# Neural Network Theory and Applications

Homework Assignment 1

March 7, 2019

Due at March 27, 2019

#### 1. Problem 1

One variation of the perceptron rule is:

$$W^{new} = W^{old} + \alpha e p^{T}$$
$$b^{bew} = b^{old} + \alpha e$$

where  $\alpha$  is the learning rate. Prove convergence of this algorithm. Does the proof require a limit on the learning rate? Please explain.

#### 2. Problem 2 - 01

Suppose the output of each neuron in a multilayer perceptron network is

$$x_{kj} = f\left(\sum_{i=1}^{N_{k-1}} \left(u_{kji} x_{k-1,i}^2 + v_{kji} x_{k-1,i}\right) + b_{kj}\right)$$

for k = 2,3,..., M and  $j = 1,2,..., N_k$ 

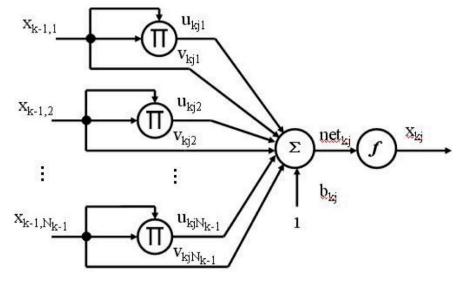
where both  $u_{kji}$  and  $v_{kji}$  are the weights connecting the *i*-th unit in the layer k-1 to the *j*-th unit in the layer k,  $b_{kj}$  is the bias of the j-th unit in the layer k,  $N_k$  is the number of units if the  $k(1 \le k \le M)$ , and  $f(\cdot)$  is the sigmoidal activation function.

### 3. Problem 2 - 02

The structure of the unit is shown as the following figure, and this network is called multi-layer quadratic perceptron (MLQP).

□ Please derive the back-propagation algorithms for MLQPs in both on-line learning and batch learning

ways.



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Figure 1: The structure of MLQP

#### 4. Problem 3 - 01

- In problem 3, you should program a deep neural network with TensorFlow or PyTorch to solve an emotion recognition task.
- Model Structure
  - The deep neural network for this task is a three layer network: an input layer, an hidden layer, and an output layer. The neurons in the input layer should be the same as input feature dimensions. The number of hidden neurons is a hyperparameter which is chosen by yourself. And there are 3 output units for 3 emotions.

#### 5. Problem 3 - 02

- Data Description
  - The provided data contains differential entropy (DE) features extracted from emotional EEG signals
  - Emotions: positive, neutral, negative
  - The data can be downloaded from this link:

http://gofile.me/4gVYW/24rIP0NRX

#### 6. Problem 3 -03

#### Questions

Run your code to classify three emotion states (positive, neutral, negative) and compare the training time and generalization performance of different hidden units and learning rates.

## 7. Report Format Requirement

- □ You must submit a complete report with solution details. And it it recommended to write your report with Latex.
- □ You must compress all your files into a ".zip" file or a ".rar" file, and the name of the compressed file is in the format "student id \_ your name \_ homework number" (1234567\_newton\_1.zip).
- Submitting your homework from this link:
   <a href="http://bcmicloud.quickconnect.to/sharing/MRSSpGF">http://bcmicloud.quickconnect.to/sharing/MRSSpGF</a>
   4S and filling your student number in the webpage to upload.

## 8. Grading policy

- □ The basic rule is, if any cheating activities are identified, both participants will be given ZERO scores for that homework.
- □ Grading
  - Submission with excellent codes and report, will be given
     A+.
  - Submission with both good codes and report, will be given A.
  - Submission with some deficiencies in codes or report,
     and basically no big problems, will be given A- or B+.
  - Thought submission is not good enough, it can be given at least B, if we can identify that you have tried your best with independent and hard work

### 8. Late submission

- Homework is scored with full credit on the due date.
- ☐ It is scored with one less grade for late submission, i.e., your late submission will degraded from A to B, or from B to C, if you miss the due date.