

pdf for normal distribution

$$\Rightarrow \prod_{i=1}^n \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{1}{2} \left( \frac{x_i - \mu}{\sigma} \right)^2}$$

$$\prod p(x_i) = \frac{1}{(\sigma \sqrt{2\pi})^n} e^{-\frac{1}{2} \sum \left( \frac{x_i - \mu}{\sigma} \right)^2}$$

$$\log(\text{pdf}(\mu, \sigma)) = -n \log(\sigma \sqrt{2\pi}) - \frac{1}{2} \sum \left( \frac{x_i - \mu}{\sigma} \right)^2$$

$$\log(\mu, \sigma) = -\frac{n}{2} \log(\sigma^2 2\pi) - \frac{1}{2} \sum \left( \frac{x_i - \mu}{\sigma} \right)^2$$

$$\frac{\partial \log(\mu, \sigma)}{\partial \sigma} = \frac{-n \cancel{\log} \times 2\pi}{2\sigma \times 2\pi} - \frac{1}{2}$$

$\partial \sigma$  for measuring  $\sigma$ .

$$\frac{\partial \log(\mu, \sigma)}{\partial \sigma} = 0 - \frac{1}{2\sigma^2} \sum x_i - n\sigma$$

↓

$$0 = -\sum x_i + n\sigma$$

$$\sum x_i = n\sigma$$

$$\sigma = \frac{\sum x_i}{n}$$

for measuring  $\theta_2$

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$$\frac{\partial \log(\theta_1, \theta_2)}{\partial \theta_2} = -\frac{n}{2\theta_2} + \frac{1}{2\theta_2^2} \sum (x_i - \theta_1)^2$$

$$0 = -\frac{n}{2\theta_2} + \frac{1}{2\theta_2^2} \sum (x_i - \theta_1)^2$$

$$\frac{\sum (x_i - \theta_1)^2}{2\theta_2^2} = \frac{n}{2\theta_2}$$

$$\theta_2 = \frac{\sum (x_i - \theta_1)^2}{n}$$



$$B(m, \theta) = m_C \times \theta^u (1-\theta)^{m-u}$$

$$\prod_{i=1}^n = \prod m_{C_{x_i}} \theta^{x_i} (1-\theta)^{m-x_i}$$

$$= m_{C_{x_1}} \times m_{C_{x_2}} \dots \times m_{C_{x_n}} \theta^{\sum x_i} (1-\theta)^{\sum m-x_i}$$

$$\sum_{i=1}^n \log(m_{C_{x_i}}) + \sum u_i \log \theta + \sum m - u_i \log(1-\theta)$$

$$= 0 + \frac{\sum u_i}{\theta} + \frac{\sum (m - x_i)}{1-\theta} (-1)$$

$$0 = \sum x_i - \sum \frac{x_i}{\theta} - nm\theta + \sum x_i \theta$$

$$\sum u_i = nm\theta$$

$$\theta = \frac{\sum x_i}{nm}$$

$$\theta = \bar{x}$$