

Assignment-1

Solve problem using Naïve bayes theorem:-

Given-

Given Birth	Can fly	live in water	have legs	class
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$$P(\text{class} / \text{attributes}) = \frac{P(\text{attributes} | \text{class}) \times P(\text{class})}{P(\text{attributes})}$$

Probabilities for each class label-

$$P(\text{mammals}) = \frac{\text{no. of mammals}}{\text{total no. of instances}}$$

$$P(\text{non mammals}) = \frac{\text{no. of non mammals}}{\text{total no. of instances}}$$

$$P(\text{attributes} / \text{class}) = \frac{\text{no. of instance with attribute \& class}}{\text{total no. instance with class}}$$

Given birth: yes, Can fly: no, live in water: yes,
have legs: yes

Probabilities (Conditional)

$$P(\text{given birth: yes} / \text{mammals}) = \frac{6}{7}$$

$$P(\text{can fly: no} / \text{mammals}) = \frac{5}{7}$$

$$P(\text{live in water: yes} / \text{mammals}) = \frac{2}{7}$$

$$P(\text{have legs: yes} / \text{mammals}) = \frac{5}{7}$$

$$P(\text{given birth: yes} / \text{non mammals}) = \frac{1}{13}$$

$$P(\text{can fly: no} / \text{non mammals}) = \frac{10}{13}$$

$$P(\text{live in water: yes} / \text{non mammals}) = \frac{3}{13}$$

$$P(\text{have legs: yes} / \text{non mammals}) = \frac{9}{13}$$

$$\text{Prior probability of mammals} = \frac{7}{20}$$

$$\text{Prior probability of non mammals} = \frac{15}{20}$$

Probabilities of "mammals" class

$$1) P(\text{mammals} / \text{attributes}) = P(\text{given birth: yes} / \text{mammals}) \times P(\text{can fly: no} / \text{mammals}) \times P(\text{live in water: yes} / \text{mammals}) \times P(\text{have legs: yes} / \text{mammals})$$

$$\begin{aligned}
 & \times P(\text{mammals}) \\
 &= \frac{6}{7} \times \frac{5}{7} \times \frac{32}{7} \times \frac{5}{7} \times \frac{7}{20} \\
 &= 0.04
 \end{aligned}$$

2] for "non mammals" class

$$\begin{aligned}
 & P(\text{non mammals/attributes}) = P(\text{given birth: yes/non mammals}) \\
 & \quad \times P(\text{can fly: no/non mammals}) \\
 & \quad \times P(\text{live in water: yes/non mammals}) \times P(\text{have legs: yes/non mammals}) \times P(\text{non mammals}) \\
 &= \frac{1}{13} \times \frac{10}{13} \times \frac{3}{13} \times \frac{9}{13} \times \frac{13}{20} \\
 &= 0.006
 \end{aligned}$$

\therefore Probability of Mammals is greater = 0.04