- Managing Multidimensional Arrays
- An xarray tutorial

Introduction

- Janukan Sivajeyan, PhD student @ UAlberta
- Reducing Heat Generated By High Intensity Lasers
- Simulations with TBs of array data

Materials

will be on github [code/presentation]

Arrays and Dimensions

An array is an ordered grouping of values (often numeric)

- "0D": Single value a.k.a. scalar
- 1D: Line of Values a.k.a vector
- 2D: Rectangle of Values a.k.a matrix
- 3D: Rectangular Prism of Values
- 4D: Rectangular Prism Movie of Values

Shape of Array

- An array's **shape** is the length of each dimension
- shape can be expressed as a 1D array
- [2,4,3] could be the **shape** of a 3D array

Indices [Plural of Index]

- Positions within the array are addressed by indices
- Indices: ordered grouping of integers [1 per dim.]
- Indices can be expressed as a 1D array

Example Array

```
# Array Values
[9, 4, 3, 5, 4]
# Array Indices
[0, 1, 2, 3, 4]
```

2D Arrays

- 2D arrays are ordered square of numbers
- Can represent matrices

Values

```
[[9, 8, 7], [6, 5, 4], [3, 2, 1]]
```

2D Arrays

The 2D arrays have 2 element indices

Position [Index]

```
[[(0,0), (0,1), (0,2)],
[(1,0), (1,1), (1,2)],
[(2,0), (2,1), (2,2)]]
```

Coordinates

- Array Indices may map to a coordinate (x,y,z,t)
- Aligned: coordinate element vary along only one dim.
- Aligned coordinates can be represented with a 1D array
- Does not require a regular interval

Coordinates Example

Example Array

```
# Values
[9, 4, 3, 5, 4]
# Indices
[0, 1, 2, 3, 4]
# Coordinate
[0.1, 0.2, 0.4, 0.5, 0.6]
```

Coordinates vs Indices

- Arrays always have **indices**
- Indices are always integer values
- Coords may be integer values
- Aligned coords have coordinate vectors

Graph on Grid Paper Analogy

The grid lines represent indices and the xticks/yticks represent the coordinate vectors

Applications

- Linear Algebra
- Quantities at various points in space and time
- Geospatial Data, Simulation Data
- Neural Network Weights [2D]
- Media [Music, Photos, Videos]

Programming

- Languages: MATLAB, Fortran, J, APL
- Libraries: numpy, dask, pytorch

Indexing Issues

Common indexing issues with arrays

- Mapping coordinates to indexes and vice-versa
- Order of coordinates: (x,y,z) vs. (x,z,y)

Example

I have a 2D array of temperatures [temp] and I want to find the values at Norquest

temp[25,46]

Indexing Issues

temp[25,46]

- 25 and 46 are indices
- the indices maps to physical coordinates
- numpy handles indices not coordinates
- "manual" translation between coords. and indices

Indexing Issues

temp[25,46]

- Which one is which?
- one dimension is longitude, other is latitude
- in numpy, you have to "keep track" of order
- flipping indices will cause issues [wrong/invalid]

Indexing Issues xarray

Python library for managing arrays with 2 main features

- Labeling: Combine arrays with coordinate vectors
- Ecosystem: Integrates with other array libraries

Reduce some of the "manual effort" with array programming

Today's talk only covers a small part of xarray

Image Arrays

Images can be represented as 3D arrays. Here is one way to describe an image.



Dimensions

- Length
- Width
- Colour: Red, Green, Blue

Values

Array values are floats between 0 and 1

Procedural Image Generation

Creating randomly generated images

- 1. Low Resolution Random Noise
- 2. "Smooth" the noise
- 3. Image manipulation [Math on arrays]

Questions?