

# Practical Computing for Scientists

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# Python First-Class Functions

by Greg Wilson

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...that variables can refer to



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A string is a sequence of bytes representing characters...



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...and yes, variables can refer to them to



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A string is a sequence of bytes representing characters...

...that variables can refer to

A function is a sequence of bytes representing instructions...

...and yes, variables can refer to them to

This turns out to be very useful, and very powerful

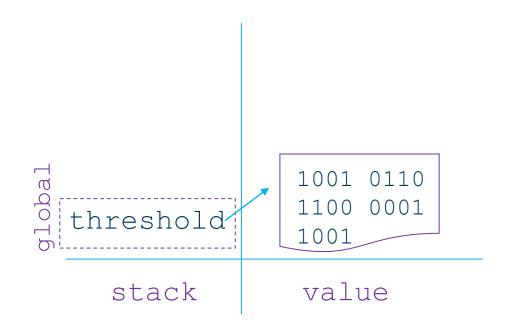




```
def threshold(signal):
    return 1.0 / sum(signal)
```



```
def threshold(signal):
    return 1.0 / sum(signal)
```

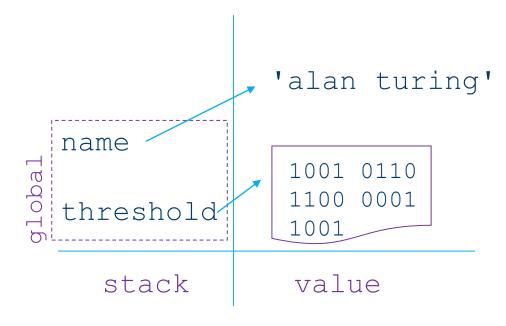




```
def threshold(signal):
    return 1.0 / sum(signal)
```

Not really very different from:

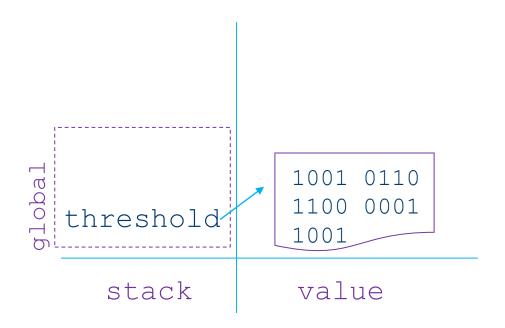
```
name = 'Alan Turing'
```







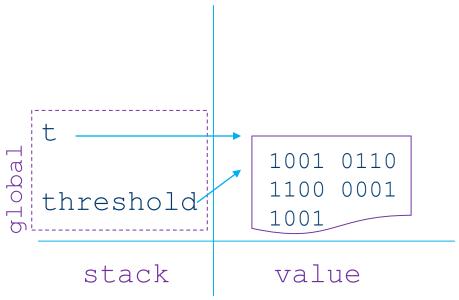
```
def threshold(signal):
    return 1.0 / sum(signal)
```





```
def threshold(signal):
    return 1.0 / sum(signal)

t = threshold
```





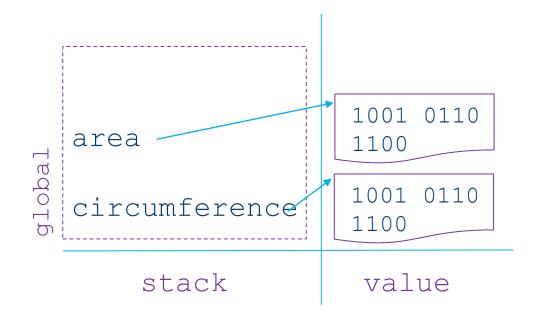
```
def threshold(signal):
  return 1.0 / sum(signal)
t = threshold
print(t([0.1, 0.4, 0.2]))
1.42857
                                         1001 0110
                                         1100 0001
                          threshold
                                         1001
                             stack
                                         value
```





```
def area(r):
    return PI * r * r

def circumference(r):
    return 2 * PI * r
```





```
def area(r):
  return PI * r * r
def circumference(r):
  return 2 * PI * r
funcs = [area, circumference]
                         funcs
                         area
```

1001 0110

1001 0110

value

1100

1100

circumference

stack



```
def area(r):
  return PI * r * r
def circumference(r):
  return 2 * PI * r
funcs = [area, circumference]
for f in funcs:
                          funcs
  print(f(1.0))
                                            1001 0110
                          area
                                            1100
                                            1001 0110
                          circumference
                                            1100
                              stack
                                            value
```

```
def area(r):
  return PI * r * r
def circumference(r):
  return 2 * PI * r
funcs = [area, circumference]
for f in funcs:
                          funcs
  print(f(1.0))
                                            1001 0110
3.14159
                          area
                                            1100
6.28318
                                            1001 0110
                          circumference
                                            1100
                              stack
                                            value
```





```
def call_it(func, value):
    return func(value)
```



```
def call_it(func, value):
    return func(value)

print(call_it(area, 1.0))
3.14159
```



```
def call_it(func, value):
    return func(value)

print(call_it(area, 1.0))
3.14159

print(call_it(circumference, 1.0))
6.28318
```





```
def do_all(func, values):
    result = []
    for v in values:
        temp = func(v)
        result.append(temp)
    return result
```







```
def do all(func, values):
  result = []
  for v in values:
    temp = func(v)
    result.append(temp)
  return result
               print(do all(area, [1.0, 2.0, 3.0]))
               [3.14159, 12.56636, 28.27431]
               def slim(text):
                 return text[1:-1]
```



```
def do all(func, values):
  result = []
  for v in values:
    temp = func(v)
    result.append(temp)
  return result
               print(do all(area, [1.0, 2.0, 3.0]))
               [3.14159, 12.56636, 28.27431]
               def slim(text):
                 return text[1:-1]
               print(do all(slim, ['abc', 'defgh']))
               b efq
```





```
def combine_values(func, values):
    current = values[0]
    for v in range(1, len(values)):
        current = func(current, v)
    return current
```



```
def combine_values(func, values):
    current = values[0]
    for v in range(1, len(values)):
        current = func(current, v)
    return current

def add(x, y): return x + y
    def mul(x, y): return x * y
```



```
def combine values (func, values):
  current = values[0]
  for v in range(1, len(values)):
    current = func(current, v)
  return current
def add(x, y): return x + y
def mul(x, y): return x * y
print(combine values(add, [1, 3, 5]))
9
```



#### Higher-order functions allow re-use of control flow

```
def combine values (func, values):
  current = values[0]
  for v in range(1, len(values)):
    current = func(current, v)
  return current
def add(x, y): return x + y
def mul(x, y): return x * y
print(combine values(add, [1, 3, 5]))
9
print(combine values(mul, [1, 3, 5]))
15
```





	op_1	op_2	op_3
data_structure_A	do_1A	do_2A	do_3A
data_structure_B	do_1B	do_2B	do_3B
data_structure_C	do_1C	do_2C	do_3C



	op_1	op_2	op_3
data_structure_A	do_1A	do_2A	do_3A
data_structure_B	do_1B	do_2B	do_3B
data_structure_C	do_1C	do_2C	do_3C

total: 9



	op_1	op_2	op_3
data_structure_A	do_1A	do_2A	do_3A
data_structure_B	do_1B	do_2B	do_3B
data_structure_C	do_1C	do_2C	do_3C

total: 9

## With higher order functions

	op_1	op_2	op_3
operate_on_A			
operate_on_B			
operate_on_C			



	op_1	op_2	op_3
data_structure_A	do_1A	do_2A	do_3A
data_structure_B	do_1B	do_2B	do_3B
data_structure_C	do_1C	do_2C	do_3C

total: 9

## With higher order functions

	op_1	op_2	op_3
operate_on_A			
operate_on_B			
operate_on_C			

total: 6



Must need to know *something* about the function in order to call it



Must need to know *something* about the function in order to call it

Like number of arguments



Must need to know *something* about the function in order to call it

Like number of arguments



```
Must need to know something about the function in order to call it

Like number of arguments
```

```
def add_all(*args):
   total = 0
   for a in args:
     total += a
   return total
```



Must need to know *something* about the function in order to call it

Like number of arguments

```
def add_all (*args):
   total = 0
   for a in args:
     total += a
   return total
```



```
Must need to know something about the function
  in order to call it
  Like number of arguments
def add all(*args):
  total = 0
  for a in args:
    total += a
  return total
print(add all())
```



```
Must need to know something about the function
  in order to call it
  Like number of arguments
def add all(*args):
  total = 0
  for a in args:
    total += a
  return total
print(add all())
print(add all(1, 2, 3))
```



```
def combine_values(func, *values):
    current = values[0]
    for i in range(1, len(values)):
        current = func(current, v)
    return current
```



```
def combine_values(func, *values):
    current = values[0]
    for i in range(1, len(values)):
        current = func(current, v)
    return current
```



```
def combine_values(func, *values):
    current = values[0]
    for i in range(1, len(values)):
        current = func(current, v)
    return current

print(combine_values(add, 1, 3, 5))
```



```
def combine_values(func, *values):
    current = values[0]
    for i in range(1, len(values)):
        current = func(current, v)
    return current

print(combine_values(add, 1, 3, 5))
```

What does combine\_values (add) do?



```
def combine_values(func, *values):
    current = values[0]
    for i in range(1, len(values)):
        current = func(current, v)
    return current

print(combine_values(add, 1, 3, 5))
```

What does combine values (add) do?

What should it do?



filter(F, S) select elements of S for which F is True



filter(F, S)	select elements of S for which F is True
map(F, S)	apply F to each element of S



filter(F, S)	select elements of S for which F is True
map(F, S)	apply F to each element of S
reduce(F, S)	use F to combine all elements of S



filter(F, S)	select elements of S for which F is True
map(F, S)	apply F to each element of S
reduce(F, S)	use F to combine all elements of S

```
def positive(x): return x >= 0
print(filter(positive, [-3, -2, 0, 1, 2]))
[0, 1, 2]
```



	filter(F, S)	select elements of S for which F is True
	map(F, S)	apply F to each element of S
	reduce(F, S)	use F to combine all elements of S
<pre>def positive(x): return x &gt;= 0 print(filter(positive, [-3, -2, 0, 1, 2])) <math>[0, 1, 2]</math></pre>		
<pre>def negate(x): return -x print(map(negate, [-3, -2, 0, 1, 2])) [3, 2, 0, -1, -2]</pre>		



```
select elements of S for which F is True
  filter(F, S)
                    apply F to each element of S
  map(F, S)
                   use F to combine all elements of S
  reduce (F, S)
def positive(x): return x >= 0
print(filter(positive, [-3, -2, 0, 1, 2]))
[0, 1, 2]
def negate(x): return -x
print (map (negate, [-3, -2, 0, 1, 2]))
[3, 2, 0, -1, -2]
def add(x, y): return x+y
print reduce (add, [-3, -2, 0, 1, 2])
```



Novice: writing instructions for the computer



Novice: writing instructions for the computer

Expert: creating and combining abstractions



Novice: writing instructions for the computer

Expert: creating and combining abstractions

figure out what the pattern is



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Expert: creating and combining abstractions

figure out what the pattern is

write it down as clearly as possible



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figure out what the pattern is

write it down as clearly as possible

build more patterns on top of it



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But limits on short-term memory still apply



Novice: writing instructions for the computer

Expert: creating and combining abstractions

figure out what the pattern is

write it down as clearly as possible

build more patterns on top of it

But limits on short-term memory still apply

Hard to understand what meta-meta-functions

actually do





# Python Libraries

by Greg Wilson

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A function is a way to turn a bunch of related statements into a single "chunk"



A function is a way to turn a bunch of related statements into a single "chunk"

Avoid duplication



- Avoid duplication
- Make code easier to read



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A *library* does the same thing for related functions



- Avoid duplication
- Make code easier to read

A *library* does the same thing for related functions

Hierarchical organization



Avoid duplication

Make code easier to read

A *library* does the same thing for related functions Hierarchical organization

family

library

genus

function



species

statement

## Every Python file can be used as a library





```
# halman.py
def threshold(signal):
  return 1.0 / sum(signal)
```



```
# halman.py
def threshold(signal):
  return 1.0 / sum(signal)
```

```
# program.py
import halman
readings = [0.1, 0.4, 0.2]
print('signal threshold is', halman.threshold(readings))
```



```
# halman.py
def threshold(signal):
  return 1.0 / sum(signal)
```

```
# program.py
import halman
readings = [0.1, 0.4, 0.2]
print('signal threshold is', halman.threshold(readings))
```

\$ python program.py
signal threshold is 1.42857





1. Executes the statements it contains



- 1. Executes the statements it contains
- 2. Creates an object that stores references to the top-level items in that module



- 1. Executes the statements it contains
- 2. Creates an object that stores references to the top-level items in that module

```
# noisy.py
print('is this module being loaded?')
NOISE_LEVEL = 1/3
```



- 1. Executes the statements it contains
- 2. Creates an object that stores references to the top-level items in that module

```
# noisy.py
print('is this module being loaded?')
NOISE_LEVEL = 1/3
```

```
>>> import noisy is this module being loaded?
```



- 1. Executes the statements it contains
- 2. Creates an object that stores references to the top-level items in that module

```
# noisy.py
print('is this module being loaded?')
NOISE_LEVEL = 1/3
```

```
>>> import noisy
is this module being loaded?
>>> print(noisy.NOISE_LEVEL)
0.333333333
```





function



module function



global module function



```
global module function
```

```
# module.py
NAME = 'Transylvania'

def func(arg):
   return NAME + ' ' + arg
```



```
global module function
```

```
# module.py
NAME = 'Transylvania'

def func(arg):
   return NAME + ' ' + arg
```



```
global module function
```

```
# module.py
NAME = 'Transylvania'

def func(arg):
   return NAME + ' ' + arg
>>> NAME = 'Hamunaptra'
>>> import module
```



```
global module function
```

```
# module.py
NAME = 'Transylvania'

def func(arg):
   return NAME + ' ' + arg
```

```
>>> NAME = 'Hamunaptra'
>>> import module
>>> print(module.func('!!!'))
Transylvania !!!
```





>>> import math



```
>>> import math
>>> print(math.sqrt(2))
1.4142135623730951
```



```
>>> import math

>>> print(math.sqrt(2))

1.4142135623730951

>>> print(math.hypot(2, 3)) # sqrt(x**2 + y**2)

3.6055512754639891
```



```
>>> import math

>>> print(math.sqrt(2))

1.4142135623730951

>>> print(math.hypot(2, 3)) # sqrt(x**2 + y**2)

3.6055512754639891

>>> print(math.e, math.pi) # as accurate as possible

2.7182818284590451 3.1415926535897931
```



# Python also provides a help function



### Python also provides a help function

```
>>> import math
>>> help(math)
Help on module math:
NAME
    math
FTT_{i}F_{i}
    /usr/lib/python2.5/lib-dynload/math.so
MODULE DOCS
    http://www.python.org/doc/current/lib/module-math.html
DESCRIPTION
    This module is always available. It provides access to
    the mathematical functions defined by the C standard.
FUNCTIONS
    acos (...)
        acos(x)
        Return the arc cosine (measured in radians) of x.
```



>>> from math import sqrt >>> sqrt(3) 1.7320508075688772



```
>>> from math import sqrt
>>> sqrt(3)
1.7320508075688772
>>> from math import hypot as euclid
>>> euclid(3, 4)
5.0
```



```
>>> from math import sqrt
>>> sqrt(3)
1.7320508075688772
>>> from math import hypot as euclid
>>> euclid(3, 4)
5.0
>>> from math import *
>>> sin(pi)
1.2246063538223773e-16
>>>
```



```
>>> from math import sqrt
>>> sqrt(3)
1.7320508075688772
>>> from math import hypot as euclid
>>> euclid(3, 4)
5.0
>>> from math import * Generally a bad idea
>>> sin(pi)
1.2246063538223773e-16
>>>
```



```
>>> from math import sqrt
>>> sqrt(3)
1.7320508075688772
>>> from math import hypot as euclid
>>> euclid(3, 4)
5.0
                               Generally a bad idea
>>> from math import * -
>>> sin (pi)
                               Someone could add to
1.2246063538223773e-16
>>>
                               the library after you
                               start using it
```





>>> import sys



```
>>> import sys
>>> print(sys.version)
3.4.3 | Anaconda 2.3.0 (64-bit) | (default, Jun 4 2015, 15:29:08)
[GCC 4.4.7 20120313 (Red Hat 4.4.7-1)]
```



```
>>> import sys
>>> print(sys.version)
3.4.3 |Anaconda 2.3.0 (64-bit)| (default, Jun 4 2015, 15:29:08)
[GCC 4.4.7 20120313 (Red Hat 4.4.7-1)]
>>> print(sys.platform)
linux
```



```
>>> import sys
>>> print(sys.version)
3.4.3 |Anaconda 2.3.0 (64-bit)| (default, Jun 4 2015, 15:29:08)
[GCC 4.4.7 20120313 (Red Hat 4.4.7-1)]
>>> print(sys.platform)
linux
>>> print(sys.maxsize)
9223372036854775807
```



```
>>> import sys
>>> print(sys.version)
3.4.3 | Anaconda 2.3.0 (64-bit) | (default, Jun 4 2015, 15:29:08)
[GCC 4.4.7 20120313 (Red Hat 4.4.7-1)]
>>> print(sys.platform)
linux
>>> print(sys.maxsize)
9223372036854775807
>>> print(sys.path)
['', '/home/asobhani/anaconda3/lib/python34.zip', '/home
/asobhani/anaconda3/lib/python3.4', '/home/asobhani/anaconda3
/lib/python3.4/plat-linux', '/home/asobhani/anaconda3/lib
/python3.4/lib-dynload', '/home/asobhani/anaconda3/lib
/python3.4/site-packages', '/home/asobhani/anaconda3/lib
/python3.4/site-packages/Sphinx-1.3.1-py3.4.egg']
```



## sys.argv holds command-line arguments





```
# echo.py
import sys
for i in range(len(sys.argv)):
  print(i, '"' + sys.argv[i] + '"')
```



```
# echo.py
import sys
for i in range(len(sys.argv)):
   print(i, '"' + sys.argv[i] + '"')

$ python echo.py
0 "echo.py"
$
```



```
# echo.py
import sys
for i in range(len(sys.argv)):
  print(i, '"' + sys.argv[i] + '"')
$ python echo.py
0 "echo.py"
$ python echo.py first second
0 "echo.py"
1 "first"
2 "second"
```

sys.stdin is standard input (e.g., the keyboard)



sys.stdin is *standard input* (e.g., the keyboard) sys.stdout is *standard output* (e.g., the screen)



sys.stdin is *standard input* (e.g., the keyboard)
sys.stdout is *standard output* (e.g., the screen)
sys.stderr is *standard error* (usually also the screen)



```
# count.py
import sys
def count lines(reader):
  return len(reader.readlines())
if len(sys.argv) == 1:
  print(count lines(sys.stdin))
else:
  rd = open(sys.argv[1], 'r')
  print(count lines(rd))
  rd.close()
```



```
count.py
import sys
def count lines (reader):
  return len(reader.readlines())
if len(sys.argv) == 1:
  print(count lines(sys.stdin))
else:
  rd = open(sys.argv[1], 'r')
  print(count lines(rd))
  rd.close()
```



```
count.py
import sys
def count lines (reader):
  return len(reader.readlines())
if len(sys.argv) == 1:
  print(count lines(sys.stdin))
else:
  rd = open(sys.argv[1], 'r')
  print(count lines(rd))
  rd.close()
```



```
# count.py
import sys
def count lines (reader):
  return len(reader.readlines())
if len(sys.argv) == 1:
  print(count lines(sys.stdin))
else:
  rd = open(sys.argv[1], 'r')
  print(count lines(rd))
  rd.close()
$ python count.py < a.txt</pre>
48
$
```



```
# count.py
import sys
def count lines (reader):
  return len(reader.readlines())
if len(sys.argv) == 1:
  print(count lines(sys.stdin))
else:
  rd = open(sys.argv[1], 'r')
  print(count lines(rd))
  rd.close()
$ python count.py < a.txt</pre>
48
$ python count.py b.txt
```

```
The more polite way
'''Count lines in files. If no filename
arguments given, read from standard input. '''
import sys
def count lines (reader):
  '''Return number of lines in text read from reader.'''
  return len (reader.readlines())
if __name__ == '__main__':
```



...as before...

#### The more polite way

```
'''Count lines in files. If no filename
arguments given, read from standard input. '''
import sys
def count lines (reader):
  '''Return number of lines in text read from reader.'''
  return len (reader.readlines())
if __name__ == '__main__':
  ...as before...
```



```
The more polite way
'''Count lines in files. If no filename
arguments given, read from standard input. '''
import sys
def count lines (reader):
  '''Return number of lines in text read from reader.'''
  return len (reader.readlines())
if __name__ == '__main__':
  ...as before...
```



If the first statement in a module or function is a string, it is saved as a *docstring* 





```
# adder.py
'''Addition utilities.'''
def add(a, b):
    '''Add arguments.'''
    return a+b
```



```
# adder.py
'''Addition utilities.'''

def add(a, b):
   '''Add arguments.'''
   return a+b
```

```
>>> import adder
>>> help(adder)

NAME

   adder - Addition utilities.
FUNCTIONS
   add(a, b)
      Add arguments.
>>>
```



```
# adder.py
'''Addition utilities.'''

def add(a, b):
   '''Add arguments.'''
   return a+b
```

```
>>> import adder
>>> help(adder)

NAME

   adder - Addition utilities.
FUNCTIONS
   add(a, b)
       Add arguments.
>>> help(adder.add)
add(a, b)
       Add arguments.
>>> Add arguments.
```





main program
'\_\_main\_\_'



main program	loaded as library
'main'	module name



```
main program loaded as library

'_main__' module name
```

```
...module definitions...
if __name__ == '__main__':
...run as main program...
```



main program	loaded as library
'main'	module name

```
...module definitions...

if __name__ == '__main__':
    ...run as main program...
```

Always executed



main program	loaded as library
'main'	module name

```
...module definitions...
```

if \_\_name\_\_ == '\_\_main\_\_':
 ...run as main program...

Always executed

Only executed when file run directly



```
# stats.py
'''Useful statistical tools.'''
def average (values):
  '''Return average of values or None if no data.'''
  if values:
    return sum(values) / len(values)
  else:
    return None
if name == ' main ':
  print('test 1 should be None:', average([]))
 print('test 2 should be 1:', average([1]))
 print('test 3 should be 2:', average([1, 2, 3]))
```



```
# test-stats.py
from stats import average
print('test 4 should be None:', average(set()))
print('test 5 should be -1:', average({0, -1, -2}))
```



```
# test-stats.py
from stats import average
print('test 4 should be None:', average(set()))
print('test 5 should be -1:', average({0, -1, -2}))
```

```
$ python stats.py
test 1 should be None: None
test 2 should be 1: 1
test 3 should be 2: 2
$
```



```
# test-stats.py
from stats import average
print('test 4 should be None:', average(set()))
print('test 5 should be -1:', average({0, -1, -2}))
```

```
$ python stats.py
test 1 should be None: None
test 2 should be 1: 1
test 3 should be 2: 2
$ python test-stats.py
test 4 should be None: None
test 5 should be -1: -1
$
```





# Python Slicing

by Greg Wilson

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Lists, strings, and tuples are all *sequences*Can be indexed by integers in the range 0...len(X)-1



Lists, strings, and tuples are all *sequences*Can be indexed by integers in the range 0...len(X)-1

Can also be sliced using a range of indices



Lists, strings, and tuples are all *sequences*Can be indexed by integers in the range 0...len(X)-1

Can also be sliced using a range of indices

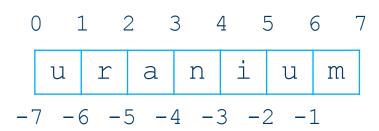
```
>>> element = 'uranium'
```



Can be indexed by integers in the range 0...len(X)-1

Can also be sliced using a range of indices

```
>>> element = 'uranium'
>>> print(element[1:4])
ran
>>>
```





Can be indexed by integers in the range 0...len(X)-1

Can also be sliced using a range of indices

```
>>> element = 'uranium'
>>> print(element[1:4])

ran
>>> print(element[:4])

uran

uran

-7 -6 -5 -4 -3 -2 -1
```



Can be indexed by integers in the range 0...len(X)-1

Can also be sliced using a range of indices

```
>>> element = 'uranium'
>>> print(element[1:4])

ran
>>> print(element[:4])

uran

>>> print(element[4:])

-7 -6 -5 -4 -3 -2 -1

ium
>>>
```



Can be indexed by integers in the range 0...len(X)-1

Can also be sliced using a range of indices

```
>>> element = 'uranium'
>>> print(element[1:4])
ran
                              1 2 3 4 5 6 7
>>> print(element[:4])
                             u
                                           u
uran
>>> print(element[4:])
                          -7 -6 -5 -4 -3 -2 -1
ium
>>> print(element[-4:])
nium
>>>
```

m



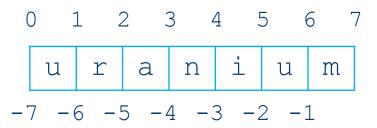


Python checks bounds when indexing But truncates when slicing



But truncates when slicing

```
>>> element = 'uranium'
>>>
```

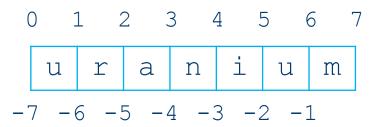




But truncates when slicing

```
>>> element = 'uranium'
```

>>> print(element[400])





But truncates when slicing

```
>>> element = 'uranium'
>>> print(element[400])
IndexError: string index out of range
>>>

0 1 2 3 4 5 6 7

u r a n i u m

-7 -6 -5 -4 -3 -2 -1
```



But truncates when slicing



But truncates when slicing

"A foolish consistency is the hobgoblin of little minds."

— Ralph Waldo Emerson
UNIVERSITY
OF ONTARIO

But truncates when slicing

"A foolish consistency is the hobgoblin of little minds."

— Ralph Waldo Emerson

"Aw, you're kidding me!"

— programmers

So text[1:3] is 0, 1, or 2 characters long



# So text[1:3] is 0, 1, or 2 characters long

1.1

'a'

'ab' 'b'

'abc' 'bc'

'abcdef' 'bc'





From index 1 up to (but not including) index 1



From index 1 up to (but not including) index 1

And text[3:1] is always the empty string



- From index 1 up to (but not including) index 1And text[3:1] is always the empty string
- Not the reverse of text[1:3]



- From index 1 up to (but not including) index 1
   And text[3:1] is always the empty string
- Not the reverse of text[1:3]

But text[1:-1] is everything except the first and last characters





Slicing always creates a new collection Beware of aliasing



```
>>> points = [[10, 10], [20, 20], [30, 30], [40, 40]] >>>
```



```
>>> points = [[10, 10], [20, 20], [30, 30], [40, 40]]
>>> middle = points[1:-1]
>>>
```



```
>>> points = [[10, 10], [20, 20], [30, 30], [40, 40]]
>>> middle = points[1:-1]
>>> middle[0][0] = 'whoops'
>>>
```



```
>>> points = [[10, 10], [20, 20], [30, 30], [40, 40]]
>>> middle = points[1:-1]
>>> middle[0][0] = 'whoops'
>>> middle[1][0] = 'aliasing'
>>>
```



```
>>> points = [[10, 10], [20, 20], [30, 30], [40, 40]]
>>> middle = points[1:-1]
>>> middle[0][0] = 'whoops'
>>> middle[1][0] = 'aliasing'
>>> print(middle)
>>> [['whoops', 20], ['aliasing', 30]]
>>>
```



```
>>> points = [[10, 10], [20, 20], [30, 30], [40, 40]]
>>> middle = points[1:-1]
>>> middle[0][0] = 'whoops'
>>> middle[1][0] = 'aliasing'
>>> print(middle)
>>> [['whoops', 20], ['aliasing', 30]]
>>> print(points)
[[10, 10], ['whoops', 20], ['aliasing', 30], [40, 40]]
>>>
```



