## TTL773: Design of Experiments and Statistical Techniques Minor Test 2

## Maximum Marks = 25

Date: March 22, 2015, Sunday

Time: 1 pm - 2 pm

Venue: IVLT3

## Answer all questions.

1) If the results of a one-factor-at-a-time experiment indicate that  $A^+B^-$  and  $A^-B^+$  give better response than  $A^-B^-$  then  $A^+B^+$  always gives even better response. Do you think that this statement is correct? If yes, why? If not, why not? Use numerical data for your reason. (2)

2) The  $R^2$  between the experimental data of a  $2^2$  factorial design with one replicate and the data predicted by a first order model of the form  $(y = \beta_0 + \beta_1 x_1 + \beta_2 x_2)$  is 0.90. Calculate  $R_{adj}^2$ . (3)

3) A 2<sup>2</sup> factorial experiment is conducted with two blocks and the design is replicated twice. Subsequently, the following two tables are prepared for analyzing the variances. Which of the two tables is correct and why?

(6)

Table 1

Sources of variation	Degrees of freedom		
Factor A	1		
Factor B	1		
Blocks (AB)			
Error	7		
Total			

Table 2

Sources of	Degrees of			
variation	freedom			
Factor A	1 1 3			
Factor B				
Blocks				
Error	2			
Total	7			

4) A 22 factorial experiment is carried out in three blocks and the results are shown below. Calculate the

sum of squares due to block.

(3)

Block 1
(1) = 28
a = 36
b = 18
ab = 31

Block 2  
(1) = 25  

$$a = 32$$
  
 $b = 19$   
 $ab = 30$ 

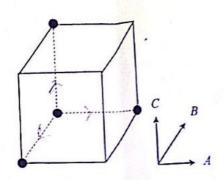
Block 3
$$(1) = 27$$

$$a = 32$$

$$b = 23$$

$$ab = 29$$

5) Somebody claims that a  $2_{111}^{3-1}$  fractional factorial design, with generating relation I = -ABC, looks like



where • refers to the design point. Do you support the claim? If yes, why? if not, why not and sketch the correct design?

(3)

6) In a 23 factorial experiment, the blocks are designed as follows.

Block 1: (1), b, ac, abc

Block 2: a, ab, c, bc

Identify the confounded effect.

(3)

7) The quantity of adhesive formed on a gummed meterial is determined under a factorial experiment with three levels of humidity and three levels of temperature. Four readings are made under each set of conditions. The resulting ANOVA table is shown below.

Sources of variation	Sum of squares	Degree of freedom	Mean square	F-value (calculated)	F-value at $\alpha = 0.05$	Significant (Write Yes or No)
Humidity	9.07					
Temperature	8.66	7 T B				
Humidity × Temperature	6.07		list.			
Error						
Total	52.30	1 - 7.				

Complete this table.

(5)