Assignment Week 5

1. Regression Evaluation Metrics

Mean Absolute Error (MAE)

• **Definition**: Measures the average magnitude of errors in predictions, ignoring their direction.

• When to Use:

- o Financial forecasting where errors are interpreted in monetary units
- o Transportation arrival time predictions where early or late predictions are equally problematic
- o Customer wait time prediction for service expectation management

Mean Squared Error (MSE)

• **Definition**: Measures the average of squared differences between actual and predicted values, penalizing larger errors more heavily.

• When to Use:

- o Scientific experiments requiring high precision
- Energy consumption prediction where underestimations could lead to power shortages
- Renewable energy output forecasting where larger errors have exponentially worse effects on grid stability

Root Mean Squared Error (RMSE)

• **Definition**: The square root of MSE, providing an error metric in the same unit as the target variable.

• When to Use:

- o Weather forecasting where understanding impact in real-world terms is critical
- o Air pollution forecasting by government agencies predicting AQI
- O University cafeteria wait time predictions where stakeholders need interpretable units (minutes)

Mean Absolute Percentage Error (MAPE)

- **Definition**: Measures errors as a percentage of actual values.
- When to Use:

- Business performance metrics where percentage-based evaluation is more interpretable
- o Retail demand forecasting for products with varying price points
- Small business sales forecasting where a \$2 error on a \$5 item is more significant than on a \$200 item

R-Squared (R2)

• **Definition**: Represents the proportion of variance in the target variable explained by the model.

• When to Use:

- o Evaluating model fit for explanatory analysis
- Music streaming popularity prediction based on multiple factors
- Environmental science projects analyzing factors affecting water quality in streams

Adjusted R-Squared

• **Definition**: Adjusts R² for the number of independent variables, preventing overfitting.

• When to Use:

- o Comparing multiple models with different numbers of predictors
- o Stock market return prediction with multiple variables
- Student performance analysis across different subjects where adding variables may not improve the model

Huber Loss

• **Definition**: A hybrid of MAE and MSE, using MSE for small errors and MAE for large errors, making it robust to outliers.

• When to Use:

- Datasets with outliers where extreme values shouldn't overly influence the model
- o Medical diagnosis prediction to handle abnormal cases
- Equipment sensor data analysis where occasional spikes can throw off calculations

Log-Cosh Loss

• **Definition**: Similar to MSE but less sensitive to large errors, behaving like MAE for big differences.

• When to Use:

- When a smooth, differentiable loss function is needed for gradient-based optimization
- o Earthquake magnitude prediction to reduce sensitivity to rare extreme events

2. Confusion Matrix and Classification Metrics

Understanding the Confusion Matrix

A confusion matrix is a performance evaluation tool that provides a detailed breakdown of classification model predictions compared to actual values. It consists of four key components:

- True Positives (TP): Correctly predicted positive cases
- True Negatives (TN): Correctly predicted negative cases
- False Positives (FP): Incorrectly predicted positive cases (Type I error)
- False Negatives (FN): Incorrectly predicted negative cases (Type II error)

Why Confusion Matrices Are Useful

- They provide insight into different types of errors a model makes
- They allow calculation of precision, recall, F1 score, and other metrics
- They help optimize classification thresholds
- They reveal model performance issues that accuracy alone might hide

Example AI Model: Medical Tumor Detection

Let's consider a model analyzing medical scans for tumors, classifying images as "tumor present" (1) or "tumor absent" (0).

Test Dataset Results:

Image #	Actual	Predicted
1	1	1
2	0	0
3	1	0
4	0	0

Image #	Actual	Predicted
5	0	1
6	1	1
7	1	0
8	0	0

Resulting Confusion Matrix:

	Predicted: Tumor (1)	Predicted: No Tumor (0)
Actual: Tumor (1)	2 (TP)	2 (FN)
Actual: No Tumor (0)	1 (FP)	3 (TN)

Performance Metrics Calculation

Precision (How many predicted positives were actually positive?)

• Precision =
$$2/(2+1) = 2/3 \approx 0.67$$
 or 67%

Recall (How many actual positives were correctly identified?)

• Recall =
$$2/(2+2) = 2/4 = 0.5$$
 or 50%

F1 Score (Harmonic mean of Precision & Recall)

•
$$F1 = 2 \times (0.67 \times 0.5) / (0.67 + 0.5) \approx 0.57 \text{ or } 57\%$$

Accuracy (Overall correct predictions)

• Accuracy =
$$(2+3)/(2+3+1+2) = 5/8 = 0.625$$
 or 62.5%

Specificity (True negative rate)

• Specificity =
$$3/(3+1) = 3/4 = 0.75$$
 or 75%

Interpretation of Results

- 1. **Precision (67%)**: When the model identifies a tumor, it's right about 2/3 of the time. This means roughly 1 in 3 patients would undergo unnecessary further testing.
- 2. **Recall (50%)**: The model only catches half of the actual tumors. This is concerning as missing tumors could delay treatment and worsen outcomes.
- 3. **F1 Score (57%)**: This moderate score reflects the balance between precision and recall, but isn't sufficient for clinical use.
- 4. **Accuracy (62.5%)**: The model gets about 5/8 cases right overall. Better than random guessing, but needs improvement.

5. **Specificity (75%)**: The model is better at ruling out tumors in healthy patients than finding tumors in sick ones.

Real-World Application Considerations

In medical contexts like cancer screening, recall might be prioritized over precision, as missing a tumor (false negative) is generally more harmful than a false alarm (false positive). This demonstrates how the application context should influence which metrics are prioritized when evaluating and optimizing a model.

For a delivery time prediction system like Timelytics, RMSE might be preferred because customer frustration increases exponentially with delay time. When predicting whether a package will be delayed, false negatives (predicting on-time delivery when actually late) are particularly damaging to customer satisfaction.

GitHub link for the code: https://github.com/JashpalsinhRana99/Ai-for-manufacturing-course-assignments/tree/main