
- Each peer will verify the transaction, and then forward it to their peers
- Eventually, every node on the network will receive the transaction
- Some special node called miner will be responsible for adding the transaction to the public ledger (i.e., blockchain).

# Generating Blocks

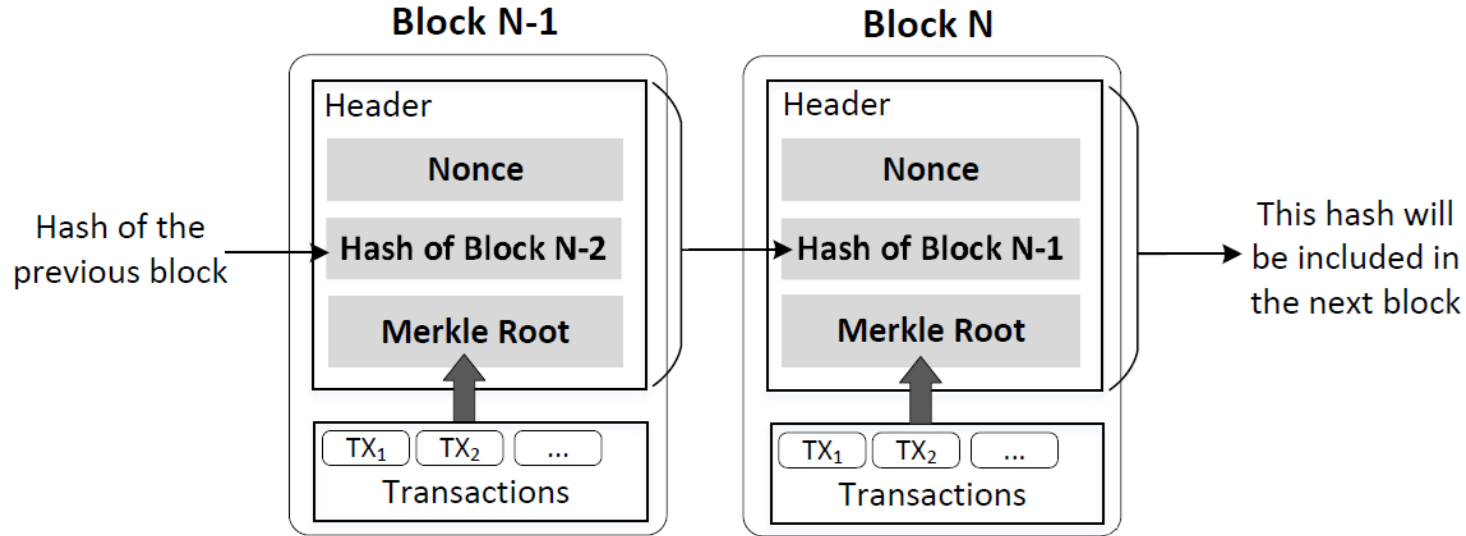
- Miners group transactions into a new block
- The new block is appended to the existing blockchain
- Check [cryptocurrency transactions](#) (mining, validation).



# Mining

- **Proof-of-Work:** find a nonce, s.t. when the hash of the block satisfies a special requirement, such as having 20 leading zeros
- **Rewarding:**
  - Coinbase transaction: new bitcoins are minted and given to the miner (50 BTC in 2008; halved every 210K blocks. Now 6.25 BTC)
  - Transaction fees
- Once a miner has found a block, it immediately sends the block to its peers, who will verify the block and then forward the block to their peers.
- Eventually, all the nodes will see this new block, and add it to their ledgers.

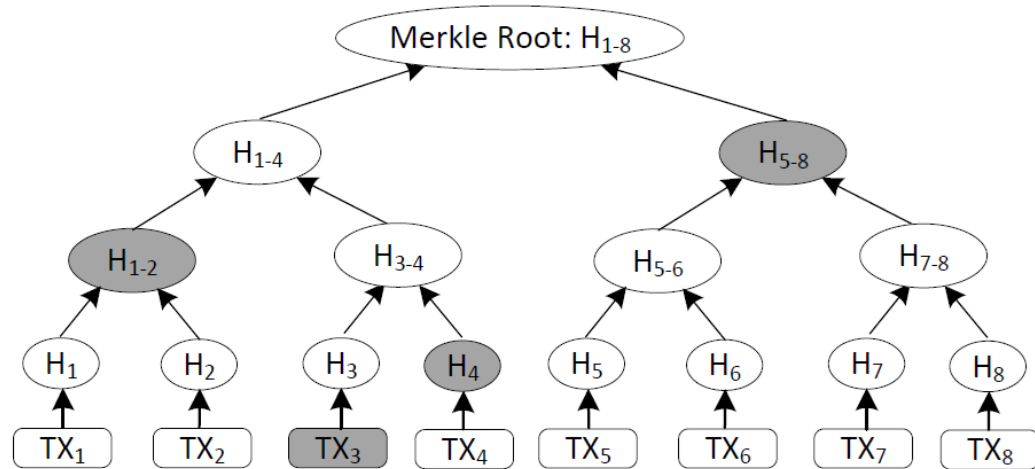
# Include Merkle Root in Block



Transactions are organised in a tree-like structure, and only the root of the tree is included into the calculation of the block hash.



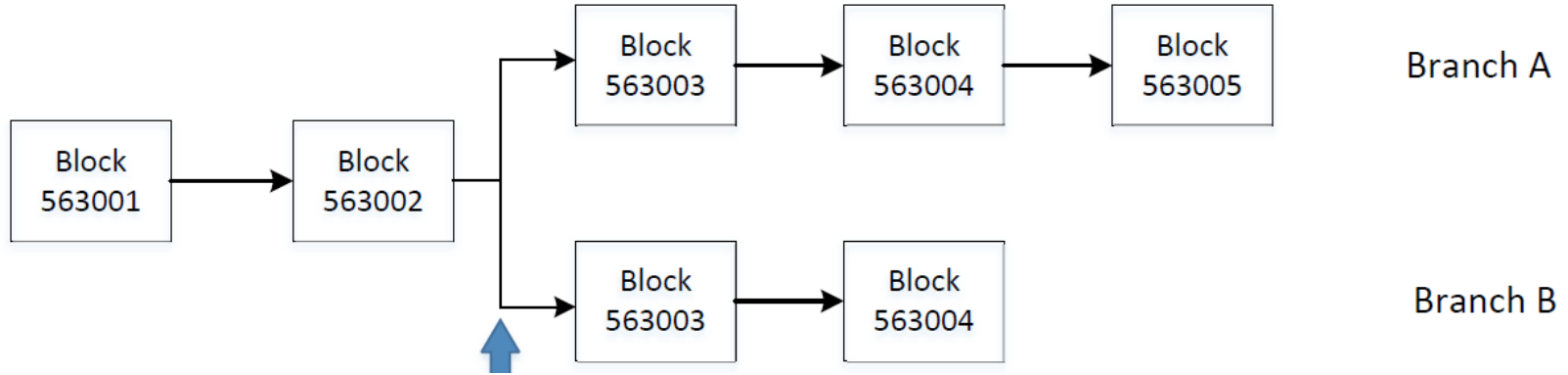
# Merkle Tree



Benefit:

- To find whether a transaction is included in a block, you don't need all the transactions.
- The cost of checking inclusion is  $O(\log n)$  rather than  $O(n)$

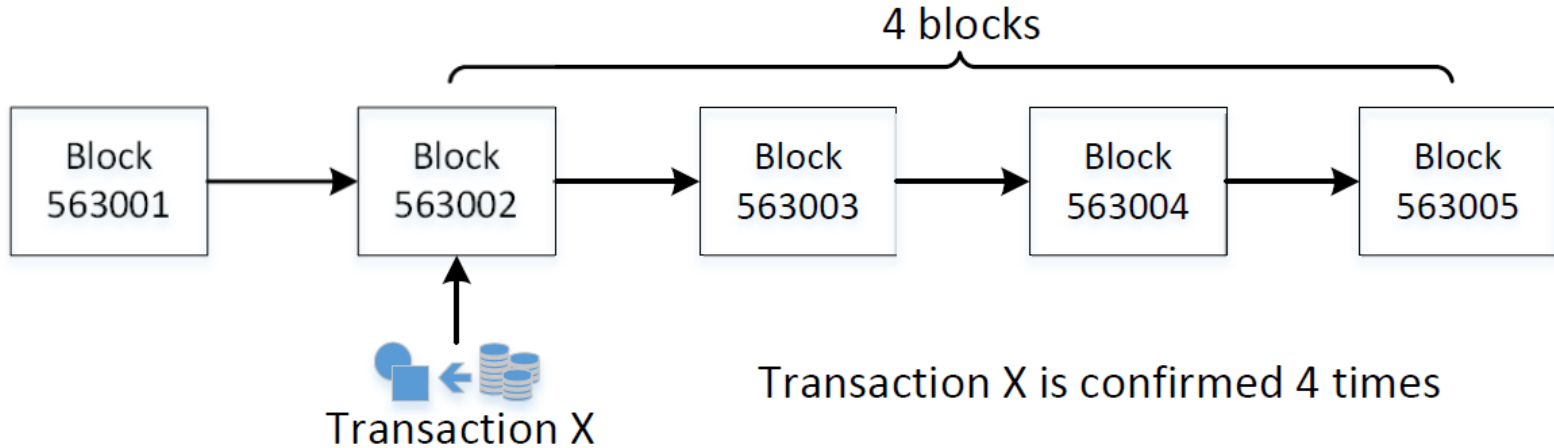
# Branching



Branching occurs when two valid blocks are found at about the same time

**The longest chain wins**

# Confirmation Number

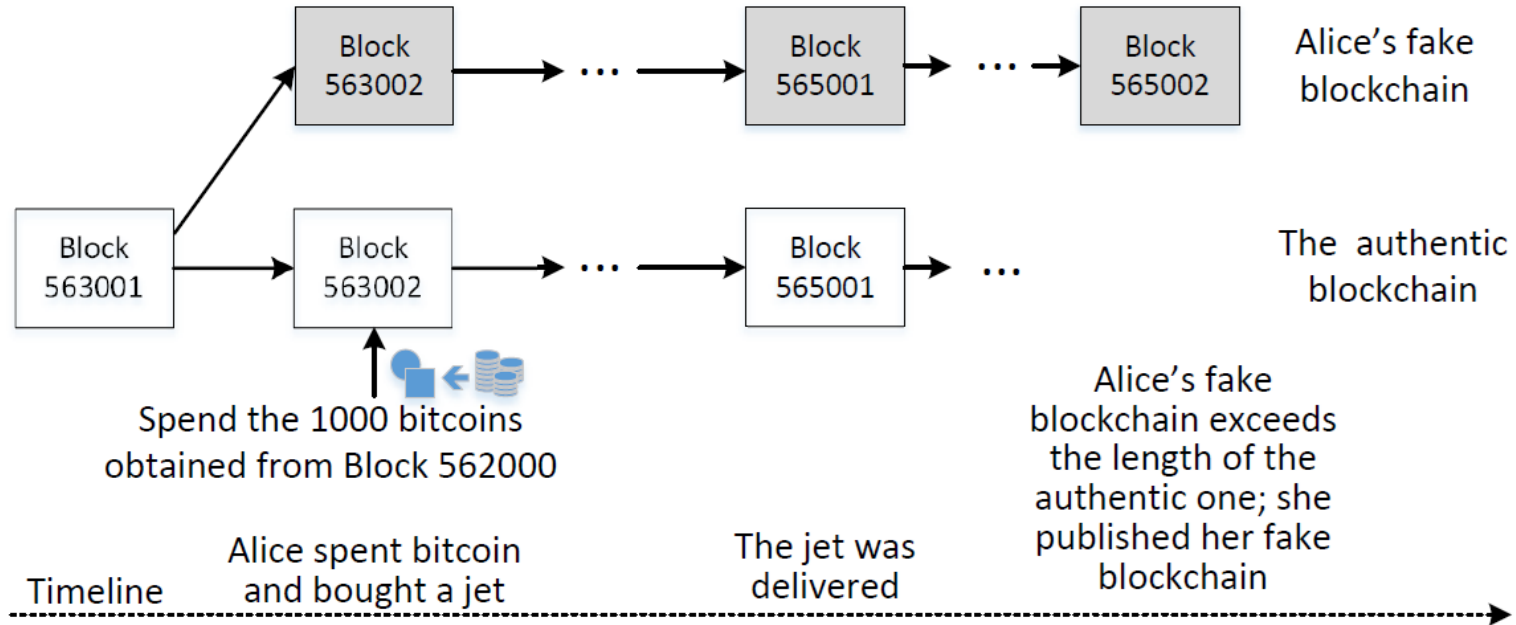


The larger a block's confirmation number is, the less likely it will be removed from the blockchain

# Probability of Double Spending

| Confirmation | 2%     | 8%     | 10%           | 20%     | 30%     | 40%     | 50%         |
|--------------|--------|--------|---------------|---------|---------|---------|-------------|
| 1            | 4%     | 16%    | 20%           | 40%     | 60%     | 80%     | <u>100%</u> |
| 2            | 0.237% | 3.635% | <u>5.600%</u> | 20.800% | 43.200% | 70.400% | 100%        |
| 3            | 0.016% | 0.905% | 1.712%        | 11.584% | 32.616% | 63.488% | 100%        |
| 4            | 0.001% | 0.235% | 0.546%        | 6.669%  | 25.207% | 57.958% | 100%        |
| 5            | ≈ 0    | 0.063% | 0.178%        | 3.916%  | 19.762% | 53.314% | 100%        |
| 6            | ≈ 0    | 0.017% | 0.059%        | 2.331%  | 15.645% | 49.300% | 100%        |
| 7            | ≈ 0    | 0.005% | 0.020%        | 1.401%  | 12.475% | 45.769% | 100%        |
| 8            | ≈ 0    | 0.001% | 0.007%        | 0.848%  | 10.003% | 42.621% | 100%        |

# Double Spending with Majority Hash Power



# Actual incidents

- July 2014, the mining pool ghash.io briefly exceeded 50% of the bitcoin network hash power.
- It voluntarily reduced the mining power to 40%
- 2018, Bitmain mined 42% of the Bitcoin blocks during a week in June.
- With 42% computing, the success rate to do double spending is high: 58% with 5 confirmation.
- Hence, double spending is feasible for major mining pools, but this doesn't mean the mining pools have the incentive to do the attack.

# Hardware security – Crypto wallet

- Currently, an [HSM can cost](#) between £20.000 to £40.000
- How secure are crypto wallets (e.g., Ledger, Trezor)?
- It turns out that there are [several attacks against these wallets](#) using side-channel attacks and voltage glitching.
- You may check this [YouTube video](#) where Joe Grand was able to retrieve the PIN from a Trezor wallet

# Summary

- Bitcoin address
- Transactions, locking and unlocking script
- Bitcoin mining
- Blockchain, branching, confirmation number, and double spending