

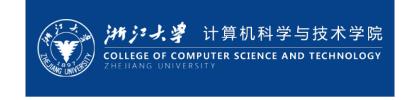


WELCOME TO TUTORIAL

Session 4.1 Janus-FEM: Fast and Accurate Quantum Readout Calibration Using the Finite Element Method







https://janusq.github.io/tutorials/

College of Computer Science and Technology,
Zhejiang University

ASPLOS 2024

Outline of Presentation





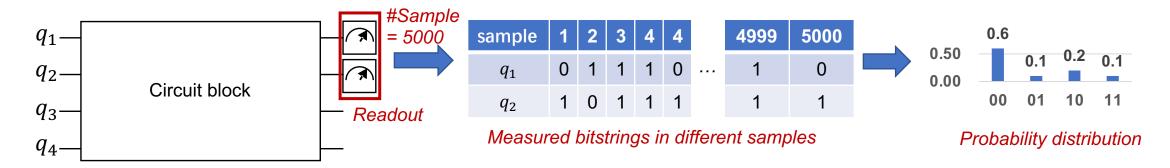
- Background and challenges
- Overview of Janus-FEM
- Janus-FEM Characterization And Calibration
- Experiment
- API Of Janus-FEM

Background





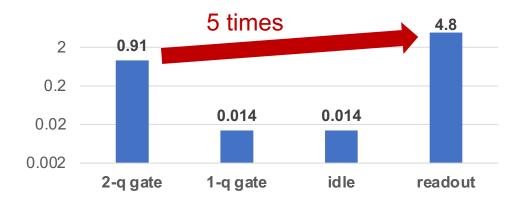
Quantum readout is an operation to read the information from quantum bits to classical bits.



Readout error is significant on current quantum hardware.



Noise on 127-qubit IBM Sherbrooke quantum device



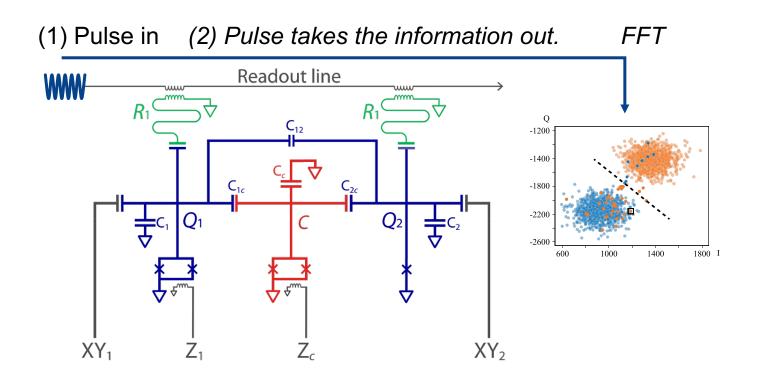
Noise on 10-qubit Tianmu quantum device

Background

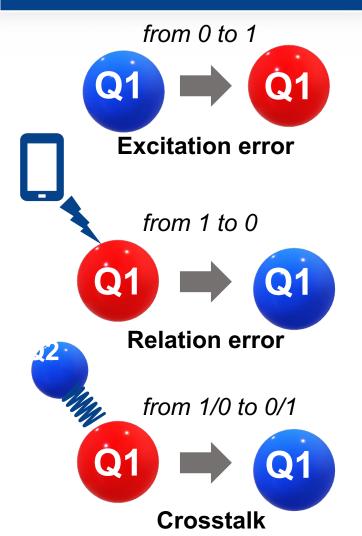




Implementation of readout on superconducting qubits



Source of readout error

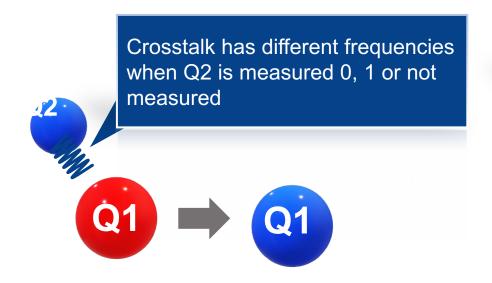


State-dependent Readout Error



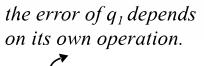


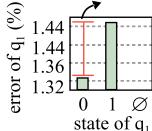
Readout errors vary in different combination of measured qubits

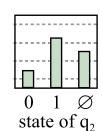


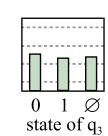
Similar to entanglement

Example of state-dependent and readoutdependent noises on the IBMQ Perth quantum device.

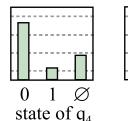


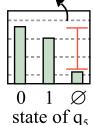






the error also depends on the readout of q_5 .

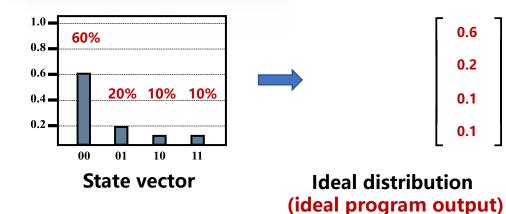




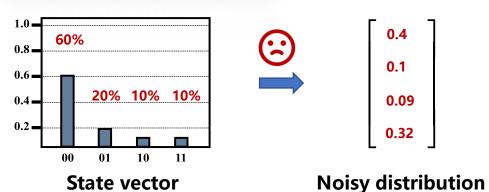
Background



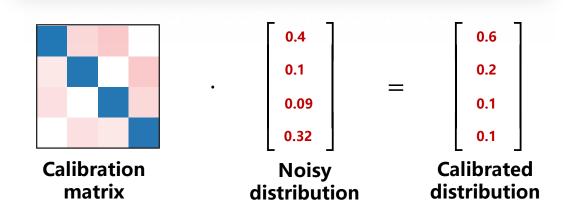
Ideal readout

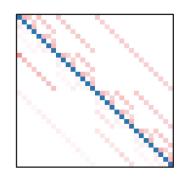


Readout with noise



Matrix-based readout error calibration





The size exponentially increases!

(noisy program output)

Calibration matrix of a 5-qubit readout 25 × 25

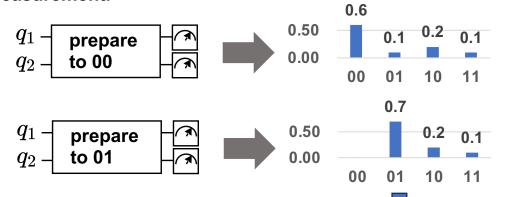
Basic Matrix-based readout calibration





Step 1. Matrix characterization

Prepares qubits to different basis states and apply measurement.



Fill in a noise matrix.

$$M = \begin{bmatrix} 0.6 & 0.1 & 0.2 & 0.1 \\ 0 & 0.7 & 0.6 & 0 \\ 0 & 0.1 & 0.1 & 0.8 \end{bmatrix}$$

Inverse the noise matrix

$$M^{-1} =$$

calibration matrix

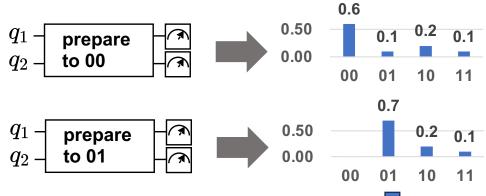
Basic Matrix-based readout calibration





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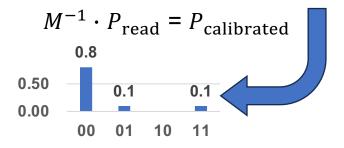
Step 2. Calibration for any input

Represent the measured distribution as a vector.



Apply matrix-vector multiplication.

$$\begin{bmatrix} 0.6 & 0.1 & 0.2 & 0.1 \\ 0 & 0.7 & 0.2 & 0.1 \\ 0.2 & 0.2 & 0.6 & 0 \\ 0 & 0.1 & 0.1 & 0.8 \end{bmatrix}^{-1} \cdot \begin{bmatrix} 0.6 \\ 0.1 \\ 0.2 \\ 0.1 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.1 \\ 0 \\ 0.1 \end{bmatrix}$$



Basic Matrix-based readout calibration





Step 1. Matrix characterization

Prepares qubits to different basis states and apply measurement.

 2^N circuits are executed to measure qubits on all basis states.

Fill in a noise matrix.

The size of the noise matrix is $2^N \times 2^N$.

Inverse the noise matrix

Calcaute the inverse has $O(4^N)$ complexity.

Step 2. Calibration for any input

Represent the measured distribution as a vector.

Transformation has linear complexity.

Apply matrix-vector multiplication.

Multiplication has $\mathcal{O}(4^N)$ complexity.

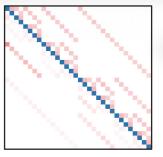
8.8 TB and 10 hours for a 32-qubit calibration on a server with AMD EPYC 2.25GHz 64-core CPUs

Limitations of Current Methods

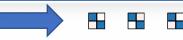




IBU (Google Science 2021) Realizing topologically ordered states on a quantum processor.



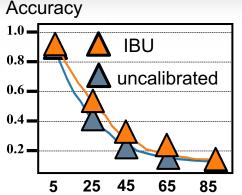
Crosstalk makes the matrix not simple tensor-product result.



Real calibration matrix

Single-qubit matrix

use tensor product of a series of single-qubit metamatrices

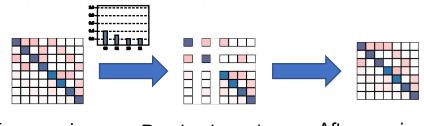


Fail to calibrate on 80-qubit readout output

#qubit

Fast but not accurate: ignore the qubit interactions.

M3 (IBM PRA 2021): Scalable mitigation of measurement errors on quantum computers

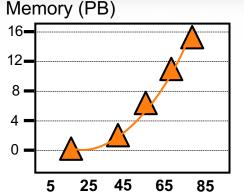


Before pruning

Pruning based on program output

After pruning

use a sparsity-aware method prune the matrix under a threshold of Hamming distance



Require 16PB to calibrate a 85-qubit result.

(4 times the Fugaku supercomputer)

qubit

Accurate but not fast: many matrix elements cannot be ignored

Outline of Presentation





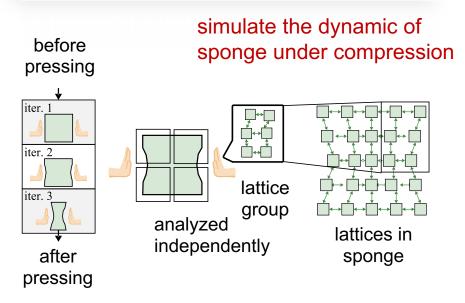
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Calibration based on Finite Element method (FEM)





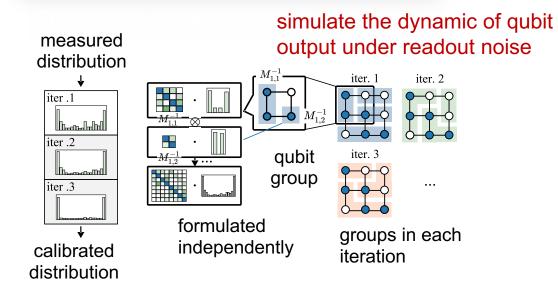
Classical Finite Element Method



- 1 partitions the sponge into lattices
- ② analyzes the state of each lattice independently
- 3 simulate the interaction
- (4) update the state of sponge



Quantum Finite Element Method



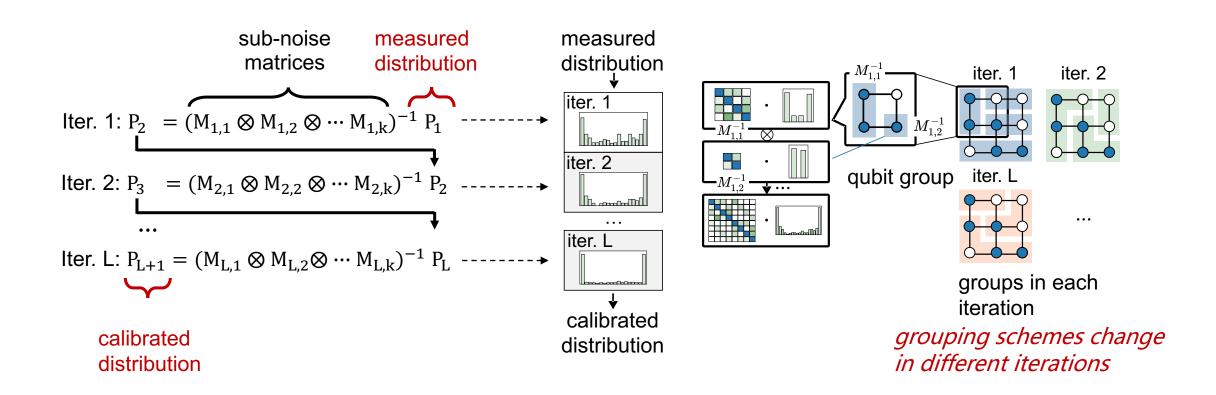
- ① partitions qubits into groups
- 2 analyze the noise in each group independently
- 3 simulate the interaction
- 4 update the calibration result of qubits

A divide-and-conquer strategy to calibrate measured distribution

Calibration formulation



QuFEM reformulates the calibration as an iterative process with a series of sub-noise matrices.



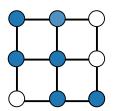
An example



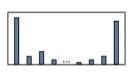


Input:

measured qubits



measured distribution



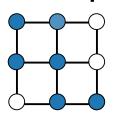
An example



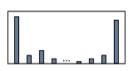


Input:

measured qubits

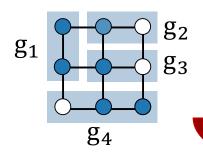


measured distribution

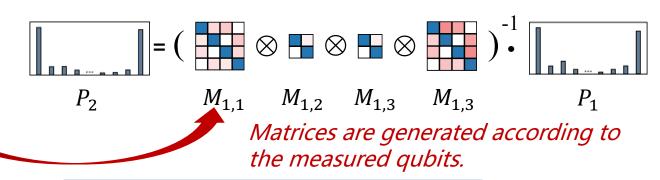


Iteration 1:

grouping scheme



computation formulation



Since crosstalk varies in different combinations of measured qubits

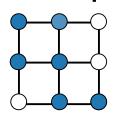
An example



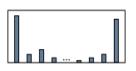


Input:

measured qubits

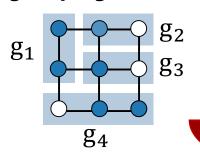


measured distribution

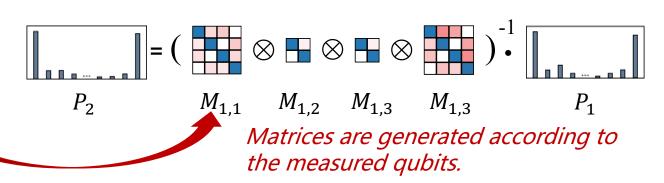


Iteration 1:

grouping scheme

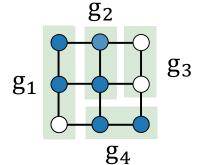


computation formulation

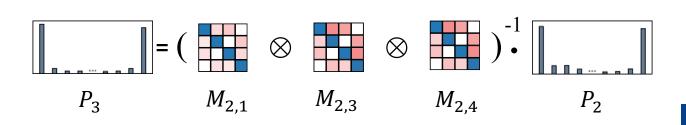


Iteration 2:

grouping scheme



computation formulation



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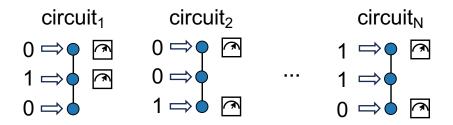




Technique 1: determine the grouping scheme

Data collection

Run benchmarking circuits.



Possible states of a qubit in a benchmarking circuit:

- 0: qubit is set 0 and measured
- 1: qubit is set 1 and measured
- 2: qubit is set 0 or 1 and not measured

Not all qubits are measured to maximize the variety.

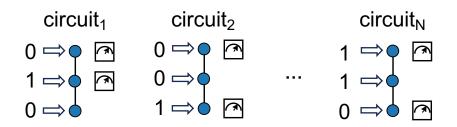




Technique 1: determine the grouping scheme

Data collection

Run benchmarking circuits.



Possible states of a qubit in a benchmarking circuit:

- 1: qubit is set 0 and measured
- 2: qubit is set 1 and measured
- 3: qubit is set 0 or 1 and not measured

Not all qubits are measured to maximize the variety.

Qubit partition

Characterize the **interaction** from one qubit to another qubit under different states:

$$interact(q_i. state = x \rightarrow q_i. state = x)$$

=
$$|P(q_j. error = 1 | C1, C2) - P(q_j. error = 1 | C2)|$$

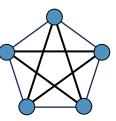
error rate of q_i under C1, C2

average error rate of qzi

C1:
$$q_i$$
. state = x, C2: q_i . state = y

Construct weighted graph





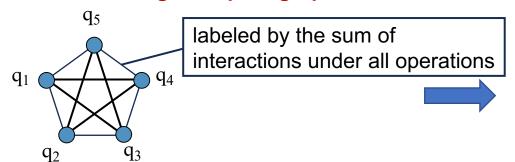




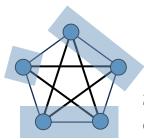
Technique 1: determine the grouping scheme

Qubit partition

Construct a weighted qubit graph:



Partitions with a **MAX-CUT solver**:



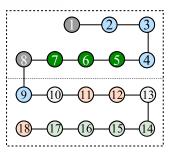
try to comprehensively capture the interactions between qubits

An Example

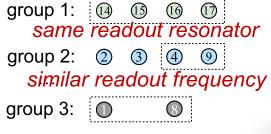
Prior knowledge of hardware helps grouping

Readout resonator 1

Readout resonator 2



18-qubit topology



overlapping frequency shift region

- demonstrated in the results from other quantum devices
- can be used as prior knowledge to facilitate the partition.





Technique 2: sub-noise matrix generation

Perform matrix-vector multiplication

Iter. i:
$$P_{i+1} = (M_{i,1} \otimes M_{i,2} \otimes \cdots M_{i,k})^{-1} P_i$$

Matrix generation

Noise matrix formulates the transformation probability from the ideal state to measured state.

									sets	state	$\overline{}$
								00	01	10	11
			0.]				00	0.6	0	0.1	0
$\begin{bmatrix} 0.1 \\ 0.2 \end{bmatrix}$	0.7 0.2	0.2 0.6	0.1	=	read state		01	0.1	0.7	0.2	0.1
$\begin{bmatrix} 0.2 \\ 0.1 \end{bmatrix}$	0.1	0.1	0.8		state		01	0.2	0.2	0.6	0.1
						l	11	0.1	0.1	0.1	8.0





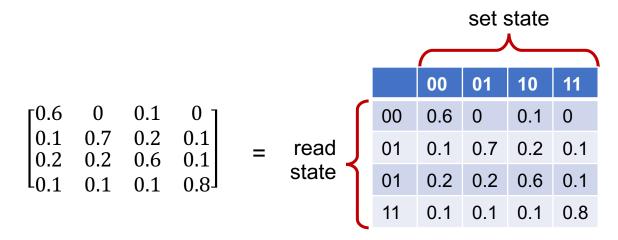
Technique 2: sub-noise matrix generation

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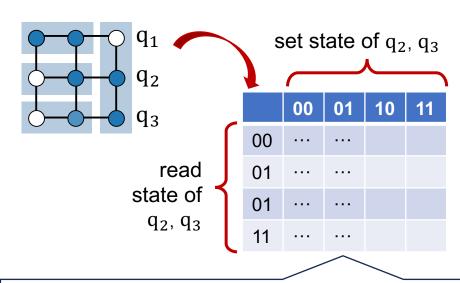
Iter. i:
$$P_{i+1} = (M_{i,1} \otimes M_{i,2} \otimes \cdots M_{i,k})^{-1} P_i$$

Matrix generation

Noise matrix formulates the transformation probability from the ideal state to measured state.



Sub-noise matrices of QuFEM formulates the transformation probability of states inside the qubit groups.



$$M[x][y]=$$
 $P(\{q_2, q_3\}. read = x | \{q_2, q_3\}. set = y, q_1 = 2)$

Transformation probability when q_1 is not measured

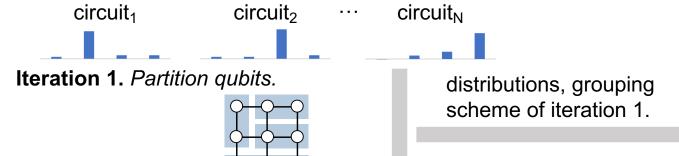
Put all together





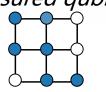
Characterization

Iteration 1. Run benchmarking circuits.



Calibration

Input. measured qubits measured distribution





Iteration 1. Generate sub-noise matrices.









Iteration 1. Calibrate.



Iteration 1. Calibrate.



distributions, grouping scheme of iteration 2.

Iteration 2. Generate sub-noise matrices.







Iteration 2. Calibrate.



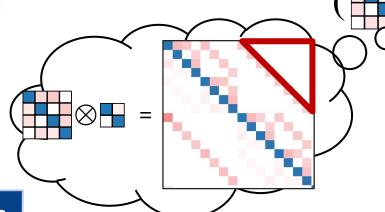
2

Sparse Tensor-Product Engine





Observation



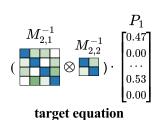
A large number of sparse intermediate vectors is generated in the tensor-product.

Implementation

Use a key-value table to store sparse vector

Calculate the tensor product

Aggregate the tensorproduct result



х	prob.	1		value	2		value	
$P_1(000)$	0.47	→	00	0.50	\otimes	0	0.99	• 0.47 =
$P_1(011)$	0.53		01	-0.02		1	0.01	
			10	0.01				•
			11	0.01			3	$value \le \beta$

For each basis states

- ① calculate the matrix-vector multiplication
- ② calculate the tensor-product
- 3 prune intermediate values
- 4 sum intermediate values to obtain output.

1		value	(4)	X	prob.
	000	0.49	$\rightarrow \tilde{\Sigma} \rightarrow$	$P_2(000)$	0.48
	001	0.01	/	$P_2(001)$	6×10 ⁻³
	010	-0.01		$P_2(010)$	6×10 ⁻³
	100	0.01		$P_2(011)$	0.50
	101	10-4		$P_2(111)$	6×10 ⁻³
	110	10-4-		1 2(111)	010

Prune values < threshold (e.g., 10⁻⁵)

Compute the tensor-product of other basis states

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Experiment



Setup

Platform	#Qubits	1-q fidelity	2-q fidelity	Instructions
Ourfu	136	94.6±3.1%	94.6±3.0%	ID,RX,RY,RZ,H,CX
Quafu	18	95.9±1.3%	95.9±1.3%	ID,RX,RY,RZ,H,CX
Rigetti	79	99.5±1.1%	90.0±6.4%	CPHASE,XY
Self-developed	36	99.9±0.1%	98.7±0.8%	U3,CZ
IBMQ	7	99.9±0.1%	99.2±0.1%	CX,ID,RZ,SX,X

Evaluated hardware

IBU: KJ Satzinger, et al. Realizing topologically ordered states on a quantum processor. Science 2021

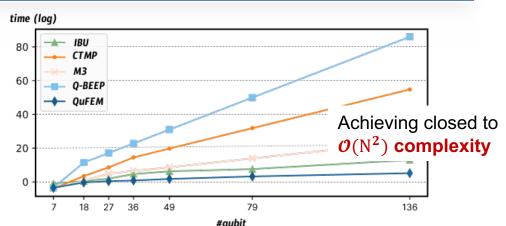
CTMP: Sergey, et al. Mitigating measurement errors in multiqubit experiments. PRA 2021.

M3: Paul D Nation, et al. Scalable mitigation of measurement errors on quantum computers. PRX Quantum 2021.

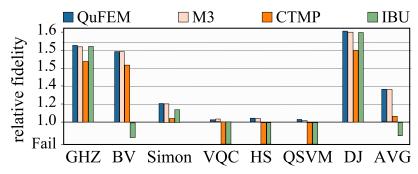
Q-BEEP: Nathan Wiebe, et al. QBEEP: Quantum Bayesian error mitigation employing Poisson modeling over the hamming spectrum. ISCA 2023.

Baselines

Result



QuFEM reduces the calibration time of the 136-qubit program output from 119.44 hours (IBU) to 169.65 seconds (119.44 \times reduction).



QuFEM shows an average improvement in relative fidelity of 1.003×, 1.2×, and 1.4× compared to M3, CTMP, and IBU, respectively.

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API Of Janus-FEM





File:

- examples/3-2.readout_calibration_realqc.ipynb
- https://janusq.github.io/tutorials/Demonstrations/3-2.readout_calibration_realqc

```
from janusq.optimizations.readout_mitigation.fem import Mitigator
                               from giskit.guantum info.analysis import hellinger fidelity
    Import package
                               from janusq.optimizations.readout_mitigation.fem.tools import npformat_to_statuscnt
    and data
                               from janusq.dataset import protocol_8 as benchmark_circuits_and_results, ghz_8qubit as
                                ghz_output
                                qubits = 8
 Construct mitigator = Mitigator(qubits, n_iters = 2)
scores = mitigator.init(benchmark_circuits_and_results, group_size = 2,multi_process=False,
draw_grouping = True)
Calibrate GHz circuit output

output

n_qubits = 4
outout_ideal = {'1'*n_qubits:0.5,'0'*n_qubits:0.5}
output_fem = mitigator.mitigate(ghz_output[0],[i for i in range(n_qubits)], cho = 1)
                                output_fem = npformat_to_statuscnt(output_fem)
                               print("Janus-FEM fidelity: ",hellinger_fidelity(outout_ideal,output_fem))
```



Thanks for listening

Janus-FEM: Fast and Accurate Quantum Readout Calibration Using the Finite Element Method

Siwei Tan, Liqiang Lu*, Hanyu Zhang, Jia Yu, Congliang Lang, Yongheng Shang, Xinkui Zhao, Mingshuai Chen, Yun Liang, and Jianwei Yin*