

Write predicates to evaluate propositional programs, in particular: the least model for definite logic programs.

This assignment will give you training on writing “interpreters” in Prolog. The assignment is structured in a sequence of steps: ranging starting from simpler basic ones that are used to construct the subsequent, more complex ones.

Propositional programs manipulated by your program will be given by a list where each element is of the form `rule(p, b)` where `p` is a proposition and `b` is a (possibly empty) list of literals. Each literal is a proposition (i.e. a positive literal).

Example propositional program and its representation:

```
(a) p <- r.  
q <- q.  
r.
```

```
[rule(p, [r]),  
rule(q, [q]),  
rule(r, [])]
```

Write a predicate `propositions(P, L)` that finds the list `L` of all propositions in the given propositional program `P`. For example, when `P` is the example program (a), `propositions(P, L)` should succeed with `L = [p,q,r]`.

For the above question, the list (the answer) should not have duplicates; the order of elements in the list does not matter.

Write a predicate `tp(P, M1, M2)` that, given a list of predicates `M1` finds a list `M2` such that `M2` is the immediate consequence of the propositional program `P` with respect to `M1`: i.e. `M2 = TP(M1)`.

For this predicate, assume that the given propositional program is definite.

For instance, when `P` is the example program (a), `tp(P, [r], M)` will succeed with `M = [p,r]`.

Use library predicate `sort/2` to ensure that the list `M2` will always be given in the same order.

Write a predicate `leastmodel(P, M)` that returns a list `M` of propositions in the least model of the given propositional definite program `P`. For instance,

- when `P` is the example program (a), `leastmodel(P, M)` will succeed with `M = [p, r]`.