

Computer Vision 1

The background is a dark blue gradient with a faint grid. On the right side, there are several concentric circles and arcs in a lighter blue color. Some of these are solid, while others are dashed. On the left side, there are some horizontal lines with arrowheads pointing to the right, and a few small white dots. The overall aesthetic is technical and futuristic.

THEO GEVERS

MASTER AI

UNIVERSITY OF AMSTERDAM

Lectures/Theory

- 06-02-2018, 17:00-19:00, C0.05, **Introduction** (*Szeliski 1*)
- 13-02-2018, 17:00-19:00, C0.05, **Image Formation** (*Szeliski: 2.1.1 + 2.1.2 + 2.2 + 2.3.2 + 2.3.3*)
- 20-02-2018, 17:00-19:00, C0.05, **Color and Image Processing** (*Szeliski: 3.1 + 3.2 + 3.3*)
- 27-02-2018, 17:00-19:00, C0.05, **Feature Detection, Motion and Classification** (*Szeliski: 4, 8.1.1 + 8.1.3 + 8.2.1 + 8.4; Bengio: 4 + 5.1 + 5.2 + 5.3 + 5.7 + 5.8 + 5.9*)
- 06-03-2018, 17:00-19:00, C0.05, **Object Recognition: BoW and ConvNets** (*Szeliski: 5.1.1 + 5.1.4 + 5.1.5 + 5.2 + 5.3 + 5.4, 6.1 + 6.3, 14.1 + 14.2.1 + 14.3 + 14.4.1; Bengio: 7.2 + 7.4 + 9.1 + 9.2 + 9.3*)
- 13-03-2018, 17:00-19:00, C0.05, **Deep Learning, Stereo and 3D Reconstruction** (*Szeliski: 11.1 + 11.2 + 11.3 + 11.4, 12.1 + 12.2; Bengio: 12.1 + 12.2*)
- 20-03-2018, 17:00-19:00, C0.05, **Applications** (*Szeliski: 12.6.2 + 12.6.3 + 12.2.4*)
- 26-03-2018, Monday, 9:00-12:00, **Written Exam**

Today's class: Image Formation

1. Projective Geometry and Camera Models

2. Light and Color Models

3. Reflection Models

Including slides from Derek Hoiem, Alexei Efros, Steve Seitz, and David Forsyth, James Hays, Jinxiang Chai

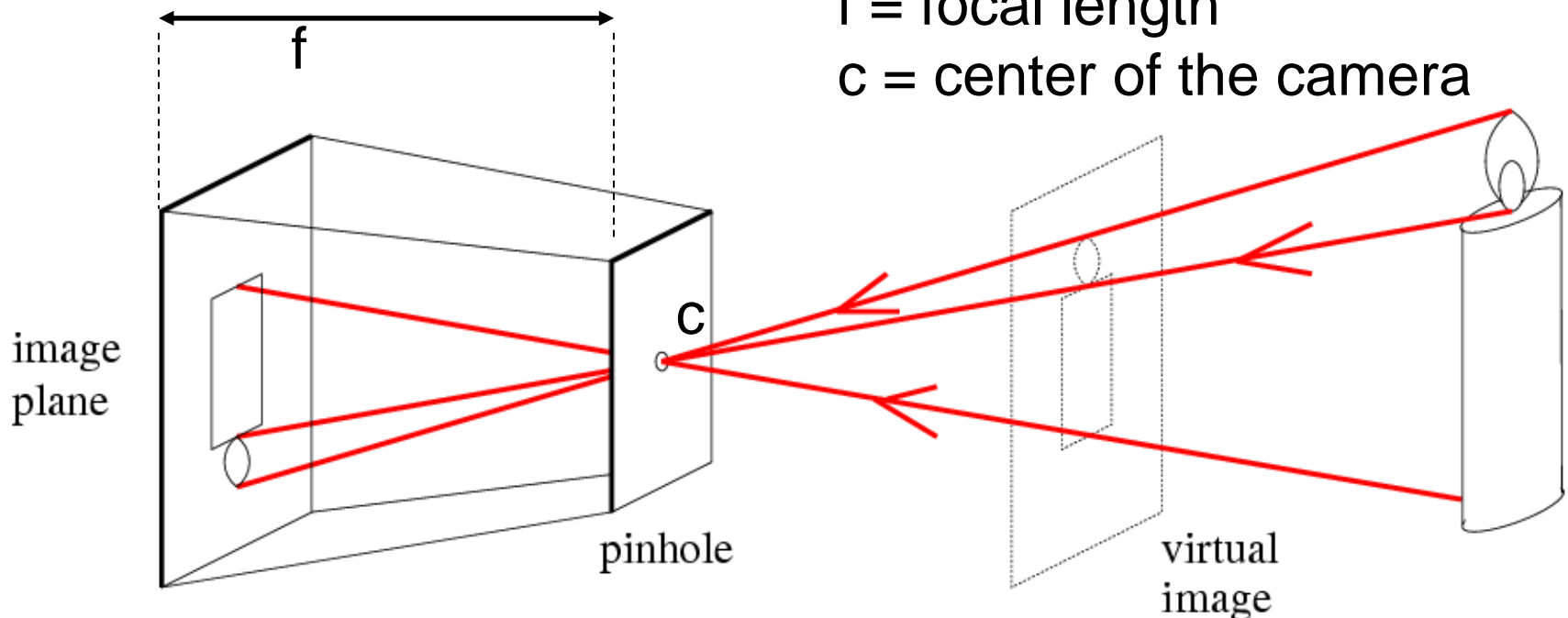
Image formation

- There are two parts to the image formation process:
 - The **geometry of image formation**, which determines where in the image plane the projection of a point in the scene will be located.
 - The **physics of light**, which determines the brightness of a point in the image plane as a function of illumination and surface properties.

Pinhole Camera

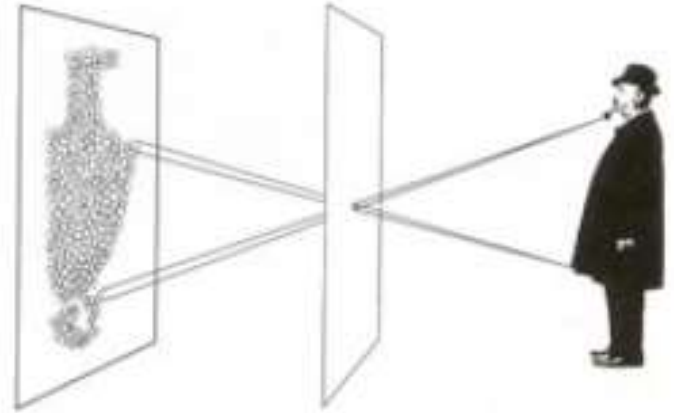
- Abstract camera model - box with a small hole in it
- The simplest device to form an image of a 3D scene on a 2D surface.
- Rays of light pass through a "pinhole" and form an inverted image of the object on the image plane.
- Pinhole cameras work in practice

f = focal length
 c = center of the camera

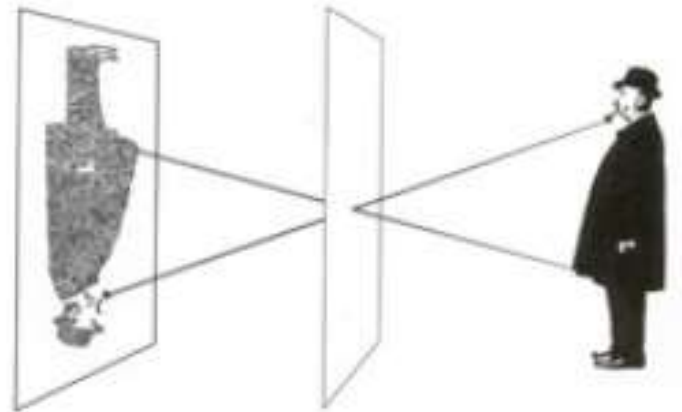


Effect of Aperture Size

- Large aperture: light from the source spreads across the image (i.e., not properly focused), making it **blurry**!



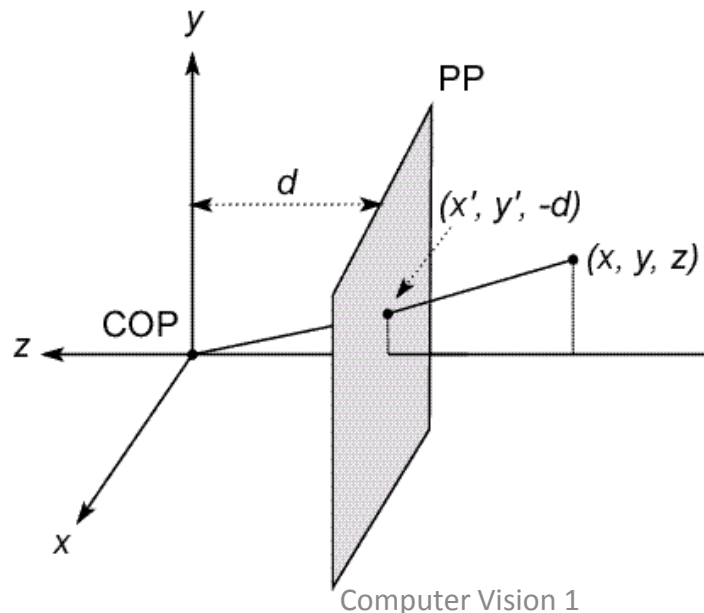
- Small aperture: reduces **blurring** but (i) it limits the amount of light entering the camera and (ii) causes light **diffraction**.



Modeling Projection: 3D->2D

The coordinate system

- We will use the pin-hole model as an approximation
- Put the optical center (**C**enter **O**f **P**rojection) at the origin
- Put the image plane (**P**rojection **P**lane) *in front* of the COP
- The camera looks down the *negative z axis*



Modeling Projection: 3D->2D

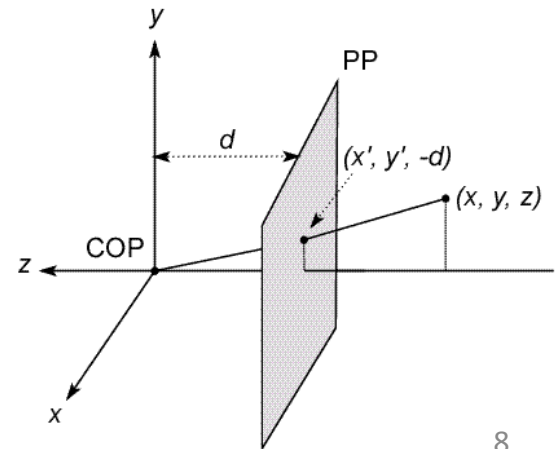
Projection equations

- Compute intersection with PP of ray from (x,y,z) to COP
- Derived using similar triangles

$$(x, y, z) \rightarrow \left(-d\frac{x}{z}, -d\frac{y}{z}, -d\right)$$

- We get the projection by throwing out the last coordinate:

$$(x, y, z) \rightarrow \left(-d\frac{x}{z}, -d\frac{y}{z}\right)$$



Perspective Projection

Projection is a matrix multiply using homogeneous coordinates:

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1/d & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ y \\ -z/d \end{bmatrix} \Rightarrow \left(-d\frac{x}{z}, -d\frac{y}{z}\right)$$

divide by third coordinate

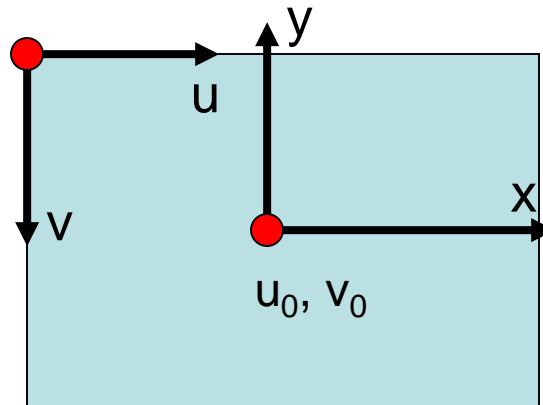
- This is known as **perspective projection**
 - The matrix is the **projection matrix**
 - Can also formulate as a 4x4

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -1/d & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \\ -z/d \end{bmatrix} \Rightarrow \left(-d\frac{x}{z}, -d\frac{y}{z}\right)$$

divide by fourth coordinate

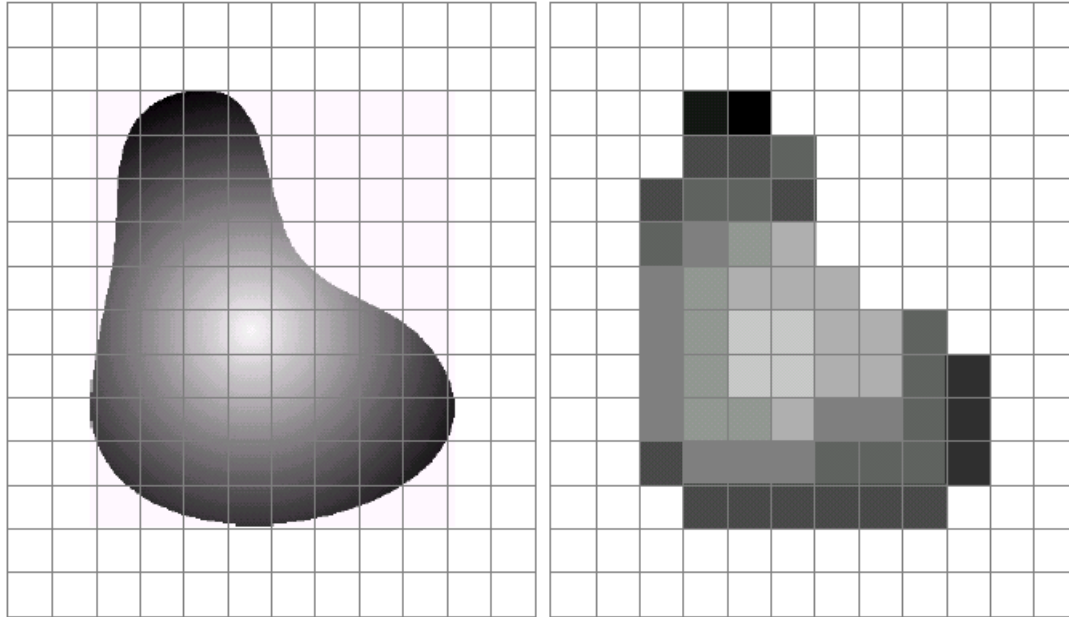
Viewport Transformation

From projection coordinate to image coordinate



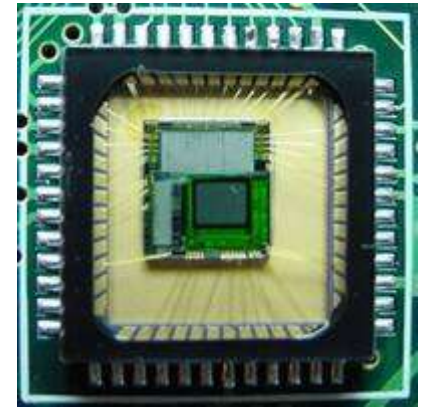
$$\begin{pmatrix} u \\ v \\ 1 \end{pmatrix} \longleftrightarrow \begin{bmatrix} s_x & 0 & u_0 \\ 0 & -s_y & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$$

Sensor Array



a b

FIGURE 2.17 (a) Continuous image projected onto a sensor array. (b) Result of image sampling and quantization.



CMOS sensor

Putting It Together

From world coordinate to image coordinate

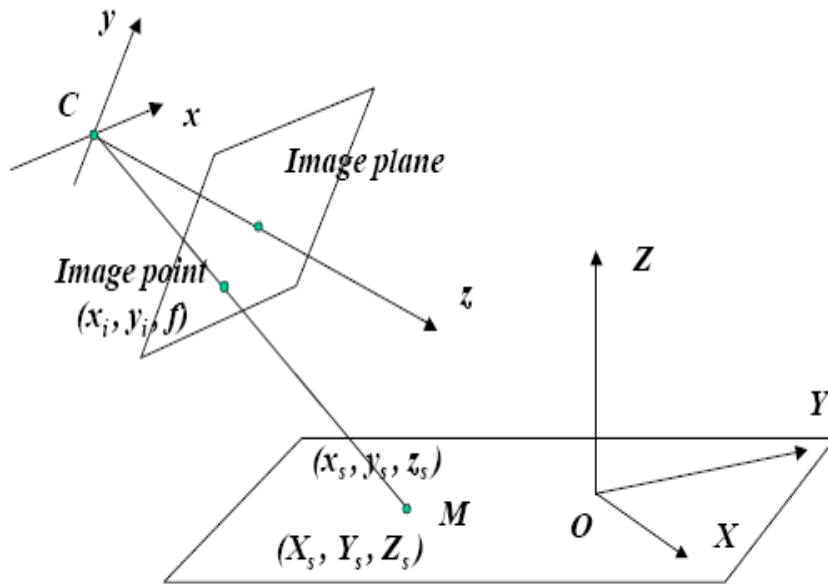
	Viewport projection	Perspective projection	View transformation
$\begin{bmatrix} u \\ v \\ 1 \end{bmatrix}$	$\begin{bmatrix} s_x & 0 & u_0 \\ 0 & -s_y & v_0 \\ 0 & 0 & 1 \end{bmatrix}$	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1/d & 0 \end{bmatrix}$	$\begin{bmatrix} \mathbf{R} & \mathbf{T} \\ \mathbf{0}_3^T & 1 \end{bmatrix} \begin{bmatrix} X_S \\ Y_S \\ Z_S \\ 1 \end{bmatrix}$
	Image resolution, aspect ratio	Focal length	The relative position & orientation between camera and objects

Camera Parameters

$$\begin{bmatrix} u \\ v \\ 1 \end{bmatrix} \longleftrightarrow \underbrace{\begin{bmatrix} s_x & 0 & u_0 \\ 0 & -s_y & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1/d & 0 \end{bmatrix}}_{\text{Intrinsic camera parameters}} \underbrace{\begin{bmatrix} \mathbf{R} & \mathbf{T} \\ \mathbf{0}_3^T & 1 \end{bmatrix}}_{\text{extrinsic camera parameters}} \begin{bmatrix} X_S \\ Y_S \\ Z_S \\ 1 \end{bmatrix}$$

View Transformation

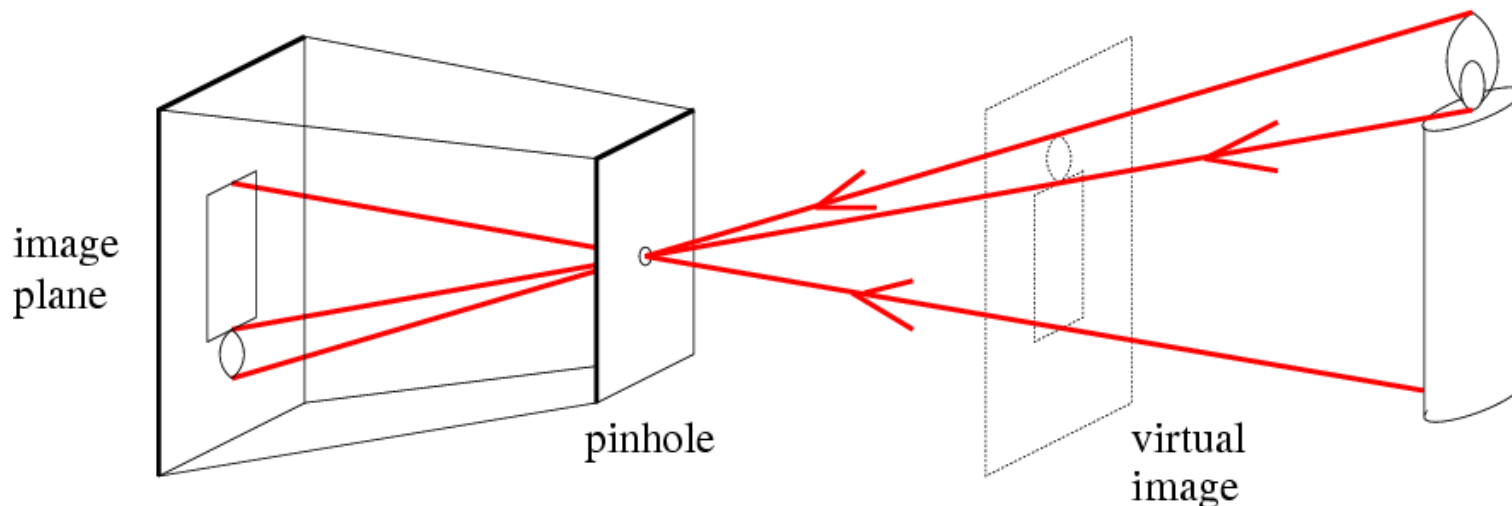
From world coordinate to camera coordinate



$$\begin{bmatrix} x_s \\ y_s \\ z_s \\ 1 \end{bmatrix} = \begin{bmatrix} \mathbf{R} & \mathbf{T} \\ \mathbf{0}_3^T & 1 \end{bmatrix} \begin{bmatrix} X_s \\ Y_s \\ Z_s \\ 1 \end{bmatrix}$$

Things to Remember

- Pinhole camera model and camera matrix



$$\begin{bmatrix} u \\ v \\ 1 \end{bmatrix} \longleftrightarrow \begin{bmatrix} s_x & 0 & u_0 \\ 0 & -s_y & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1/d & 0 \end{bmatrix} \begin{bmatrix} x_s \\ y_s \\ z_s \\ 1 \end{bmatrix}$$

Today's class: Image Formation

1. Projective Geometry and Camera Models

2. Light and Color Models (Reading 2.3, paper on color models)

3. Reflection Models

Including slides from Derek Hoiem, Alexei Efros, Steve Seitz, and David Forsyth, James Hays, Jinxiang Chai

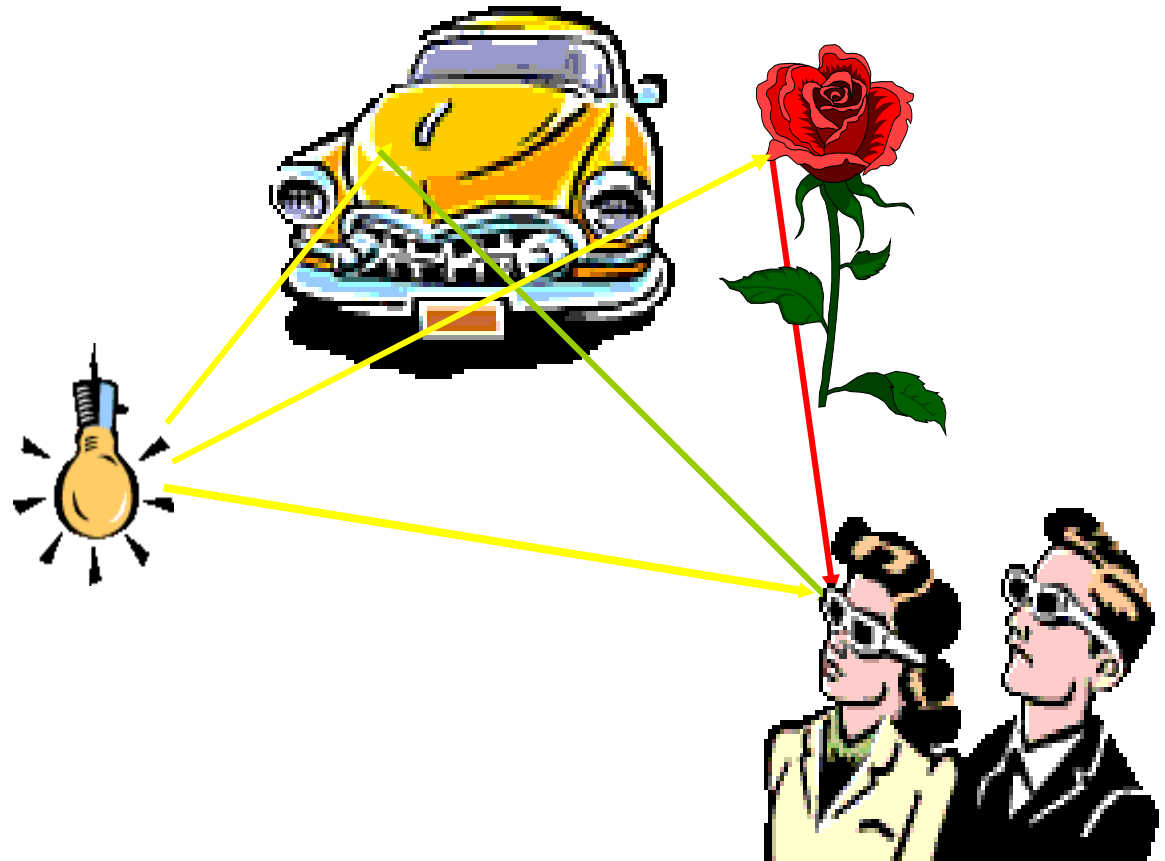
What makes an image?

the triplet light-objects-observer
















Light source

Object(s)

Sensor



Diffuse Reflection

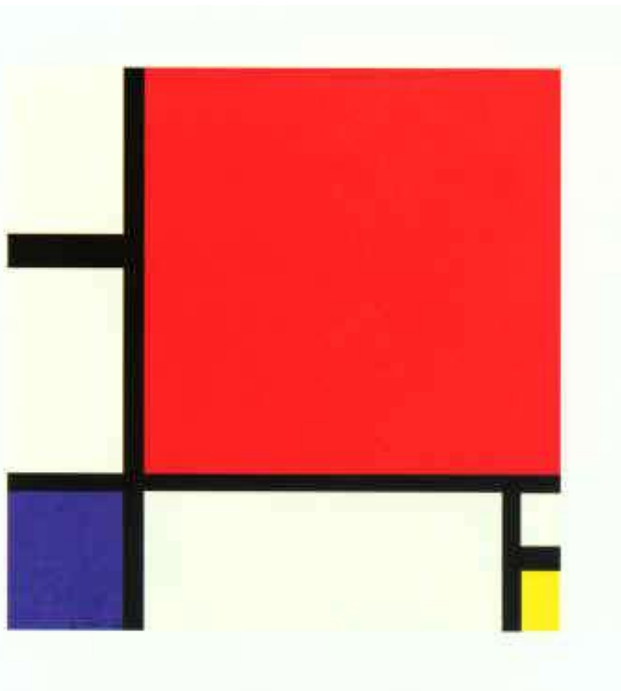
Input Image	Albedo	Lighting	Surface Normals	Reconstruction
				
				
				



The science of Light and Colour

Fundamentals of colour science

Hall of fame



Mondrian

Pythagoras: undulation theory

Aristoteles: curpus theory

Newton 1665 "Opticks"

Planck, Einstein and Bohr "Quantum mechanics"

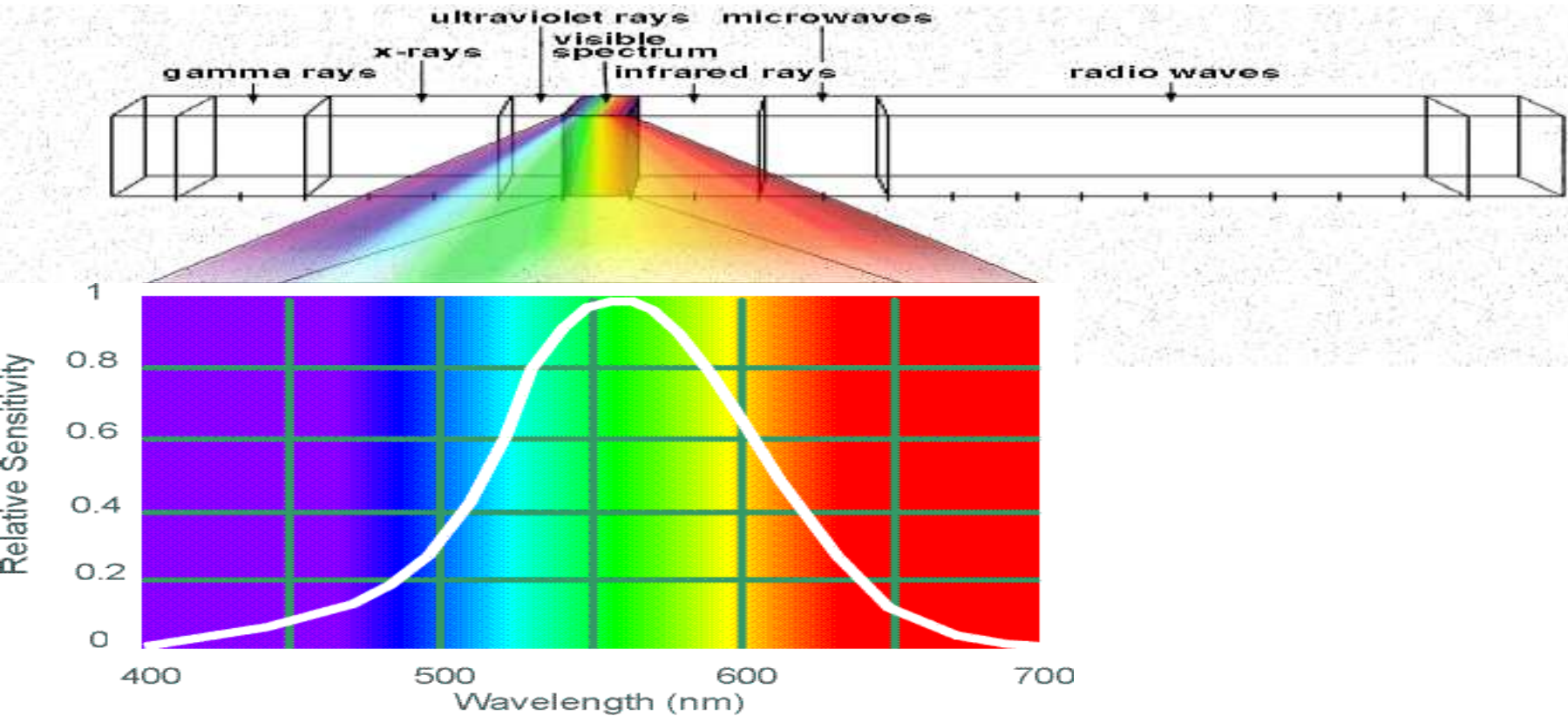
Goethe 1840 "Farbenlehre"

Munsell 1905 "A Colour Notation"

Descartes, Schopenhauer,

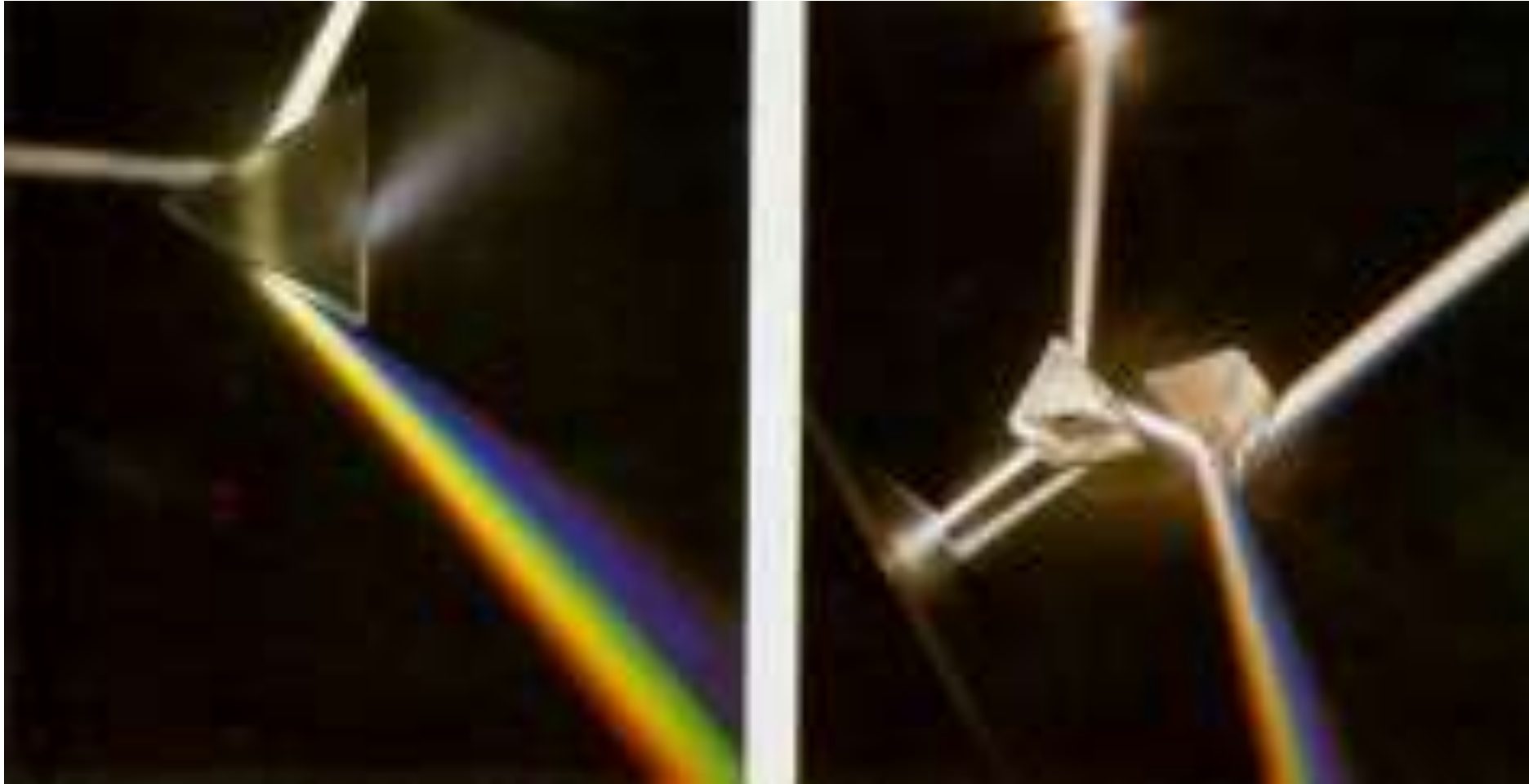
Hegel, Wittgenstein...and many others

Electromagnetic Spectrum



Human Luminance Sensitivity Function

Electromagnetic Spectrum

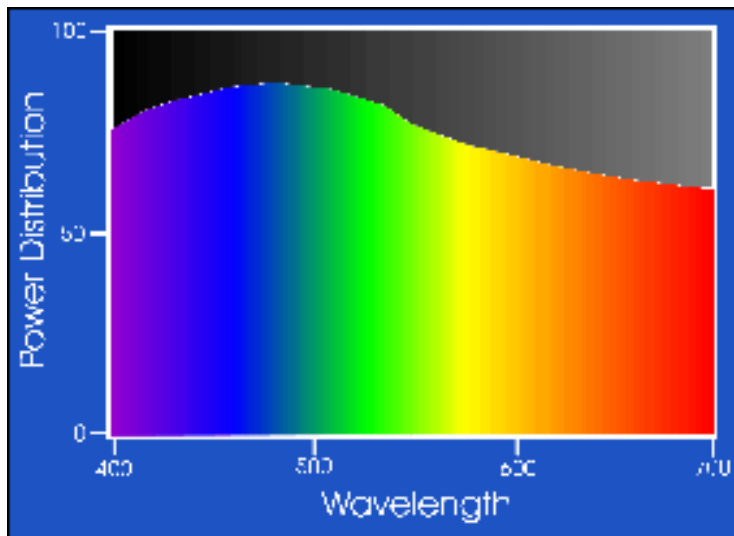


Spectral Power Distribution

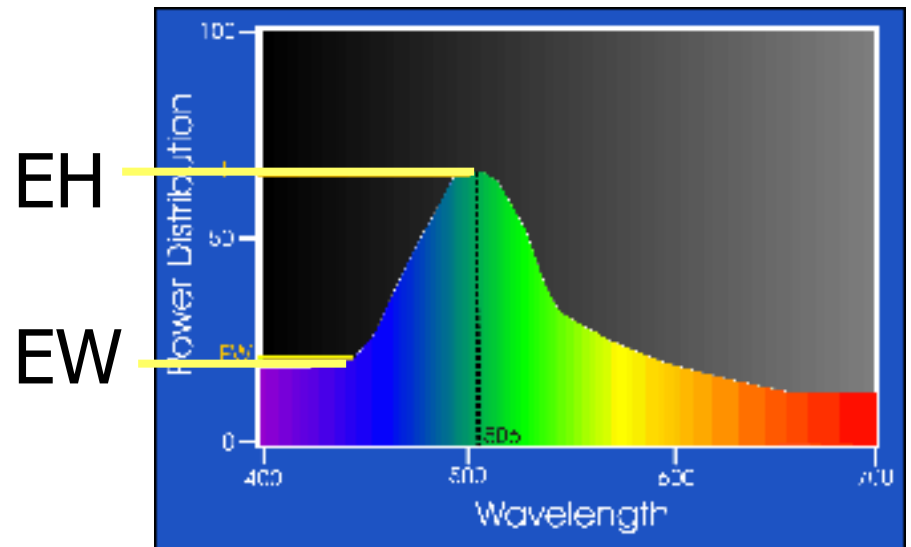
Hue: dominant wavelength of the SPD: EH

Saturation: purity of the colour: EH-EW

Intensity: brightness of the colour: EW



White light



Green light

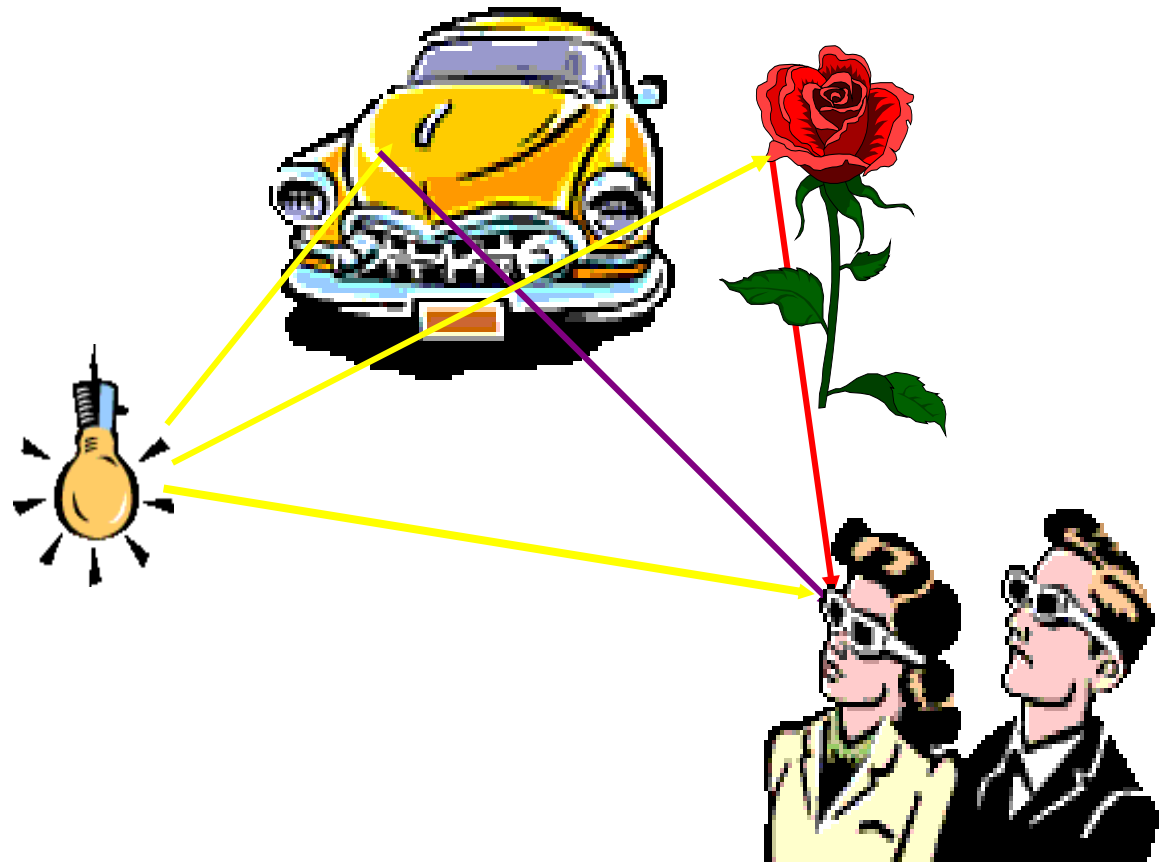
What makes an image?

the triplet light-objects-observer

Light source

Object(s)

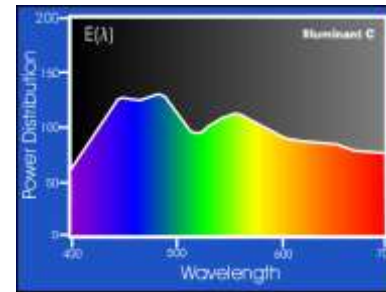
Sensor



What makes an image?

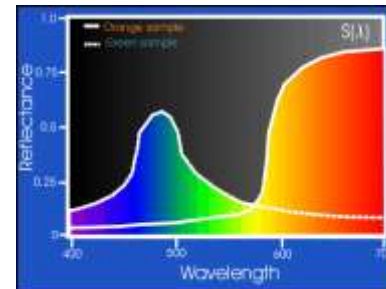
the triplet light-objects-observer

Light source



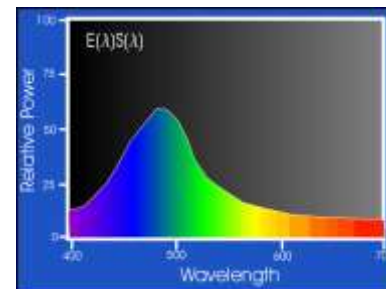
$$e(\lambda)$$

Object



$$\rho(\lambda)$$

Sensor



$$e(\lambda)\rho(\lambda)$$

Light sources and illuminants

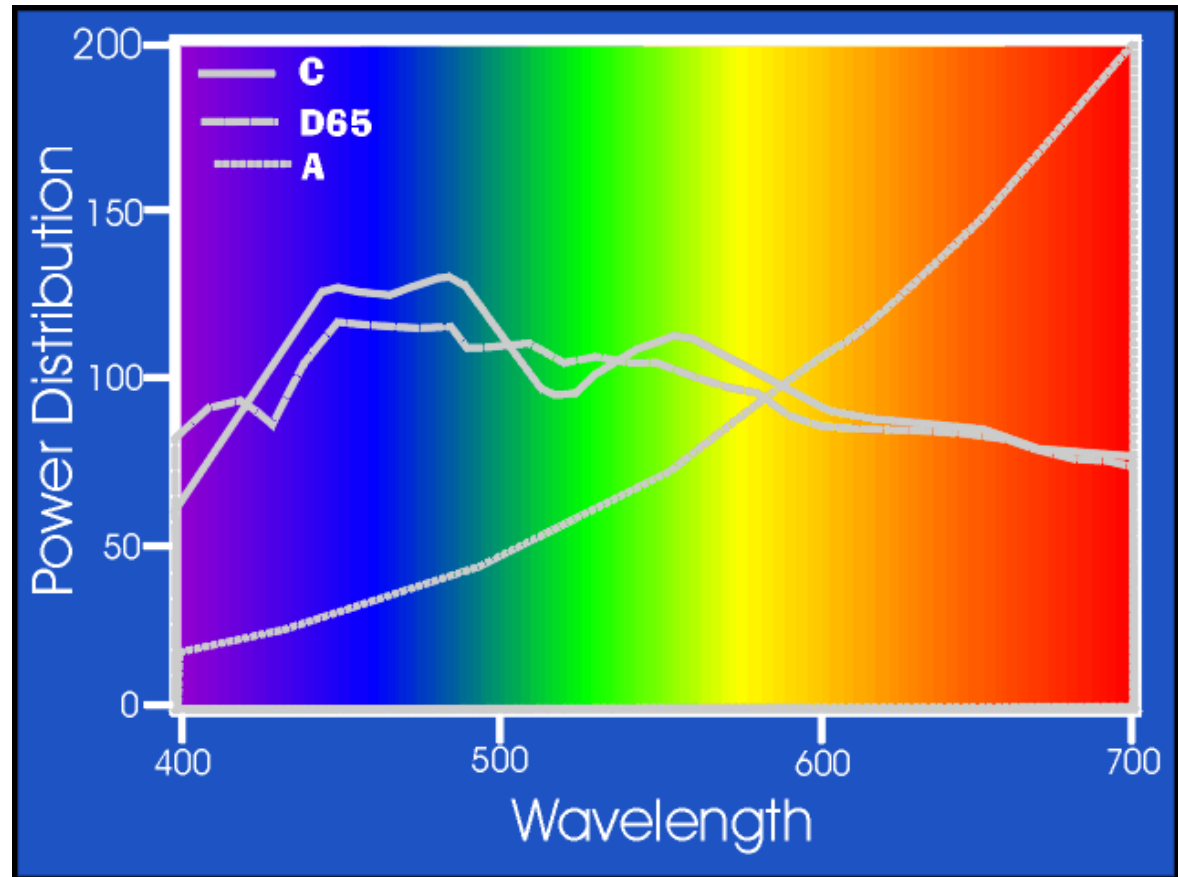


Light sources:

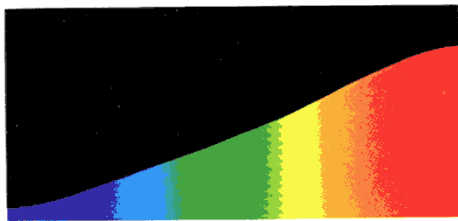
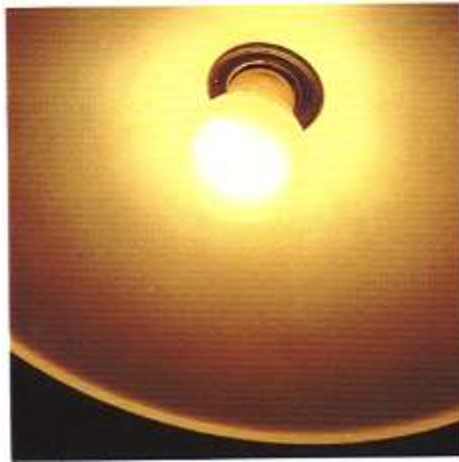
sun, candle,
fluorescent lamp,
incandescent lamp

Illuminants:

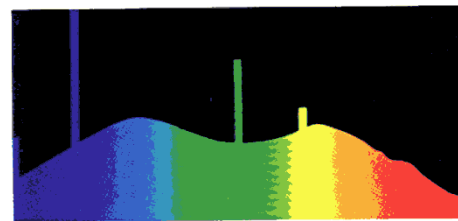
illuminant A
illuminant D65
illuminant C



Light sources and illuminants



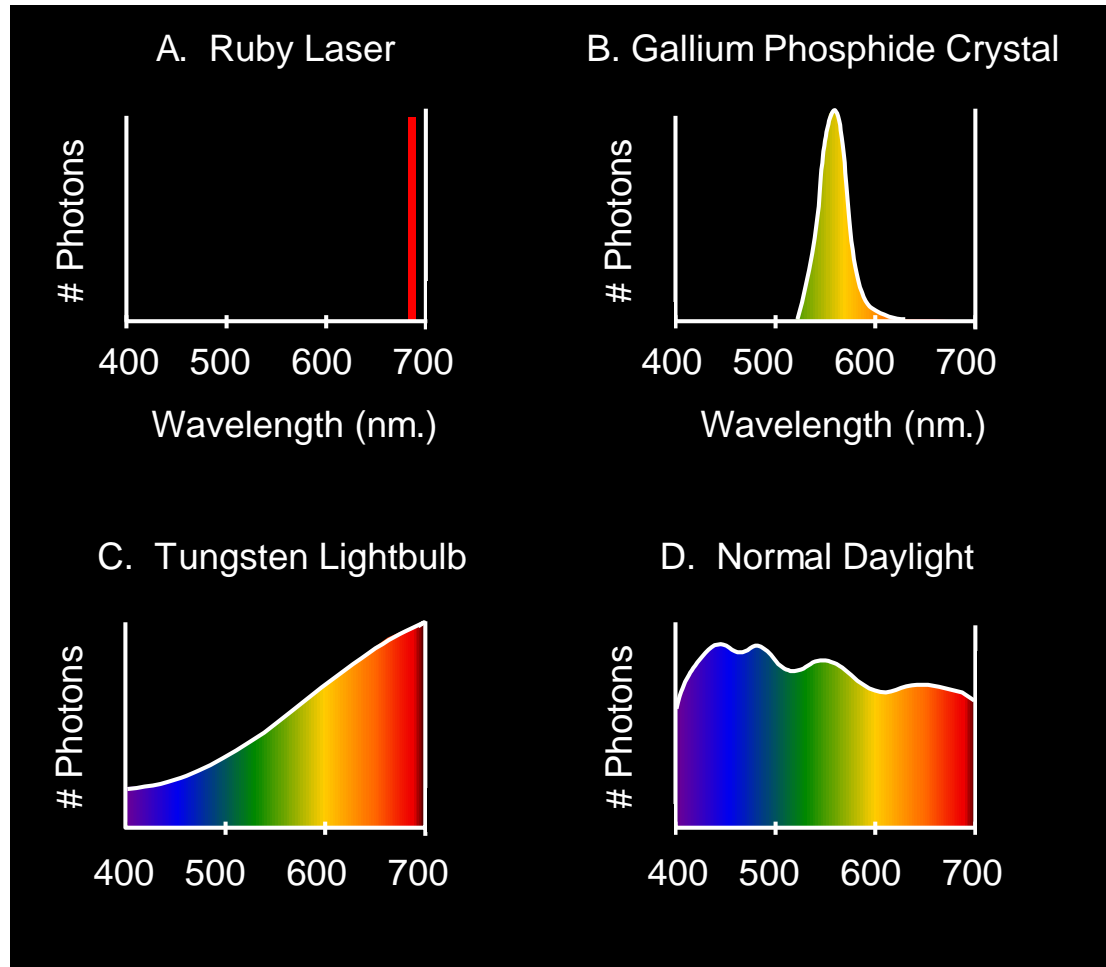
Incandescent lamp



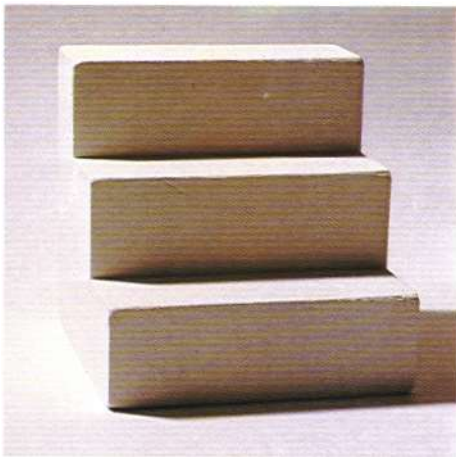
Fluorescent lamp

The Physics of Light

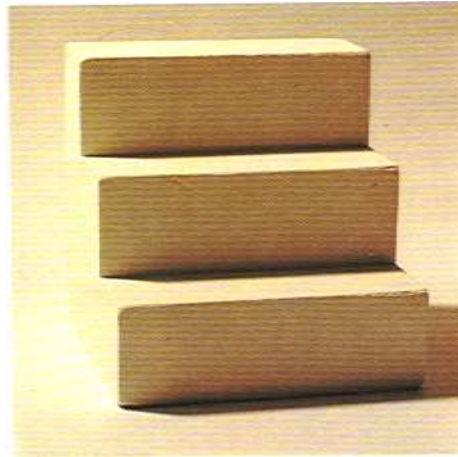
Some examples of the spectra of light sources



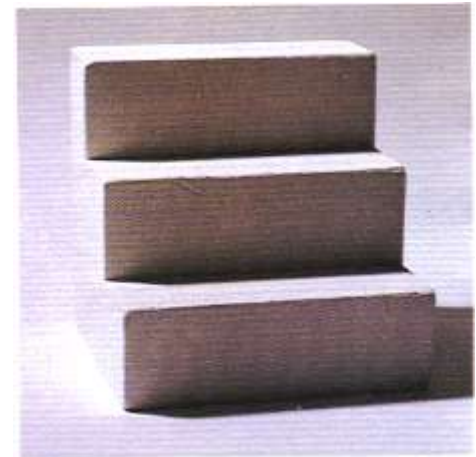
Influence of Light Sources



Average daylight



Incandescent lamp



Fluorescent lamp

Object Colours

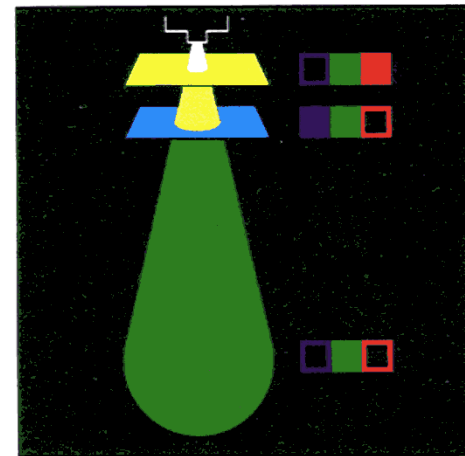
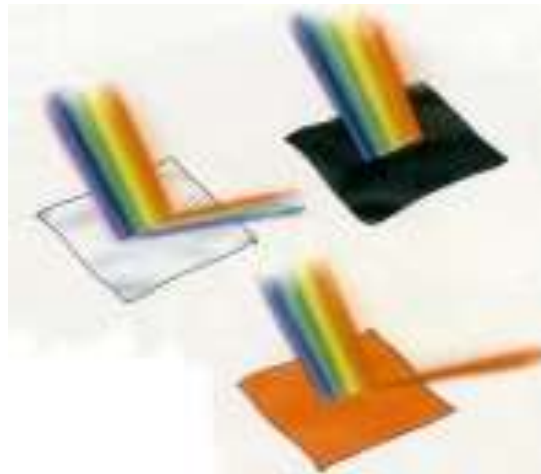
Materials:

Transparent

Opaque

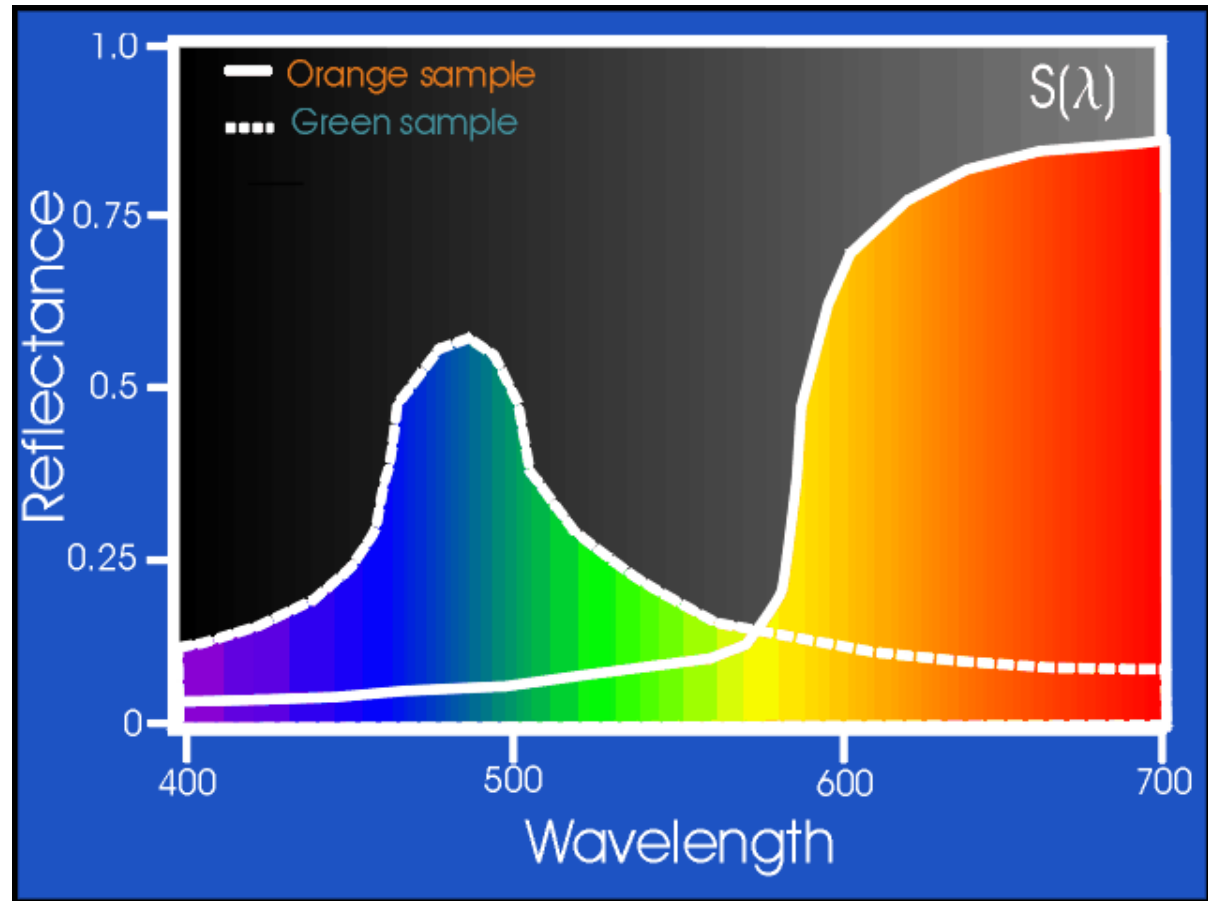
Spectral Reflectance

$$\rho(\lambda)$$



Object Colours

Material
spectrophotometer
Reflectance curve



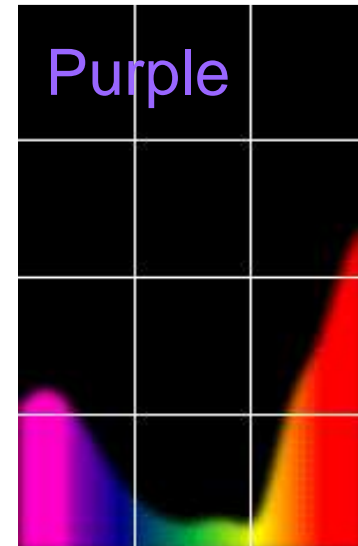
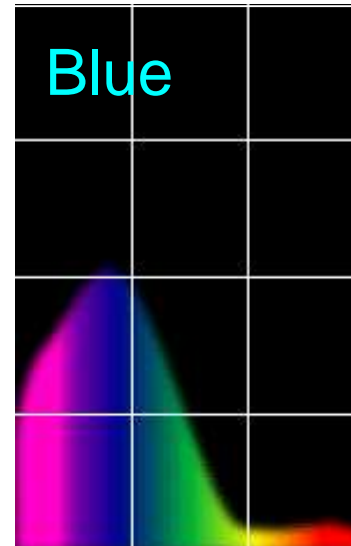
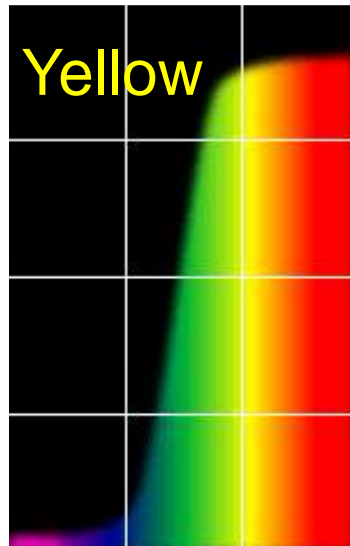
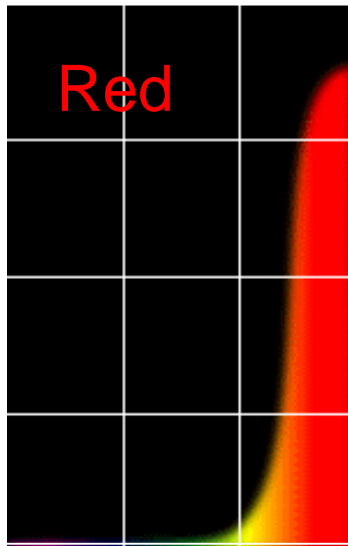


Object Colours

Some examples of the reflectance spectra of surfaces

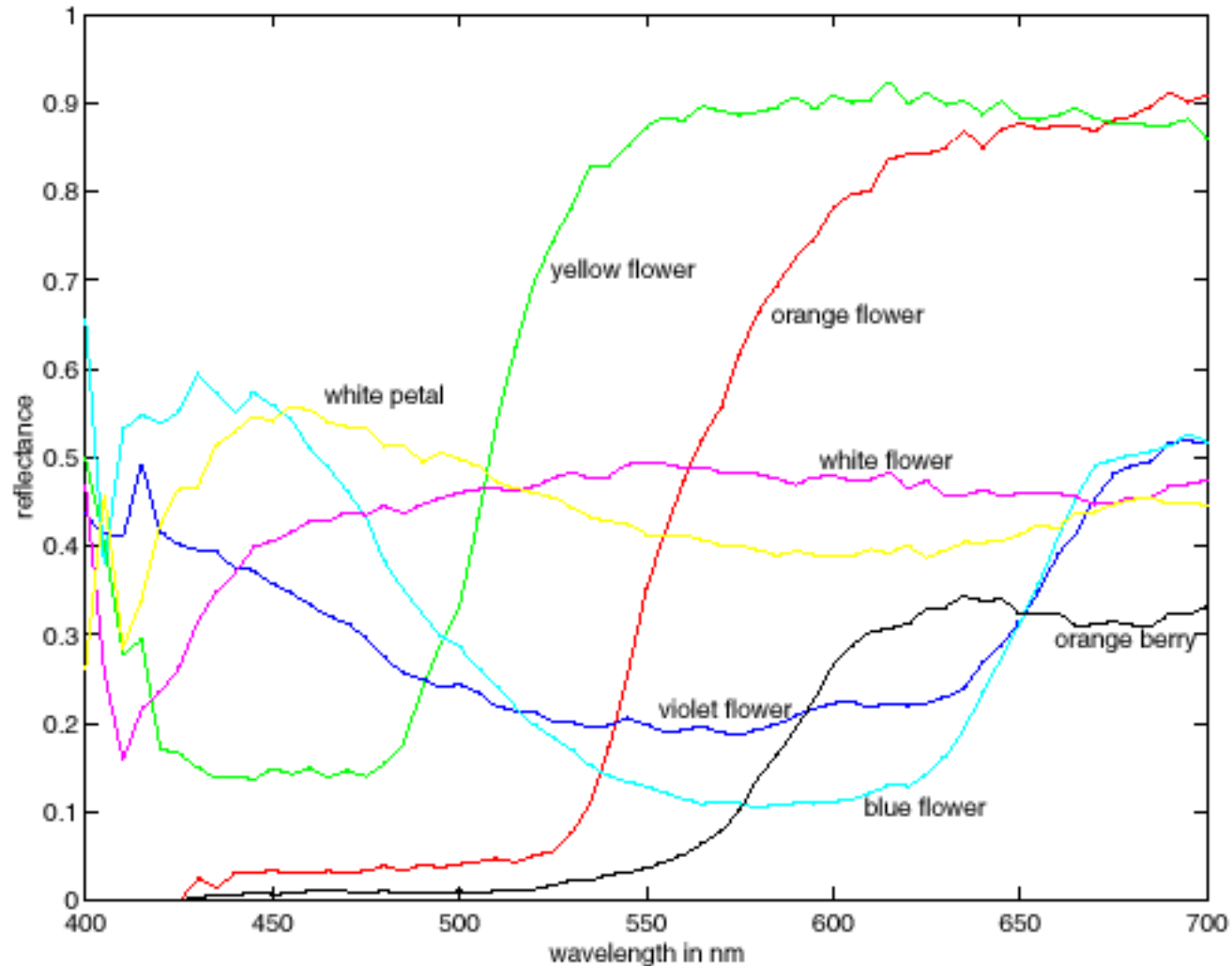


% Photons Reflected



Wavelength (nm)

More Spectra



Observer



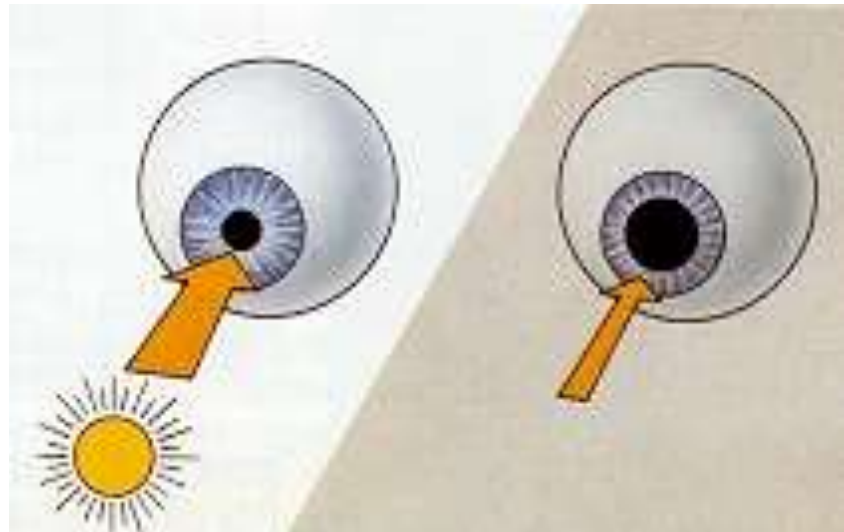
Eyes: rods and cones

Theories:

Tri-chromacy theory

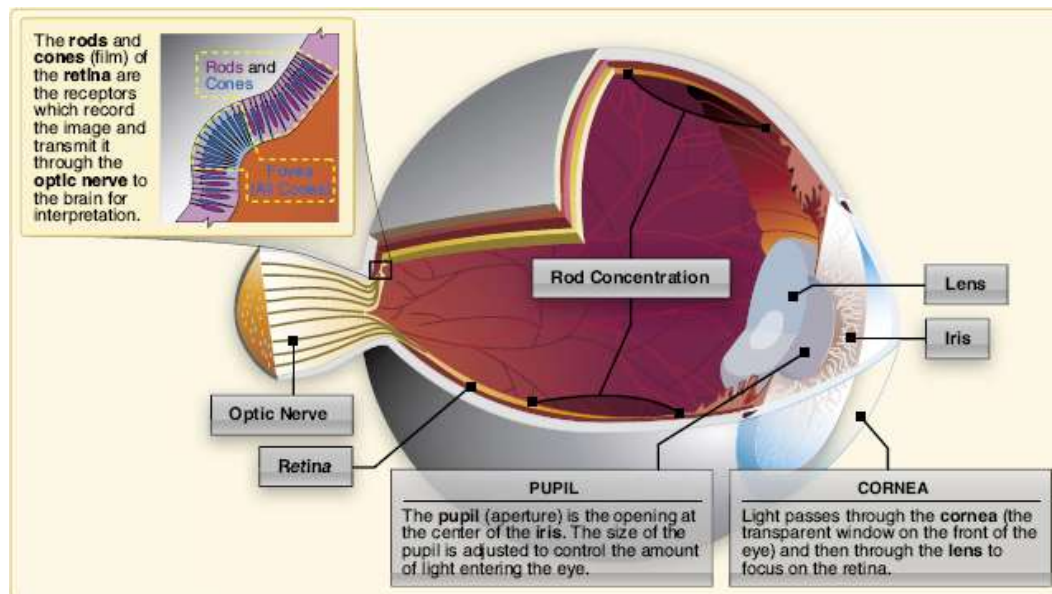
Opponent theory

Retinex theory



Human Eye

- Retina contains light sensitive cells that convert light energy into electrical impulses that travel through nerves to the brain.
- Brain interprets the electrical signals to form images.



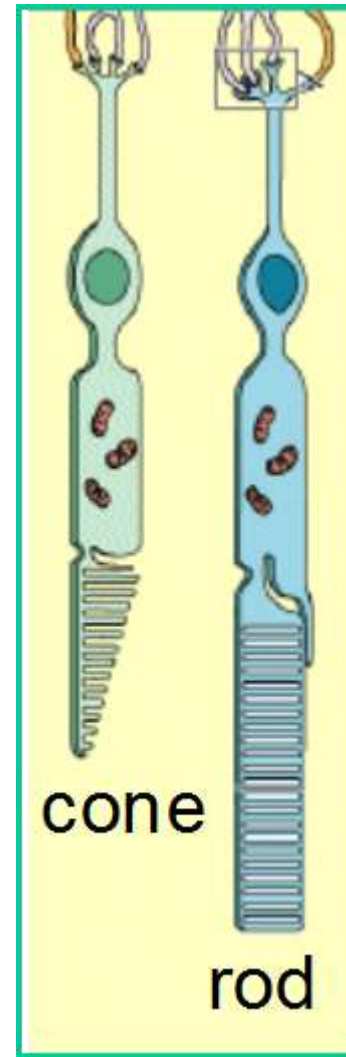
Two Types of Light-Sensitive Receptors

Cones

cone-shaped
less sensitive
operate in high light
color vision

Rods

rod-shaped
highly sensitive
operate at night
gray-scale vision



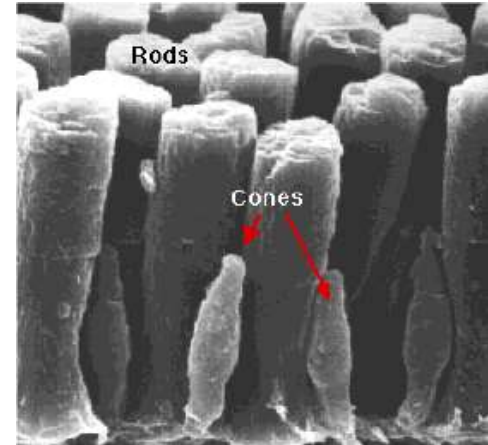
Light Detection: Rods and Cones

Rods:

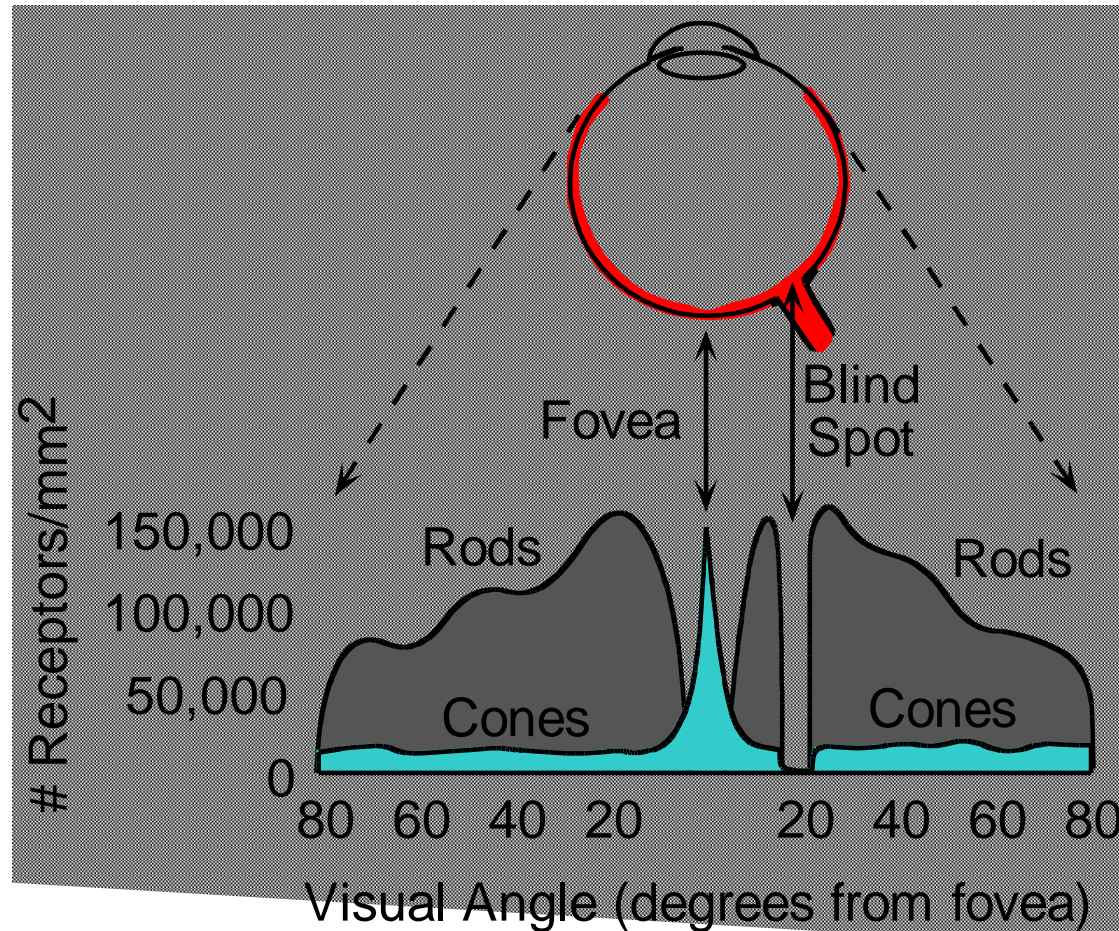
- 120 million rods in retina
- 1000X more light sensitive than Cones
- Discriminate B/W brightness in low illumination
- Short wave-length sensitive

Cons:

- 6-7 million cones in the retina
- Responsible for high-resolution vision
- Discriminate Colors
- Three types of color sensors: 64% red, 32% green, 2% blue)
- Sensitive to any combination of three colors



Distribution of Rods and Cones

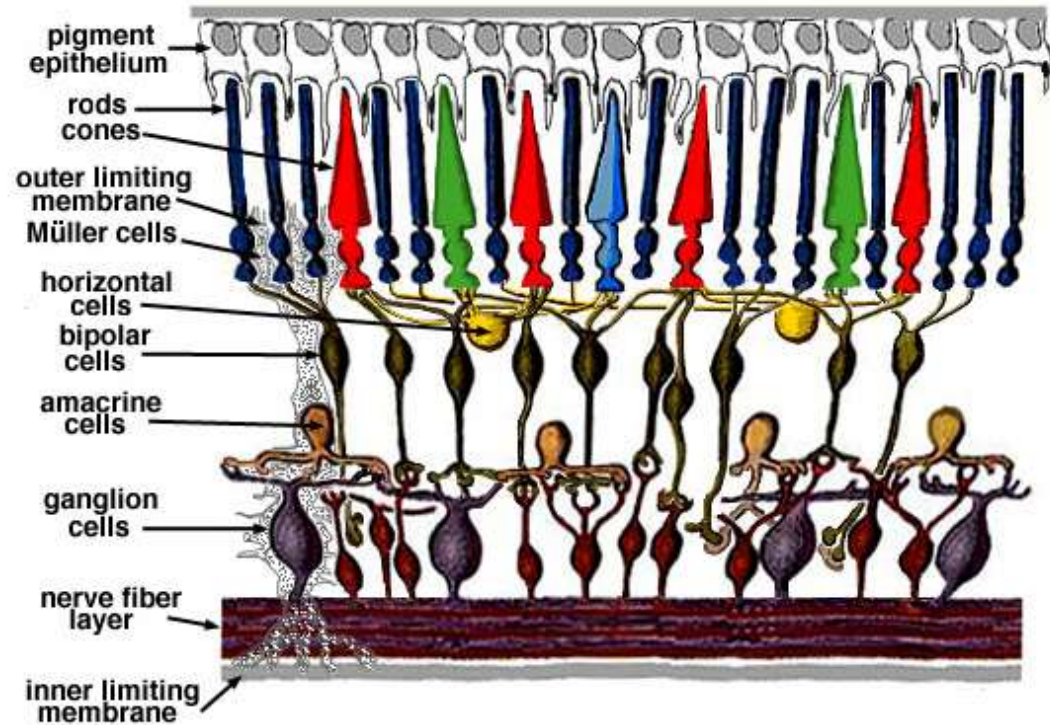


Night Sky: why are there more stars off-center?

Averted vision: http://en.wikipedia.org/wiki/Averted_vision

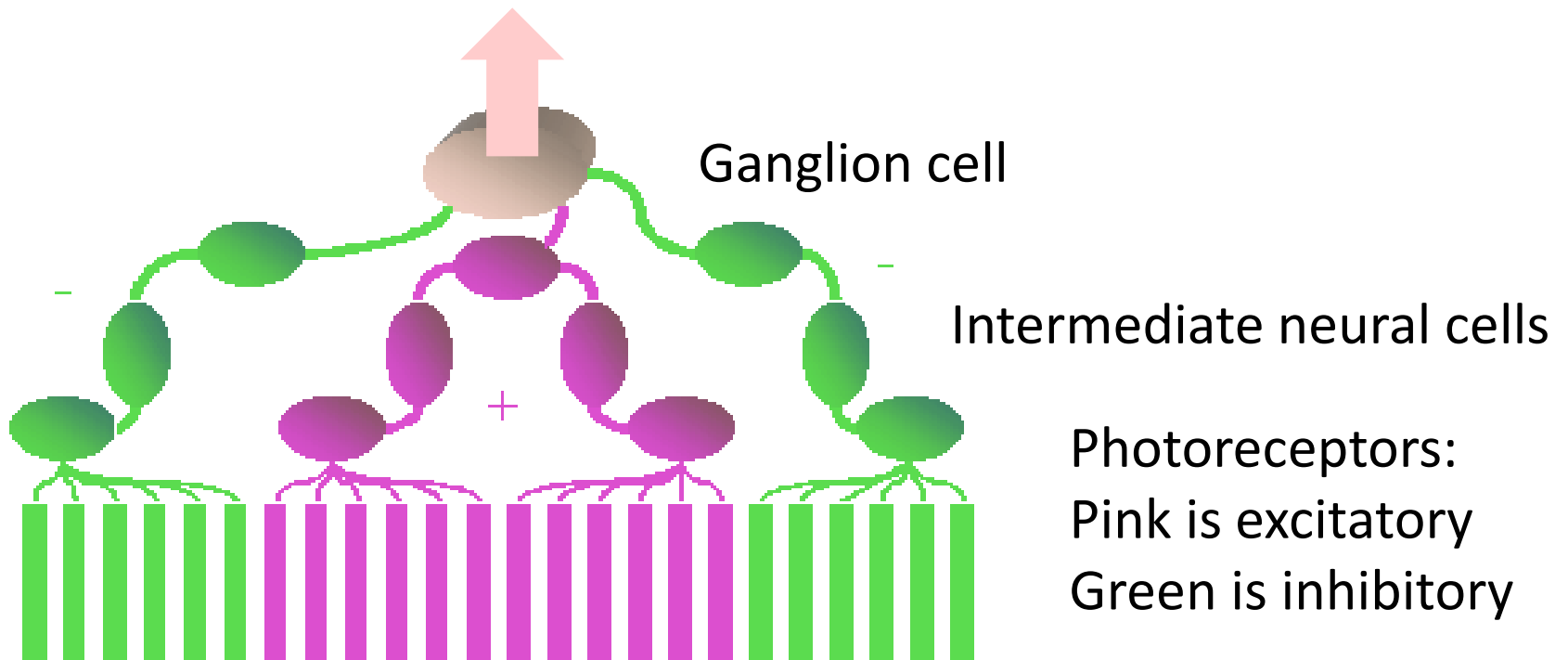
The Retina

- 0.5 mm thick
- The photosensors (the rods and cones) lie outermost in the retina.
- Interneurons
- Ganglion cells (the output neurons of the retina) lie innermost in the retina closest to the lens and front of the eye.

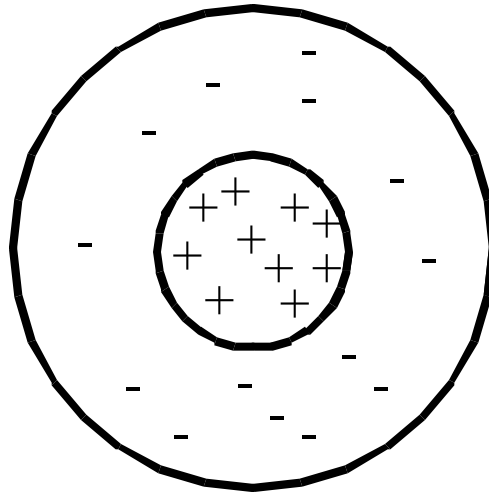


Receptive Fields

The ganglion cell produces some background response even when there is no light on its receptive field

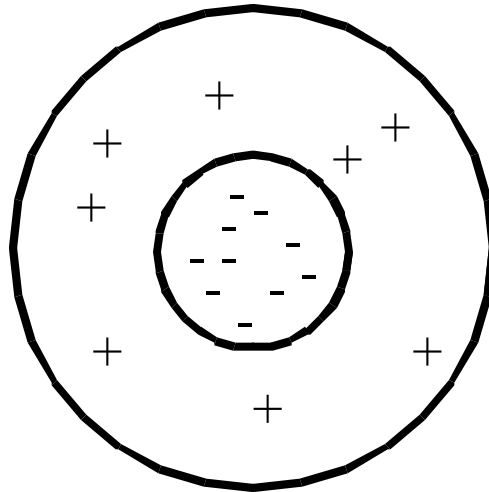


“On-Center” Ganglion Cell



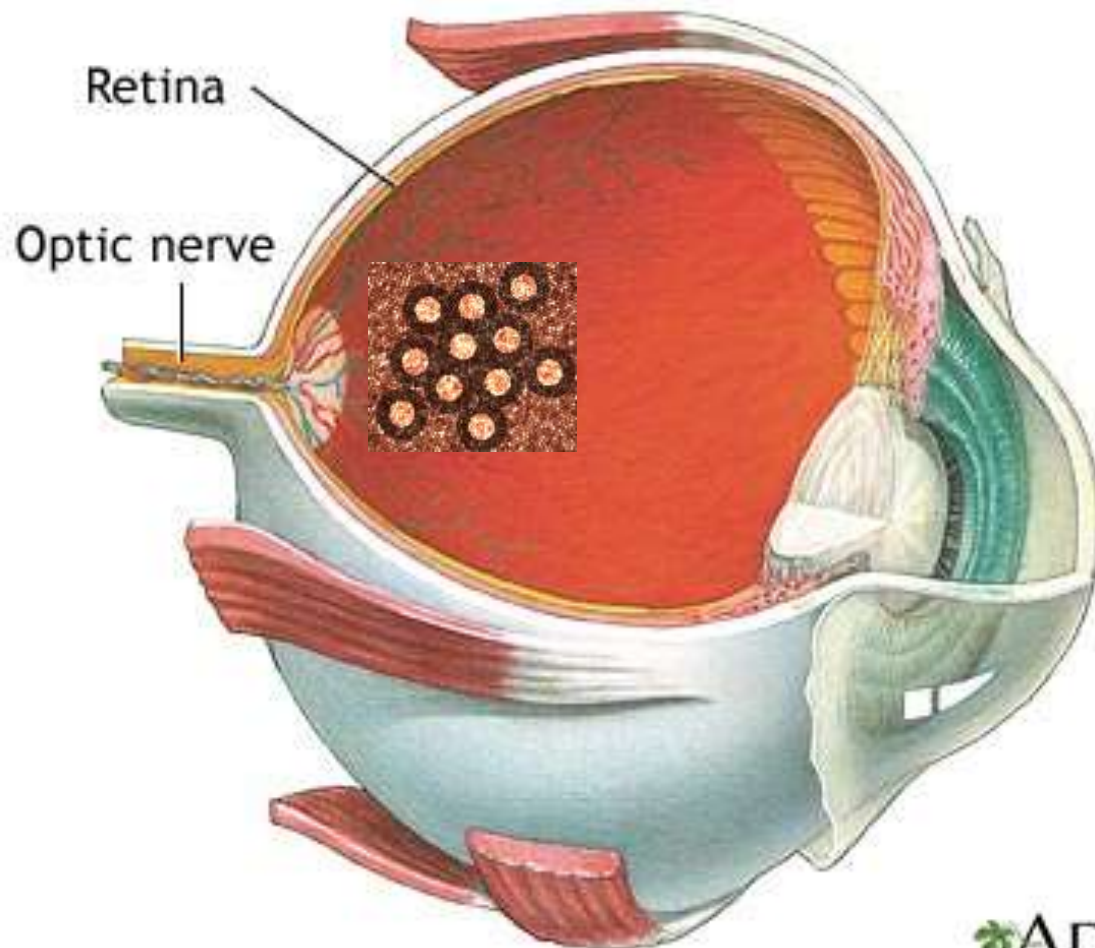
Responds maximally to light increments in the center,
and light decrements in the surround.

“Off-Center” Ganglion Cell



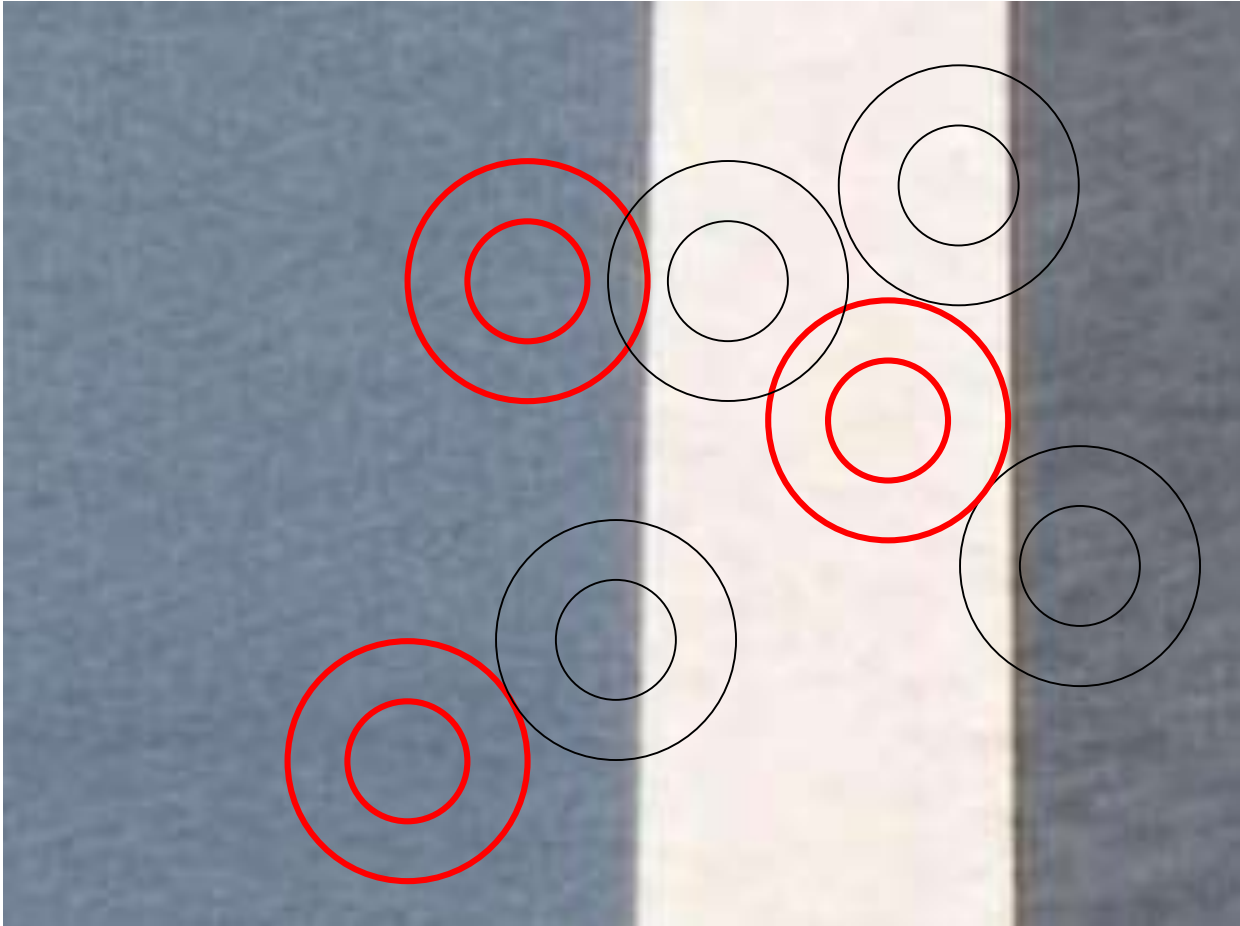
Responds maximally to light decrements in the center,
and light increments in the surround.

Receptive Fields on the Retina

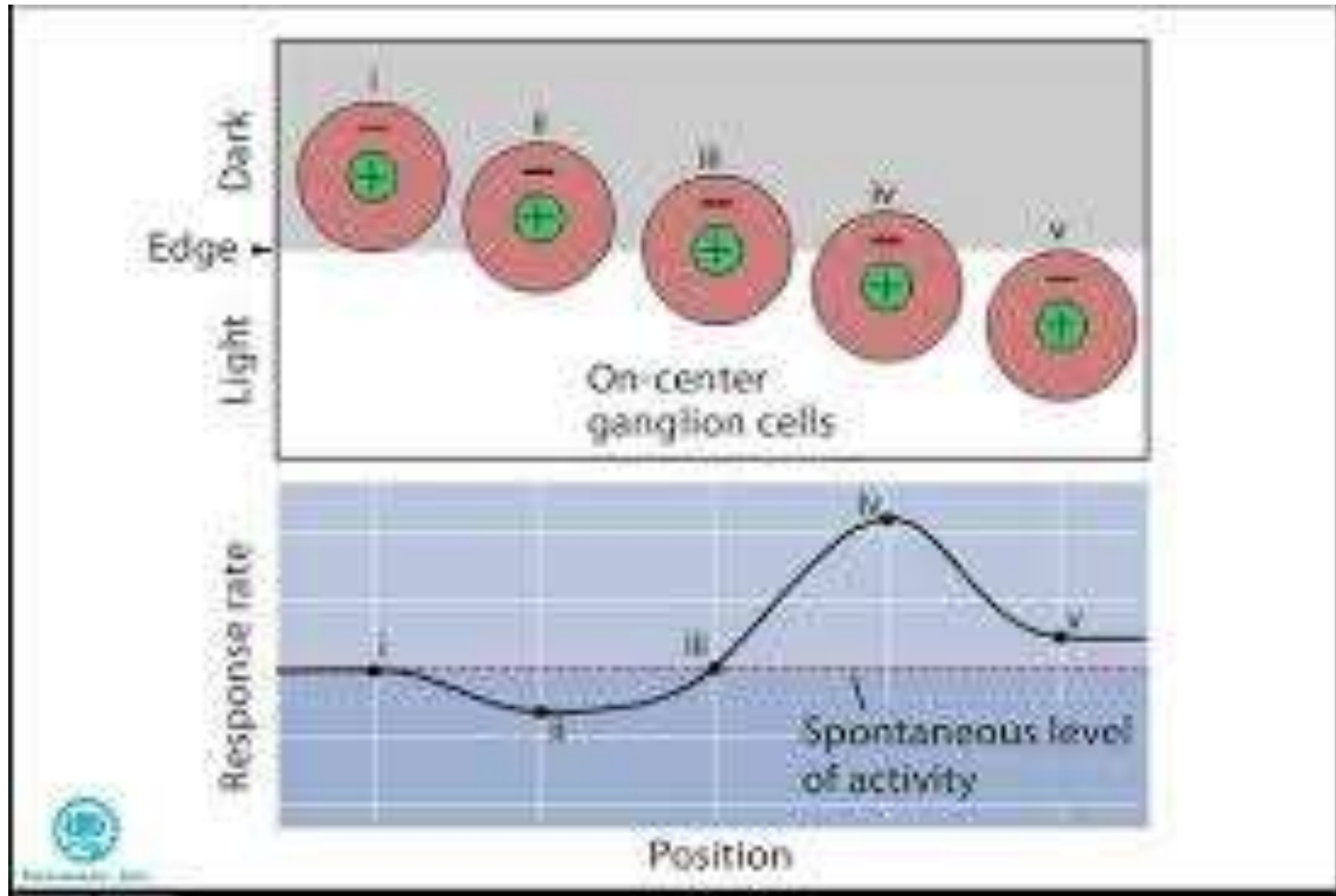


The size of the receptors and the receptive field are shown here much larger than actual size!

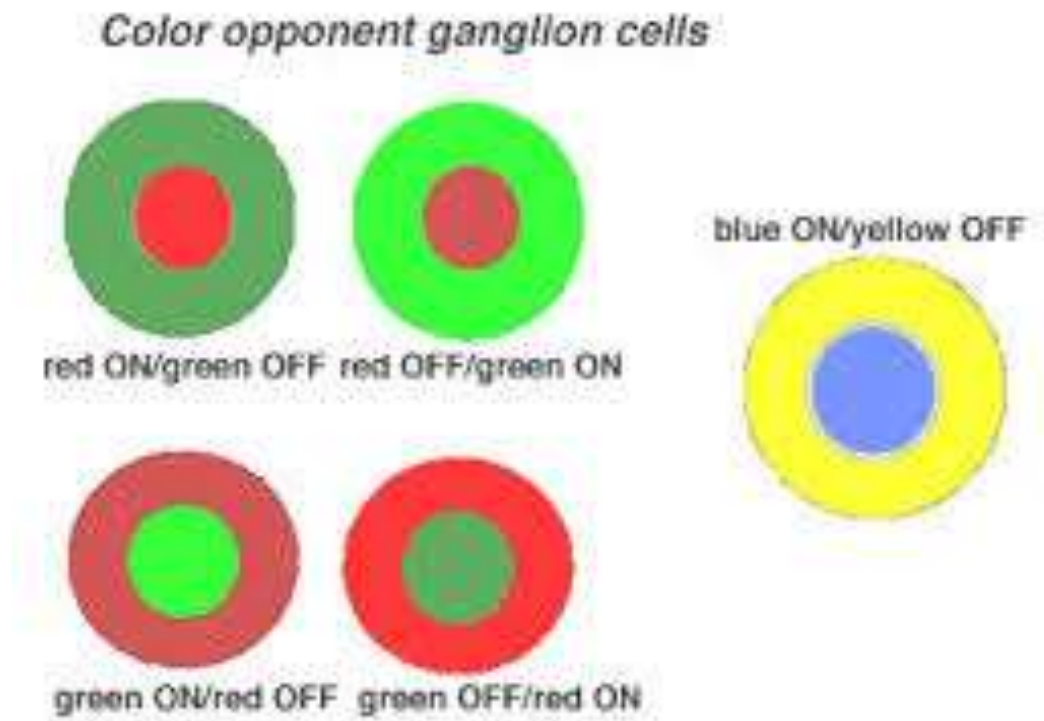
Ganglion Cells: Receptive Fields



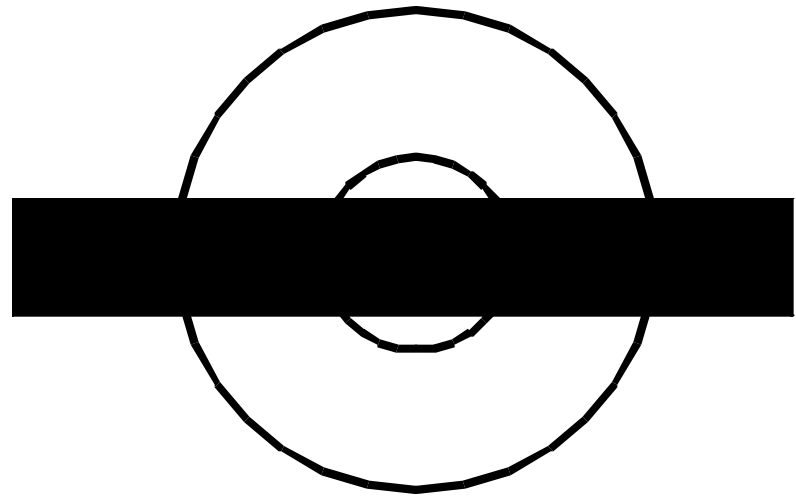
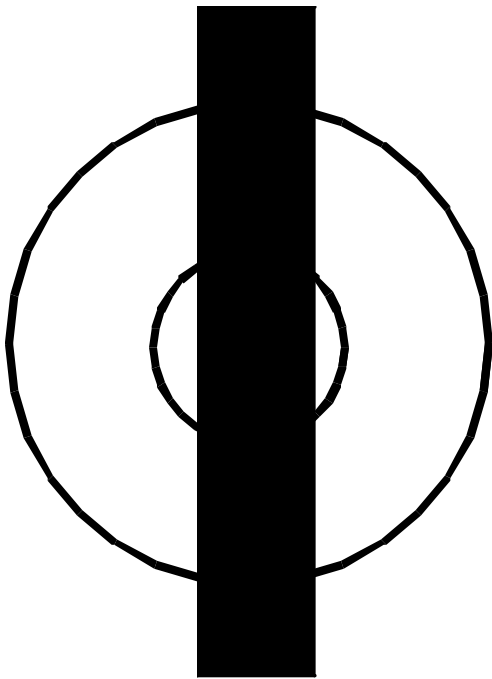
Responses: ON-Centre Ganglion Cells



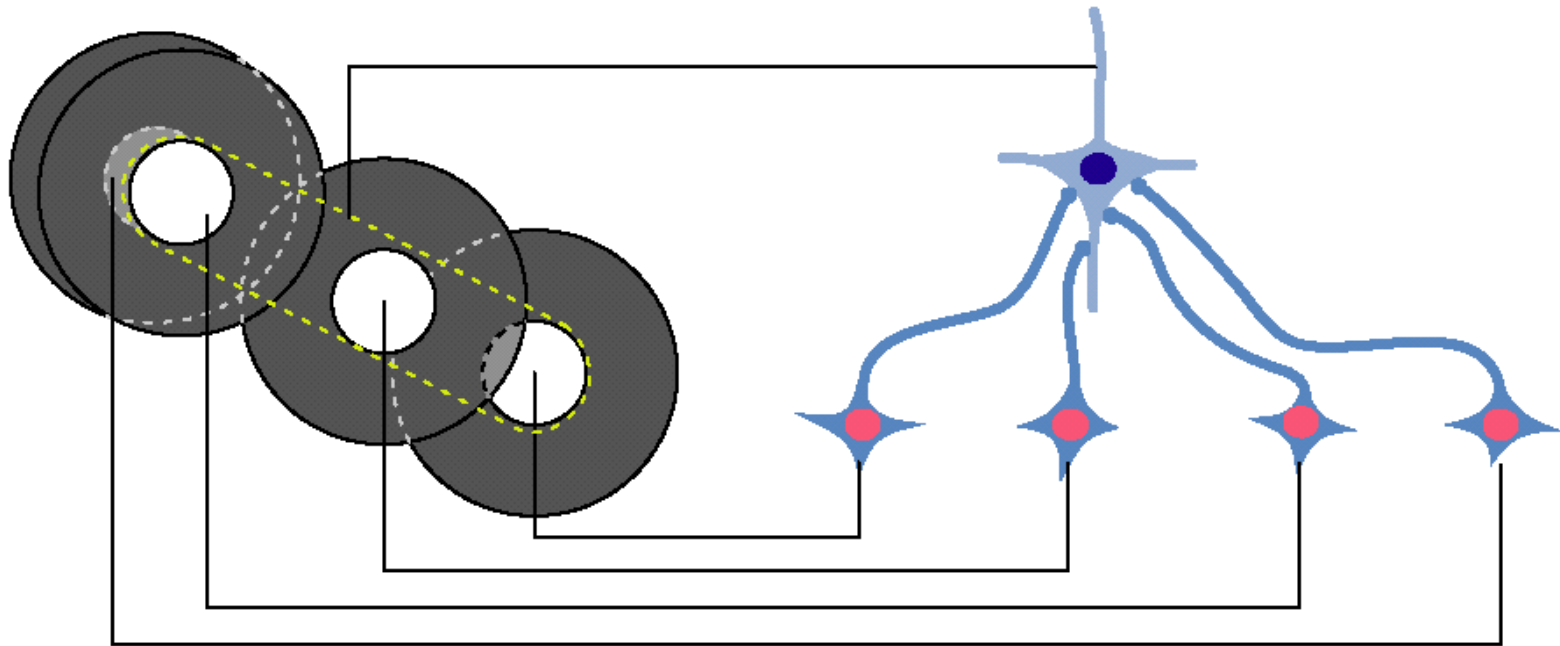
Ganglion Cells: Receptive Fields / Opponent Colors



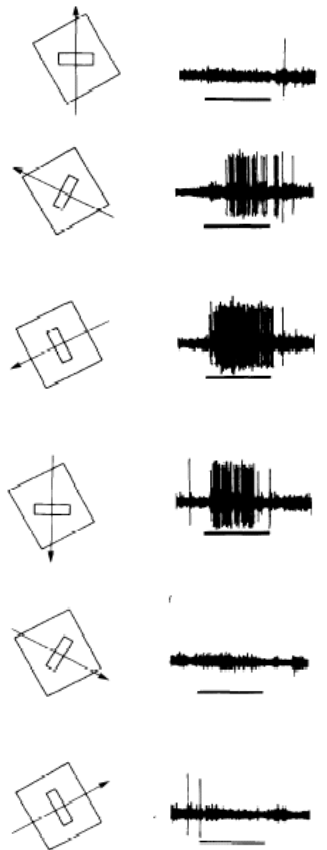
Ganglion cells have no orientation preference.



Model of how center-surround cells can be building blocks for simple cells.



Model of how center-surround cells can be building blocks for simple cells.



Retinal ganglion cells respond to edges

Input image
(cornea)

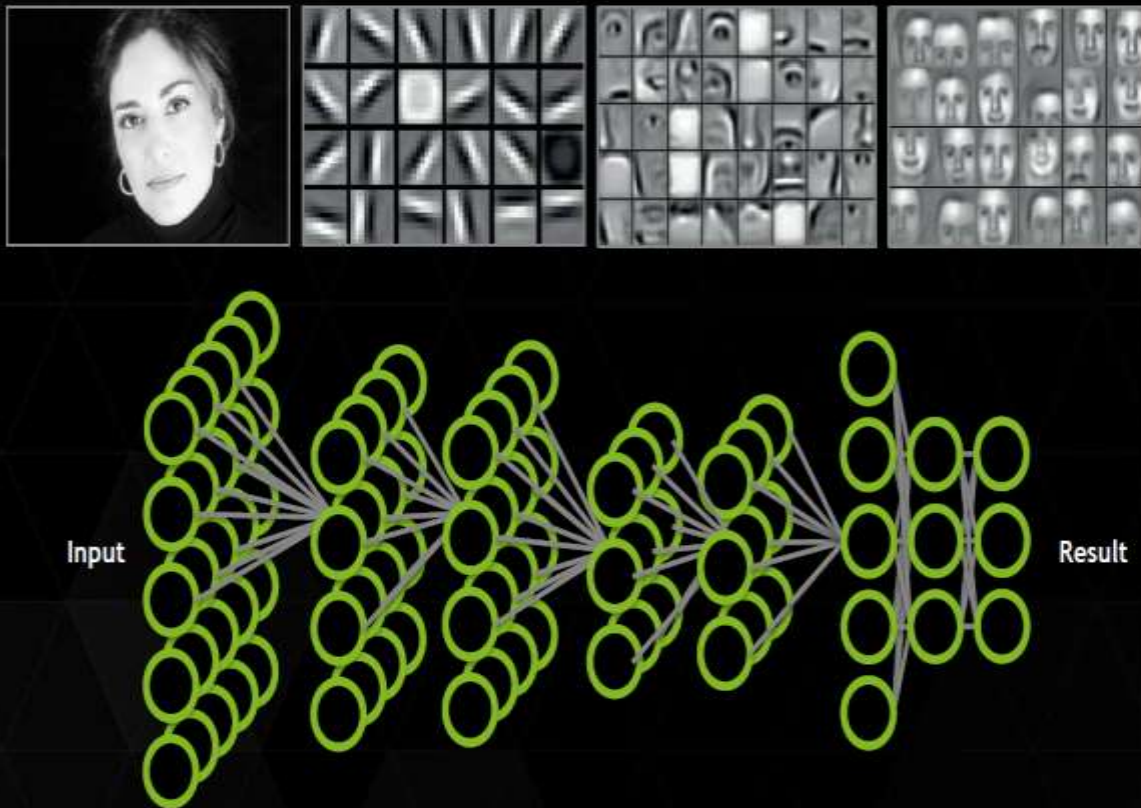


“Neural image”
(retinal ganglion cells)



Center-surround receptive fields: emphasize edges.

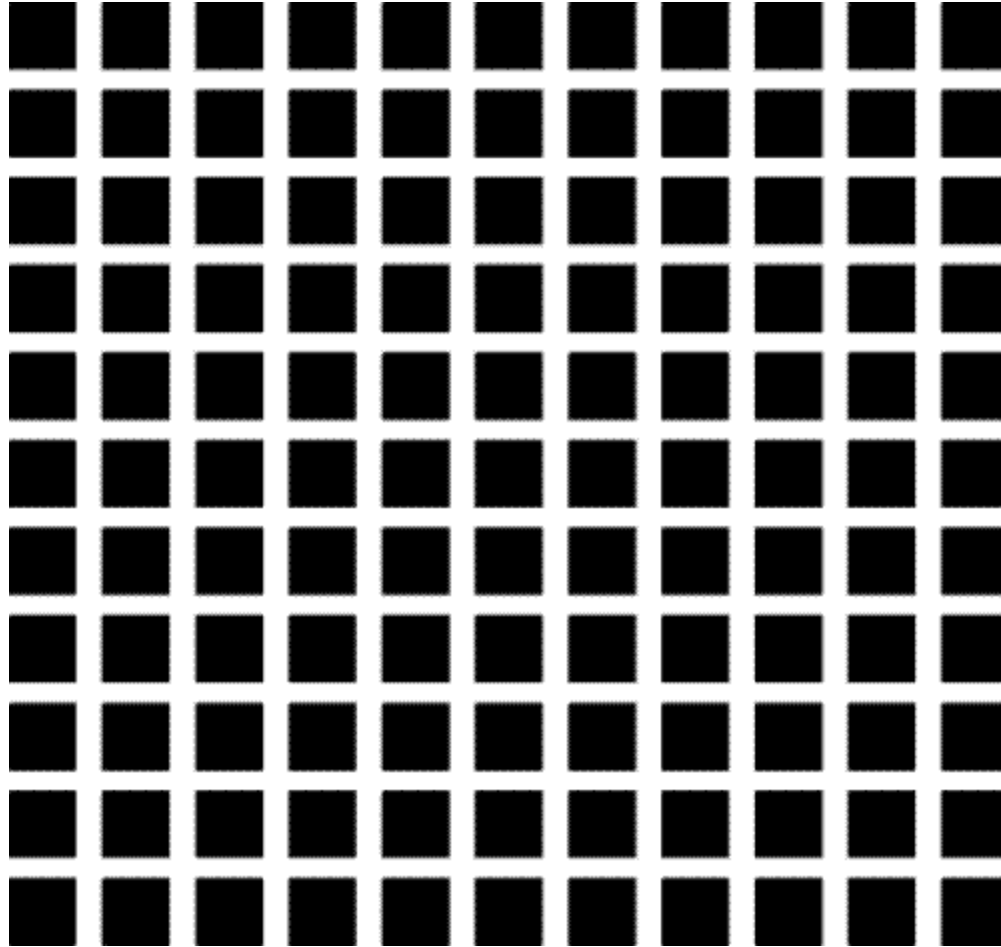
Deep Learning



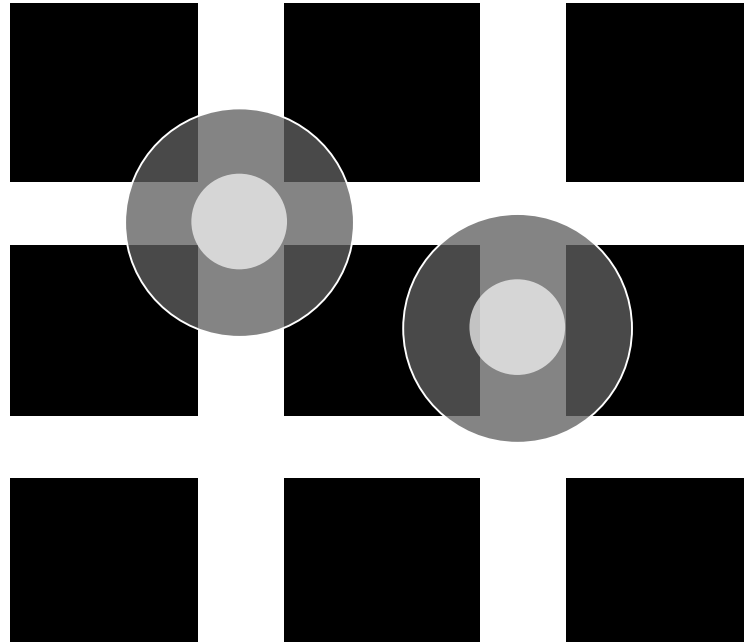
Receptive Fields



Hermann Grid Illusion



Hermann Grid Illusion: Explanation



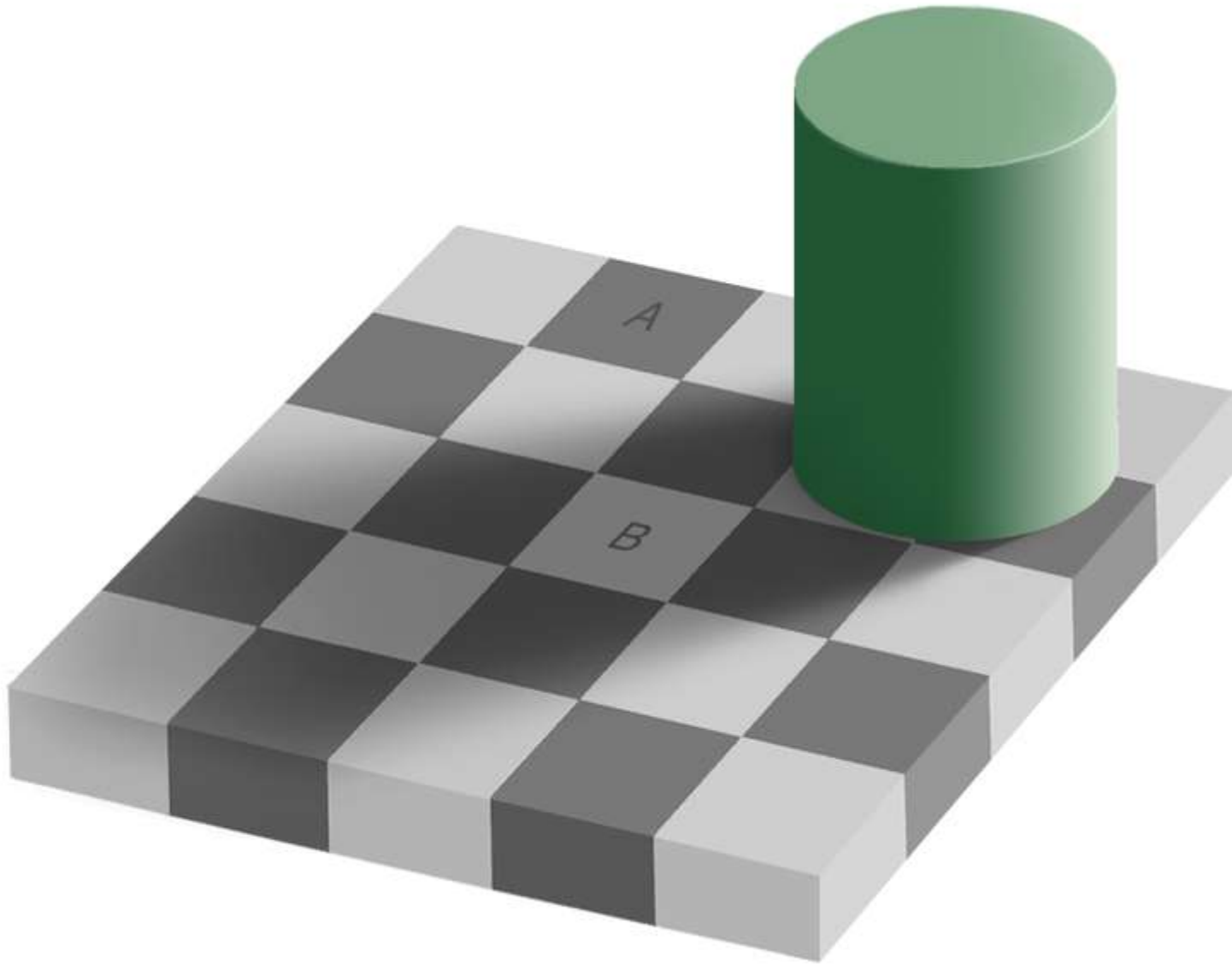
When the image is on the first receptive field there is more light falling on the surround (inhibitory) than in the second position
So there is more suppression and the illusion of a dark spot at the first location

Simultaneous Lightness Contrast

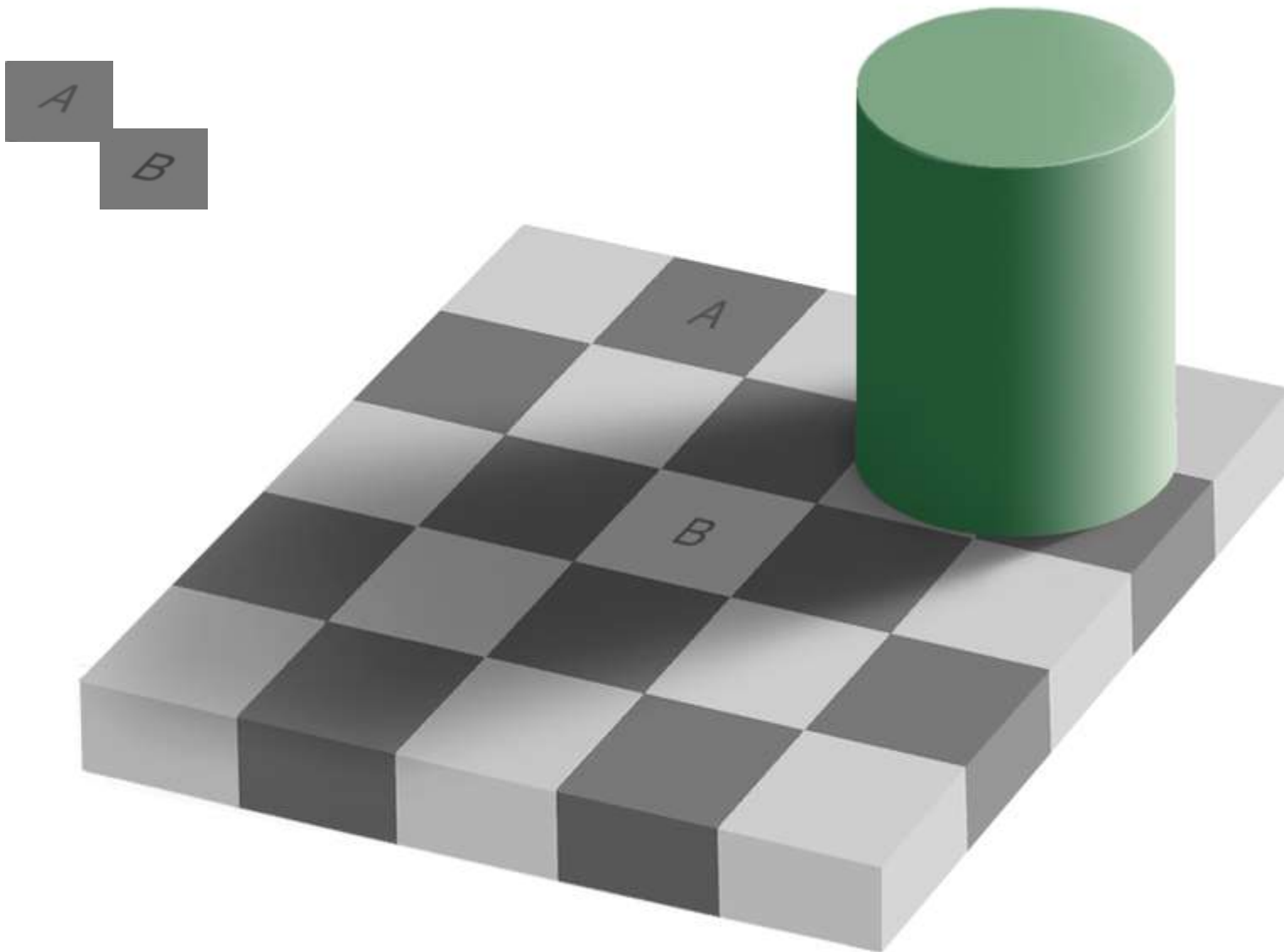


- Occurs when the lightness of an area is influenced by neighboring regions
- Our perception of lightness is not objective, but depends on the surrounding area
- The center square on the right looks lighter because the surrounding area is a darker gray

Perception of Intensity

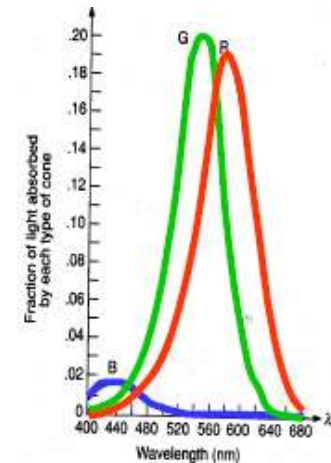


Perception of Intensity



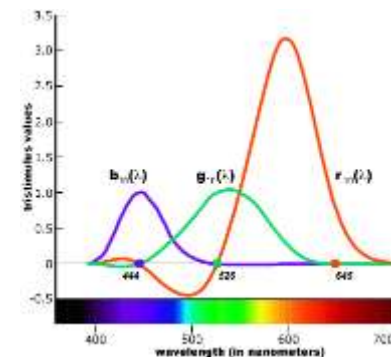
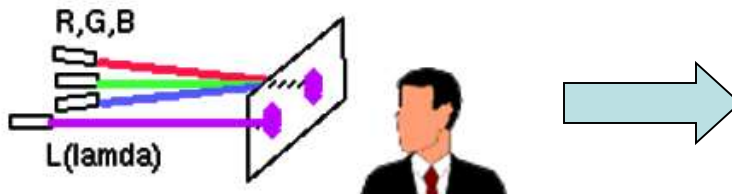
Tristimulus of Color Theory

Spectral-response functions of each of the three types of cones



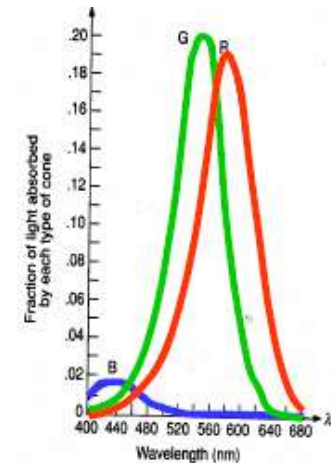
Color matching function based on RGB

- any spectral color can be represented as a linear combination of these primary colors



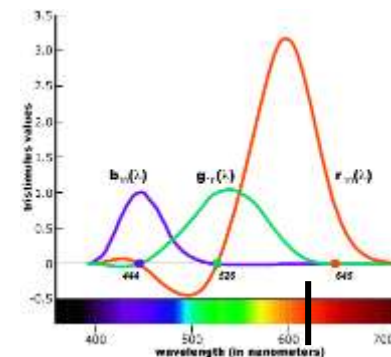
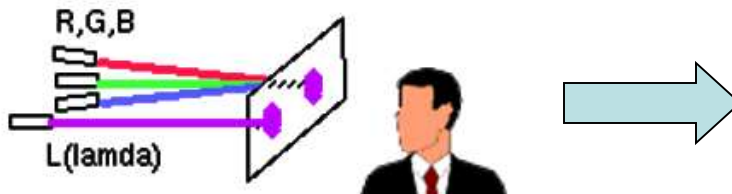
Tristimulus of Color Theory

Spectral-response functions of each of the three types of cones



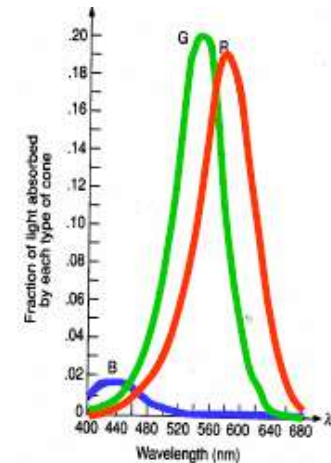
Color matching function based on RGB

- any spectral color can be represented as a linear combination of these primary colors



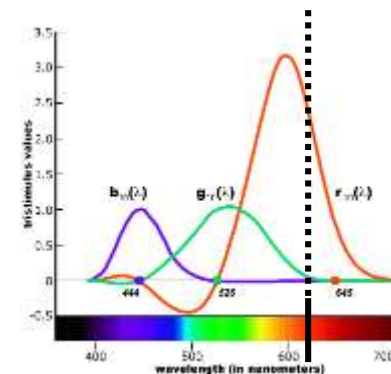
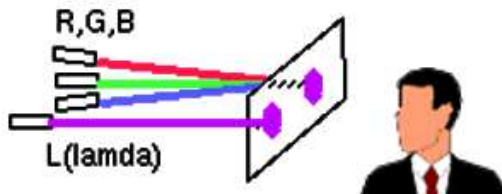
Tristimulus of Color Theory

Spectral-response functions of each of the three types of cones



Color matching function based on RGB

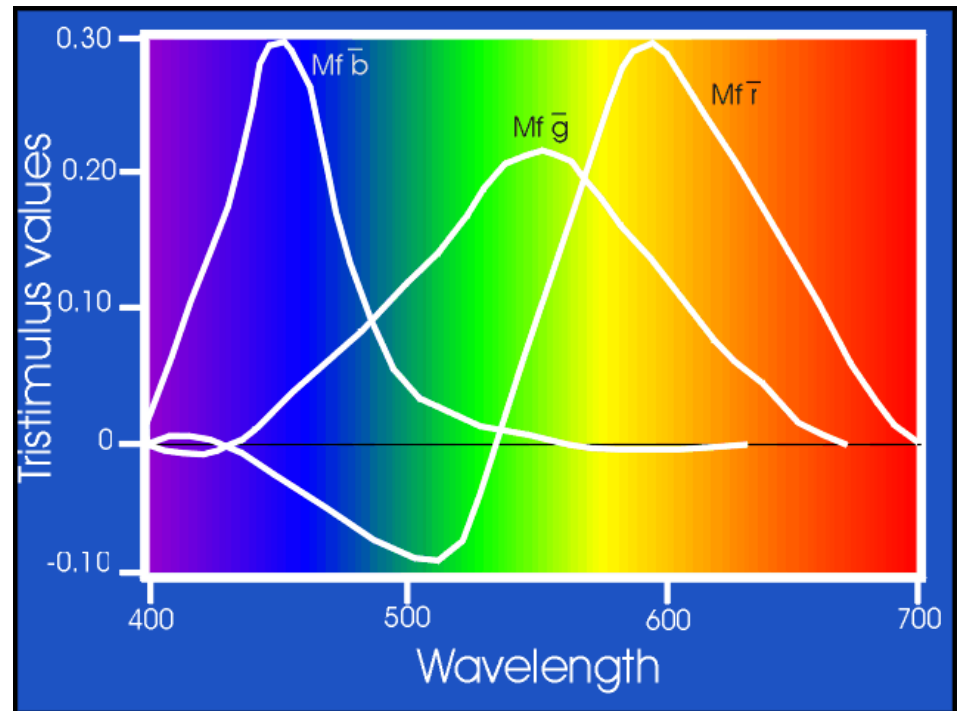
- any spectral color can be represented as a linear combination of these primary colors



Observer: Trichromacy

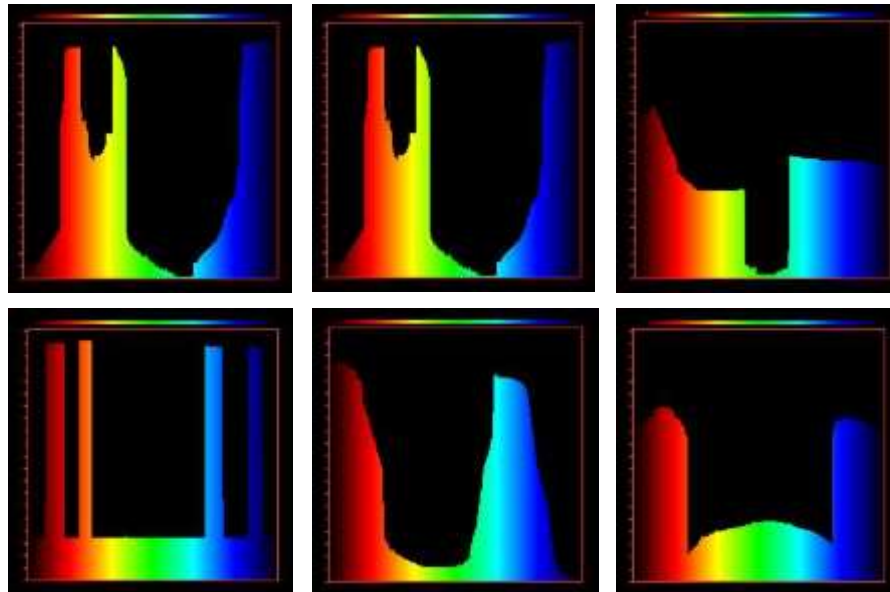


Young-Helmholtz approach
Tristimulus values R, G, and B
Wright (7) Guild (10)
Stiles and Burch (50)

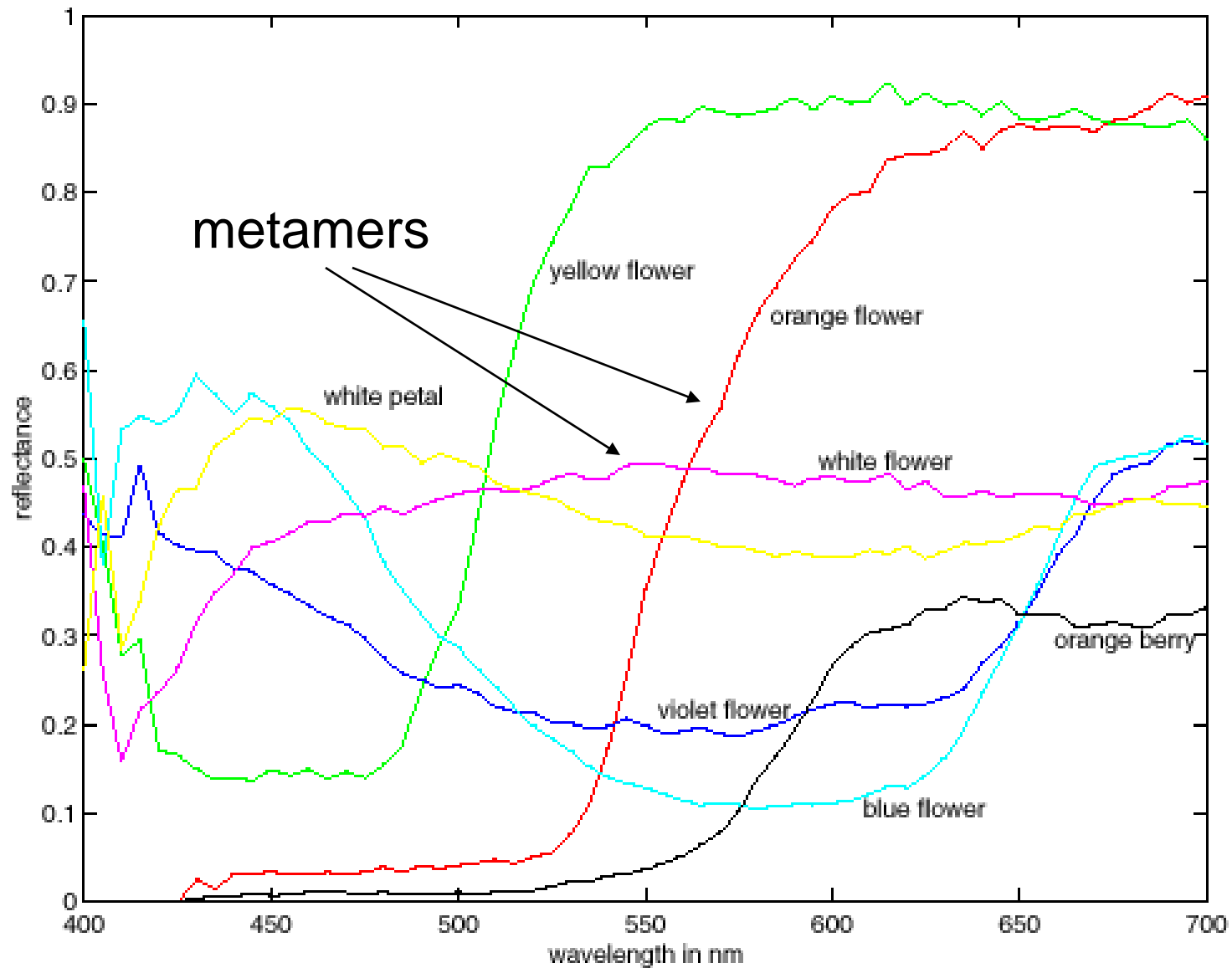


Spectral Energy Distribution

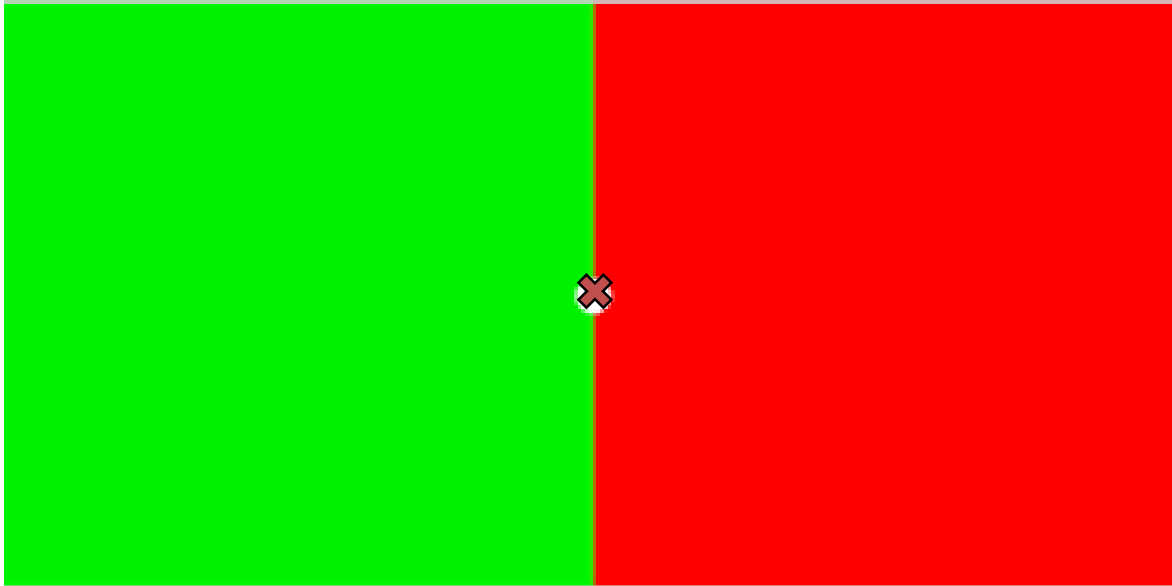
The six spectra below look the same purple to normal color-vision people



Metamers



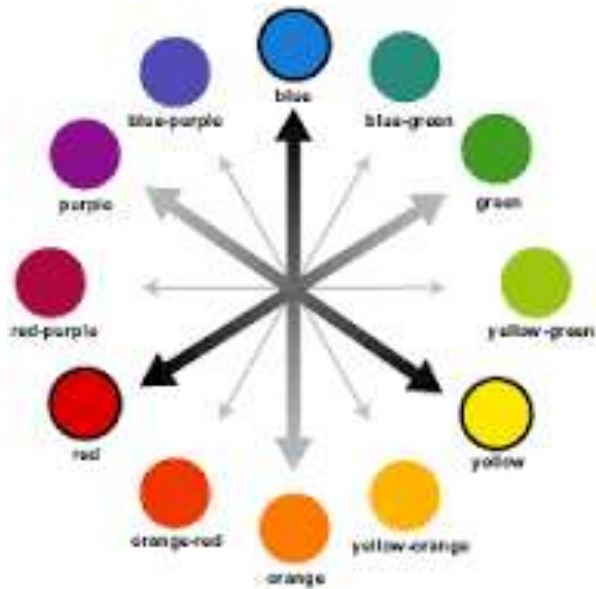
Experiment



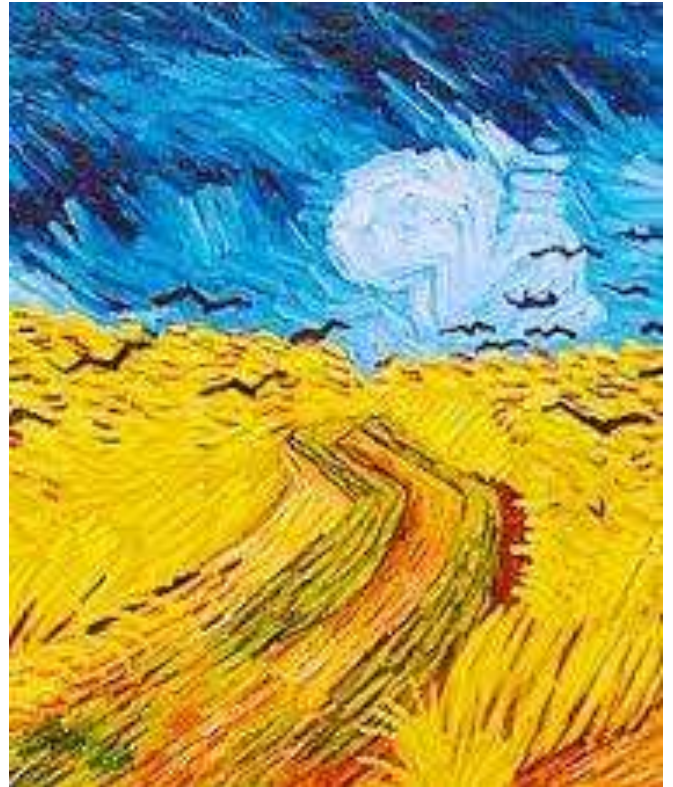
Experiment

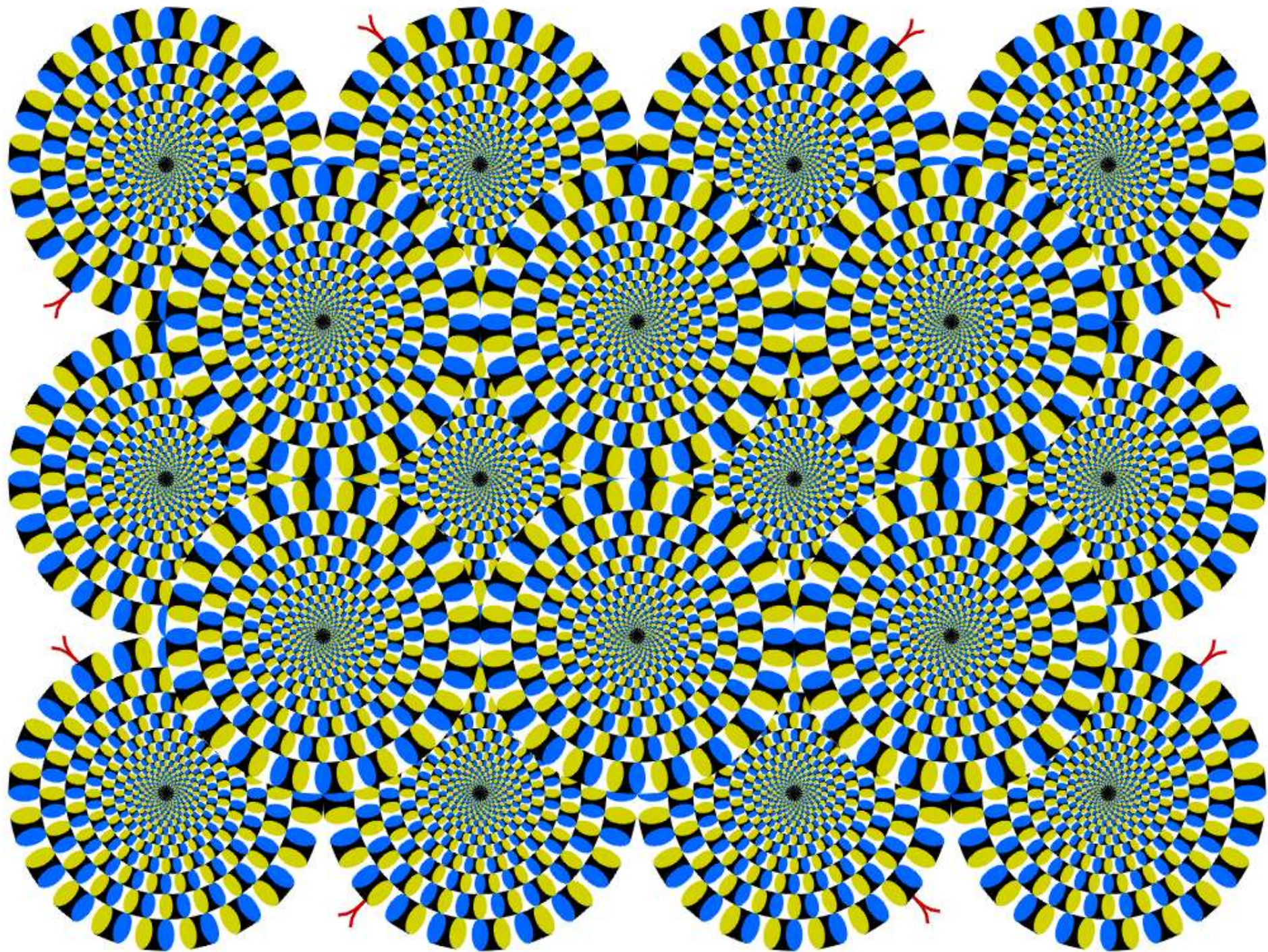


Opponent Colors



Van Gogh





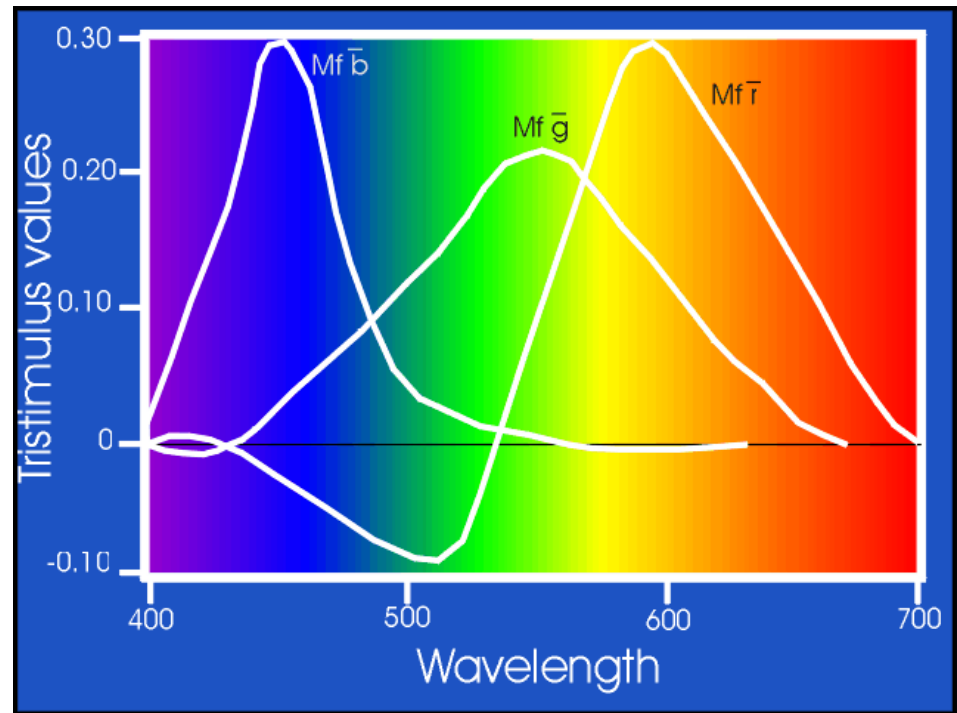
Illusions!

<http://www.michaelbach.de/>

<http://www.ritsumei.ac.jp/~akitaoka/index-e.html>

The Eye

Young-Helmholtz approach
Tristimulus values R, G, and B
Wright (7) Guild (10)
Stiles and Burch (50)

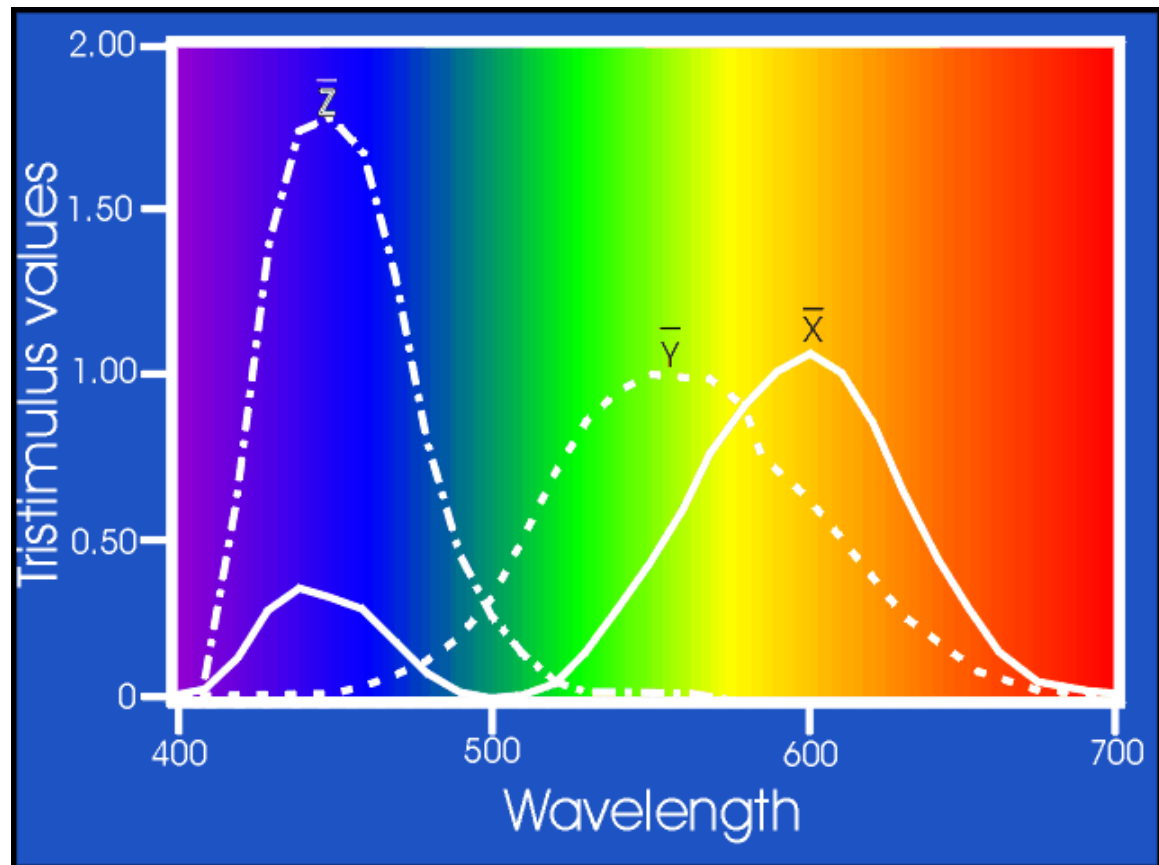


Colorimetry: CIE XYZ-system

$$X = \int_{\lambda} e(\lambda) \rho(\lambda) \bar{x}(\lambda) d\lambda$$

$$Y = \int_{\lambda} e(\lambda) \rho(\lambda) \bar{y}(\lambda) d\lambda$$

$$Z = \int_{\lambda} e(\lambda) \rho(\lambda) \bar{z}(\lambda) d\lambda$$

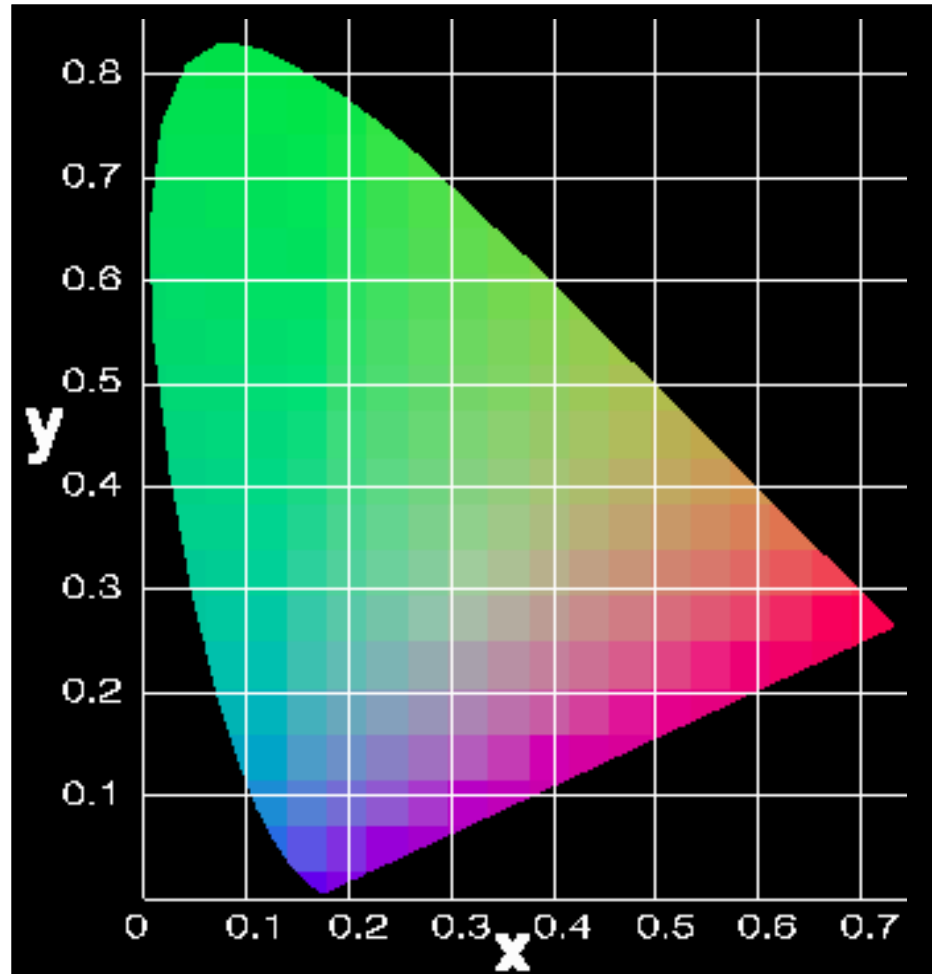


Colorimetry: CIE xy-system

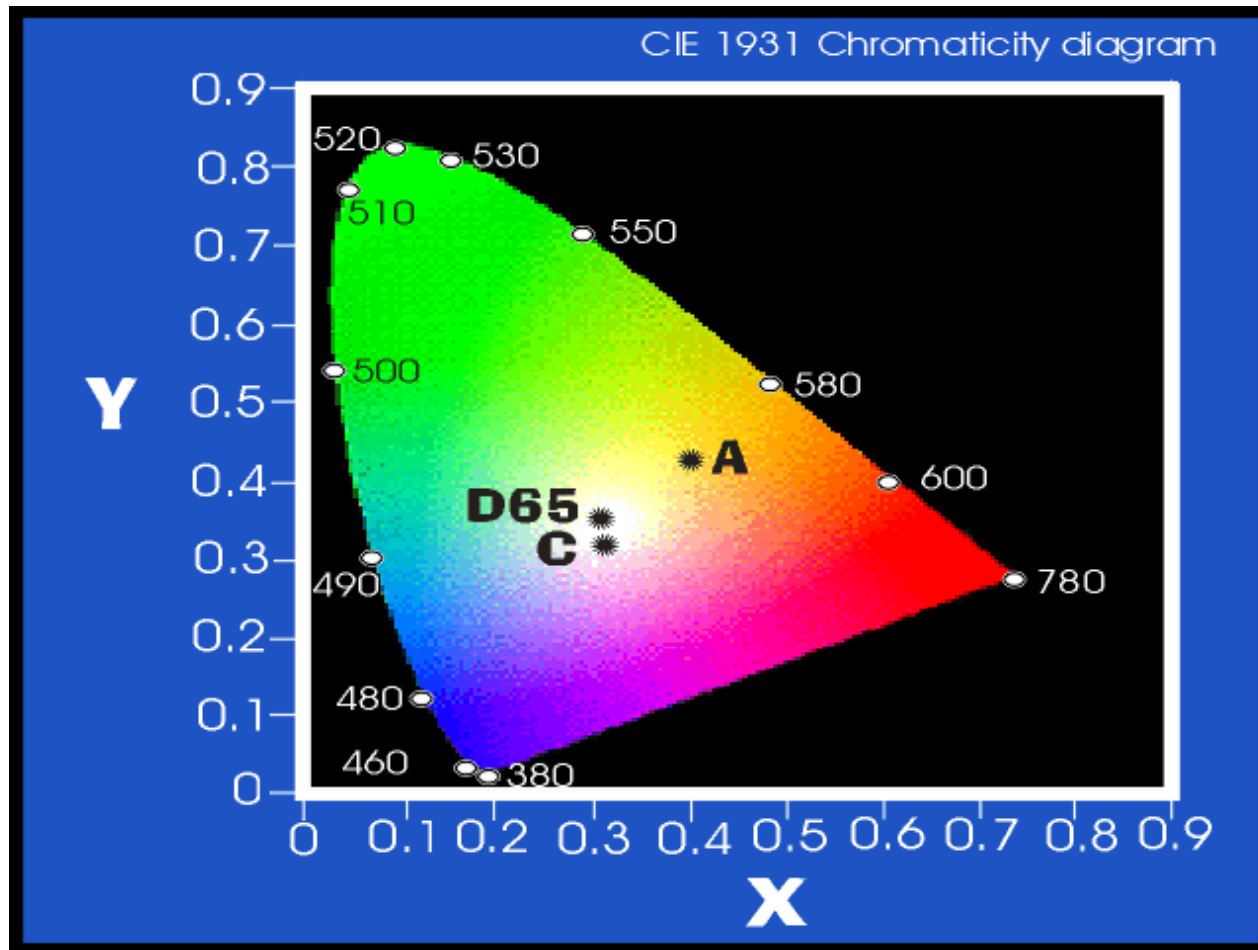
$$x = \frac{X}{X + Y + Z}$$

$$y = \frac{Y}{X + Y + Z}$$

$$z = \frac{Z}{X + Y + Z}$$



Colorimetry: Illuminants in the xy-plane



Light Sources and Illuminants

Light sources:

sun, candle,
fluorescent lamp,
incandescent lamp

Illuminants:

illuminant A
illuminant D65
illuminant C

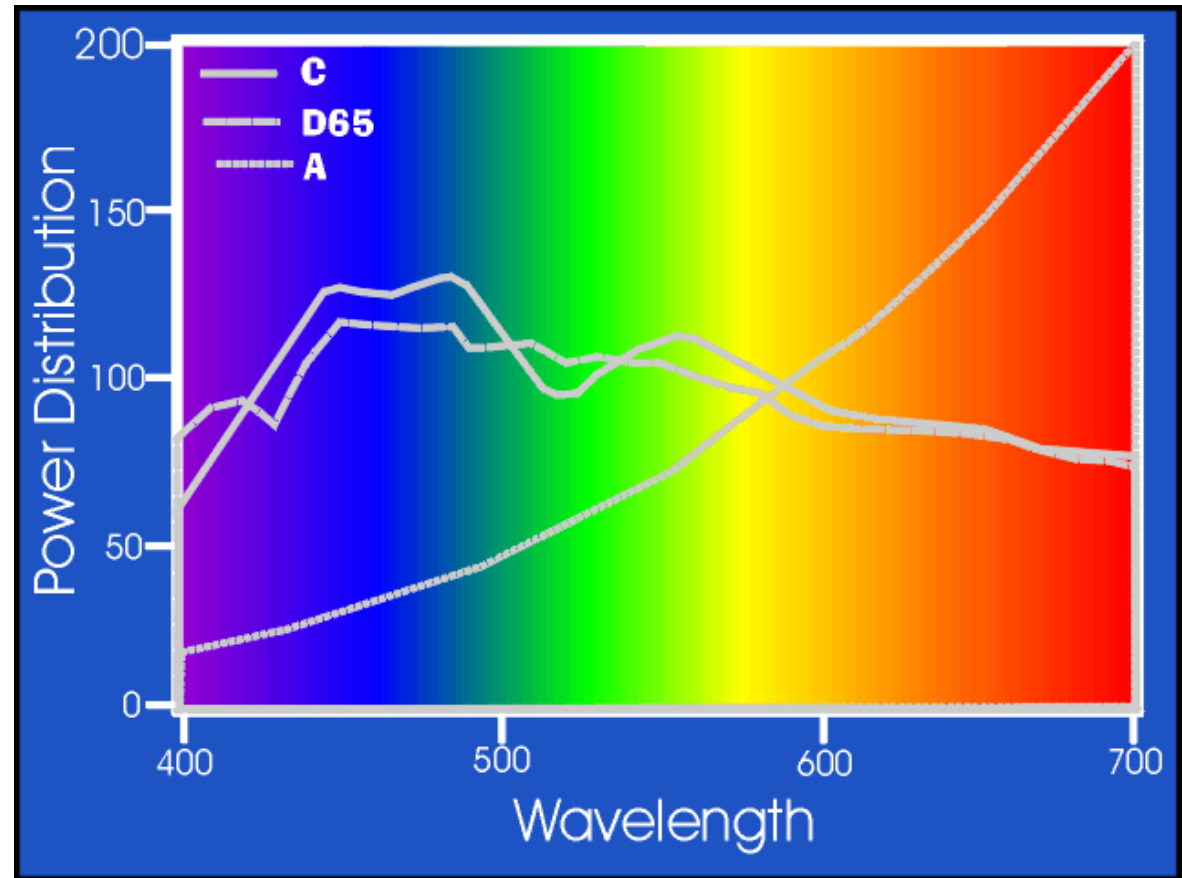
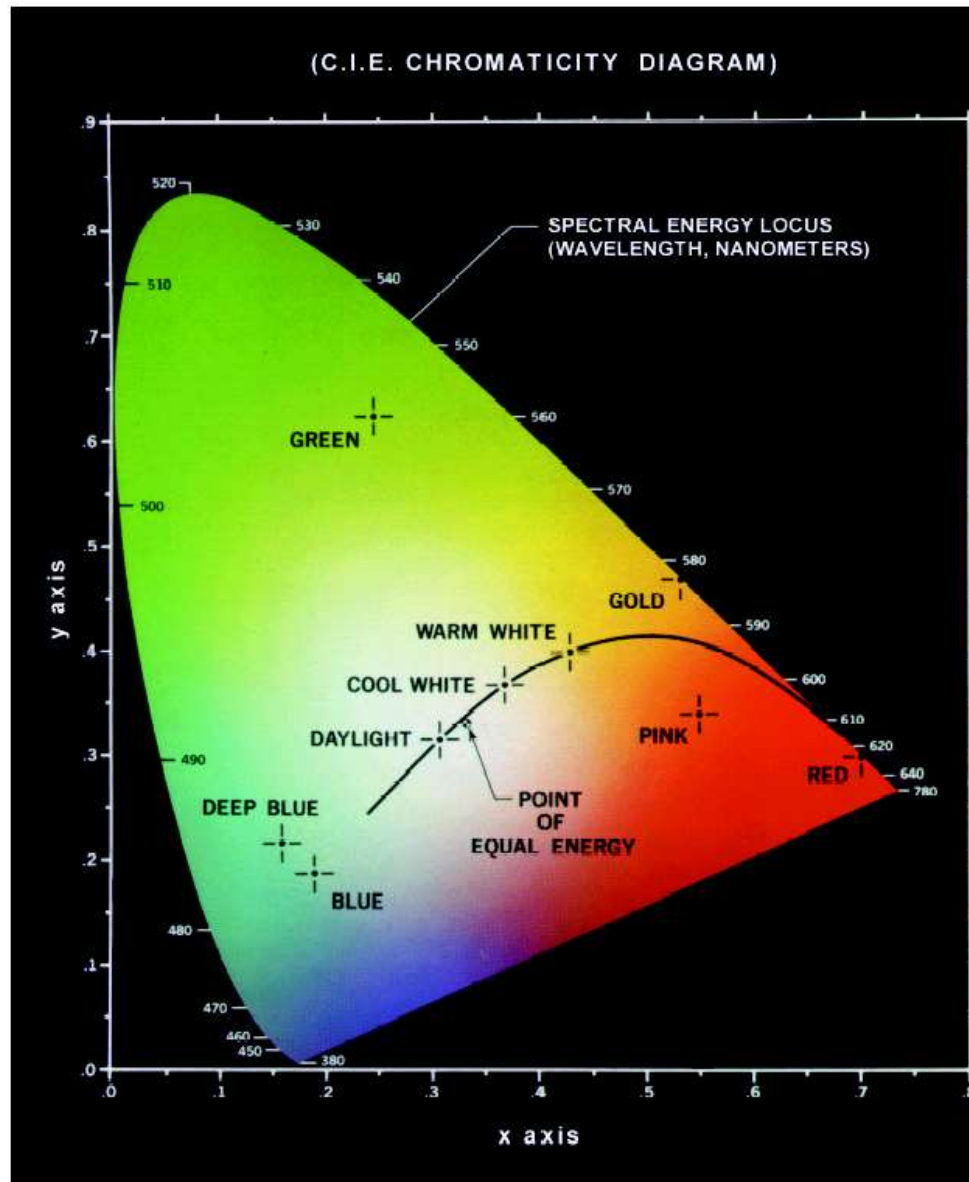
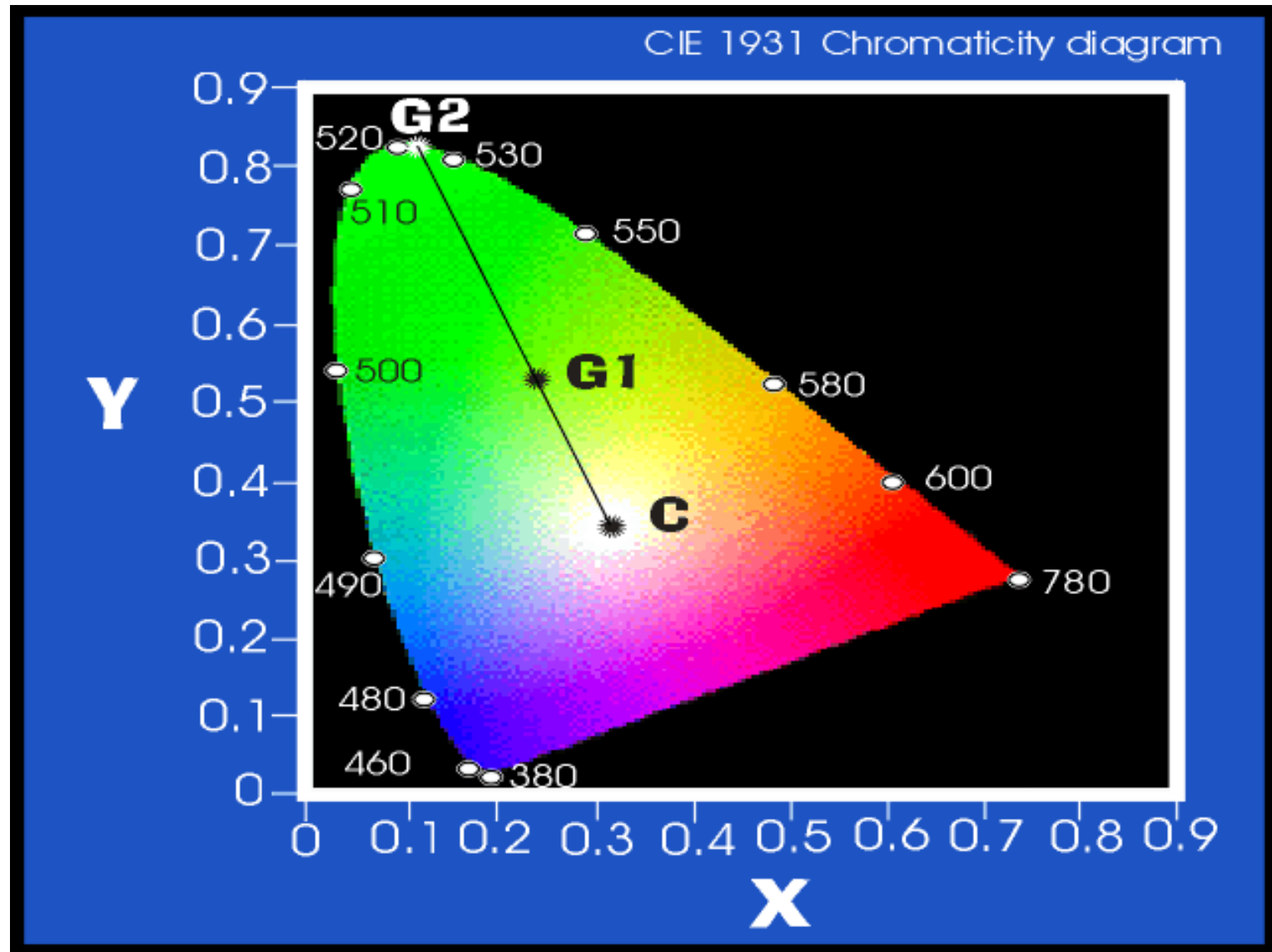


FIGURE 6.5
Chromaticity
diagram.
(Courtesy of the
General Electric
Co., Lamp
Business
Division.)



Colorimetry: HSI in the xy-plane

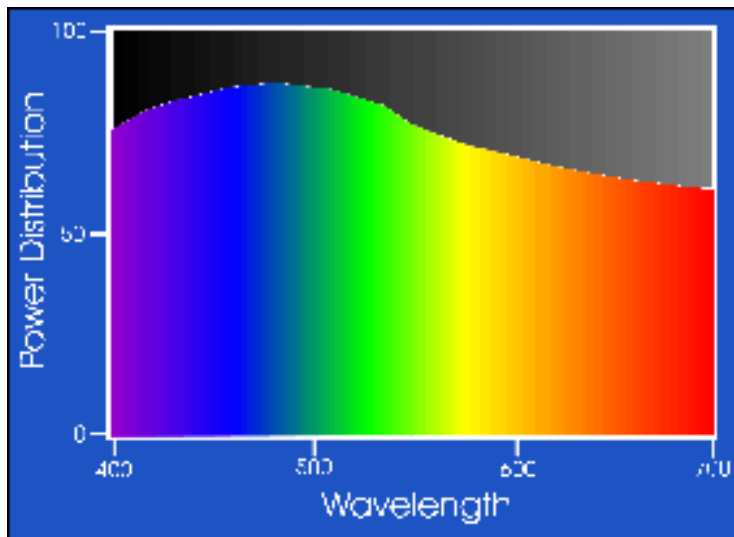


Spectral Power Distribution

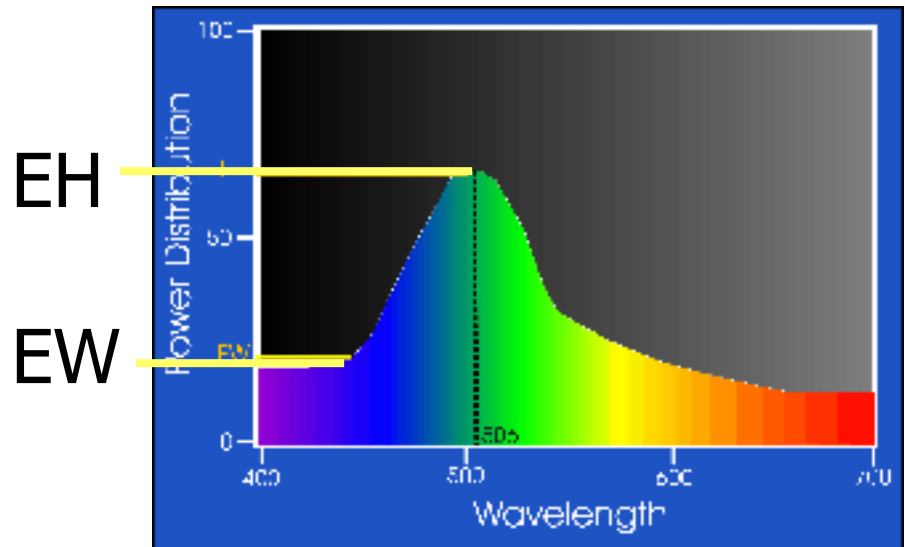
Hue: dominant wavelength of the SPD: EH

Saturation: purity of the colour: EH-EW

Intensity: brightness of the colour: EW



White light

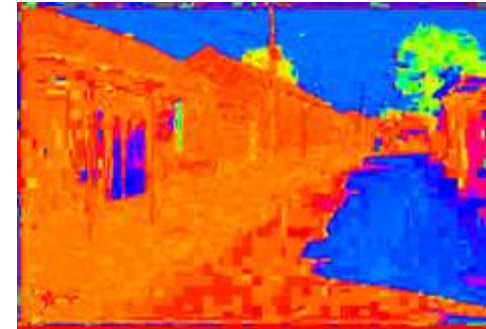
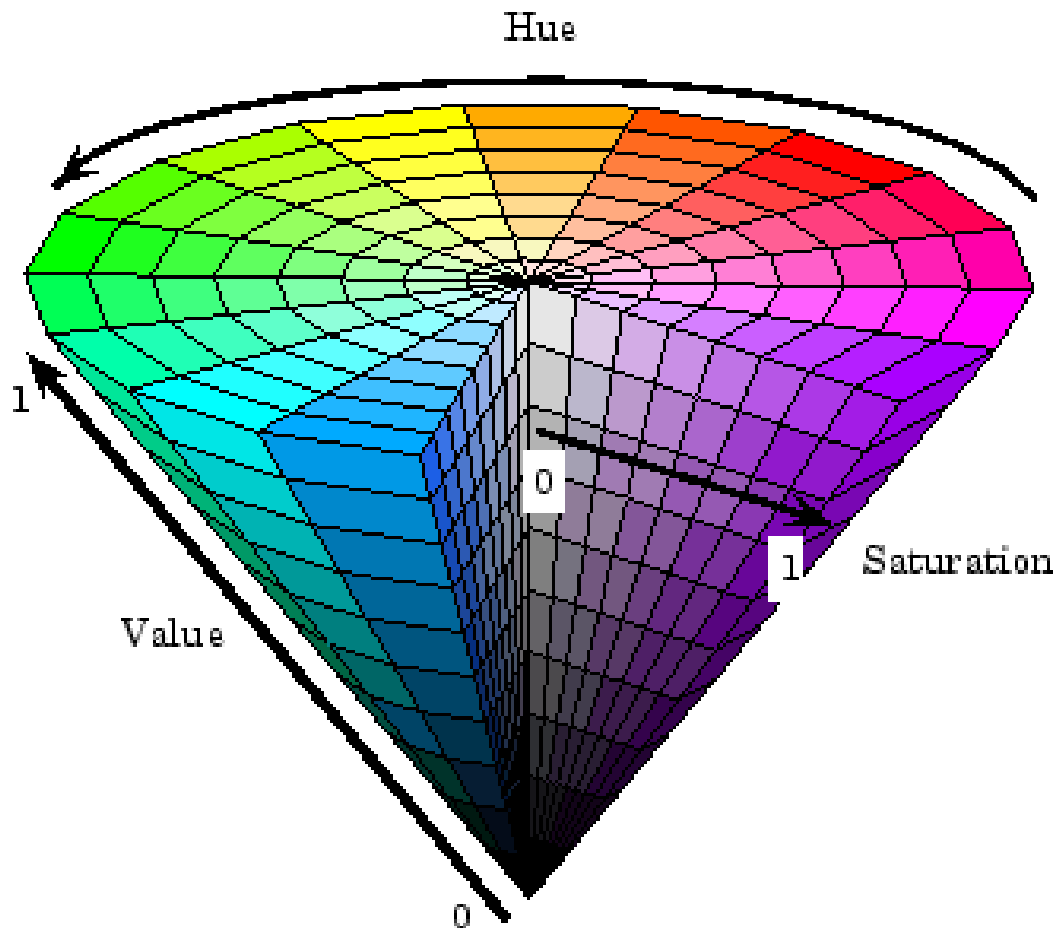


Green light

Color Spaces: HSV



Intuitive color space



H
(S=1,V=1)

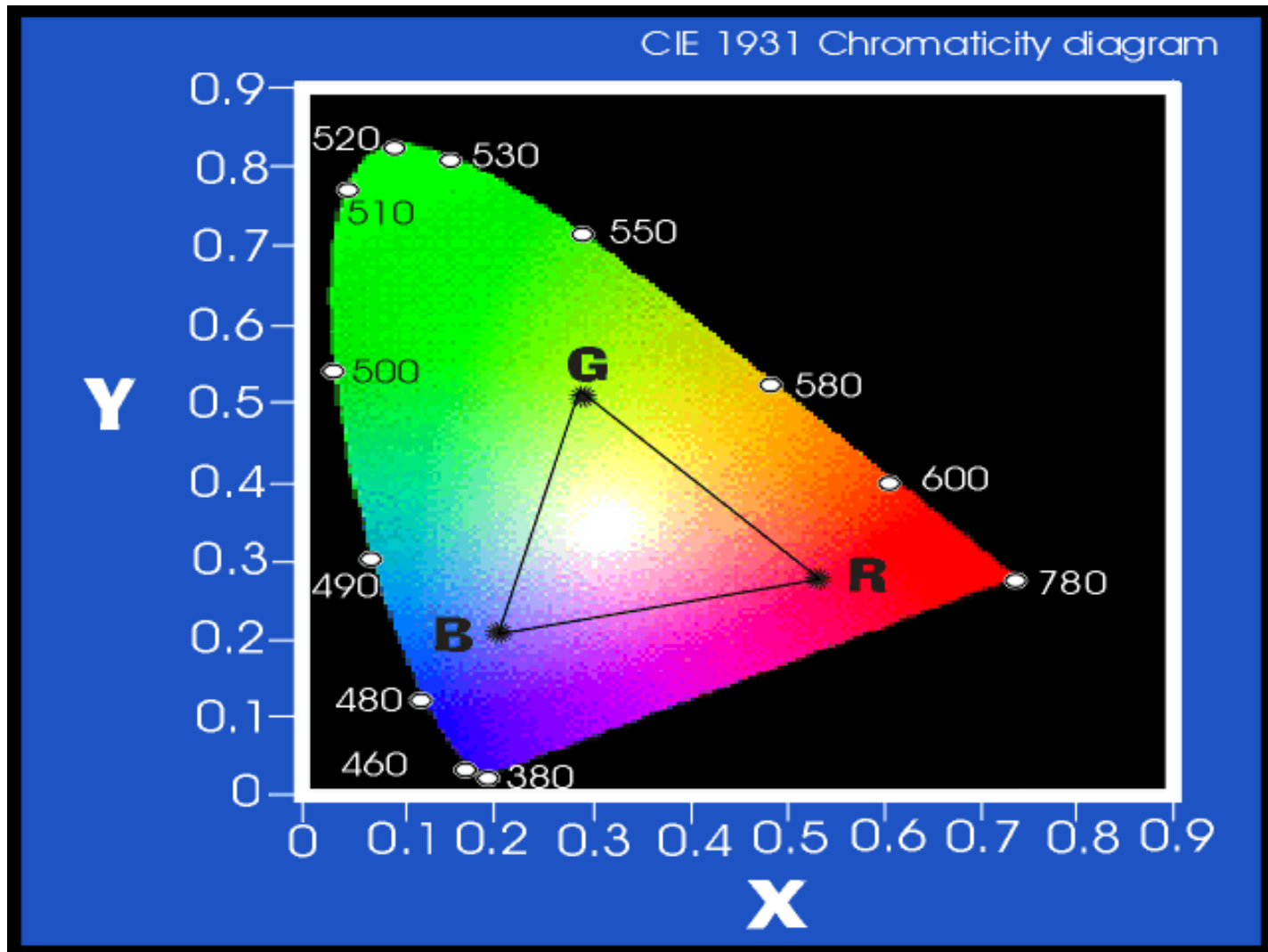


S
(H=1,V=1)



V
(H=1,S=0)

Colour Gamuts in the xy-plane



Monitor/Print/Scanner Gamut

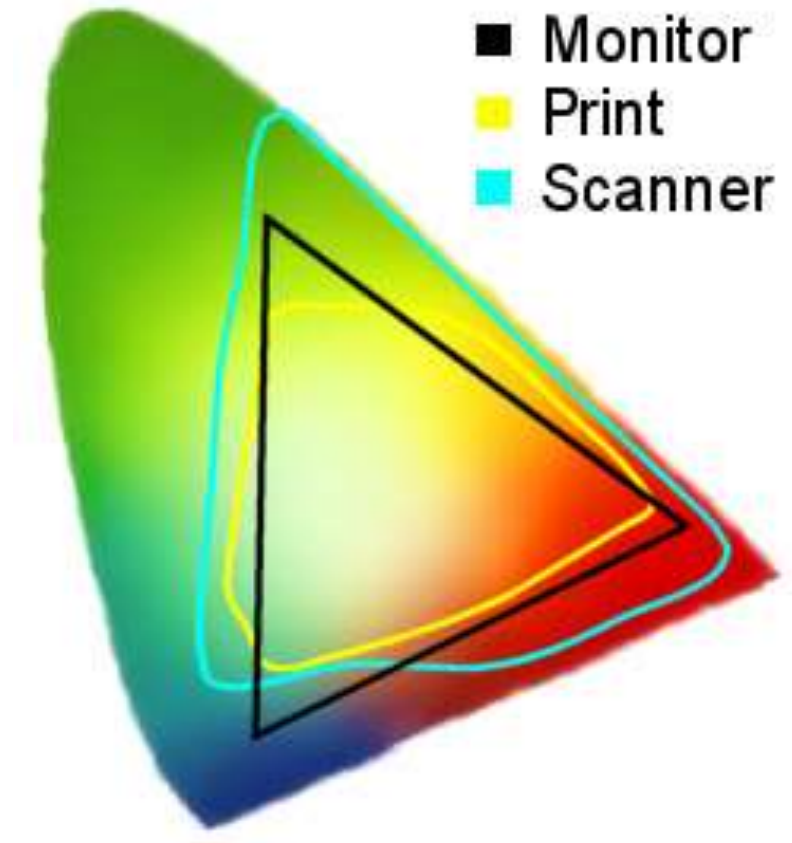
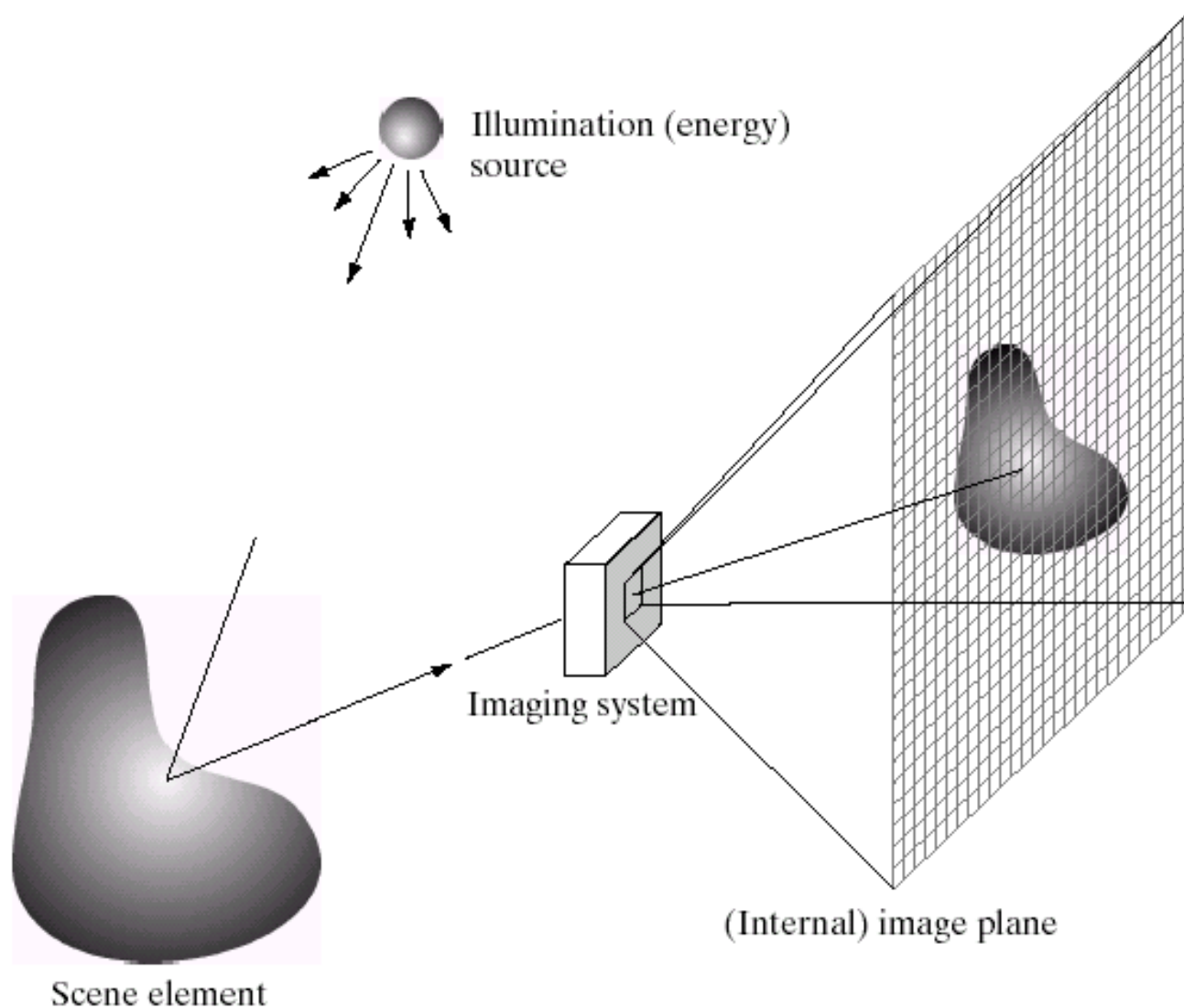


Image Formation



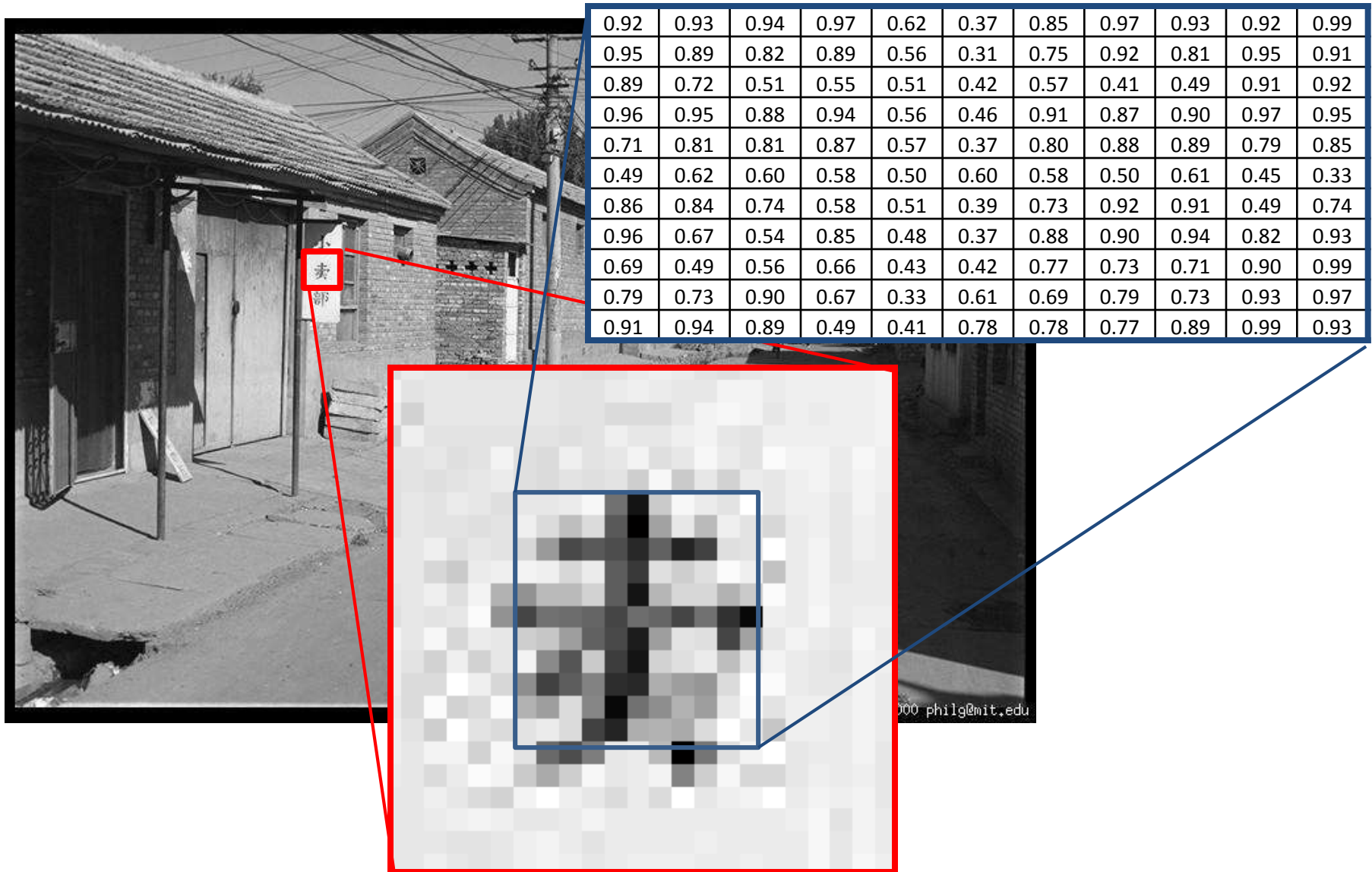
Digital camera



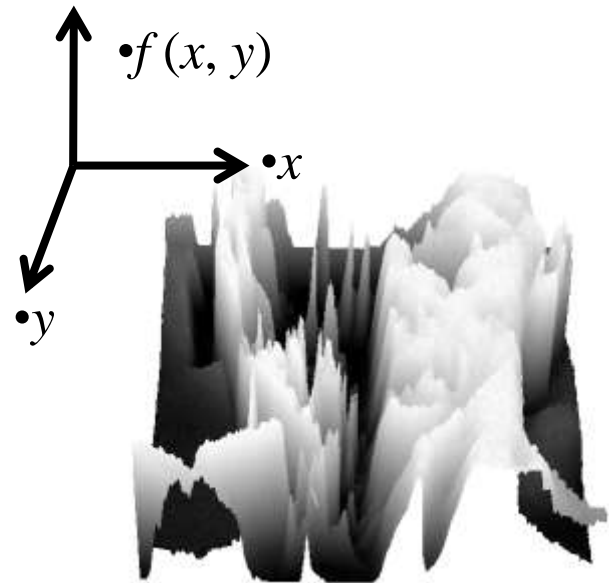
A digital camera replaces film with a sensor array

- Each cell in the array is light-sensitive diode that converts photons to electrons
- Two common types: Charge Coupled Device (CCD) and CMOS
- <http://electronics.howstuffworks.com/digital-camera.htm>

The Raster Image (Pixel Matrix)



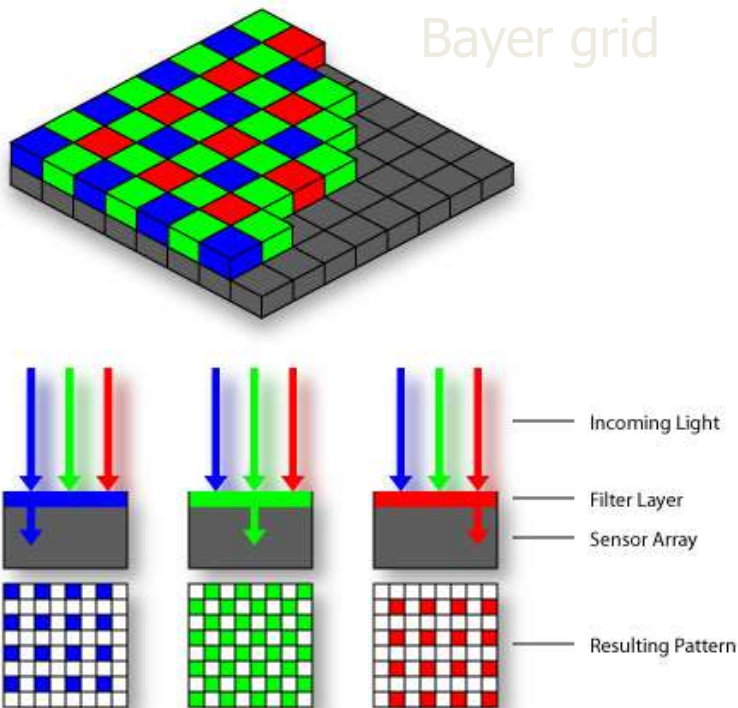
- We can think of a (grayscale) image as a **function**, f , from \mathbb{R}^2 to \mathbb{R} (or a 2D *signal*):
 - $f(x, y)$ gives the **intensity** at position (x, y)



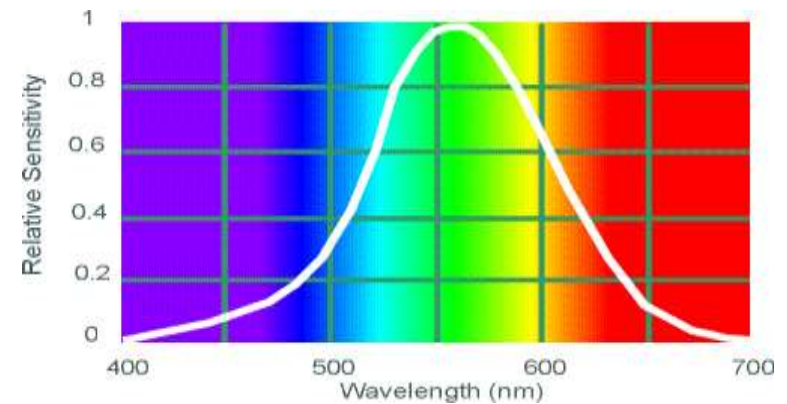
- A **digital** image is a discrete (**sampled, quantized**) version of this function

Color Sensing in Camera: Color Filter Array

- In traditional systems, color filters are applied to a single
- layer of photodetectors in a tiled mosaic pattern.



Why more green?



Human Luminance Sensitivity Function

Today's class: Image Formation

1. Projective Geometry and Camera Models

2. Light and Color Models

3. Reflection Models (Reading 2.2, paper on color models)

Including slides from Derek Hoiem, Alexei Efros, Steve Seitz, and David Forsyth, James Hays, Jinxiang Chai

Basic Principles of Surface Reflectance

Slides from Shree Nayar, Ravi Ramamoorthi, Pat Hanrahan

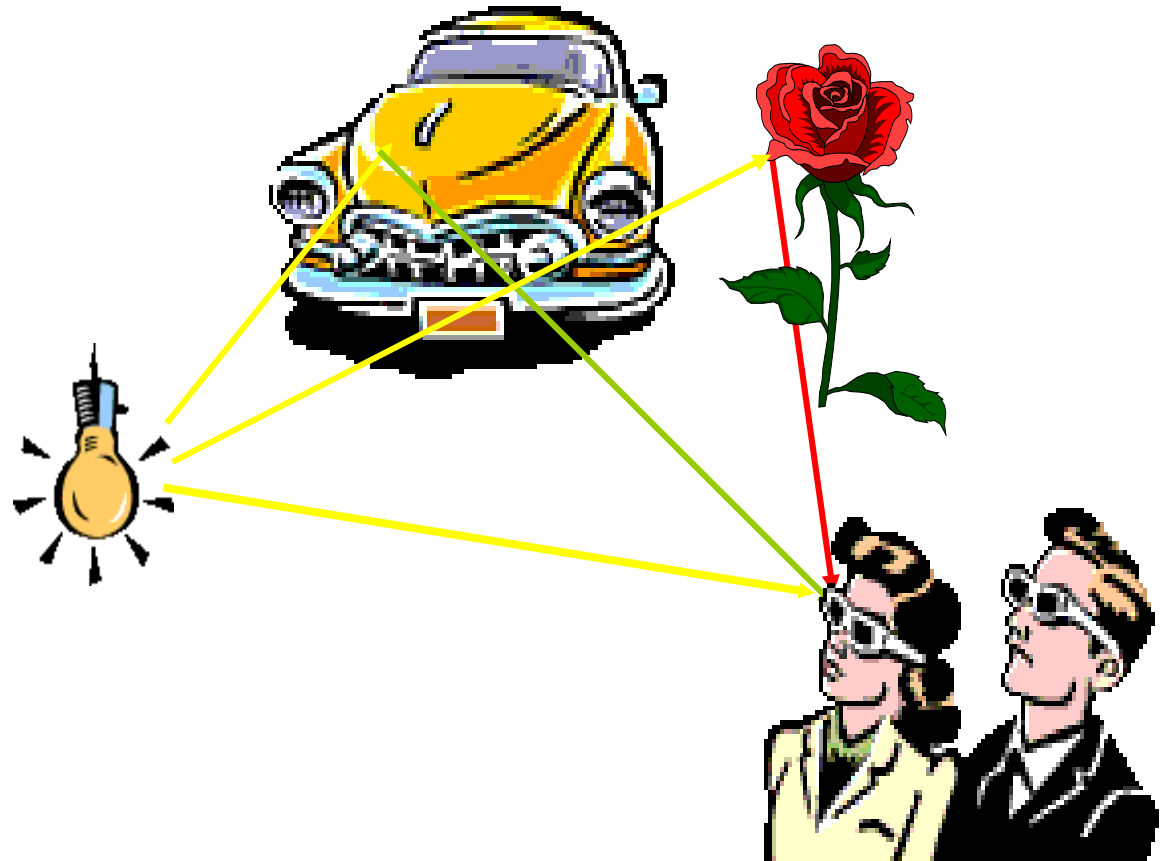
What makes an image?

the triplet light-objects-observer

Light source

Object(s)

Sensor



Surface Appearance

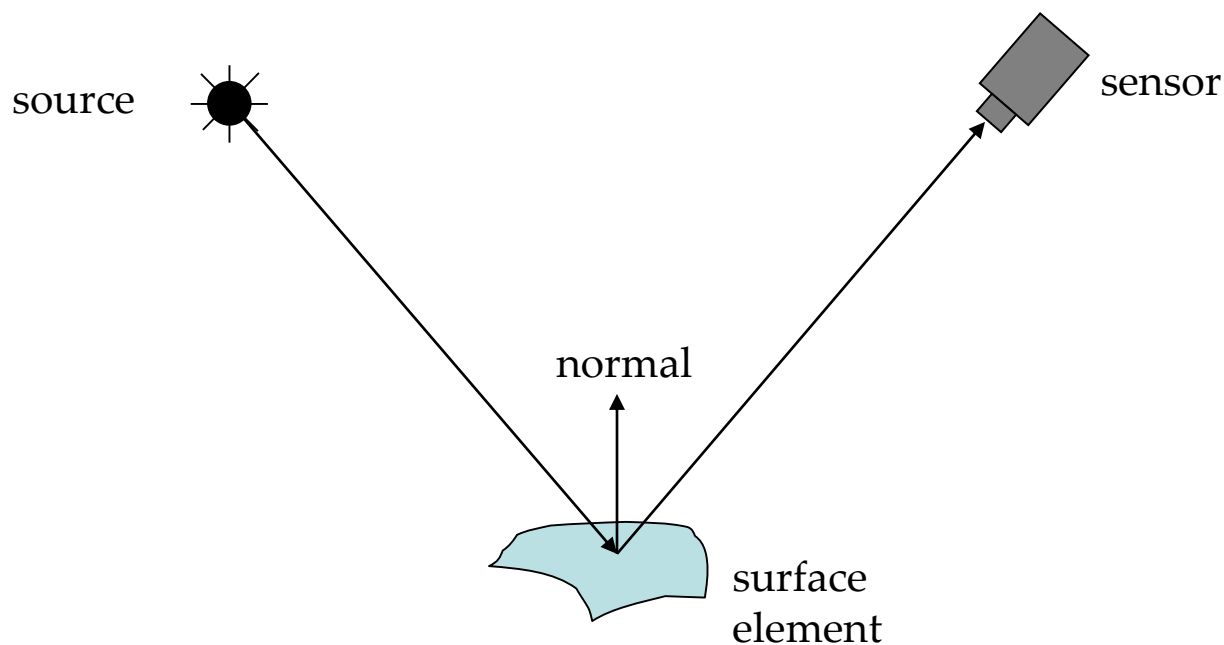
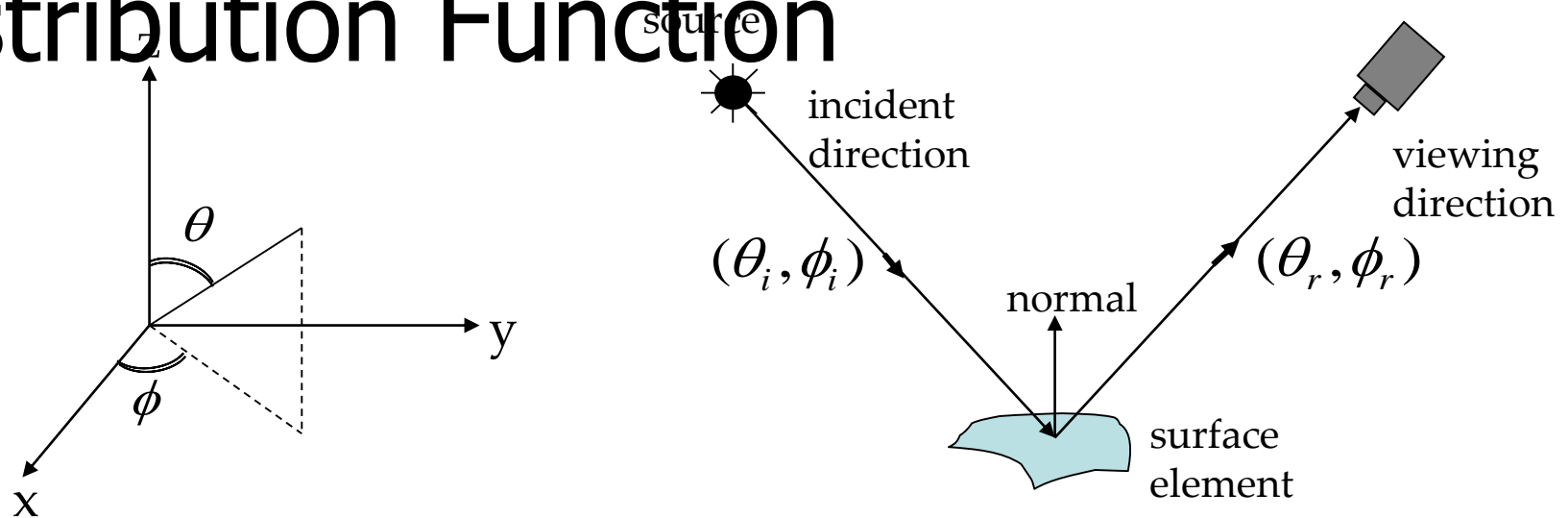


Image intensities = $f(\text{normal, surface reflectance, illumination})$

Surface Reflection depends on both the viewing and illumination direction.

BRDF: Bidirectional Reflectance Distribution Function

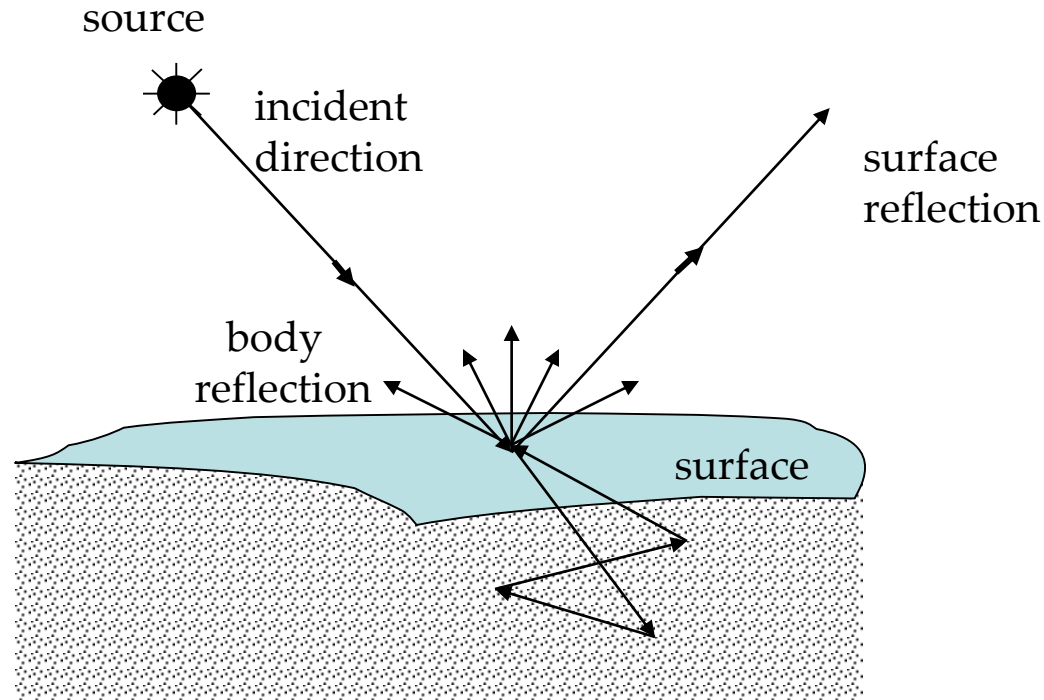


$E^{surface}(\theta_i, \phi_i)$ Irradiance at Surface in direction (θ_i, ϕ_i)

$L^{surface}(\theta_r, \phi_r)$ Radiance of Surface in direction (θ_r, ϕ_r)

$$\text{BRDF } f(\theta_i, \phi_i; \theta_r, \phi_r) = \frac{L^{surface}(\theta_r, \phi_r)}{E^{surface}(\theta_i, \phi_i)}$$

Mechanisms of Surface Reflection



Body Reflection:

Diffuse Reflection
Matte Appearance
Non-Homogeneous Medium
Clay, paper, etc

Surface Reflection:

Specular Reflection
Glossy Appearance
Highlights
Dominant for Metals

$$\text{Image Intensity} = \text{Body Reflection} + \text{Surface Reflection}$$

Mechanisms of Surface Reflection

Body Reflection:

Diffuse Reflection
Matte Appearance
Non-Homogeneous Medium
Clay, paper, etc



Surface Reflection:

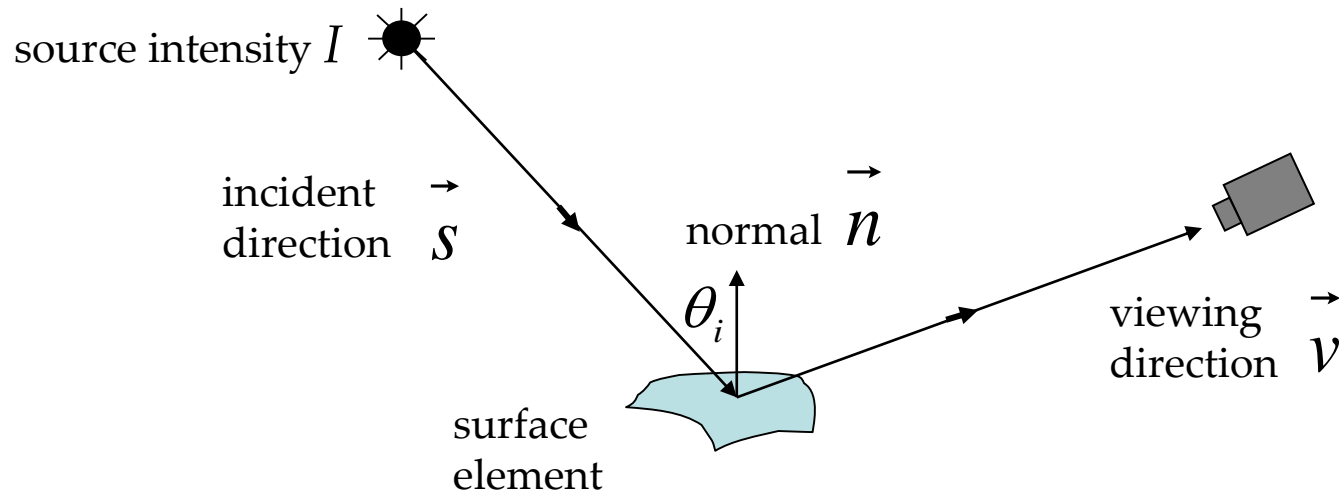
Specular Reflection
Glossy Appearance
Highlights
Dominant for Metals



Many materials exhibit both Reflections:

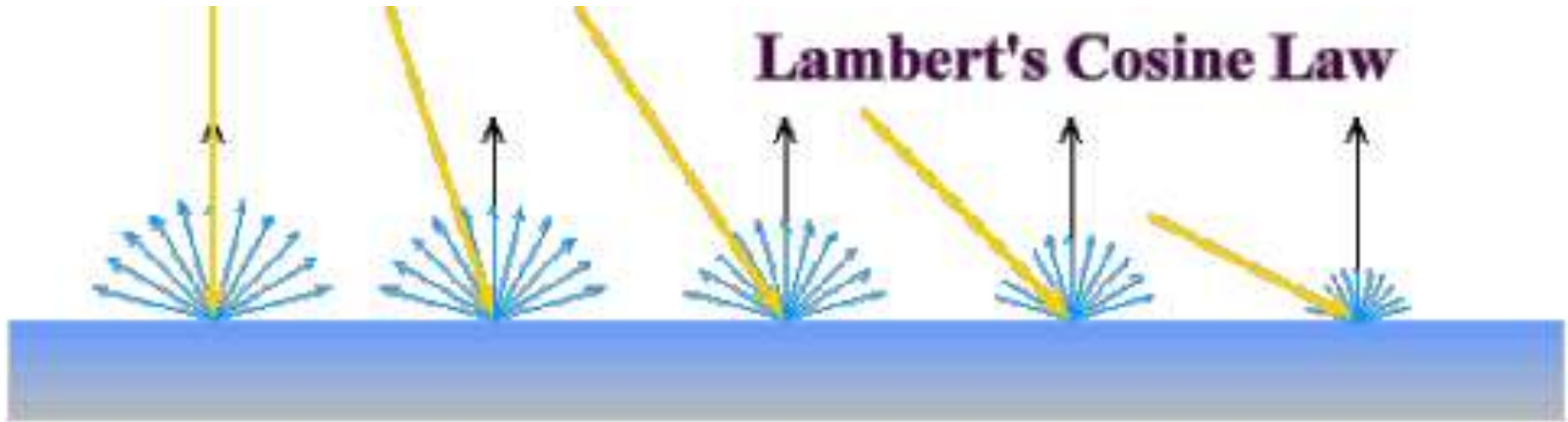


Diffuse Reflection and Lambertian BRDF



- Surface appears equally bright from ALL directions! (independent of \vec{v})
- Lambertian BRDF is simply a constant : $f(\theta_i, \phi_i; \theta_r, \phi_r) = \frac{\rho_d}{\pi}$ ↗ albedo
- Surface Radiance : $L = \frac{\rho_d}{\pi} I \cos \theta_i = \frac{\rho_d}{\pi} I \vec{n} \cdot \vec{s}$ ↘ source intensity
- Commonly used in Vision and Graphics!

Diffuse Reflection and Lambertian BRDF



Overcast Sky



Can't perceive the shape of the snow covered terrain

Face Analysis

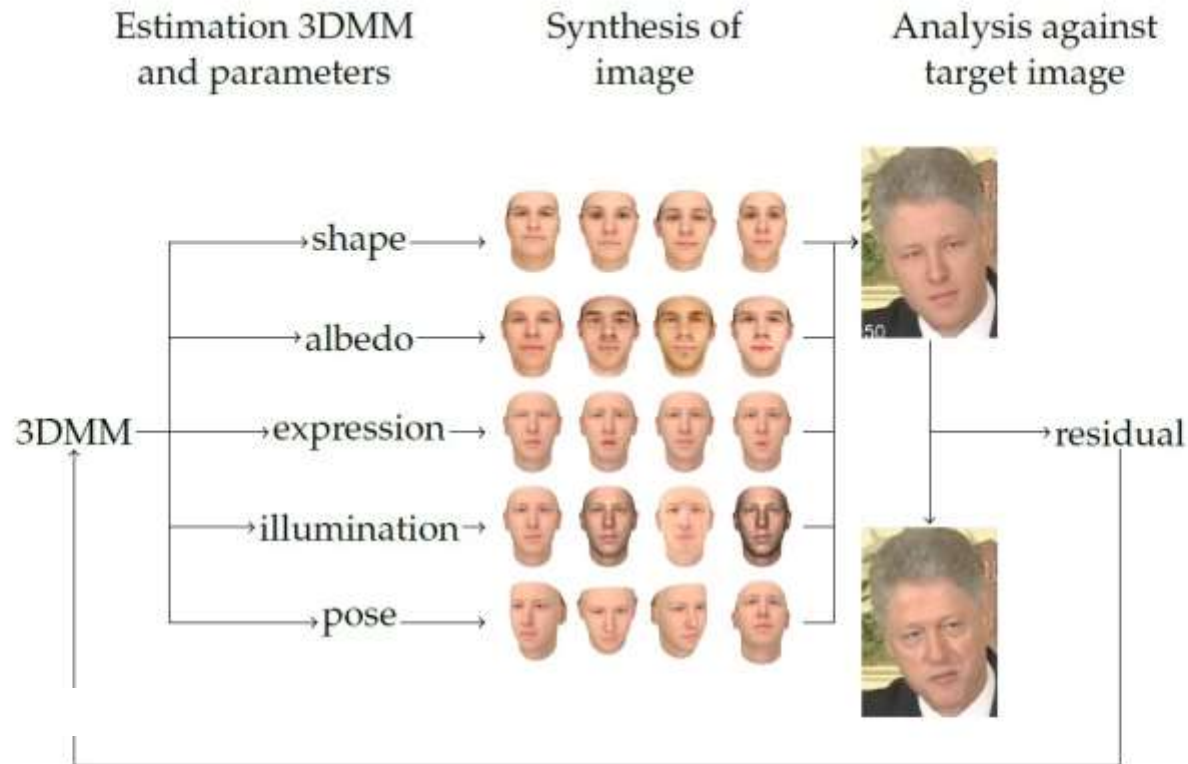

















FIGURE 1.1: Example of 3DMM fitting following an analysis-by-synthesis approach. From left to right: The 3D Morphable Model, prediction of parameters for the different components of the optimization problem and rendered results, analyses against target image, and feedback loop.

Diffuse Reflection

Input Image	Albedo	Lighting	Surface Normals	Reconstruction
				
				
				

Diffuse Reflection

Input Image	Albedo	Lighting	Surface Normals	Reconstruction
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Diffuse Reflection: Albedo



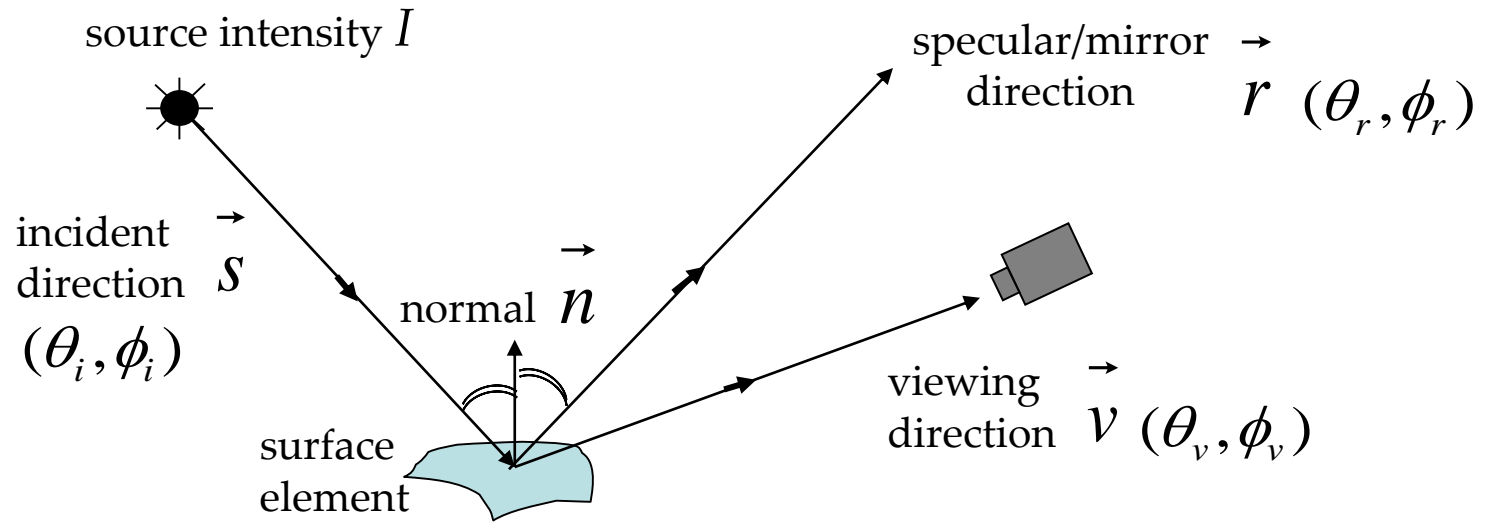
Diffuse Reflection: Illumination



Diffuse Reflection: Illumination/SH



Specular Reflection and Mirror BRDF



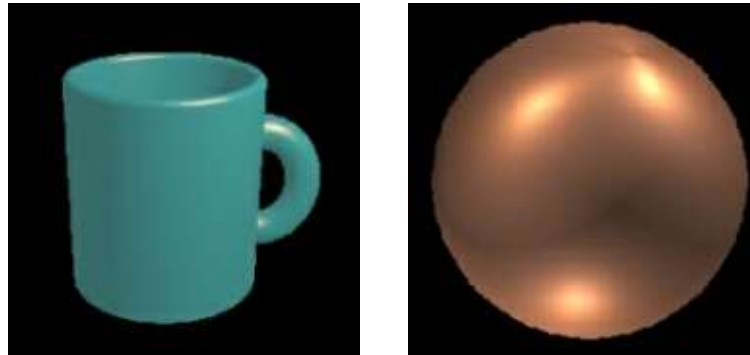
- Very smooth surface.
- All incident light energy reflected in a SINGLE direction. (only when $\vec{v} = \vec{r}$)
- Mirror BRDF is simply a double-delta function :

$$f(\theta_i, \phi_i; \theta_v, \phi_v) = \overset{\text{specular albedo}}{\rho_s} \delta(\theta_i - \theta_v) \delta(\phi_i + \pi - \phi_v)$$

- Surface Radiance : $L = I \rho_s \delta(\theta_i - \theta_v) \delta(\phi_i + \pi - \phi_v)$

Glossy Surfaces

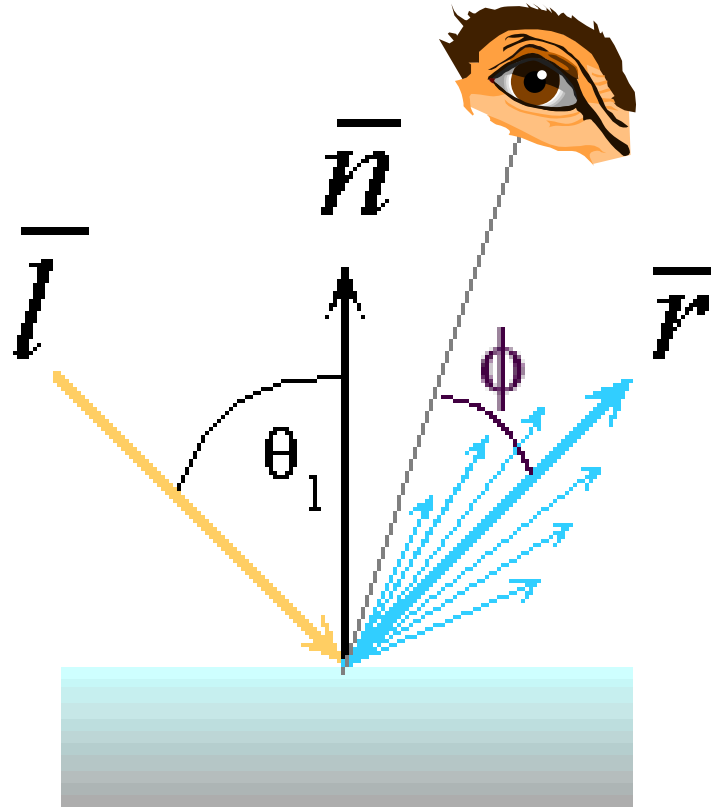
- Many glossy surfaces show broader highlights in addition to specular reflection.



- Example Models : Phong Model (no physical basis, but sort of works (empirical))

Phong Model: An Empirical Approximation

- An illustration of the angular falloff of highlights:

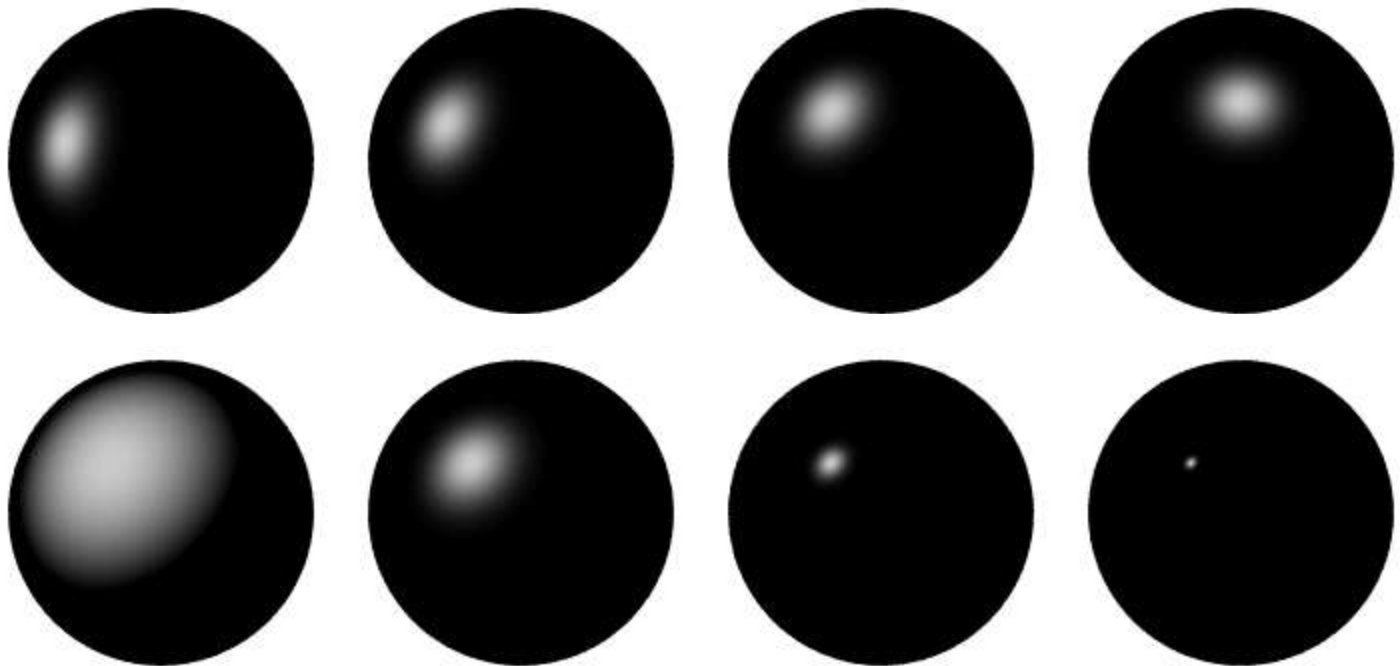


$$L = I \rho_s (\cos \phi)^{n_{shiny}}$$

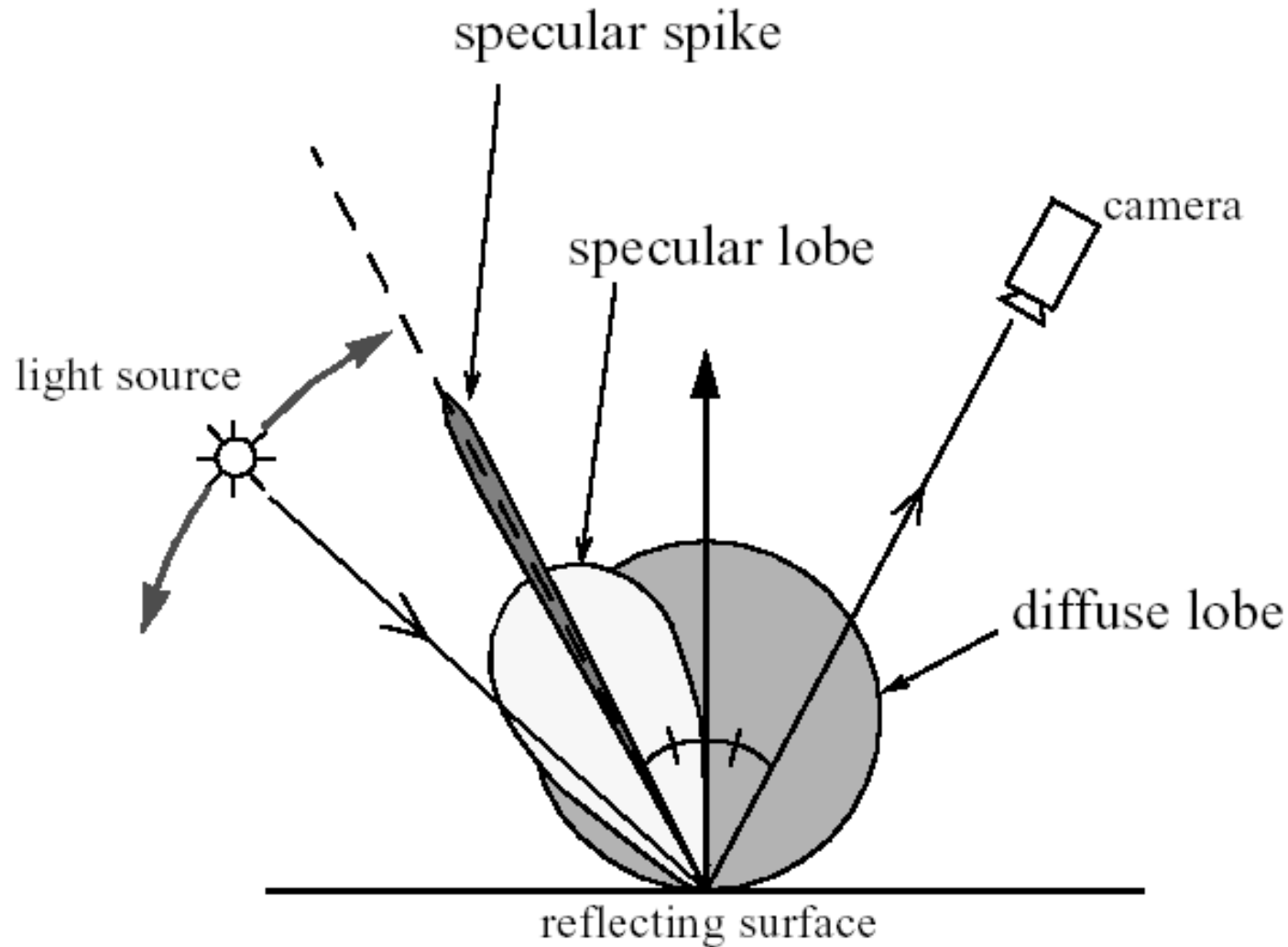
- Very commonly used in Computer Graphics

Phong Examples

- These spheres illustrate the Phong model as *lighting*
- *direction* and n_{shiny} are varied:



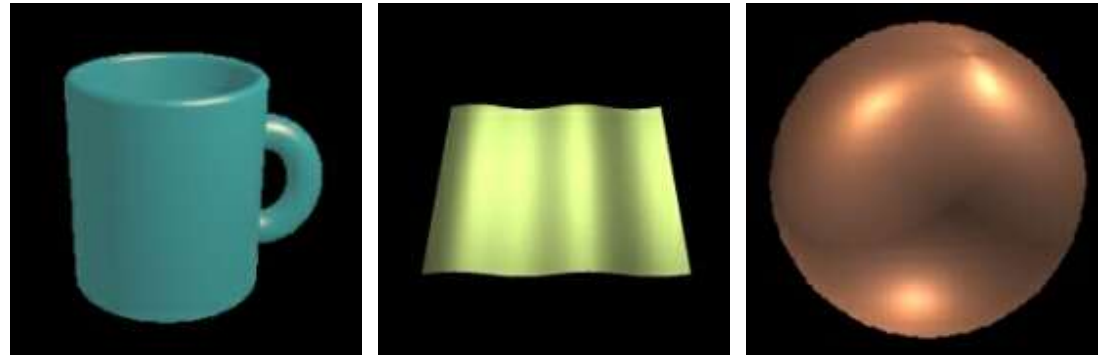
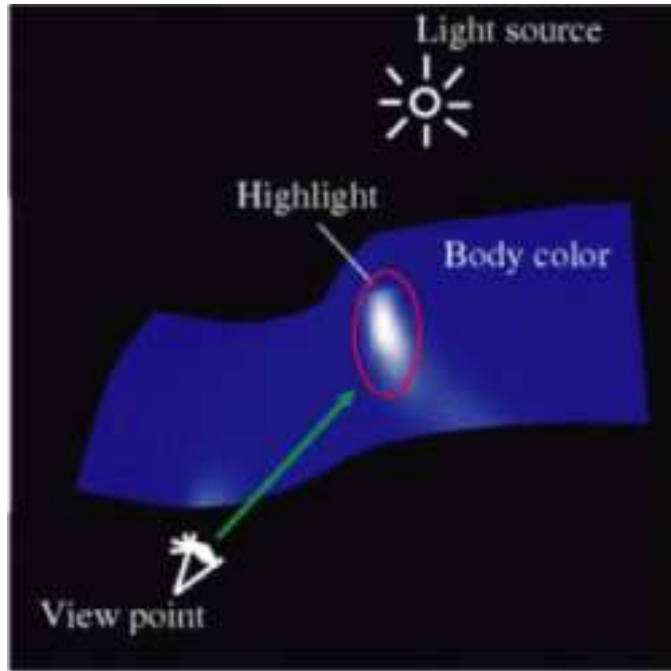
All components of Surface Reflection



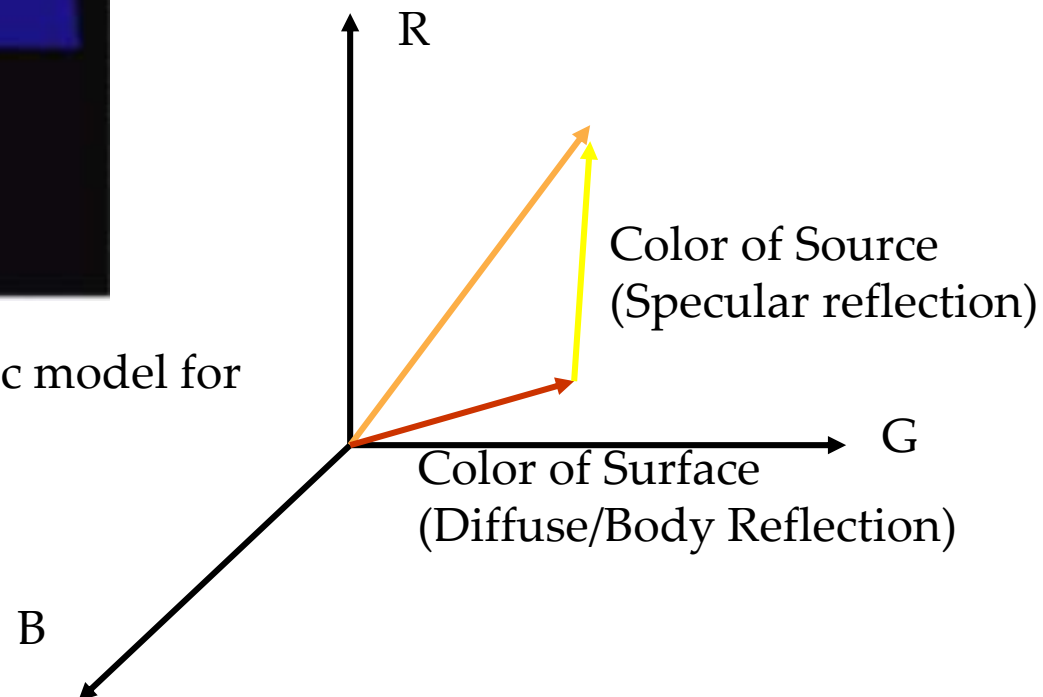
A Simple Reflection Model - Dichromatic Reflection

$$\text{Observed Image Color} = a \times \text{Body Color} + b \times \text{Specular Reflection Color}$$

Klinker-Shafer-Kanade 1988

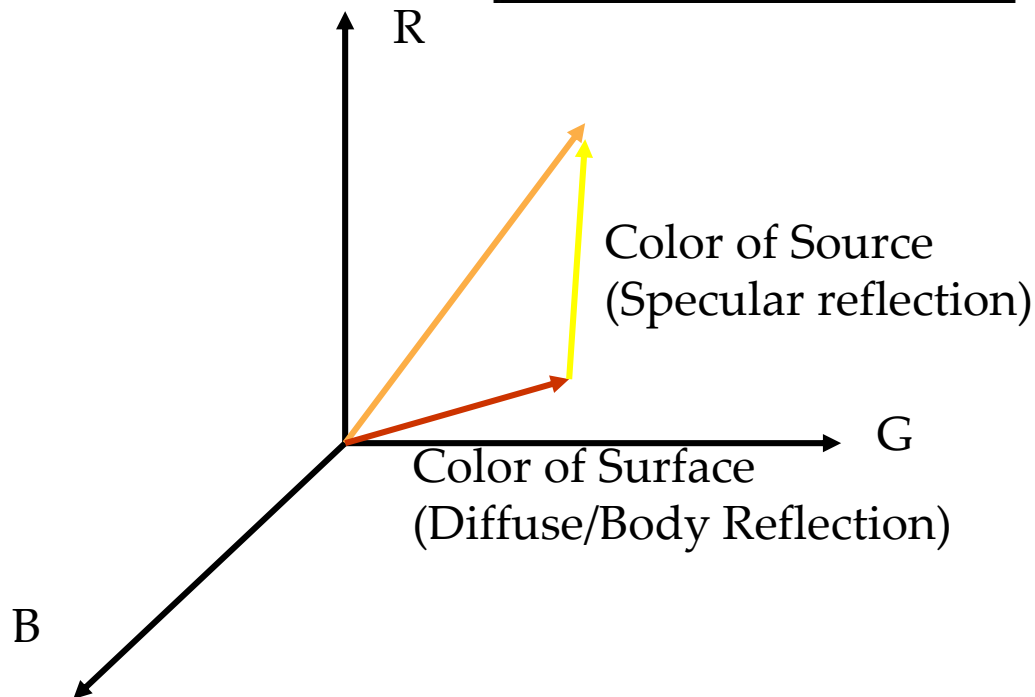
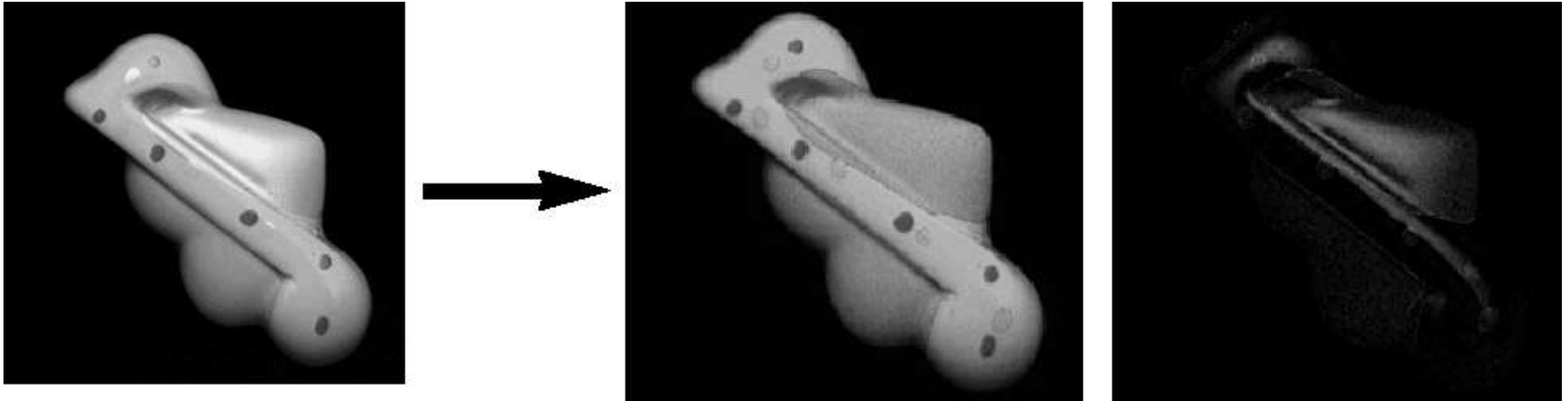


Does not specify any specific model for
Diffuse/specular reflection



Separating Diffuse and Specular Reflections

Observed Image Color = $a \times \text{Body Color} + b \times \text{Specular Reflection Color}$



Computer Vision 1

(total #slides 110 / Lecture 2)

Summary on Image Formation

1. Projective Geometry and Camera Models
2. Light and Color Models
3. Reflection Models