

6 Conclusion

We have shown that all characterizations presented in this thesis are equally expressive.

Theorem 4.2.1 and Theorem 4.2.5 show the equivalence of deterministic and non-deterministic finite automata.

Lemma `dfa_to_nfa_correct` : $\text{dfa_lang } A =_i \text{nfa_lang } \text{dfa_to_nfa } A$.

Lemma `nfa_to_dfa_correct` : $\text{nfa_lang } A =_i \text{dfa_lang } \text{nfa_to_dfa } A$.

We have shown that there is an equivalent DFA for every extended regular expression.

Lemma `re_to_dfa_correct` r : $\text{dfa_lang } (\text{re_to_dfa } r) =_i \text{re_equiv } r$.

Building on that, we proved the decidability of equivalence of regular expressions in Theorem 4.7.1 with the help of decision procedure for equivalence of finite automata.

Lemma `re_equiv_correct` r s : $\text{re_equiv } r \ s \iff r =_i s$.

Theorem 4.8.2 shows that we can give an equivalent regular expression for every automaton.

Lemma `dfa_to_re_correct`: $\text{dfa_lang } A =_i \text{dfa_to_re } A$.