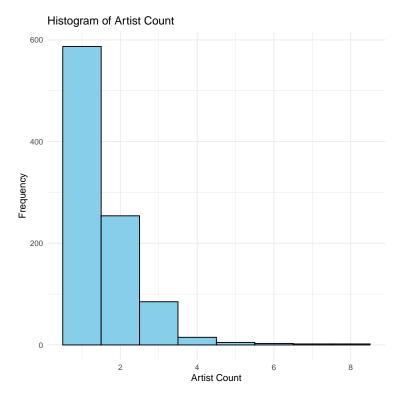
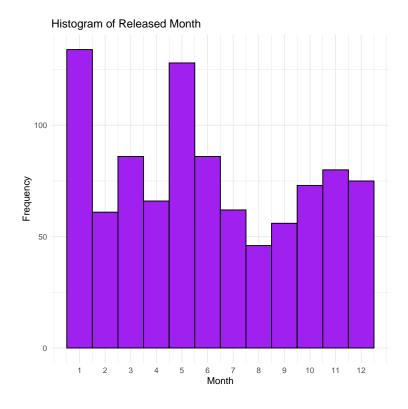
March 1, 2024

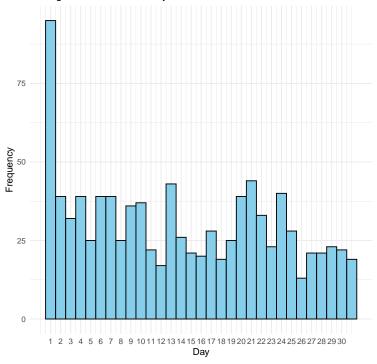
The results below are generated from an R script.

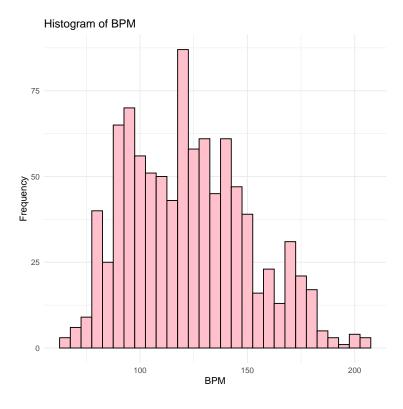


Histogram of Released Year 300 100 1925 1950 1975 Released Year



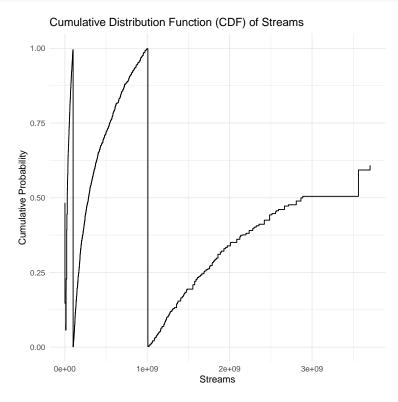
Histogram of Released Day





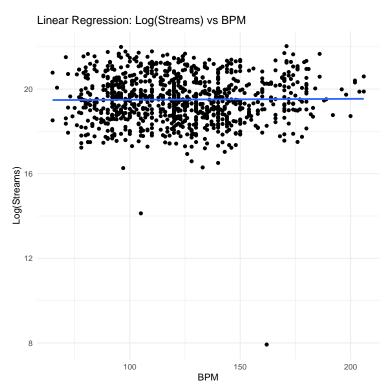
```
# Calculate statistics for each variable
statistics <- summarise(spotify_data,</pre>
                                                              artist_count_mean = mean(artist_count),
                                                              released_year_mean = mean(released_year),
                                                              released_month_mean = mean(released_month),
                                                              released_day_mean = mean(released_day),
                                                              in_spotify_charts_mean = mean(in_spotify_charts),
                                                              bpm_mean = mean(bpm),
                                                              artist_count_mode = as.numeric(names(sort(table(artist_count), decreasing = TRU)
                                                              released_year_mode = as.numeric(names(sort(table(released_year), decreasing = The table (released_year)), decreasing = The table (released_year) = The table (released_yea
                                                              released_month_mode = as.numeric(names(sort(table(released_month), decreasing =
                                                              released_day_mode = as.numeric(names(sort(table(released_day), decreasing = TRU)
                                                              in_spotify_charts_mode = as.numeric(names(sort(table(in_spotify_charts), decreas))
                                                              bpm_mode = as.numeric(names(sort(table(bpm), decreasing = TRUE)[1])),
                                                              bpm_sd = sd(bpm),
                                                              streams_quantile_25 = quantile(streams, 0.25),
                                                              streams_quantile_75 = quantile(streams, 0.75),
                                                              bpm_quantile_25 = quantile(bpm, 0.25),
                                                              bpm_quantile_75 = quantile(bpm, 0.75),
)
## Error in 'summarise()':
## i In argument: 'streams_quantile_25 = quantile(streams, 0.25)'.
## Caused by error in '(1 - h) * qs[i]':
## ! non-numeric argument to binary operator
# print statistics
print(statistics)
             artist_count_mean released_year_mean released_month_mean released_day_mean
```

```
## 1 1.556723
                                2018.289 6.038866 13.94433
## in_spotify_charts_mean bpm_mean artist_count_mode released_year_mode
## 1
                  12.02206 122.5536
                                                   1
## released_month_mode released_day_mode in_spotify_charts_mode bpm_mode bpm_sd
## 1
                                       1
                                                                     120 28.0696
                     1
## streams_quantile_25 streams_quantile_75 bpm_quantile_25 bpm_quantile_75
## 1
              141636175
                                  673869022
                                                      99.75
# PMF
# compare two scenarios in your data using a PMF
total songs <- nrow(spotify data)</pre>
# songs released in 2023
songs_2023 <- spotify_data %>%
 filter(released_year == 2023) %>%
 nrow()
pmf_2023 <- songs_2023 / total_songs
# songs released in other years
songs_other_years <- spotify_data %>%
 filter(released_year != 2023) %>%
  nrow()
pmf_other_years <- songs_other_years / total_songs</pre>
# display PMFs
print(paste("Probability of a song being released in 2023:", pmf 2023))
## [1] "Probability of a song being released in 2023: 0.183630640083945"
print(paste("Probability of a song being released in other years:", pmf_other_years))
## [1] "Probability of a song being released in other years: 0.816369359916055"
# CDF
# sort the data by streams variable
streams <- spotify_data[order(spotify_data$streams), ]</pre>
# calculate the cumulative probabilities
streams$cdf <- seq(1, nrow(streams)) / nrow(streams)</pre>
# convert streams variable to numeric, removes scientific notation
streams$streams <- as.numeric(streams$streams)</pre>
## Warning: NAs introduced by coercion
# logarithmic scaling streams variable
streams$log_streams <- log(streams$streams)</pre>
# plot the CDF
ggplot(streams, aes(x = streams, y = cdf)) +
geom_step() +
```



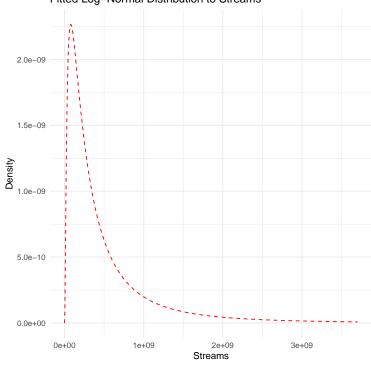
```
# Analytical Distribution
# remove rows with missing values
spotify_data$streams <- as.numeric(as.character(spotify_data$streams))
## Warning: NAs introduced by coercion
spotify_data$bpm <- as.numeric(as.character(spotify_data$bpm))
# removes invalid values from streams and bpm
spotify_data <- spotify_data[complete.cases(spotify_data$streams, spotify_data$bpm), ]
# apply logarithmic transformation to streams
spotify_data$log_streams <- log(spotify_data$streams)
# perform linear regression
regression_model <- lm(log_streams ~ bpm, data = spotify_data)
# summary of regression model
summary(regression_model)
###
## ## Call:</pre>
```

```
## lm(formula = log_streams ~ bpm, data = spotify_data)
##
## Residuals:
##
                1Q Median
       Min
                                   3Q
                                           Max
## -11.5995 -0.7411 -0.0192 0.8185
                                        2.5057
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.946e+01 1.666e-01 116.801 <2e-16 ***
              4.189e-04 1.325e-03
                                           0.752
                                   0.316
## bpm
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 1.147 on 950 degrees of freedom
## Multiple R-squared: 0.0001052, Adjusted R-squared: -0.0009473
## F-statistic: 0.09996 on 1 and 950 DF, p-value: 0.7519
# plot the regression line
ggplot(spotify_data, aes(x = bpm, y = log_streams)) +
  geom_point() +
 geom_smooth(method = "lm", se = FALSE) +
 labs(title = "Linear Regression: Log(Streams) vs BPM",
      x = "BPM",
      y = "Log(Streams)") +
 theme minimal()
## 'geom_smooth()' using formula = 'y ~ x'
```



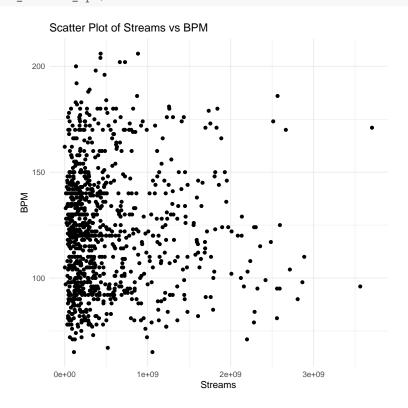
```
# plot the fitted log-normal distribution
ggplot() +
   geom_line(data = data.frame(x = x, y = y), aes(x = x, y = y), color = "red", linetype = "dashed") +
   labs(title = "Fitted Log-Normal Distribution to Streams",
        x = "Streams",
        y = "Density") +
   theme_minimal()
```

Fitted Log-Normal Distribution to Streams

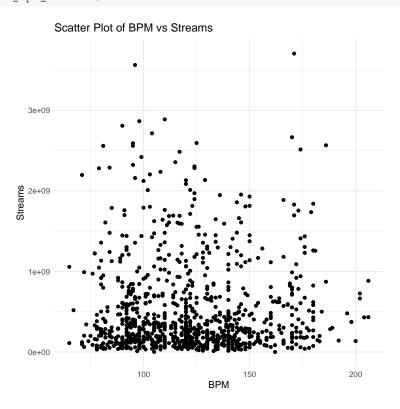


```
# scatter plot
# convert streams and bpm variables to numeric
spotify_data$streams <- as.numeric(as.character(spotify_data$streams))</pre>
spotify_data$bpm <- as.numeric(as.character(spotify_data$bpm))</pre>
# scatter plot for streams vs bpm
scatter_plot_streams_bpm <- ggplot(spotify_data, aes(x = streams, y = bpm)) +</pre>
  geom_point() +
  labs(title = "Scatter Plot of Streams vs BPM",
       x = "Streams",
       y = "BPM") +
  theme_minimal()
# scatter plot for bpm vs streams
scatter_plot_bpm_streams <- ggplot(spotify_data, aes(x = bpm, y = streams)) +</pre>
  geom_point() +
  labs(title = "Scatter Plot of BPM vs Streams",
       x = "BPM",
       y = "Streams") +
  theme_minimal()
```

Print both scatter plots
print(scatter_plot_streams_bpm)



print(scatter_plot_bpm_streams)



```
# conducted test
# perform Pearson's correlation test
cor_results <- cor.test(spotify_data$streams, spotify_data$bpm)</pre>
# print the test result
cor_results
##
## Pearson's product-moment correlation
##
## data: spotify_data$streams and spotify_data$bpm
## t = -0.075142, df = 950, p-value = 0.9401
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## -0.06596511 0.06110897
## sample estimates:
##
            cor
## -0.002437908
# conduct a regression analysis
# linear regression
regression_model <- lm(streams ~ bpm, data = spotify_data)
# summary of regression model
summary(regression_model)
##
## Call:
## lm(formula = streams ~ bpm, data = spotify_data)
## Residuals:
## Min
                     1Q
                            Median
                                           30
## -513636452 -372808926 -223552907 159316140 3192142803
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 520171081 82374227 6.315 4.15e-10 ***
                            655200 -0.075
## bpm
                 -49233
                                              0.94
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 567200000 on 950 degrees of freedom
## Multiple R-squared: 5.943e-06, Adjusted R-squared: -0.001047
## F-statistic: 0.005646 on 1 and 950 DF, p-value: 0.9401
# plot the regression line
ggplot(spotify_data, aes(x = bpm, y = streams)) +
  geom_point() +
  geom_smooth(method = "lm", se = FALSE) +
 labs(title = "Linear Regression: Streams vs BPM",
      x = "BPM"
      y = "Streams") +
 theme_minimal()
```



The R session information (including the OS info, R version and all packages used):

```
sessionInfo()
## R version 4.3.2 (2023-10-31 ucrt)
## Platform: x86_64-w64-mingw32/x64 (64-bit)
## Running under: Windows 10 x64 (build 19045)
##
## Matrix products: default
##
##
## locale:
## [1] LC_COLLATE=English_United States.utf8 LC_CTYPE=English_United States.utf8
## [3] LC_MONETARY=English_United States.utf8 LC_NUMERIC=C
## [5] LC_TIME=English_United States.utf8
## time zone: America/New_York
## tzcode source: internal
##
## attached base packages:
## [1] stats
                graphics grDevices utils
                                            datasets methods
                                                                 base
##
## other attached packages:
## [1] MASS_7.3-60
                   dplyr_1.1.4
                                  ggplot2_3.4.4
##
## loaded via a namespace (and not attached):
## [1] Matrix_1.6-1.1 gtable_0.3.4 compiler_4.3.2
                                                        highr_0.10
                                                                          tidyselect_1.2.0
## [6] tinytex_0.49 splines_4.3.2 scales_1.3.0
                                                         yaml_2.3.7
                                                                          fastmap_1.1.1
```

```
## [11] lattice_0.21-9 R6_2.5.1 labeling_0.4.3 generics_0.1.3 knitr_1.45
## [16] tibble_3.2.1
                      munsell_0.5.0 pillar_1.9.0
                                                    rlang_1.1.2
                                                                    utf8_1.2.4
## [21] xfun_0.41
                      cli_3.6.1
                                      withr_2.5.2
                                                     magrittr_2.0.3 mgcv_1.9-0
                      grid_4.3.2
## [26] digest_0.6.33
                                      lifecycle_1.0.4 nlme_3.1-163
                                                                    vctrs_0.6.5
## [31] evaluate_0.23
                                      farver_2.1.1
                      glue_1.6.2
                                                     fansi_1.0.6
                                                                    colorspace_2.1-0
## [36] rmarkdown_2.25 tools_4.3.2
                                      pkgconfig_2.0.3 htmltools_0.5.7
Sys.time()
## [1] "2024-03-01 13:25:49 EST"
```