

# AVL TREES

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## Code

```
// C++ program to delete a node from AVL Tree
```

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```
// An AVL tree node
```

```
class Node
```

```
{
```

```
public:
```

```
    int key;
```

```
    Node *left;
```

```
    Node *right;
```

```
    int height;
```

```
};
```

```
// A utility function to get maximum
```

```
// of two integers
```

```
int max(int a, int b);
```

```
// A utility function to get height
```

```
// of the tree
```

```
int height(Node *N)
```

```
{
```

```
    if (N == NULL)
```

```
        return 0;
```

```
    return N->height;
```

```
}
```

```
// A utility function to get maximum
```

```
// of two integers
```

```
int max(int a, int b)
```

```
{
```

```
    return (a > b) ? a : b;
```

```
}
```

```
/* Helper function that allocates a
```

```
new node with the given key and
```

```
NULL left and right pointers. */
```

```
Node *newNode(int key)
```

```
{
```

```
    Node *node = new Node();
```

```
    node->key = key;
```

```
    node->left = NULL;
```

```
    node->right = NULL;
```

```
    node->height = 1; // new node is initially
```

```
        // added at leaf
```

```
    return (node);
```

```
}
```

```
// A utility function to right
```

```
// rotate subtree rooted with y
```

```
// See the diagram given above.
```

```
Node *rightRotate(Node *y)
```

```
{
```

```
    Node *x = y->left;
```

```
    Node *T2 = x->right;
```

```
    // Perform rotation
```

```
    x->right = y;
```

```
    y->left = T2;
```

```
    // Update heights
```

```
    y->height = max(height(y->left),
```

```
                    height(y->right)) +
```

```
    1;
```

```
    x->height = max(height(x->left),
```

```
                    height(x->right)) +
```

```
    1;
```

```
// Return new root  
return x;  
}
```

```
// A utility function to left  
// rotate subtree rooted with x  
// See the diagram given above.
```

```
Node *leftRotate(Node *x)  
{  
    Node *y = x->right;  
    Node *T2 = y->left;  
  
    // Perform rotation  
    y->left = x;  
    x->right = T2;  
  
    // Update heights  
    x->height = max(height(x->left),  
                    height(x->right)) +  
    1;
```

```

y->height = max(height(y->left),
                height(y->right)) +
                1;

// Return new root
return y;
}

// Get Balance factor of node N
int getBalance(Node *N)
{
    if (N == NULL)
        return 0;
    return height(N->left) -
           height(N->right);
}

Node *insert(Node *node, int key)
{
    /* 1. Perform the normal BST rotation */
    if (node == NULL)

```

```
return (newNode(key));
```

```
if (key < node->key)
```

```
    node->left = insert(node->left, key);
```

```
else if (key > node->key)
```

```
    node->right = insert(node->right, key);
```

```
else // Equal keys not allowed
```

```
    return node;
```

```
/* 2. Update height of this ancestor node */
```

```
node->height = 1 + max(height(node->left),  
                        height(node->right));
```

```
/* 3. Get the balance factor of this
```

```
    ancestor node to check whether
```

```
    this node became unbalanced */
```

```
int balance = getBalance(node);
```

```
// If this node becomes unbalanced,
```

```
// then there are 4 cases
```

```
// Left Left Case
```

```
if (balance > 1 && key < node->left->key)
```

```
    return rightRotate(node);
```

```
// Right Right Case
```

```
if (balance < -1 && key > node->right->key)
```

```
    return leftRotate(node);
```

```
// Left Right Case
```

```
if (balance > 1 && key > node->left->key)
```

```
{
```

```
    node->left = leftRotate(node->left);
```

```
    return rightRotate(node);
```

```
}
```

```
// Right Left Case
```

```
if (balance < -1 && key < node->right->key)
```

```
{
```

```
    node->right = rightRotate(node->right);
```

```
    return leftRotate(node);
```

```
}
```



```
    /* return the (unchanged) node pointer */  
    return node;  
}
```

```
/* Given a non-empty binary search tree,  
return the node with minimum key value  
found in that tree. Note that the entire  
tree does not need to be searched. */
```

```
Node *minValueNode(Node *node)
```

```
{  
    Node *current = node;
```

```
    /* loop down to find the leftmost leaf */
```

```
    while (current->left != NULL)
```

```
        current = current->left;
```

```
    return current;
```

```
}
```

```
// Recursive function to delete a node
```

```
// with given key from subtree with  
// given root. It returns root of the  
// modified subtree.
```

```
Node *deleteNode(Node *root, int key)  
{
```

```
    // STEP 1: PERFORM STANDARD BST DELETE
```

```
    if (root == NULL)
```

```
        return root;
```

```
    // If the key to be deleted is smaller
```

```
    // than the root's key, then it lies
```

```
    // in left subtree
```

```
    if (key < root->key)
```

```
        root->left = deleteNode(root->left, key);
```

```
    // If the key to be deleted is greater
```

```
    // than the root's key, then it lies
```

```
    // in right subtree
```

```
    else if (key > root->key)
```

```
        root->right = deleteNode(root->right, key);
```

```

// if key is same as root's key, then
// This is the node to be deleted
else
{
    // node with only one child or no child
    if ((root->left == NULL) ||
        (root->right == NULL))
    {
        Node *temp = root->left ? root->left : root->right;

        // No child case
        if (temp == NULL)
        {
            temp = root;
            root = NULL;
        }
        else // One child case
            *root = *temp; // Copy the contents of
                           // the non-empty child
        free(temp);
    }
}

```

```

    }
else
{
    // node with two children: Get the inorder
    // successor (smallest in the right subtree)
    Node *temp = minValueNode(root->right);

    // Copy the inorder successor's
    // data to this node
    root->key = temp->key;

    // Delete the inorder successor
    root->right = deleteNode(root->right,
                            temp->key);
}
}

// If the tree had only one node
// then return
if (root == NULL)
    return root;

```

```
// STEP 2: UPDATE HEIGHT OF THE CURRENT NODE
```

```
root->height = 1 + max(height(root->left),  
                        height(root->right));
```

```
// STEP 3: GET THE BALANCE FACTOR OF
```

```
// THIS NODE (to check whether this
```

```
// node became unbalanced)
```

```
int balance = getBalance(root);
```

```
// If this node becomes unbalanced,
```

```
// then there are 4 cases
```

```
// Left Left Case
```

```
if (balance > 1 &&
```

```
    getBalance(root->left) >= 0)
```

```
    return rightRotate(root);
```

```
// Left Right Case
```

```
if (balance > 1 &&
```

```
    getBalance(root->left) < 0)
```

```

{
    root->left = leftRotate(root->left);
    return rightRotate(root);
}

// Right Right Case
if (balance < -1 &&
    getBalance(root->right) <= 0)
    return leftRotate(root);

// Right Left Case
if (balance < -1 &&
    getBalance(root->right) > 0)
{
    root->right = rightRotate(root->right);
    return leftRotate(root);
}

return root;
}

```

```
// A utility function to print preorder
```

```
// traversal of the tree.
```

```
// The function also prints height
```

```
// of every node
```

```
void preOrder(Node *root)
```

```
{
```

```
    if (root != NULL)
```

```
    {
```

```
        cout << root->key << " ";
```

```
        preOrder(root->left);
```

```
        preOrder(root->right);
```

```
    }
```

```
}
```

```
// Driver Code
```

```
int main()
```

```
{
```

```
    Node *root = NULL;
```

```
    /* Constructing tree given in
```

```
       the above figure */
```

```

root = insert(root, 9);
root = insert(root, 5);
root = insert(root, 10);
root = insert(root, 0);
root = insert(root, 6);
root = insert(root, 11);
root = insert(root, -1);
root = insert(root, 1);
root = insert(root, 2);

```

/\* The constructed AVL Tree would be

```

      9
     /\
    1 10
   /\ \
  0 5 11
 /\ \
-1 2 6
*/

```

cout << "Preorder traversal of the "



```

        "constructed AVL tree is \n";
preOrder(root);

root = deleteNode(root, 10);

/* The AVL Tree after deletion of 10
        1
      /\
     0 9
    /\
   -1 5 11
  /\
 2 6

*/

cout << "\nPreorder traversal after"
      << " deletion of 10 \n";
preOrder(root);

return 0;
}

```

## Output

```
Preorder traversal of the constructed AVL tree is
9 1 0 -1 5 2 6 10 11
Preorder traversal after deletion of 10
1 0 -1 9 5 2 6 11
Process returned 0 (0x0)   execution time : 29.540 s
Press any key to continue.
```