Marks will not be awarded if appropriate arguments are not provided.

Do not write the questions before answering them.

Do not waste time describing what is not asked.

Maximum Marks: 25

 $W_1 + W_2 = \{u + v \in V : u \in W_1, v \in W_2\}.$ 

$$\dim V = 4$$
,  $\dim W_1 = \dim W_2 = 3$ ,  $\dim (W_1 \cap W_2) = 1$ .

 $X = \{u, u + v, u + v + w\}$  and  $Y = \{v, v + w, u + v - w\}$ Show that if X is linearly independent then Y is linearly independent. Suppose V is a vector space over  $\mathbb{R}$  and  $u, v, w \in V$ . Let

Find a basis of the range space of the linear transformation  $T: \mathbb{R}^4 \to \mathbb{R}^5$  defined by T(x, y, z, w) = (x + y + z + w, x - y + z + 2w, 2y + z, 2y - w, z + w). (4) (4) Suppose  $T: \mathbb{R}^2 \to \mathbb{R}^2$  is a linear tranformation. Is it possible to have the following T(1,1) = (1,0); T(2,3) = (1,2); T(3,2) = (2,1).

(b) Find a linear transformation  $T: \mathbb{R}^2 \to \mathbb{R}^2$  such that the null space of T and the range space of T are the same (i.e.,  $\ker T = T(\mathbb{R}^2)$ ).

Consider the following system of four equations in four unknowns x, y, z, w:

$$x + y + z + w = 4$$

$$x + 2y + 3z + 4w = 3$$

$$x + y + 2z = 6$$

$$y + 9z + aw = b$$

- Apply suitable elementary row operations on the augmented matrix of this system to
- Using part (a) find all possible  $a, b \in \mathbb{R}$  such that the system has i) no solutions, ii) unique solution, iii) infinitely many solutions.
- a solution)

- ( Back) -

::: END :::

T(2(@10)=0) TANS= DEATH 1) TO

Nothing - RETITION

Cretory =0