### Softwaretechnik

Lecture 21: Featherweight Java

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### Featherweight Java

The language shown in examples Formal Definition Operational Semantics Typing Rules

# Type Safety of Java

- ▶ 1995 public presentation of Java
- obtain importance very fast
- Questions
  - type safety?
  - What does Java mean?
- ▶ 1997/98 resolved
  - Drossopoulou/Eisenbach
  - ► Flatt/Krishnamurthi/Felleisen
  - ▶ Igarashi/Pierce/Wadler (Featherweight Java, FJ)

# Featherweight Java

- Construction of a formal model: consideration of completeness and compactness
- ► FJ: minimal model (compactness)
- complete definition: one page
- ambition:
  - the most important language features
  - short proof of type soundness
  - ightharpoonup FJ  $\subseteq$  Java

# The Language FJ

- class definition
- object creation new
- method call (dynamic dispatch), recursion with this
- ▶ field access
- type cast
- override of methods
- subtypes

### **Omitted**

- assignments
- interfaces
- overload
- **super**-calls
- null-references
- primitive types
- abstract methods
- inner classes
- shadowing of fields of super classes
- access control (private, public, protected)
- exceptions
- concurrency
- reflections

# **Example Programs**

```
class A extends Object { A() { super (); } }
class B extends Object { B() { super (); } }
class Pair extends Object {
  Object fst:
  Object snd;
  // Constructor
  Pair (Object fst, Object snd) {
    super(); this.fst = fst; this.snd = snd;
  // Method definition
  Pair setfst (Object newfst) {
    return new Pair (newfst, this.snd);
```

### **Explanation**

- class definition: always define super class
- constructors:
  - one per class, always defined
  - arguments correspond to fields
  - always the same form: super-call, then copy the arguments into the fields
- field accesses and method calls always with recipient object
- method body: always in the form return...

### method call

```
new Pair (new A(), new B()).setfst (new B())
// will be evaluated to
new Pair (new B(), new B())
```

### method call

```
new Pair (new A(), new B()).setfst (new B())
// will be evaluated to
new Pair (new B(), new B())
```

### type cast

```
((Pair) new Pair (new Pair (new A(), new B ()), new A()).fst).snd
```

- ▶ includes type cast (Pair)
- ▶ It's needed, because new Pair (...).fst has the type Object.

### field access

```
new Pair (new A (), new B ()).snd
// will be evaluated to
new B()
```

### field access

```
new Pair (new A (), new B ()).snd
// will be evaluated to
new B()
```

### method call

```
new Pair (new A(), new B()).setfst (new B())
```

yields a substitution

```
[\mathsf{new}\ \mathsf{B}()/\mathsf{newfst},\quad \mathsf{new}\ \mathsf{Pair}\ (\mathsf{new}\ \mathsf{A}(),\ \mathsf{new}\ \mathsf{B}())/\mathsf{this}]
```

We have to evaluate the method body **new** Pair (newfst, **this**.snd) under this this substitution. The substitution yields

```
new Pair (new B(), new Pair (new A(), new B()).snd)
```

### type cast

```
(Pair)new Pair (new A (), new B ())
// evaluates to
new Pair (new A (), new B ())
```

runtime check if Pair is a subtype of Pair.

### type cast

```
(Pair)new Pair (new A (), new B ())
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```

runtime check if Pair is a subtype of Pair.

### call-by-Value evaluation

```
((Pair) new Pair (new Pair (new A(), new B ()), new A()).fst).snd // \rightarrow ((Pair) new Pair (new A(), new B ())).snd // \rightarrow new Pair (new A(), new B ()).snd // \rightarrow new B()
```

### Runtime Error

### access to non existing field

new A().fst

no value, no evaluation rule matches

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new A().fst

no value, no evaluation rule matches

### call of non existing method

new A().setfst (new B())

no value, no evaluation rule matches

### failing type cast

(B)new A ()

- ► A is not subtype of B
- ⇒ no value, no evaluation rule matches



# Guarantees of Java's Type System

If a Java program is type correct, then

- all field accesses refer to existing fields
- all method calls refer to existing methods, but
- failing type casts are possible.

# Formal Definition

# Syntax

# Syntax—Conventions

- this
  - special variable, do not use it as field name or parameter
  - implicit bound in each method body
- sequences of field names, parameter names and method names include no repetition
- ▶ class C extends D { $C_1$   $f_1$ ; . . . K  $M_1$  . . . }
  - defines class C as subclass of D
  - fields  $f_1 \dots$  with types  $C_1 \dots$
  - constructor K
  - ightharpoonup methods  $M_1 \dots$
  - ▶ fields from *D* will be added to *C*, shadowing is not supported

# Syntax—Conventions

- ▶  $C(D_1 g_1, ..., C_1 f_1, ...)$  {super( $g_1, ...$ ); this. $f_1 = f_1; ...$ }
  - define the constructor of class C
  - fully specified by the fields of *C* and the fields of the super classes.
  - ▶ number of parameters is equal to number of fields in *C* and all its super classes.
  - **b** body start with  $\mathbf{super}(g_1, \dots)$ , where  $g_1, \dots$  corresponds to the fields of the super classes
- $D m(C_1 x_1, \dots) \{ return t; \}$ 
  - defines method m
  - ► result type *D*
  - ▶ parameter  $x_1$  ... with types  $C_1$  ...
  - body is a return statement

### Class Table

- ▶ The *class table CT* is a map from class names to class definitions
  - ⇒ each class has exactly one definition
  - the CT is global, it corresponds to the program
  - "arbitrary but fixed"
- Each class except Object has a superclass
  - Object is not part of CT
  - Object has no fields
  - ▶ Object has no methods (≠ Java)
- ▶ The class table defines a subtype relation *C* <: *D* over class names
  - ▶ the reflexive and transitive closure of subclass definitions.

# Subtype Relation

REFL 
$$\overline{C <: C}$$

TRANS  $\overline{C <: D \quad D <: E}$ 
 $C <: E$ 

EXT  $\overline{C <: C}$ 

# Consistency of CT

- 1. CT(C) =**class**  $C \dots$  for all  $C \in dom(CT)$
- 2. Object  $\notin dom(CT)$
- 3. For each class name C mentioned in CT:  $C \in dom(CT) \cup \{Object\}$
- 4. The relation <: is antisymmetric (no cycles)

# Example: Classes Do Refer to Each Other

```
class Author extends Object {
  String name; Book bk;
  Author (String name, Book bk) {
    super();
    this.name = name;
    this.bk = bk;
class Book extends Object {
  String title; Author ath;
  Book (String title, Author ath) {
    super();
    this.title = title:
    this.ath = ath;
```

collect Fields of classes

$$fields(Object) = ullet$$

$$CT(C) = \textbf{class } C \ \textbf{extends } D \ \{C_1 \ f_1; \dots \ K \ M_1 \dots\}$$

$$fields(D) = D_1 \ g_1, \dots$$

$$fields(C) = D_1 \ g_1, \dots, C_1 \ f_1, \dots$$

- ▶ — empty list
- fields(Author) = String name; Book bk;
- Usage: evaluation steps, typing rules



detect type of methods

$$CT(C) = \textbf{class } C \textbf{ extends } D \{C_1 \ f_1; \dots K \ M_1 \dots\}$$

$$M_j = E \ m(E_1 \ x_1, \dots) \{\textbf{return } t; \}$$

$$mtype(m, C) = (E_1, \dots) \rightarrow E$$

$$CT(C) = \textbf{class } C \textbf{ extends } D \{C_1 \ f_1; \dots K \ M_1 \dots\}$$

$$(\forall j) \ M_j \neq F \ m(F_1 \ x_1, \dots) \{\textbf{return } t; \}$$

$$mtype(m, D) = (E_1, \dots) \rightarrow E$$

$$mtype(m, C) = (E_1, \dots) \rightarrow E$$

► Usage: typing rules

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determine body of method

$$CT(C) = \mathbf{class} \ C \ \mathbf{extends} \ D \ \{C_1 \ f_1; \dots \ K \ M_1 \dots\}$$

$$M_j = E \ m(E_1 \ x_1, \dots) \ \{\mathbf{return} \ t; \}$$

$$mbody(m, C) = (x_1 \dots, t)$$

$$CT(C) = \mathbf{class} \ C \ \mathbf{extends} \ D \ \{C_1 \ f_1; \dots \ K \ M_1 \dots\}$$

$$(\forall j) \ M_j \neq F \ m(F_1 \ x_1, \dots) \ \{\mathbf{return} \ t; \}$$

$$mbody(m, D) = (y_1 \dots, u)$$

$$mbody(m, C) = (y_1 \dots, u)$$

Usage: evaluation steps



correct overriding of methods

$$override(m, Object, (E_1 ...) \rightarrow E)$$

$$CT(C) = \textbf{class } C \textbf{ extends } D \{C_1 \ f_1; ... \ K \ M_1 ...\}$$

$$M_j = E \ m(E_1 \ x_1, ...) \{\textbf{return } t; \}$$

$$override(m, C, (E_1 ...) \rightarrow E)$$

$$CT(C) = \textbf{class } C \textbf{ extends } D \{C_1 \ f_1; ... \ K \ M_1 ...\}$$

$$(\forall j) \ M_j \neq F \ m(F_1 \ x_1, ...) \{\textbf{return } t; \}$$

$$override(m, D, (E_1, ...) \rightarrow E)$$

$$override(m, C, (E_1, ...) \rightarrow E)$$

Usage: typing rules

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# Example

```
class Recording extends Object {
    int high; int today; int low;
    Recording (int high, int today, int low) { ... }
    int dHigh() { return this.high; }
    int dLow() { return this.low }
    String unit() { return "not set"; }
    String asString() {
        return String.valueOf(high)
             .concat("-")
             .concat (String.valueOf(low))
             .concat (unit());
class Temperature extends ARecording {
  Temperature (int high, int today, int low) { super(high, today, low); }
  String unit() { return "°C"; }
```

- ▶ fields(Object) = •
- fields(Temperature) = fields(Recording) = int high; int today; int low;
- ▶  $mtype(unit, Recording) = () \rightarrow String$
- ▶  $mtype(unit, Temperature) = () \rightarrow String$
- mtype(dHigh, Recording) = () → int
- ▶  $mtype(dHigh, Temperature) = () \rightarrow int$
- verride(dHigh, Object, () → int)
- verride(dHigh, Recording, () → int)
- ightharpoonup override(dHigh, Temperature, ()  $\rightarrow$  int)
- ▶  $mbody(unit, Recording) = (\varepsilon, "not set")$
- ▶  $mtype(unit, Temperature) = (\varepsilon, "\circ C")$

# Operational Semantics (definition of the evaluation steps)

# Direct Evaluation Steps

ightharpoonup evaluation: relation  $t\longrightarrow t'$  for one evaluation step

E-ProjNew 
$$\frac{\text{fields}(C) = C_1 \ f_1, \dots}{(\text{new } C(v_1, \dots)).f_i \longrightarrow v_i}$$

$$\text{E-InvkNew} \ \frac{\textit{mbody}(\textit{m}, \textit{C}) = (\textit{x}_1 \ldots, \textit{t})}{(\textit{new} \ \textit{C}(\textit{v}_1, \ldots)).\textit{m}(\textit{u}_1, \ldots)} \\ \longrightarrow \textit{t}[\textit{new} \ \textit{C}(\textit{v}_1, \ldots)/\textit{this}, \textit{u}_1, \ldots /\textit{x}_1, \ldots]$$

E-CASTNEW 
$$\frac{C <: D}{(D)(\text{new } C(v_1, \dots)) \longrightarrow \text{new } C(v_1, \dots)}$$

# Evaluation Steps in Context

$$\begin{array}{c} \text{E-Field} \ \frac{t \longrightarrow t'}{t.f \longrightarrow t'.f} \\ \\ \text{E-Invk-Recv} \ \frac{t \longrightarrow t'}{t.m(t_1,\ldots) \longrightarrow t'.m(t_1,\ldots)} \\ \\ \text{E-Invk-Arg} \ \frac{t_i \longrightarrow t'_i}{v.m(v_1,\ldots,t_i,\ldots) \longrightarrow v.m(v_1,\ldots,t'_i,\ldots)} \\ \\ \text{E-New-Arg} \ \frac{t_i \longrightarrow t'_i}{\mathsf{new} \ C(v_1,\ldots,t_i,\ldots) \longrightarrow \mathsf{new} \ C(v_1,\ldots,t'_i,\ldots)} \\ \\ \text{E-Cast} \ \frac{t \longrightarrow t'}{(C)t \longrightarrow (C)t'} \end{array}$$

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# Example: Evaluation Steps

```
((Pair) (new Pair (new Pair (new A(), new B()).setfst (new B()), new B()).fst)).fst
// \rightarrow [E-Field], [E-Cast], [E-New-Arg], [E-InvkNew]
((Pair) (new Pair (new Pair (new B(), new B()), new B()).fst)).fst
// \rightarrow [E-Field], [E-Cast], [E-ProjNew]
((Pair) (new Pair (new B(), new B()))).fst
// \rightarrow [E-Field], [E-CastNew]
(new Pair (new B(), new B())).fst
// \rightarrow [E-ProjNew]
new B()
```

# Typing Rules

# Typing Rules

### involved type judgments

- C <: D</p>
  C is subtype of D
- A ⊢ t : C
  Under type assumption A, the expression t has type C.
- F m(C₁ x₁,...) {return t; } OK in C Method declaration is accepted in class C.
- ► class C extends D {C<sub>1</sub> f<sub>1</sub>; ... K M<sub>1</sub>...} OK Class declaration is accepted
- Type assumptions defined by

$$A ::= \emptyset \mid A, x : C$$



# Accepted Class Declaration

$$K = C(D_1 \ g_1, \ldots, C_1 \ f_1, \ldots) \ \{ \mathbf{super}(g_1, \ldots); \mathbf{this}. f_1 = f_1; \ldots \}$$

$$fields(D) = D_1 \ g_1 \ldots$$

$$(\forall j) \ M_j \ \mathsf{OK} \ \mathsf{in} \ C$$

$$\mathbf{class} \ C \ \mathbf{extends} \ D \ \{ C_1 \ f_1; \ldots \ K \ M_1 \ldots \}$$

# Accepted Method Declaration

$$x_1: C_1, \ldots, \text{this}: C \vdash t: E$$
 $E \lt: F$ 
 $CT(C) = \text{class } C \text{ extends } D \ldots$ 
 $override(m, D, (C_1, \ldots) \rightarrow F)$ 
 $F m(C_1 x_1, \ldots) \text{ {return } t; } OK \text{ in } C$ 

T-VAR 
$$\frac{x: C \in A}{A \vdash x: C}$$

T-FIELD 
$$\frac{A \vdash t : C \quad fields(C) = C_1 \ f_1, \dots}{A \vdash t.f_i : C_i}$$

F-Invk 
$$\frac{A \vdash t : C \quad (\forall i) \ A \vdash t_i : C_i \quad (\forall i) \ C_i <: D_i}{mtype(m, C) = (D_1, \dots) \to D}$$
$$A \vdash t.m(t_1, \dots) : D$$

F-New 
$$\frac{(\forall i) \ A \vdash t_i : C_i \quad (\forall i) \ C_i <: D_i}{fields(C) = D_1 \ f_1, \dots}$$
$$A \vdash \mathbf{new} \ C(t_1, \dots) : C$$

# Type Rules for Type Casts

T-UCAST 
$$A \vdash t : D \qquad D <: C$$
 $A \vdash (C)t : C$ 

T-DCAST 
$$\frac{A \vdash t : D \quad C \leq D \quad C \neq D}{A \vdash (C)t : C}$$

# Type Safety for Featherweight Java

- "Preservation" and "Progress" yields type safety
- "Preservation":

If 
$$A \vdash t : C$$
 and  $t \longrightarrow t'$ , then  $A \vdash t' : C'$  with  $C' \lt : C$ .

"Progress": (short version) If  $A \vdash t : C$ , then  $t \equiv v$  is a value or t contains a subexpression e'

$$e' \equiv (C)(\mathbf{new}\ D(v_1,\dots))$$

with  $D \not<: C$ .



- All method calls and field accesses evaluate without errors.
- Type casts can fail.



### Problems in the Preservation Proof

#### Type casts destroy preservation

- ► Consider the expression (A) ((Object)new B())
- ▶ It holds  $\emptyset \vdash (A) ((Object)new B()): A$
- ▶ It holds (A)  $((Object)new B()) \longrightarrow (A) (new B())$
- ▶ But (A) (new B()) has no type!

### Problems in the Preservation Proof

### Type casts destroy preservation

- Consider the expression (A) ((Object)new B())
- ▶ It holds  $\emptyset \vdash (A)$  ((Object)new B()): A
- ▶ It holds (A) ((Object)new B())  $\longrightarrow$  (A) (new B())
- But (A) (new B()) has no type!
- workaround: add additional rule for this case (stupid cast) —next evaluation step fail

T-SCAST 
$$A \vdash t : D$$
  $C \nleq D$   $D \nleq C$ 

▶ We can prove preservation with this rule.



# Statement of Type Safety

If  $A \vdash t : C$ , then one of the following cases applies:

1. t does not terminate i.e., there exists an infinite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow t_2 \longrightarrow \dots$$

2. t evaluates to a value v after a finite number of evaluation steps i.e., there exists a finite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow \ldots \longrightarrow t_n = v$$

3. t gets stuck at a failing cast i.e., there exists a finite sequence of evaluation steps

$$t = t_0 \longrightarrow t_1 \longrightarrow \ldots \longrightarrow t_n$$

where  $t_n$  contains a subterm (C) (**new**  $D(v_1, ...)$ ) such that  $D \nleq C$ .