## ----- MLR - Multi Linear Regression Model -----

```
In [2]: # importing libraries
    import numpy as np
    import pandas as pd
    import matplotlib.pyplot as plt

In [3]: # Load the dataset
    dataset = pd.read_csv(r"C:\Users\Jan Saida\OneDrive\Documents\Desktop\Excel sheets\Investment.csv")
    dataset
```

| Out[3]: |    | DigitalMarketing | Promotion | Research  | State     | Profit    |
|---------|----|------------------|-----------|-----------|-----------|-----------|
|         | 0  | 165349.20        | 136897.80 | 471784.10 | Hyderabad | 192261.83 |
|         | 1  | 162597.70        | 151377.59 | 443898.53 | Bangalore | 191792.06 |
|         | 2  | 153441.51        | 101145.55 | 407934.54 | Chennai   | 191050.39 |
|         | 3  | 144372.41        | 118671.85 | 383199.62 | Hyderabad | 182901.99 |
|         | 4  | 142107.34        | 91391.77  | 366168.42 | Chennai   | 166187.94 |
|         | 5  | 131876.90        | 99814.71  | 362861.36 | Hyderabad | 156991.12 |
|         | 6  | 134615.46        | 147198.87 | 127716.82 | Bangalore | 156122.51 |
|         | 7  | 130298.13        | 145530.06 | 323876.68 | Chennai   | 155752.60 |
|         | 8  | 120542.52        | 148718.95 | 311613.29 | Hyderabad | 152211.77 |
|         | 9  | 123334.88        | 108679.17 | 304981.62 | Bangalore | 149759.96 |
|         | 10 | 101913.08        | 110594.11 | 229160.95 | Chennai   | 146121.95 |
|         | 11 | 100671.96        | 91790.61  | 249744.55 | Bangalore | 144259.40 |
|         | 12 | 93863.75         | 127320.38 | 249839.44 | Chennai   | 141585.52 |
|         | 13 | 91992.39         | 135495.07 | 252664.93 | Bangalore | 134307.35 |
|         | 14 | 119943.24        | 156547.42 | 256512.92 | Chennai   | 132602.65 |
|         | 15 | 114523.61        | 122616.84 | 261776.23 | Hyderabad | 129917.04 |
|         | 16 | 78013.11         | 121597.55 | 264346.06 | Bangalore | 126992.93 |
|         | 17 | 94657.16         | 145077.58 | 282574.31 | Hyderabad | 125370.37 |
|         | 18 | 91749.16         | 114175.79 | 294919.57 | Chennai   | 124266.90 |
|         | 19 | 86419.70         | 153514.11 | 0.00      | Hyderabad | 122776.86 |
|         | 20 | 76253.86         | 113867.30 | 298664.47 | Bangalore | 118474.03 |
|         | 21 | 78389.47         | 153773.43 | 299737.29 | Hyderabad | 111313.02 |

|    | DigitalMarketing | Promotion | Research  | State     | Profit    |
|----|------------------|-----------|-----------|-----------|-----------|
| 22 | 73994.56         | 122782.75 | 303319.26 | Chennai   | 110352.25 |
| 23 | 67532.53         | 105751.03 | 304768.73 | Chennai   | 108733.99 |
| 24 | 77044.01         | 99281.34  | 140574.81 | Hyderabad | 108552.04 |
| 25 | 64664.71         | 139553.16 | 137962.62 | Bangalore | 107404.34 |
| 26 | 75328.87         | 144135.98 | 134050.07 | Chennai   | 105733.54 |
| 27 | 72107.60         | 127864.55 | 353183.81 | Hyderabad | 105008.31 |
| 28 | 66051.52         | 182645.56 | 118148.20 | Chennai   | 103282.38 |
| 29 | 65605.48         | 153032.06 | 107138.38 | Hyderabad | 101004.64 |
| 30 | 61994.48         | 115641.28 | 91131.24  | Chennai   | 99937.59  |
| 31 | 61136.38         | 152701.92 | 88218.23  | Hyderabad | 97483.56  |
| 32 | 63408.86         | 129219.61 | 46085.25  | Bangalore | 97427.84  |
| 33 | 55493.95         | 103057.49 | 214634.81 | Chennai   | 96778.92  |
| 34 | 46426.07         | 157693.92 | 210797.67 | Bangalore | 96712.80  |
| 35 | 46014.02         | 85047.44  | 205517.64 | Hyderabad | 96479.51  |
| 36 | 28663.76         | 127056.21 | 201126.82 | Chennai   | 90708.19  |
| 37 | 44069.95         | 51283.14  | 197029.42 | Bangalore | 89949.14  |
| 38 | 20229.59         | 65947.93  | 185265.10 | Hyderabad | 81229.06  |
| 39 | 38558.51         | 82982.09  | 174999.30 | Bangalore | 81005.76  |
| 40 | 28754.33         | 118546.05 | 172795.67 | Bangalore | 78239.91  |
| 41 | 27892.92         | 84710.77  | 164470.71 | Chennai   | 77798.83  |
| 42 | 23640.93         | 96189.63  | 148001.11 | Bangalore | 71498.49  |
| 43 | 15505.73         | 127382.30 | 35534.17  | Hyderabad | 69758.98  |

|    | DigitalMarketing | Promotion | Research  | State     | Profit   |
|----|------------------|-----------|-----------|-----------|----------|
| 44 | 22177.74         | 154806.14 | 28334.72  | Bangalore | 65200.33 |
| 45 | 1000.23          | 124153.04 | 1903.93   | Hyderabad | 64926.08 |
| 46 | 1315.46          | 115816.21 | 297114.46 | Chennai   | 49490.75 |
| 47 | 0.00             | 135426.92 | 0.00      | Bangalore | 42559.73 |
| 48 | 542.05           | 51743.15  | 0.00      | Hyderabad | 35673.41 |
| 49 | 0.00             | 116983.80 | 45173.06  | Bangalore | 14681.40 |

```
In [4]: # Selecting the independent variables (X) and dependent variable (y)
    x = dataset.iloc[:, :-1] # independent variable
    y = dataset.iloc[:, 4] # dependent variable
In [5]: x
```

| Out[5]: |    | DigitalMarketing | Promotion | Research  | State     |
|---------|----|------------------|-----------|-----------|-----------|
|         | 0  | 165349.20        | 136897.80 | 471784.10 | Hyderabad |
|         | 1  | 162597.70        | 151377.59 | 443898.53 | Bangalore |
|         | 2  | 153441.51        | 101145.55 | 407934.54 | Chennai   |
|         | 3  | 144372.41        | 118671.85 | 383199.62 | Hyderabad |
|         | 4  | 142107.34        | 91391.77  | 366168.42 | Chennai   |
|         | 5  | 131876.90        | 99814.71  | 362861.36 | Hyderabad |
|         | 6  | 134615.46        | 147198.87 | 127716.82 | Bangalore |
|         | 7  | 130298.13        | 145530.06 | 323876.68 | Chennai   |
|         | 8  | 120542.52        | 148718.95 | 311613.29 | Hyderabad |
|         | 9  | 123334.88        | 108679.17 | 304981.62 | Bangalore |
|         | 10 | 101913.08        | 110594.11 | 229160.95 | Chennai   |
|         | 11 | 100671.96        | 91790.61  | 249744.55 | Bangalore |
|         | 12 | 93863.75         | 127320.38 | 249839.44 | Chennai   |
|         | 13 | 91992.39         | 135495.07 | 252664.93 | Bangalore |
|         | 14 | 119943.24        | 156547.42 | 256512.92 | Chennai   |
|         | 15 | 114523.61        | 122616.84 | 261776.23 | Hyderabad |
|         | 16 | 78013.11         | 121597.55 | 264346.06 | Bangalore |
|         | 17 | 94657.16         | 145077.58 | 282574.31 | Hyderabad |
|         | 18 | 91749.16         | 114175.79 | 294919.57 | Chennai   |
|         | 19 | 86419.70         | 153514.11 | 0.00      | Hyderabad |
|         | 20 | 76253.86         | 113867.30 | 298664.47 | Bangalore |
|         | 21 | 78389.47         | 153773.43 | 299737.29 | Hyderabad |

|    | DigitalMarketing | Promotion | Research  | State     |
|----|------------------|-----------|-----------|-----------|
| 22 | 73994.56         | 122782.75 | 303319.26 | Chennai   |
| 23 | 67532.53         | 105751.03 | 304768.73 | Chennai   |
| 24 | 77044.01         | 99281.34  | 140574.81 | Hyderabad |
| 25 | 64664.71         | 139553.16 | 137962.62 | Bangalore |
| 26 | 75328.87         | 144135.98 | 134050.07 | Chennai   |
| 27 | 72107.60         | 127864.55 | 353183.81 | Hyderabad |
| 28 | 66051.52         | 182645.56 | 118148.20 | Chennai   |
| 29 | 65605.48         | 153032.06 | 107138.38 | Hyderabad |
| 30 | 61994.48         | 115641.28 | 91131.24  | Chennai   |
| 31 | 61136.38         | 152701.92 | 88218.23  | Hyderabad |
| 32 | 63408.86         | 129219.61 | 46085.25  | Bangalore |
| 33 | 55493.95         | 103057.49 | 214634.81 | Chennai   |
| 34 | 46426.07         | 157693.92 | 210797.67 | Bangalore |
| 35 | 46014.02         | 85047.44  | 205517.64 | Hyderabad |
| 36 | 28663.76         | 127056.21 | 201126.82 | Chennai   |
| 37 | 44069.95         | 51283.14  | 197029.42 | Bangalore |
| 38 | 20229.59         | 65947.93  | 185265.10 | Hyderabad |
| 39 | 38558.51         | 82982.09  | 174999.30 | Bangalore |
| 40 | 28754.33         | 118546.05 | 172795.67 | Bangalore |
| 41 | 27892.92         | 84710.77  | 164470.71 | Chennai   |
| 42 | 23640.93         | 96189.63  | 148001.11 | Bangalore |
| 43 | 15505.73         | 127382.30 | 35534.17  | Hyderabad |

|    | DigitalMarketing | Promotion | Research  | State     |
|----|------------------|-----------|-----------|-----------|
| 44 | 22177.74         | 154806.14 | 28334.72  | Bangalore |
| 45 | 1000.23          | 124153.04 | 1903.93   | Hyderabad |
| 46 | 1315.46          | 115816.21 | 297114.46 | Chennai   |
| 47 | 0.00             | 135426.92 | 0.00      | Bangalore |
| 48 | 542.05           | 51743.15  | 0.00      | Hyderabad |
| 49 | 0.00             | 116983.80 | 45173.06  | Bangalore |

In [6]: **y** 

```
Out[6]: 0
              192261.83
              191792.06
         1
         2
              191050.39
              182901.99
         3
         4
              166187.94
              156991.12
         6
              156122.51
         7
              155752.60
         8
              152211.77
         9
              149759.96
        10
              146121.95
        11
              144259.40
        12
              141585.52
        13
              134307.35
        14
              132602.65
        15
              129917.04
        16
              126992.93
        17
              125370.37
              124266.90
        18
        19
              122776.86
        20
              118474.03
        21
              111313.02
        22
              110352.25
        23
              108733.99
        24
              108552.04
        25
              107404.34
        26
              105733.54
        27
              105008.31
        28
              103282.38
        29
              101004.64
        30
               99937.59
        31
               97483.56
        32
               97427.84
        33
               96778.92
        34
               96712.80
        35
               96479.51
        36
               90708.19
        37
               89949.14
        38
               81229.06
        39
               81005.76
```

```
40
               78239.91
        41
               77798.83
        42
               71498.49
        43
               69758.98
        44
               65200.33
        45
               64926.08
        46
               49490.75
        47
               42559.73
        48
               35673.41
        49
               14681.40
        Name: Profit, dtype: float64
In [7]: # Apply one-hot encoding to the features (categorical variables)
       X = pd.get_dummies(x, dtype=int)
```

| ıt[7]: | D  | DigitalMarketing | Promotion | Research  | State_Bangalore | State_Chennai | State_Hyderabad |
|--------|----|------------------|-----------|-----------|-----------------|---------------|-----------------|
|        | 0  | 165349.20        | 136897.80 | 471784.10 | 0               | 0             | 1               |
|        | 1  | 162597.70        | 151377.59 | 443898.53 | 1               | 0             | 0               |
|        | 2  | 153441.51        | 101145.55 | 407934.54 | 0               | 1             | 0               |
|        | 3  | 144372.41        | 118671.85 | 383199.62 | 0               | 0             | 1               |
|        | 4  | 142107.34        | 91391.77  | 366168.42 | 0               | 1             | 0               |
|        | 5  | 131876.90        | 99814.71  | 362861.36 | 0               | 0             | 1               |
|        | 6  | 134615.46        | 147198.87 | 127716.82 | 1               | 0             | 0               |
|        | 7  | 130298.13        | 145530.06 | 323876.68 | 0               | 1             | 0               |
|        | 8  | 120542.52        | 148718.95 | 311613.29 | 0               | 0             | 1               |
|        | 9  | 123334.88        | 108679.17 | 304981.62 | 1               | 0             | 0               |
|        | 10 | 101913.08        | 110594.11 | 229160.95 | 0               | 1             | 0               |
| •      | 11 | 100671.96        | 91790.61  | 249744.55 | 1               | 0             | 0               |
| •      | 12 | 93863.75         | 127320.38 | 249839.44 | 0               | 1             | 0               |
| •      | 13 | 91992.39         | 135495.07 | 252664.93 | 1               | 0             | 0               |
| •      | 14 | 119943.24        | 156547.42 | 256512.92 | 0               | 1             | 0               |
| •      | 15 | 114523.61        | 122616.84 | 261776.23 | 0               | 0             | 1               |
| •      | 16 | 78013.11         | 121597.55 | 264346.06 | 1               | 0             | 0               |
| •      | 17 | 94657.16         | 145077.58 | 282574.31 | 0               | 0             | 1               |
|        | 18 | 91749.16         | 114175.79 | 294919.57 | 0               | 1             | 0               |
| •      | 19 | 86419.70         | 153514.11 | 0.00      | 0               | 0             | 1               |
| 2      | 20 | 76253.86         | 113867.30 | 298664.47 | 1               | 0             | 0               |
| 2      | 21 | 78389.47         | 153773.43 | 299737.29 | 0               | 0             | 1               |

|    | DigitalMarketing | Promotion | Research  | State_Bangalore | State_Chennai | State_Hyderabad |
|----|------------------|-----------|-----------|-----------------|---------------|-----------------|
| 22 | 73994.56         | 122782.75 | 303319.26 | 0               | 1             | 0               |
| 23 | 67532.53         | 105751.03 | 304768.73 | 0               | 1             | 0               |
| 24 | 77044.01         | 99281.34  | 140574.81 | 0               | 0             | 1               |
| 25 | 64664.71         | 139553.16 | 137962.62 | 1               | 0             | 0               |
| 26 | 75328.87         | 144135.98 | 134050.07 | 0               | 1             | 0               |
| 27 | 72107.60         | 127864.55 | 353183.81 | 0               | 0             | 1               |
| 28 | 66051.52         | 182645.56 | 118148.20 | 0               | 1             | 0               |
| 29 | 65605.48         | 153032.06 | 107138.38 | 0               | 0             | 1               |
| 30 | 61994.48         | 115641.28 | 91131.24  | 0               | 1             | 0               |
| 31 | 61136.38         | 152701.92 | 88218.23  | 0               | 0             | 1               |
| 32 | 63408.86         | 129219.61 | 46085.25  | 1               | 0             | 0               |
| 33 | 55493.95         | 103057.49 | 214634.81 | 0               | 1             | 0               |
| 34 | 46426.07         | 157693.92 | 210797.67 | 1               | 0             | 0               |
| 35 | 46014.02         | 85047.44  | 205517.64 | 0               | 0             | 1               |
| 36 | 28663.76         | 127056.21 | 201126.82 | 0               | 1             | 0               |
| 37 | 44069.95         | 51283.14  | 197029.42 | 1               | 0             | 0               |
| 38 | 20229.59         | 65947.93  | 185265.10 | 0               | 0             | 1               |
| 39 | 38558.51         | 82982.09  | 174999.30 | 1               | 0             | 0               |
| 40 | 28754.33         | 118546.05 | 172795.67 | 1               | 0             | 0               |
| 41 | 27892.92         | 84710.77  | 164470.71 | 0               | 1             | 0               |
| 42 | 23640.93         | 96189.63  | 148001.11 | 1               | 0             | 0               |
| 43 | 15505.73         | 127382.30 | 35534.17  | 0               | 0             | 1               |

|    | DigitalMarketing | Promotion | Research  | State_Bangalore | State_Chennai | State_Hyderabad |
|----|------------------|-----------|-----------|-----------------|---------------|-----------------|
| 44 | 22177.74         | 154806.14 | 28334.72  | 1               | 0             | 0               |
| 45 | 1000.23          | 124153.04 | 1903.93   | 0               | 0             | 1               |
| 46 | 1315.46          | 115816.21 | 297114.46 | 0               | 1             | 0               |
| 47 | 0.00             | 135426.92 | 0.00      | 1               | 0             | 0               |
| 48 | 542.05           | 51743.15  | 0.00      | 0               | 0             | 1               |
| 49 | 0.00             | 116983.80 | 45173.06  | 1               | 0             | 0               |

```
In [8]: # Train-test split
```

from sklearn.model\_selection import train\_test\_split
x\_train, x\_test, y\_train, y\_test = train\_test\_split(X, y, test\_size=0.2, random\_state=0)

In [9]: x\_train

| Out[9]: |    | DigitalMarketing | Promotion | Research  | State_Bangalore | State_Chennai | State_Hyderabad |
|---------|----|------------------|-----------|-----------|-----------------|---------------|-----------------|
|         | 33 | 55493.95         | 103057.49 | 214634.81 | 0               | 1             | 0               |
|         | 35 | 46014.02         | 85047.44  | 205517.64 | 0               | 0             | 1               |
|         | 26 | 75328.87         | 144135.98 | 134050.07 | 0               | 1             | 0               |
|         | 34 | 46426.07         | 157693.92 | 210797.67 | 1               | 0             | 0               |
|         | 18 | 91749.16         | 114175.79 | 294919.57 | 0               | 1             | 0               |
|         | 7  | 130298.13        | 145530.06 | 323876.68 | 0               | 1             | 0               |
|         | 14 | 119943.24        | 156547.42 | 256512.92 | 0               | 1             | 0               |
|         | 45 | 1000.23          | 124153.04 | 1903.93   | 0               | 0             | 1               |
|         | 48 | 542.05           | 51743.15  | 0.00      | 0               | 0             | 1               |
|         | 29 | 65605.48         | 153032.06 | 107138.38 | 0               | 0             | 1               |
|         | 15 | 114523.61        | 122616.84 | 261776.23 | 0               | 0             | 1               |
|         | 30 | 61994.48         | 115641.28 | 91131.24  | 0               | 1             | 0               |
|         | 32 | 63408.86         | 129219.61 | 46085.25  | 1               | 0             | 0               |
|         | 16 | 78013.11         | 121597.55 | 264346.06 | 1               | 0             | 0               |
|         | 42 | 23640.93         | 96189.63  | 148001.11 | 1               | 0             | 0               |
|         | 20 | 76253.86         | 113867.30 | 298664.47 | 1               | 0             | 0               |
|         | 43 | 15505.73         | 127382.30 | 35534.17  | 0               | 0             | 1               |
|         | 8  | 120542.52        | 148718.95 | 311613.29 | 0               | 0             | 1               |
|         | 13 | 91992.39         | 135495.07 | 252664.93 | 1               | 0             | 0               |
|         | 25 | 64664.71         | 139553.16 | 137962.62 | 1               | 0             | 0               |
|         | 5  | 131876.90        | 99814.71  | 362861.36 | 0               | 0             | 1               |
|         | 17 | 94657.16         | 145077.58 | 282574.31 | 0               | 0             | 1               |

|    | DigitalMarketing | Promotion | Research  | State_Bangalore | State_Chennai | State_Hyderabad |
|----|------------------|-----------|-----------|-----------------|---------------|-----------------|
| 40 | 28754.33         | 118546.05 | 172795.67 | 1               | 0             | 0               |
| 49 | 0.00             | 116983.80 | 45173.06  | 1               | 0             | 0               |
| 1  | 162597.70        | 151377.59 | 443898.53 | 1               | 0             | 0               |
| 12 | 93863.75         | 127320.38 | 249839.44 | 0               | 1             | 0               |
| 37 | 44069.95         | 51283.14  | 197029.42 | 1               | 0             | 0               |
| 24 | 77044.01         | 99281.34  | 140574.81 | 0               | 0             | 1               |
| 6  | 134615.46        | 147198.87 | 127716.82 | 1               | 0             | 0               |
| 23 | 67532.53         | 105751.03 | 304768.73 | 0               | 1             | 0               |
| 36 | 28663.76         | 127056.21 | 201126.82 | 0               | 1             | 0               |
| 21 | 78389.47         | 153773.43 | 299737.29 | 0               | 0             | 1               |
| 19 | 86419.70         | 153514.11 | 0.00      | 0               | 0             | 1               |
| 9  | 123334.88        | 108679.17 | 304981.62 | 1               | 0             | 0               |
| 39 | 38558.51         | 82982.09  | 174999.30 | 1               | 0             | 0               |
| 46 | 1315.46          | 115816.21 | 297114.46 | 0               | 1             | 0               |
| 3  | 144372.41        | 118671.85 | 383199.62 | 0               | 0             | 1               |
| 0  | 165349.20        | 136897.80 | 471784.10 | 0               | 0             | 1               |
| 47 | 0.00             | 135426.92 | 0.00      | 1               | 0             | 0               |
| 44 | 22177.74         | 154806.14 | 28334.72  | 1               | 0             | 0               |
|    |                  |           |           |                 |               |                 |

In [10]: x\_test

| Out[10]: |    | DigitalMarketing | Promotion | Research  | State_Bangalore | State_Chennai | State_Hyderabad |
|----------|----|------------------|-----------|-----------|-----------------|---------------|-----------------|
|          | 28 | 66051.52         | 182645.56 | 118148.20 | 0               | 1             | 0               |
|          | 11 | 100671.96        | 91790.61  | 249744.55 | 1               | 0             | 0               |
|          | 10 | 101913.08        | 110594.11 | 229160.95 | 0               | 1             | 0               |
|          | 41 | 27892.92         | 84710.77  | 164470.71 | 0               | 1             | 0               |
|          | 2  | 153441.51        | 101145.55 | 407934.54 | 0               | 1             | 0               |
|          | 27 | 72107.60         | 127864.55 | 353183.81 | 0               | 0             | 1               |
|          | 38 | 20229.59         | 65947.93  | 185265.10 | 0               | 0             | 1               |
|          | 31 | 61136.38         | 152701.92 | 88218.23  | 0               | 0             | 1               |
|          | 22 | 73994.56         | 122782.75 | 303319.26 | 0               | 1             | 0               |
|          | 4  | 142107.34        | 91391.77  | 366168.42 | 0               | 1             | 0               |

In [11]: y\_train

```
Out[11]: 33
                96778.92
         35
                96479.51
         26
               105733.54
                96712.80
         34
         18
               124266.90
               155752.60
          7
         14
               132602.65
         45
                64926.08
         48
                35673.41
         29
               101004.64
         15
               129917.04
         30
                99937.59
         32
                97427.84
         16
               126992.93
         42
                71498.49
         20
               118474.03
         43
                69758.98
               152211.77
          8
               134307.35
         13
         25
               107404.34
          5
               156991.12
         17
               125370.37
         40
                78239.91
         49
                14681.40
         1
               191792.06
         12
               141585.52
         37
                89949.14
         24
               108552.04
               156122.51
          6
         23
               108733.99
         36
                90708.19
         21
               111313.02
         19
               122776.86
          9
               149759.96
         39
                81005.76
         46
                49490.75
          3
               182901.99
               192261.83
          0
         47
                42559.73
```

```
Name: Profit, dtype: float64
In [12]: y_test
Out[12]: 28
              103282.38
         11
             144259.40
         10
            146121.95
             77798.83
         41
         2
              191050.39
         27 105008.31
         38 81229.06
         31 97483.56
         22 110352.25
              166187.94
         Name: Profit, dtype: float64
In [13]: # Create and train the regressor model
         from sklearn.linear model import LinearRegression
         regressor = LinearRegression()
         regressor.fit(x train, y train)
Out[13]:
             LinearRegression
         LinearRegression()
In [14]: y pred = regressor.predict(x test)
        y_pred
Out[14]: array([103015.20159796, 132582.27760816, 132447.73845174, 71976.09851258,
                178537.48221055, 116161.24230165, 67851.69209676, 98791.73374687,
                113969.43533012, 167921.0656955 ])
In [15]: m = regressor.coef_
         print(m)
        [ 7.73467193e-01 3.28845975e-02 3.66100259e-02 8.66383692e+01
         -8.72645791e+02 7.86007422e+02]
```

65200.33

44

```
Out[17]: array([[1.0000000e+00, 1.6534920e+05, 1.3689780e+05, 4.7178410e+05,
                  0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
                 [1.00000000e+00, 1.6259770e+05, 1.5137759e+05, 4.4389853e+05,
                  1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
                 [1.0000000e+00, 1.5344151e+05, 1.0114555e+05, 4.0793454e+05,
                  0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
                 [1.0000000e+00, 1.4437241e+05, 1.1867185e+05, 3.8319962e+05,
                  0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
                 [1.0000000e+00, 1.4210734e+05, 9.1391770e+04, 3.6616842e+05,
                  0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
                 [1.0000000e+00, 1.3187690e+05, 9.9814710e+04, 3.6286136e+05,
                  0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
                 [1.0000000e+00, 1.3461546e+05, 1.4719887e+05, 1.2771682e+05,
                  1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
                 [1.00000000e+00, 1.3029813e+05, 1.4553006e+05, 3.2387668e+05,
                  0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
                 [1.0000000e+00, 1.2054252e+05, 1.4871895e+05, 3.1161329e+05,
                  0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
                 [1.0000000e+00, 1.2333488e+05, 1.0867917e+05, 3.0498162e+05,
                 1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
                 [1.00000000e+00, 1.0191308e+05, 1.1059411e+05, 2.2916095e+05,
                  0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
                 [1.0000000e+00, 1.0067196e+05, 9.1790610e+04, 2.4974455e+05,
                  1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
                 [1.00000000e+00, 9.3863750e+04, 1.2732038e+05, 2.4983944e+05,
                  0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
                 [1.0000000e+00, 9.1992390e+04, 1.3549507e+05, 2.5266493e+05,
                  1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
                 [1.00000000e+00, 1.1994324e+05, 1.5654742e+05, 2.5651292e+05,
                  0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
                 [1.0000000e+00, 1.1452361e+05, 1.2261684e+05, 2.6177623e+05,
                  0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
                 [1.00000000e+00, 7.8013110e+04, 1.2159755e+05, 2.6434606e+05,
                  1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
                 [1.00000000e+00, 9.4657160e+04, 1.4507758e+05, 2.8257431e+05,
                  0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
                 [1.0000000e+00, 9.1749160e+04, 1.1417579e+05, 2.9491957e+05,
                  0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
                 [1.00000000e+00, 8.6419700e+04, 1.5351411e+05, 0.0000000e+00,
                  0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
```

```
[1.0000000e+00, 7.6253860e+04, 1.1386730e+05, 2.9866447e+05,
1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
[1.0000000e+00, 7.8389470e+04, 1.5377343e+05, 2.9973729e+05,
0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
[1.0000000e+00, 7.3994560e+04, 1.2278275e+05, 3.0331926e+05,
0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
[1.00000000e+00, 6.7532530e+04, 1.0575103e+05, 3.0476873e+05,
0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
[1.00000000e+00, 7.7044010e+04, 9.9281340e+04, 1.4057481e+05,
0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
[1.00000000e+00, 6.4664710e+04, 1.3955316e+05, 1.3796262e+05,
1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
[1.0000000e+00, 7.5328870e+04, 1.4413598e+05, 1.3405007e+05,
0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
[1.0000000e+00, 7.2107600e+04, 1.2786455e+05, 3.5318381e+05,
0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
[1.0000000e+00, 6.6051520e+04, 1.8264556e+05, 1.1814820e+05,
0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
[1.00000000e+00, 6.5605480e+04, 1.5303206e+05, 1.0713838e+05,
0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
[1.0000000e+00, 6.1994480e+04, 1.1564128e+05, 9.1131240e+04,
0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
[1.00000000e+00, 6.1136380e+04, 1.5270192e+05, 8.8218230e+04,
0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
[1.0000000e+00, 6.3408860e+04, 1.2921961e+05, 4.6085250e+04,
1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
[1.0000000e+00, 5.5493950e+04, 1.0305749e+05, 2.1463481e+05,
0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
[1.00000000e+00, 4.6426070e+04, 1.5769392e+05, 2.1079767e+05,
1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
[1.00000000e+00, 4.6014020e+04, 8.5047440e+04, 2.0551764e+05,
0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
[1.0000000e+00, 2.8663760e+04, 1.2705621e+05, 2.0112682e+05,
0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
[1.00000000e+00, 4.4069950e+04, 5.1283140e+04, 1.9702942e+05,
1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
[1.00000000e+00, 2.0229590e+04, 6.5947930e+04, 1.8526510e+05,
0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
[1.0000000e+00, 3.8558510e+04, 8.2982090e+04, 1.7499930e+05,
1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
[1.00000000e+00, 2.8754330e+04, 1.1854605e+05, 1.7279567e+05,
```

```
1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
                 [1.0000000e+00, 2.7892920e+04, 8.4710770e+04, 1.6447071e+05,
                  0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
                 [1.00000000e+00, 2.3640930e+04, 9.6189630e+04, 1.4800111e+05,
                  1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
                 [1.0000000e+00, 1.5505730e+04, 1.2738230e+05, 3.5534170e+04,
                  0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
                 [1.00000000e+00, 2.2177740e+04, 1.5480614e+05, 2.8334720e+04,
                  1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
                 [1.00000000e+00, 1.0002300e+03, 1.2415304e+05, 1.9039300e+03,
                  0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
                 [1.0000000e+00, 1.3154600e+03, 1.1581621e+05, 2.9711446e+05,
                  0.0000000e+00, 1.0000000e+00, 0.0000000e+00],
                 [1.00000000e+00, 0.0000000e+00, 1.3542692e+05, 0.0000000e+00,
                  1.0000000e+00, 0.0000000e+00, 0.0000000e+00],
                 [1.0000000e+00, 5.4205000e+02, 5.1743150e+04, 0.0000000e+00,
                  0.0000000e+00, 0.0000000e+00, 1.0000000e+00],
                 [1.00000000e+00, 0.0000000e+00, 1.1698380e+05, 4.5173060e+04,
                  1.0000000e+00, 0.0000000e+00, 0.0000000e+00]])
In [18]: # --- 1
         import statsmodels.api as sm
         X \text{ opt } = X[:,[0,1,2,3,4,5]]
         # Ordinary Least Sqaures
         regressor OLS = sm.OLS(endog=y , exog=X opt).fit()
         regressor OLS.summary()
         # --- 2
         import statsmodels.api as sm
         X \text{ opt} = X[:,[0,1,2,3,5]]
         regressor OLS =sm.OLS(endog=y,exog=X opt).fit()
         regressor_OLS.summary()
         # --- 3
         import statsmodels.api as sm
         X \text{ opt } = X[:,[0,1,2,3]]
         regressor OLS =sm.OLS(endog=y,exog=X opt).fit()
```

```
regressor_OLS.summary()

# --- 4
import statsmodels.api as sm
X_opt = X[:,[0,1,3]]

regressor_OLS =sm.OLS(endog=y,exog=X_opt).fit()
regressor_OLS.summary()

# --- 5
import statsmodels.api as sm
X_opt = X[:,[0,1]]

regressor_OLS =sm.OLS(endog=y,exog=X_opt).fit()
regressor_OLS =sm.OLS(endog=y,exog=X_opt).fit()
regressor_OLS.summary()
```

Out[18]:

## **OLS Regression Results**

| De          | ep. Variable:                           | •   | Profit                                  | F                                | R-squared:                           | 0.947    |
|-------------|---|---|---|----------------------------------|--------------------------------------|----------|
|             | Model:                                  | :   | OLS                                     | Adj. F                           | R-squared:                           | 0.945    |
|             | Method:                                 | : Least   | Squares                                 | I                                | F-statistic:                         | 849.8    |
|             | Date:                                   | : Sat, 25 .   | Jan 2025                                | Prob (F                          | -statistic):                         | 3.50e-32 |
|             | Time                                    | :   | 23:41:53                                | Log-L                            | ikelihood:                           | -527.44  |
| No. O       | bservations:                            | :   | 50                                      |                                  | AIC:                                 | 1059.    |
|             | of Residuals:                           | :   | 48                                      |                                  | BIC:                                 | 1063.    |
|             | Df Model:                               | :   | 1                                       |                                  |                                      |          |
| Cova        | riance Type:                            | : no  | onrobust                                |                                  |                                      |          |
|             | •                                       |   |   |                                  |                                      |          |
|             | coef                                    |   | r t                                     | P> t                             | [0.025                               | 0.975]   |
| const       |   | std er  |   |                                  | -                                    |          |
|             | coef                                    | std er  | 7 19.320                                |                                  | -                                    |          |
| const       | <b>coef</b> 4.903e+04                   | <b>std er</b> 2537.89                                 | 7 19.320                                | 0.000                            | 4.39e+04                             | 5.41e+04 |
| const<br>x1 | <b>coef</b> 4.903e+04 0.8543            | std er<br>2537.89<br>0.02<br>13.727                   | 7 19.320<br>9 29.151                    | 0.000<br>0.000<br><b>Vatson:</b> | 4.39e+04<br>0.795                    | 5.41e+04 |
| const<br>x1 | coef<br>4.903e+04<br>0.8543<br>Omnibus: | std er<br>2537.89<br>0.02<br>13.727<br>0.001 <b>J</b> | 7 19.320<br>9 29.151<br><b>Durbin-V</b> | 0.000<br>0.000<br><b>Vatson:</b> | 4.39e+04<br>0.795<br>1.116<br>18.536 | 5.41e+04 |

## Notes:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.65e+05. This might indicate that there are strong multicollinearity or other numerical problems.

In [19]: bias = regressor.score(x\_train,y\_train) bias

Out[19]: 0.9501847627493607

In [20]: variance = regressor.score(x\_test,y\_test)

variance

Out[20]: 0.9347068473282424