# Section A

2.4/9/22 Date
M. J. Angriment -1
A11) zi = ao + a, x;
* y, = âo + â, X,  y, = âo + â, X,
$y_m = \hat{a}_0 + \hat{a}_1 \times n$
) \(\hat{\partial}_{1=1}^{2} \frac{2}{3} = \hat{\hat{\hat{\hat{\hat{\hat{\hat{
= 1 3 = n 20 + 2, 3 Xi
$\frac{\partial}{\partial x} = \frac{\partial}{\partial x} + \frac{\partial}{\partial x} = \frac{\partial}{\partial x} = \frac{\partial}{\partial x} = \frac{\partial}{\partial x} + \frac{\partial}{\partial x} = \frac{\partial}$
$\frac{1}{2} = \hat{a_0} + \hat{a_1} \times \hat{x_1}$
Hence, proved
2) given X and Y are highly correlated with a third variable 2.
a there variable a that X and Y are also
This does not imply a that X and Y are also highly correlated with each other.
we know that
Xx = 2(2; - 1)(y; - 3)
1 2 (2 x - \bar{z}) 2 2 (3 x - \bar{z})2
Spiral Mis,

Date
From Chebyshew is Inequality,
P[ (30 - F(2n) 78] < Vol. (5n
P[15m-H2178] < 760 (5m)
$= \frac{\sigma^2}{\pi \varepsilon^2}$
1 1 P[15/2 - 1/2   2/8] = 0
Hence, proved
4) For Maximum & Posteriori (MAP), we find the relights for our model, given datal.  So we find the most likely relights occording
P(W\$1D) = P(DIW) X P(W)
4 dala P(0) P(z/z,w)
= P(W 3,x) = P(N) xP(W) P(Y)x)
where x, z are input and output.
log(W y,x) = log P(z/12/W) + log(P(W)) const.
Now, P(x/4,02) 2 1 = 202 (a-4)
$P(W) = \frac{1}{2\beta^2} \left( \frac{1}{W^T W} \right)$
$\log p(w) = \log(1) - 1(w^T w)$
Spiral Spiral

## **Section B**

#### Part A

The optimal value of K comes out to be **5** using a learning rate of 0.005 and 250 iterations as it has the lowest RMSE.

Mean RMSE for two folds =

```
[[24.27175085]
[26.55671597]]
25.41423341087223
```

Mean RMSE for three folds =

```
[[17.03602849]
[18.29575654]
[17.81114237]]
17.71430913347759
```

Mean RMSE for four folds =

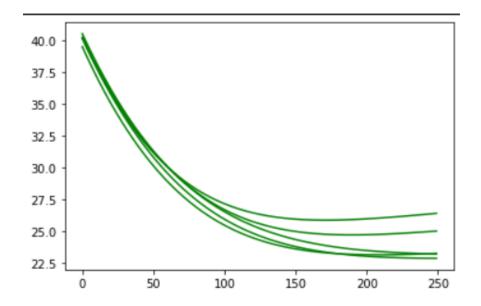
```
[[14.04036726]
[13.41370044]
[12.93641638]
[14.27863578]]
13.667279963273687
```

Mean RMSE for five folds =

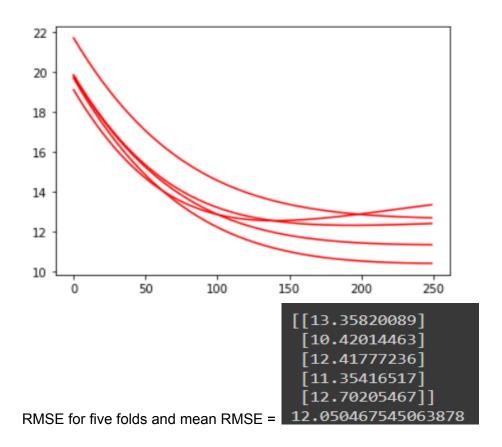
```
[[13.35820089]
[10.42014463]
[12.41777236]
[11.35416517]
[12.70205467]]
12.050467545244437
```

Part B

#### Training RMSE for K=5 folds



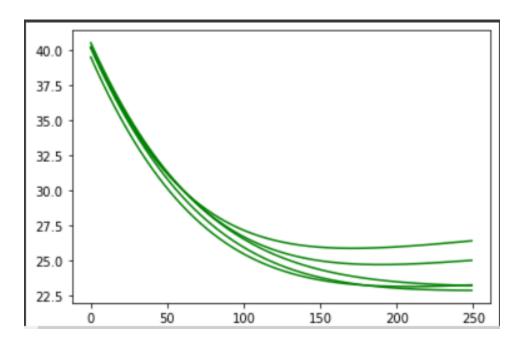
Testing RMSE for K=5 folds



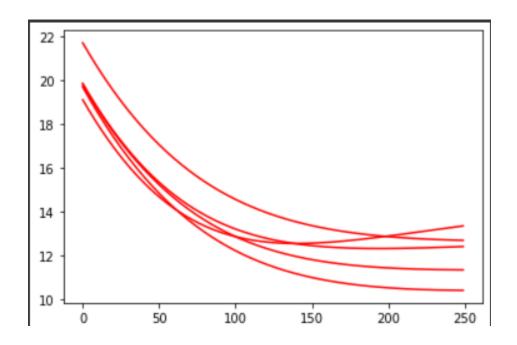
## Part C

### **Lasso Regularisation**

Best value for lambda = 0.01 Training RMSE for K=5 folds

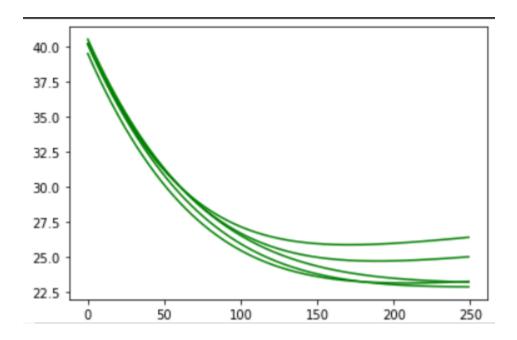


Testing RMSE for K=5 folds

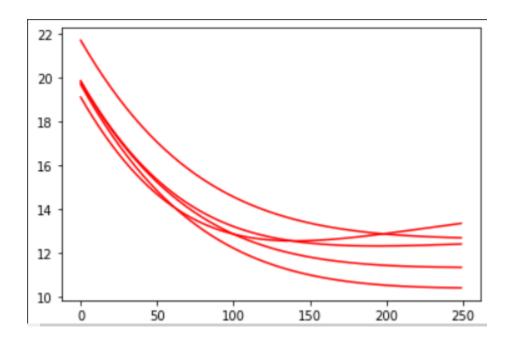


## **Ridge Regularisation**

Best value for lambda = 0.01 Training RMSE for K=5 folds



Testing RMSE for K=5 folds



#### Part D

Optimal weights for the five folds calculated using the normal equation for K=5 folds

```
optimal w: [[ 3.97633140e+01]
  [ 2.73821385e+00]
  [ 3.57592419e+00]
  [ 8.46625470e-01]
  [-2.46099176e-02]
  [-1.52748522e+00]
  [ 3.15362468e+00]]
```

```
optimal w: [[41.97103137]

[-0.57925151]

[-0.38977173]

[10.10153711]

[ 3.13242102]

[14.5801302 ]

[-3.91963092]]
```

```
optimal w: [[40.13677321]
[-5.98685118]
[-3.46558272]
[ 1.73218711]
[ 9.27583032]
[ 4.904223 ]
[ 2.64615697]]
```

```
optimal w: [[37.3288643 ]
  [10.05438414]
  [-1.02983935]
  [ 7.11600963]
  [35.72708814]
  [-6.03310701]
  [ 1.39155563]]
```

```
optimal w: [[ 33.43554971]
  [ -5.46069733]
  [-17.03040667]
  [ 47.88648587]
  [-20.4587385 ]
  [ 43.34701419]
  [ 37.31003219]]
```

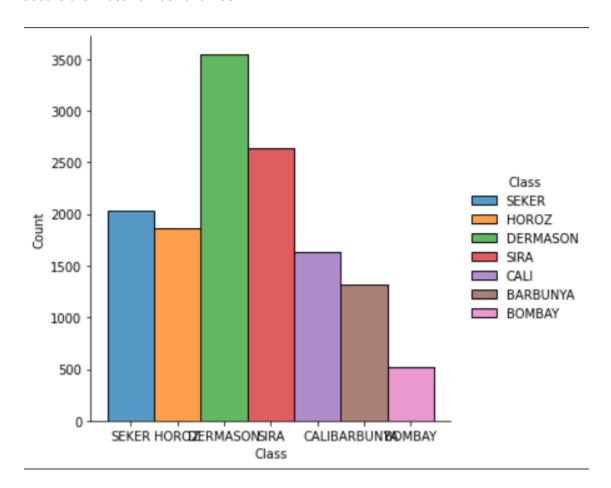
#### Mean RMSE =

```
[[13.35820089]
[10.42014463]
[12.41777236]
[11.35416517]
[12.70205467]]
12.050467545244437
```

## **Section C**

#### Part A

From the displot, we infer that Bombay occurs the least number of times, whereas Dermason occurs the most number of times.



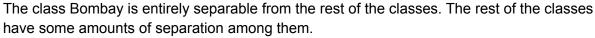
### Part B

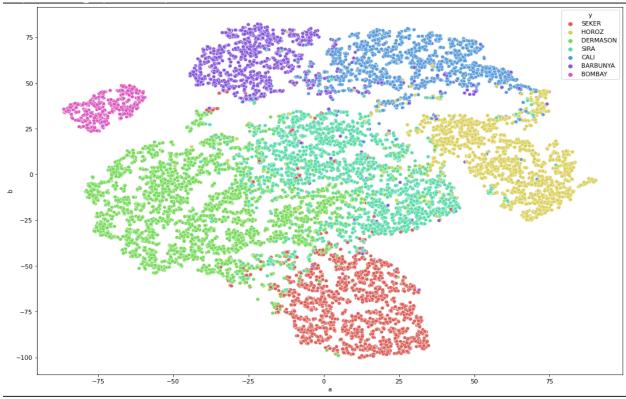
We get the following inferences from the data:

- a) Some features are very skewed, and there are outliers in the distribution.
- b) Bombay class differs significantly from other classes in that it has a larger Area, Perimeter and Minor/Major Axis Length.
- c) Barbunaya and Cali have similar distributions.
- d) There is a lot of overlap between the Dermason and Sira Classes.
- e) There are a lot of linearly correlated features, as can be seen through the heatmap.

f)

#### Part C





### Part D

Gaussian Naive Bayes is for a continuous feature dataset, whereas Bernoulli Naive Bayes is for a binary feature dataset. This is why Gaussian NB gives better accuracy than Bernoulli NB.

```
Gaussian Naive Bayes model accuracy(in %): 89.34998163789938
Gaussian Naive Bayes model precision(in %): 89.44691361783833
Gaussian Naive Bayes model recall(in %): 89.34998163789938
```

```
Bernoulli Naive Bayes model accuracy(in %): 71.31839882482555
Bernoulli Naive Bayes model precision(in %): 72.61726000532246
Bernoulli Naive Bayes model recall(in %): 71.31839882482555
```

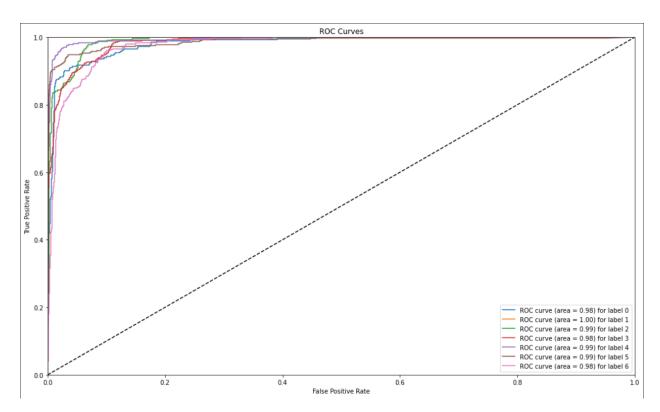
#### Part E

PCA is changing due to change in number of components. PCA reduces the dimensionality of the dataset, which results in different accuracy and other metric scores.

```
PCA model accuracy(in %) for n = 4: 87.0062753783684
PCA model precision(in %) for n = 4: 87.16021324806914
PCA model recall(in %) for n = 4: 87.0062753783684
PCA model f1 score(in %) for n = 4: 86.90930051552206
PCA model accuracy(in %) for n = 6: 89.11037283130307
PCA model precision(in %) for n = 6: 89.53578296026893
PCA model recall(in %) for n = 6: 89.11037283130307
PCA model f1 score(in %) for n = 6: 89.19194994959248
PCA model accuracy(in %) for n = 8: 89.03654485049833
PCA model precision(in %) for n = 8: 89.72577457079089
PCA model recall(in %) for n = 8: 89.03654485049833
PCA model f1 score(in %) for n = 8: 89.14878509619865
PCA model accuracy(in %) for n = 10: 88.33517903285345
PCA model precision(in %) for n = 10: 89.5965329244226
PCA model recall(in %) for n = 10: 88.33517903285345
PCA model f1 score(in %) for n = 10: 88.46856405249926
PCA model accuracy(in %) for n = 12: 88.26135105204872
PCA model precision(in %) for n = 12: 89.48966576549992
PCA model recall(in %) for n = 12: 88.26135105204872
PCA model f1 score(in %) for n = 12: 88.38576161812856
```

### Part F

The following curve shows high AUC scores for the classes. It represents the high performance of the model at distinguishing between the positive and the negative classes.



### Part G

The parameter "multi\_class" is set to "multinomial" instead of "ovr" as it has higher accuracy among the two models.

The accuracy of Logistic Regression with the label "multinomial" is slightly higher than the accuracy of the Gaussian Naive Bayes model.