

Q1. Derive the Laplace transform of the periodic function shown in Fig 1.

[4 M]

Q2. Derive the expression for finding the time constant of the liquid level system shown in Fig 2 with variable cross sectional area. The resistance R is linear. The tank has three vertical walls and one which slopes at an angle α from the vertical as shown. The distance separating the parallel walls is w .

[4 M]

Q3. Consider a two-tank interacting system as shown in Fig 3 where R_1 is a nonlinear resistance and R_2 is a linear resistance. The valve characteristic for R_1 is $q_1 = 4\sqrt{h_1 - h_2}$. (a) Write the balances for each tank and derive the general expression for overall transfer function $\frac{H_2(s)}{Q(s)}$. (b) Determine $H_2(t)$ for a unit step change in $Q(t)$, assuming $A_1 = A_2 = 1$ and $R_1 = R_2 = 1$.

[12 M]

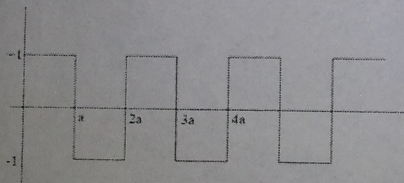


Fig 1. Periodic function

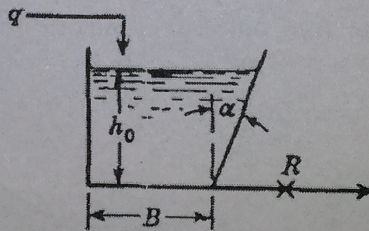


Fig 2. Liquid level system

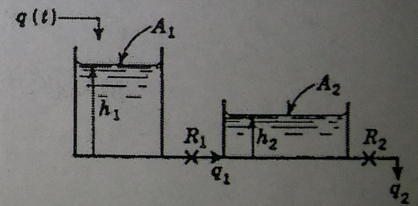


Fig 3. Two-tank interacting system