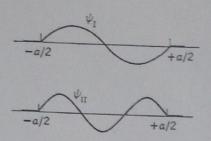
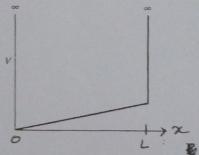
Duration: 60 Minutes

Q.1. (a) Two possible eigenfunctions for a particle moving freely in a region of length 'a', but strictly confined to that region, are shown in the figure below. When the particle is in the state corresponding to the eigenfunction  $\psi_l$ , its total energy is 4 eV. (i) What is its total energy in the state corresponding to  $\psi_{II}$ ? (ii) What is the lowest possible total energy for the particle in this system?



(b) Sketch the possible wave function of a particle in the potential well shown in the figure below. Justify/explain the sketched wavefunction.



Q.2. (a) Which one of the following will exert the greatest and the least pressure at the same temperature?

(i) A gas of classical molecules Justify your answer.

(ii) A gas of bosons

(iii) A gas of fermions

- (b) Why the electronic contribution to the specific heat is detectable only at very low and high temperatures?
- Q.3. (a) Find the ratio between the kinetic energies of an electron in a two dimensional square lattice which has  $k_x = k_y = \pi/a$  and an electron which has  $k_x = \pi/a$ ,  $k_y = 0$ .

(b) State two conditions under which Fermi-Dirac and Bose-Einstein distributions go over to Maxwell- Boltzmann distribution.

(c) Draw N(E) versus E cuves for of one and two dimensional systems.

[2+2+1]

Q.4.(a) How does the energy-band structure of a solid determine whether it is a conductor, a semiconductor or an insulator?

(b) Represent a monovalent metal, a divalent metal and an insulator in k-space corresponding to a