

Survey Index Estimation and Simulation using EBS Survey Data.

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September 29, 2020

1 Model

Survey indices are calculated using the methodology described in [2] and the `surveyIndex` package [1], although the response variable is CPUE in weight rather than numbers-at-age and we consider time-varying spatial effects.

The following equation describes the model:

$$\log(\mu_i) = \text{Year}(i) + f_1(\text{sx}_i, \text{sy}_i) + f_2(\text{Year}_i, \text{sx}_i, \text{sy}_i) \quad (1)$$

$$+ f_3(\text{depth}_i) + f_4(\log(\text{temperature}_i + 3)) \quad (2)$$

where μ_i is the expected value of the CPUE in weight of the i th haul. The spatial effects are described by a high resolution time-invariant average distribution (f_1) and independent yearly deviations from that average (f_2). The maximal basis dimension of f_1 and f_2 are set to 376 and 50 per year respectively, and the smoothing penalty and spline basis is the same for all years in f_2 . The last two splines (f_3 and f_4) describe the effect of bottom depth and gear temperature. The latter was added 3 and log-transformed because preliminary runs suggested that most variation occurred on a narrow interval at the coldest end of the observed interval. The chosen transformation stretches this interval out such that the resulting splines are more smooth and can be fitted using fewer knots while ensuring that numbers are positive before taking the logarithm. All splines are thin plate splines with shrinkage.

2 Results

2.1 Arrowtooth Flounder

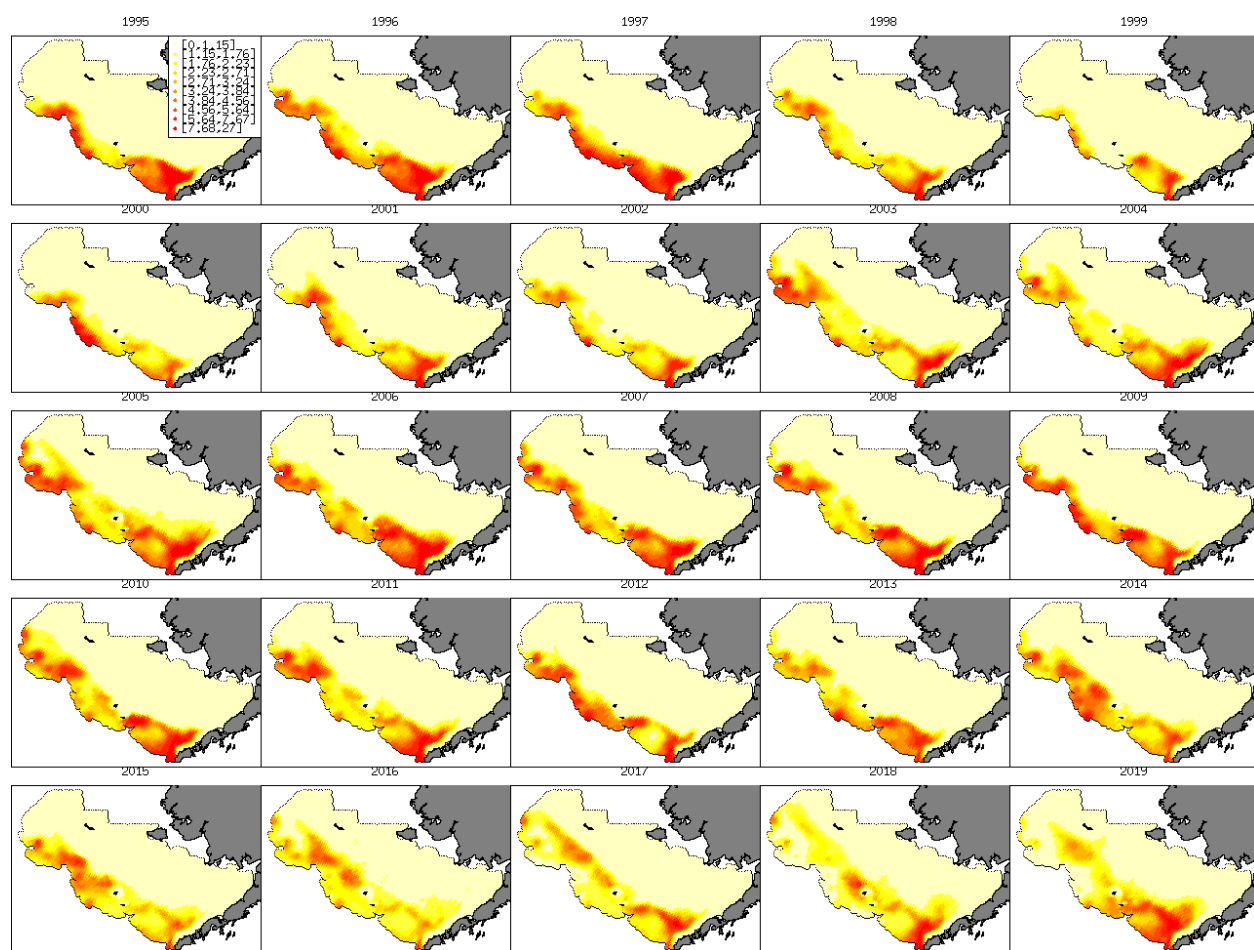


Figure 1

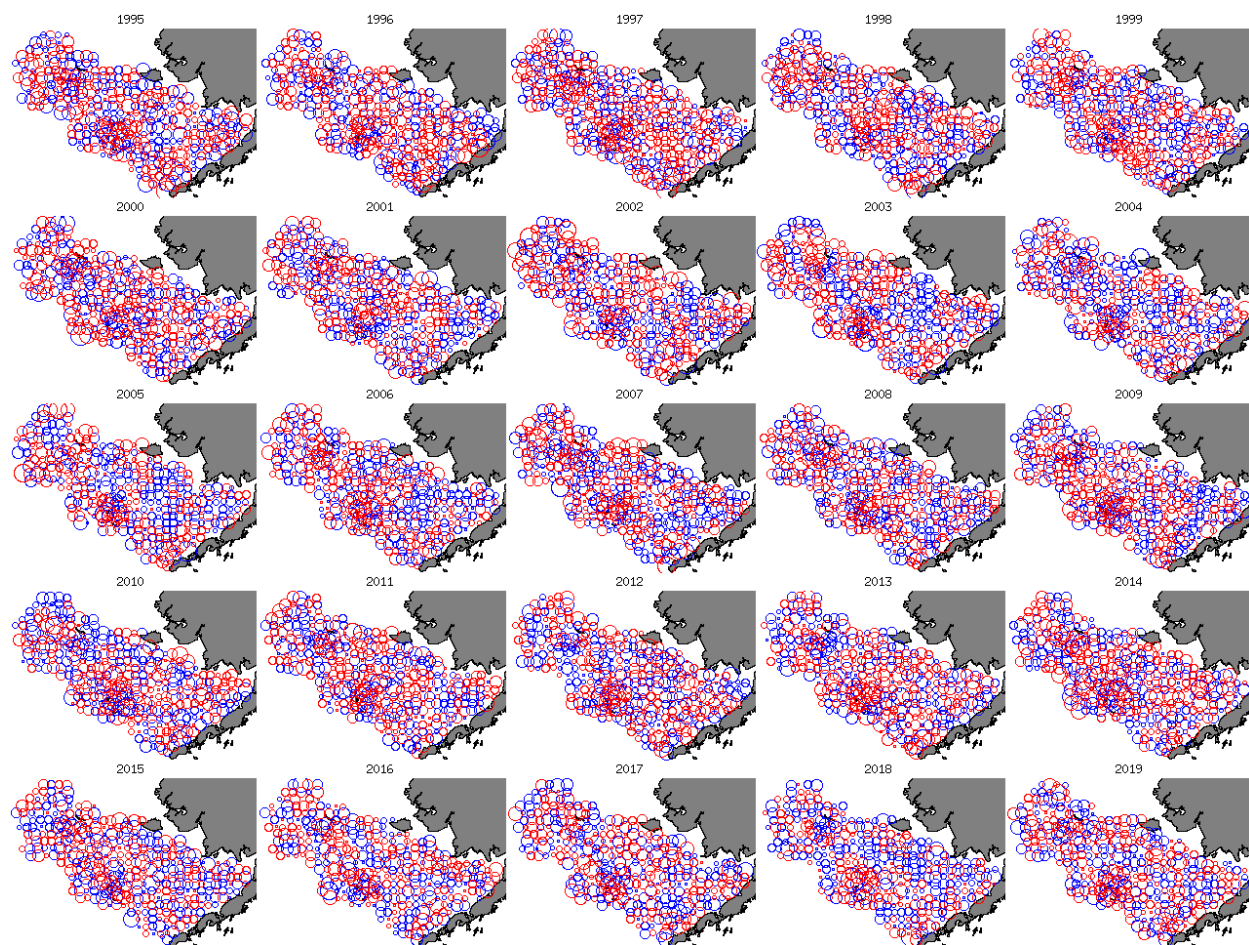


Figure 2

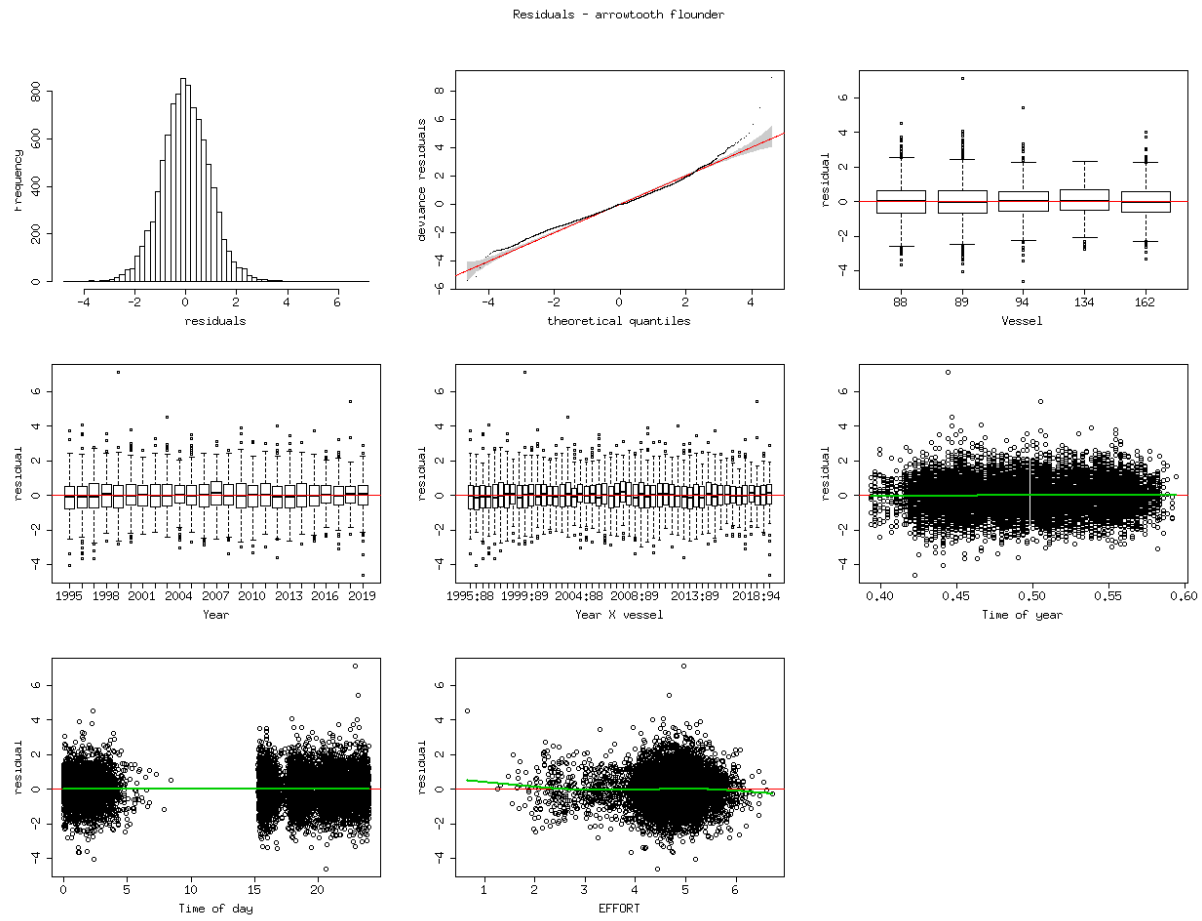


Figure 3

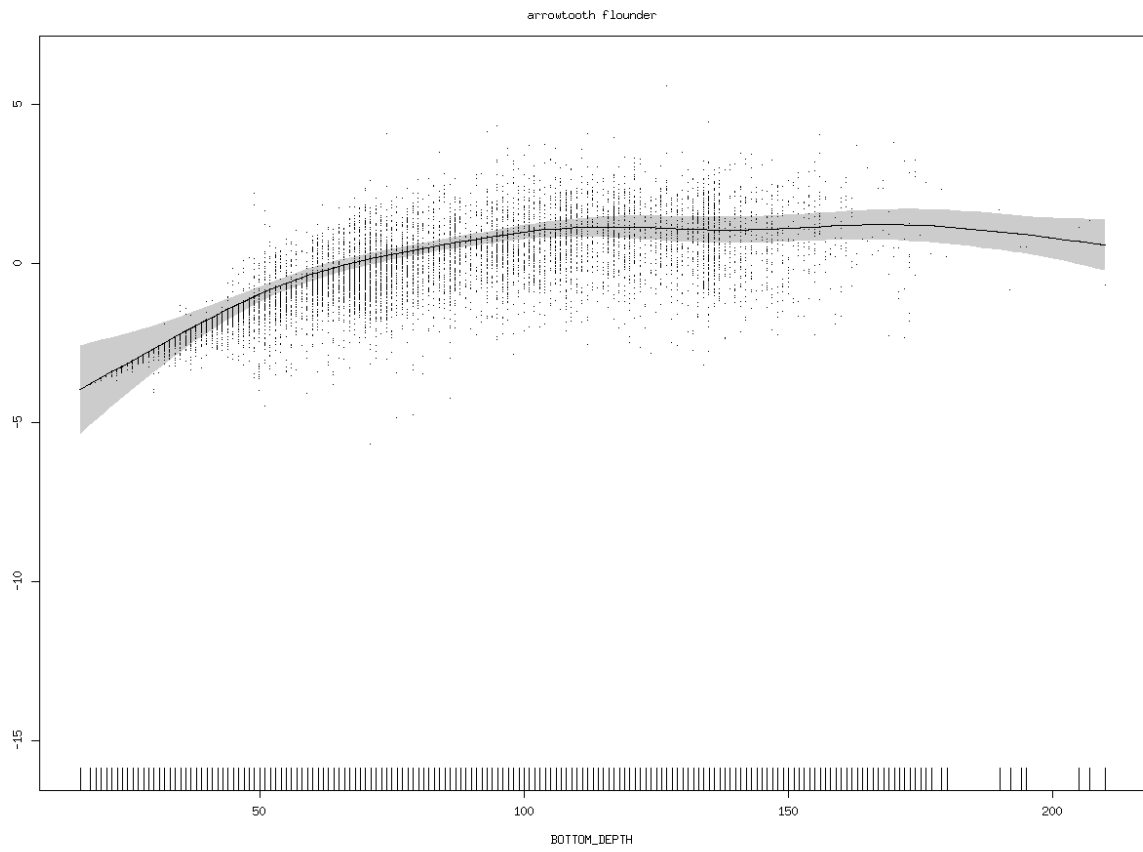


Figure 4

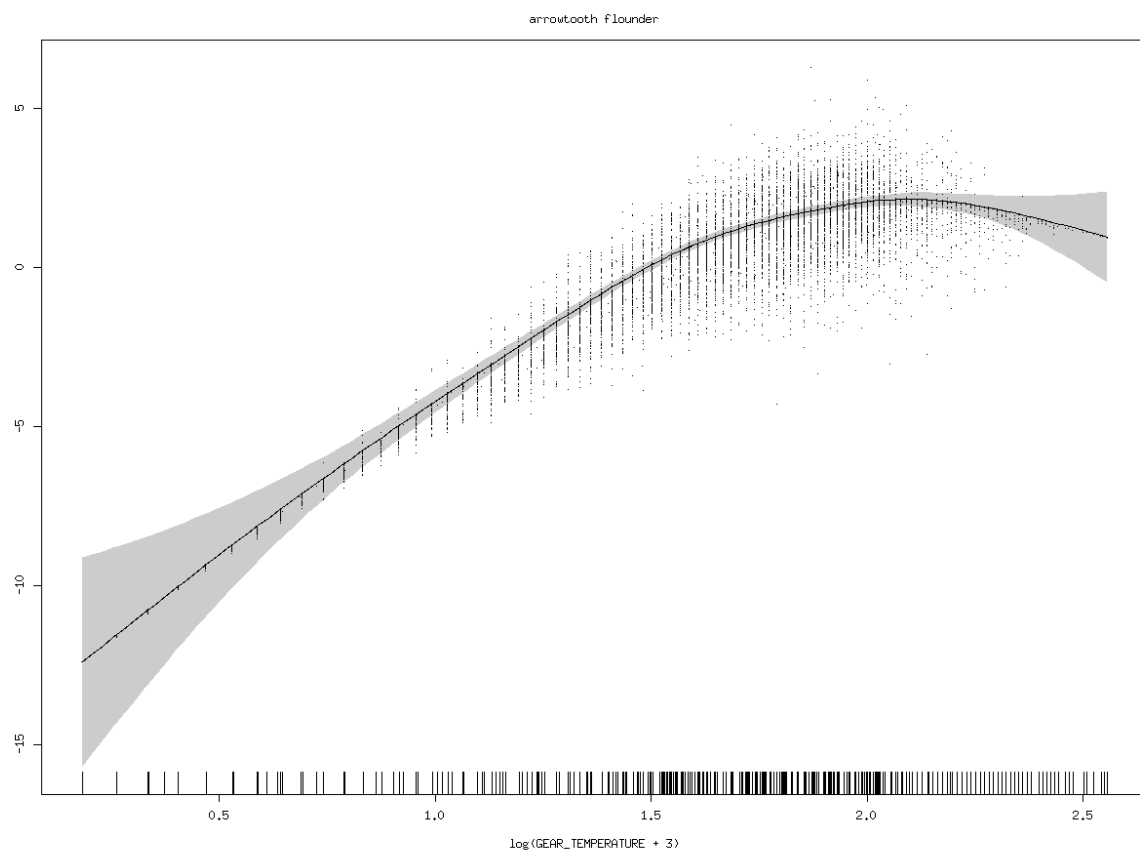


Figure 5

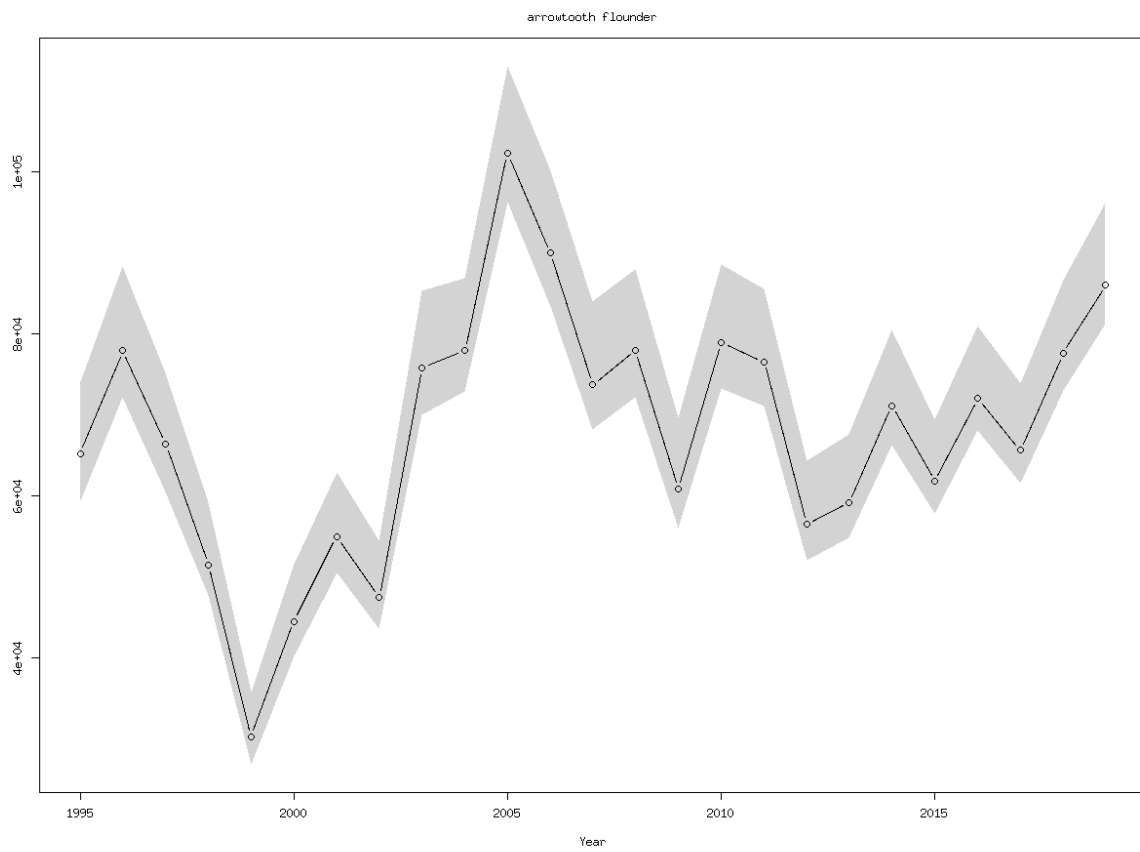


Figure 6

2.2 Pacific cod

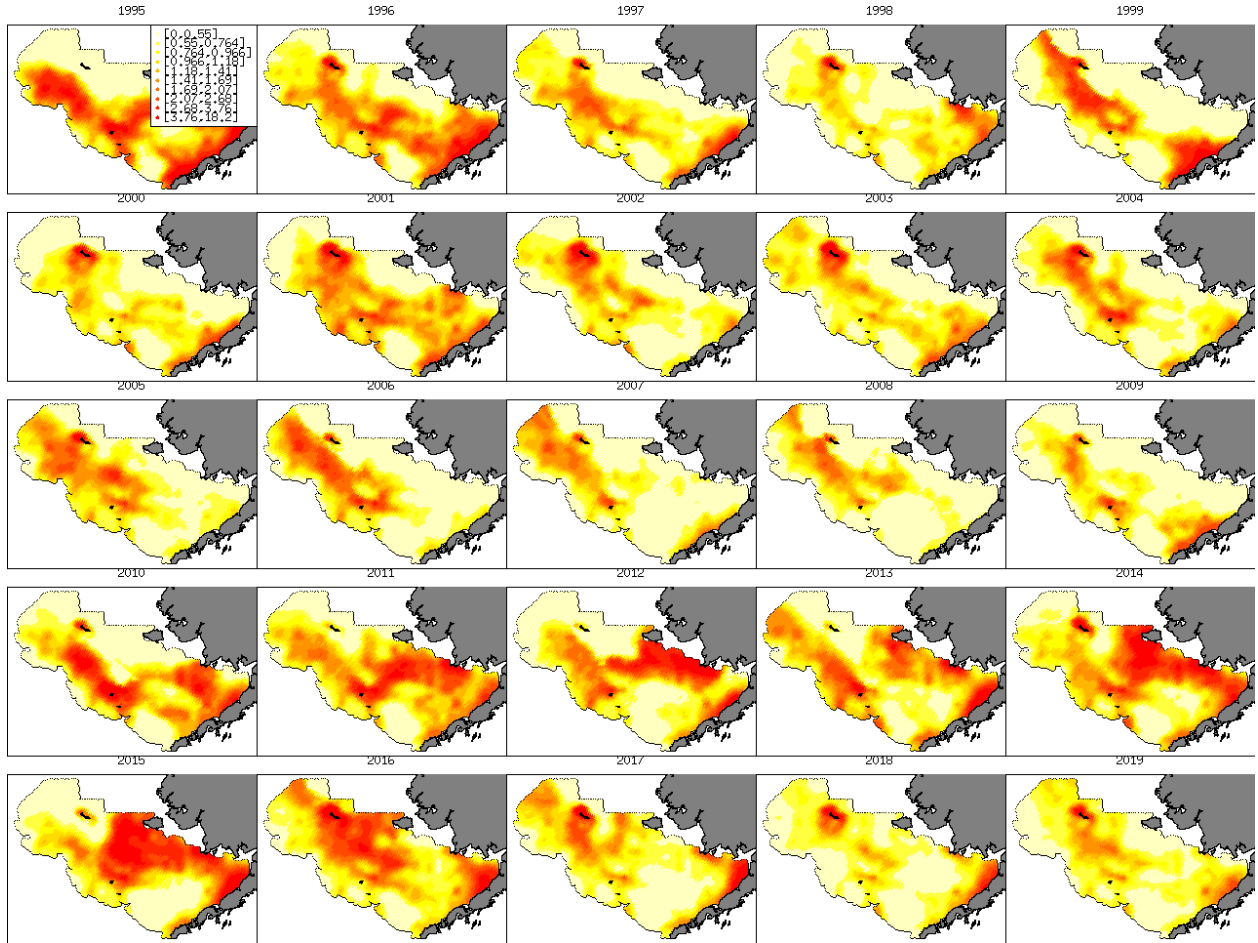


Figure 7

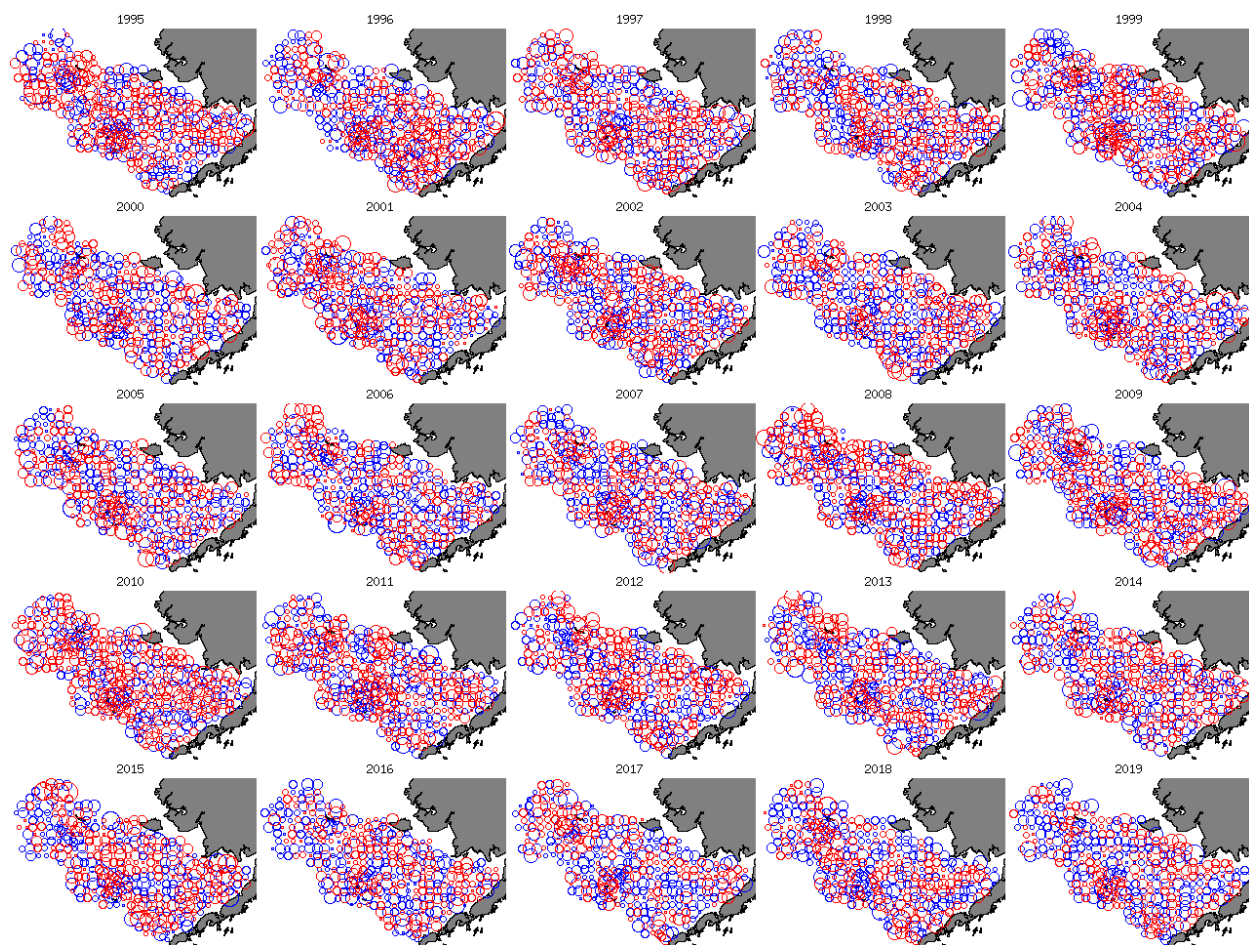


Figure 8

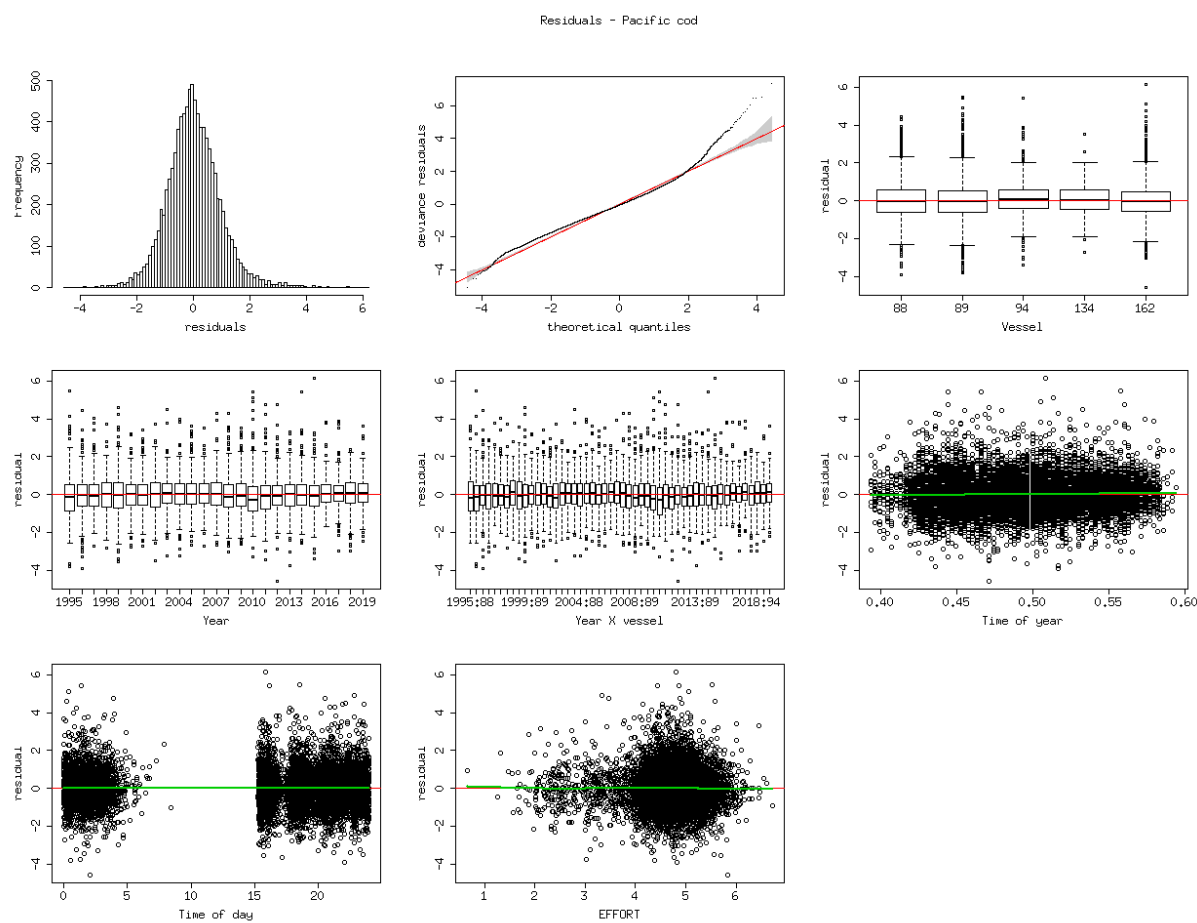


Figure 9

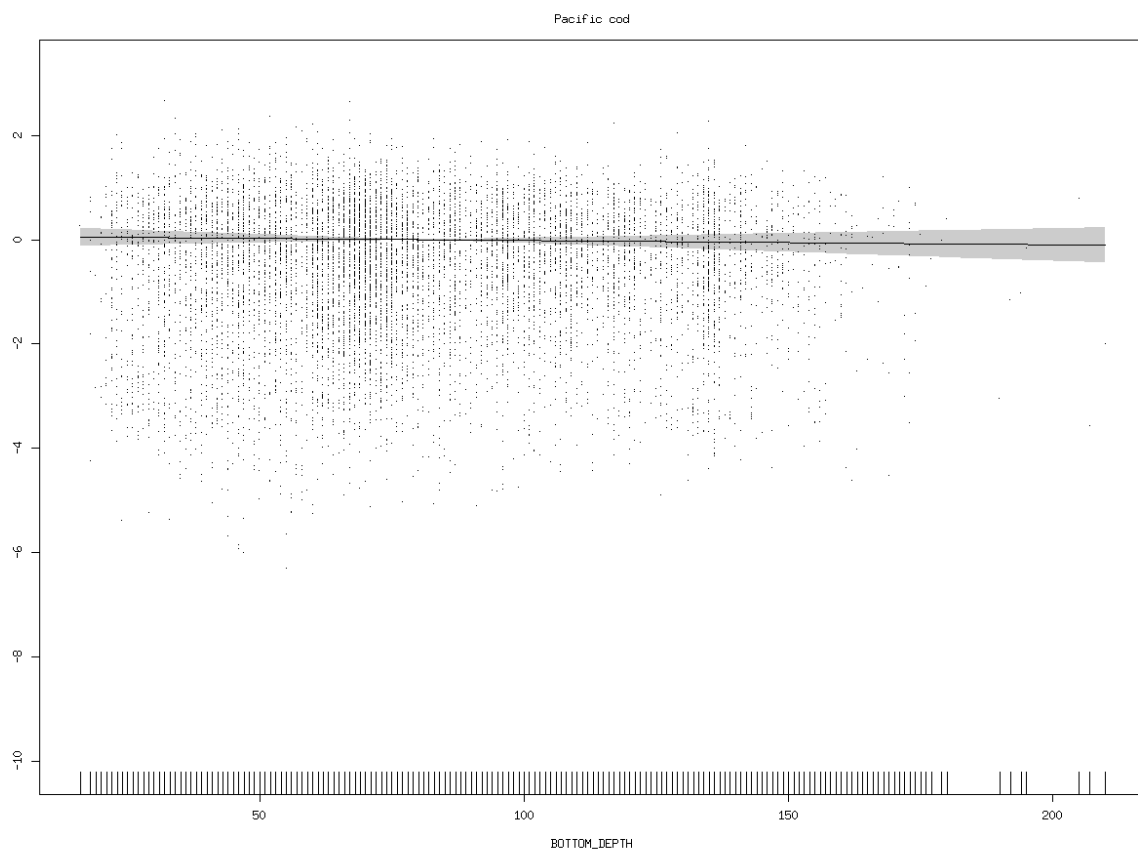


Figure 10

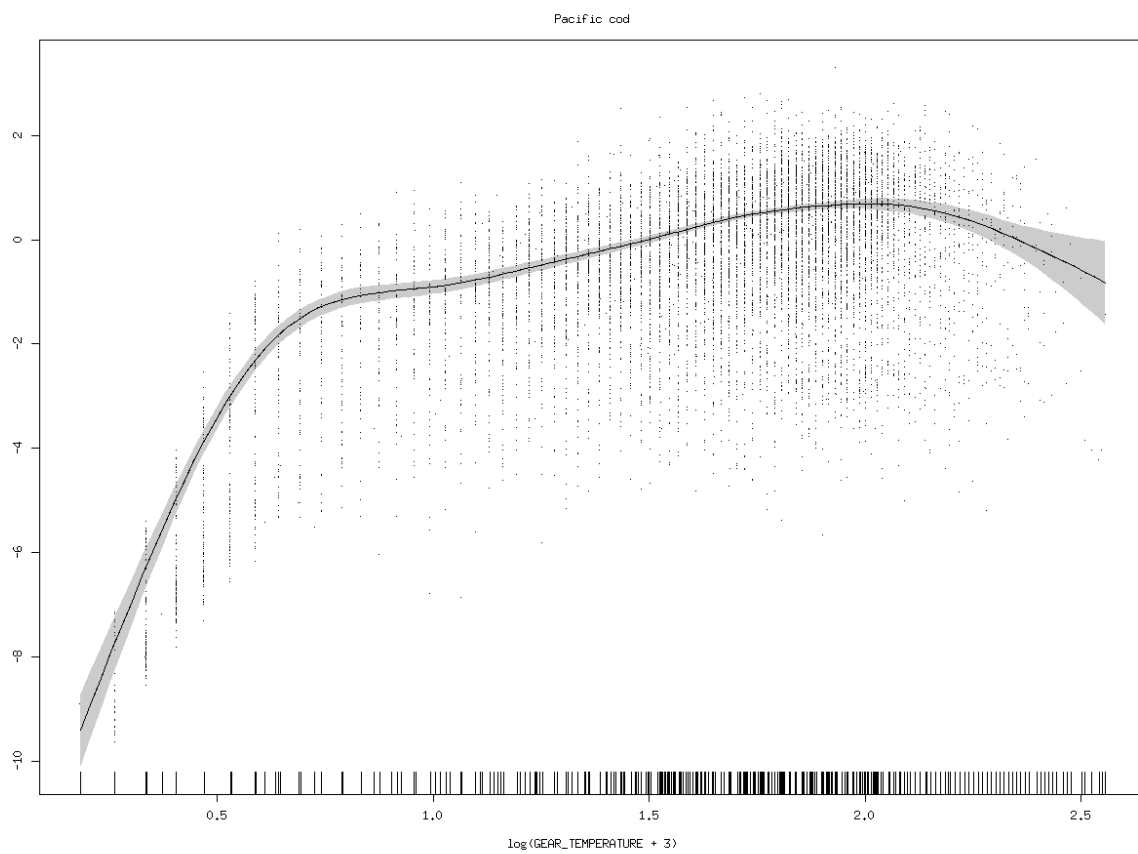


Figure 11

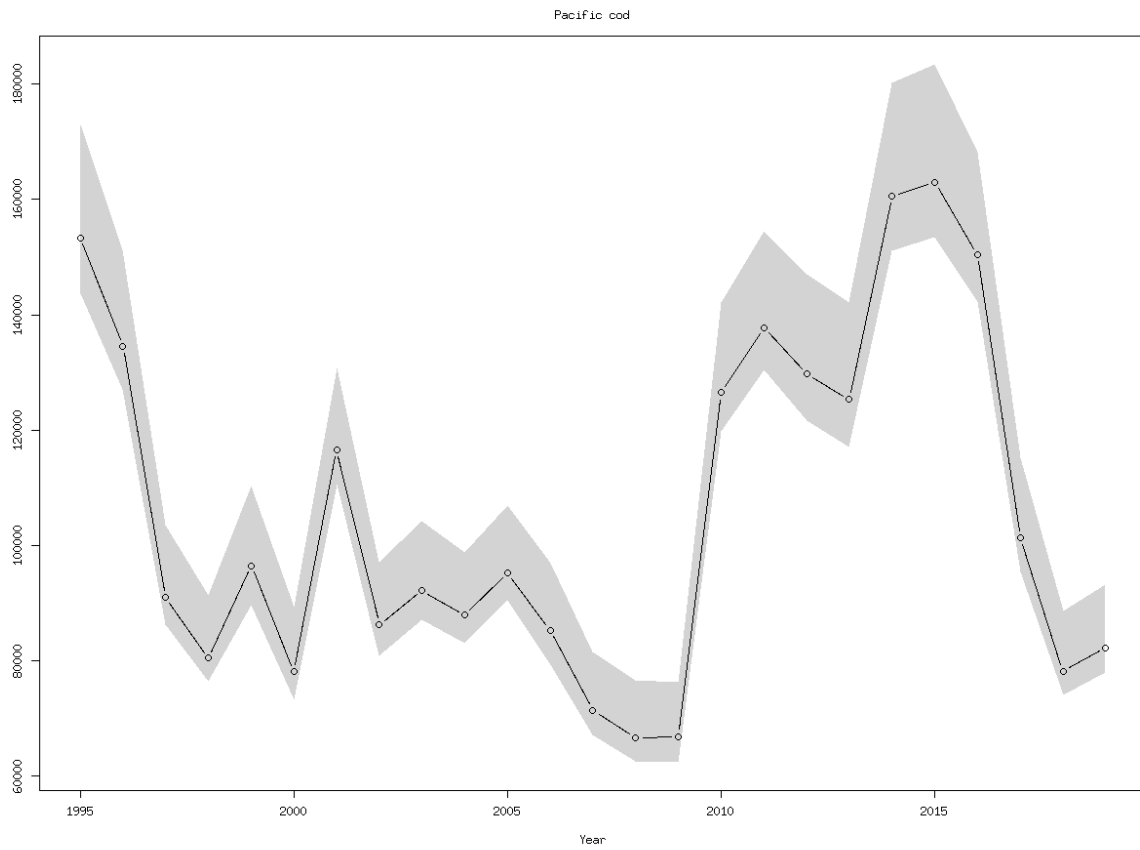


Figure 12

2.3 Walleye Pollock

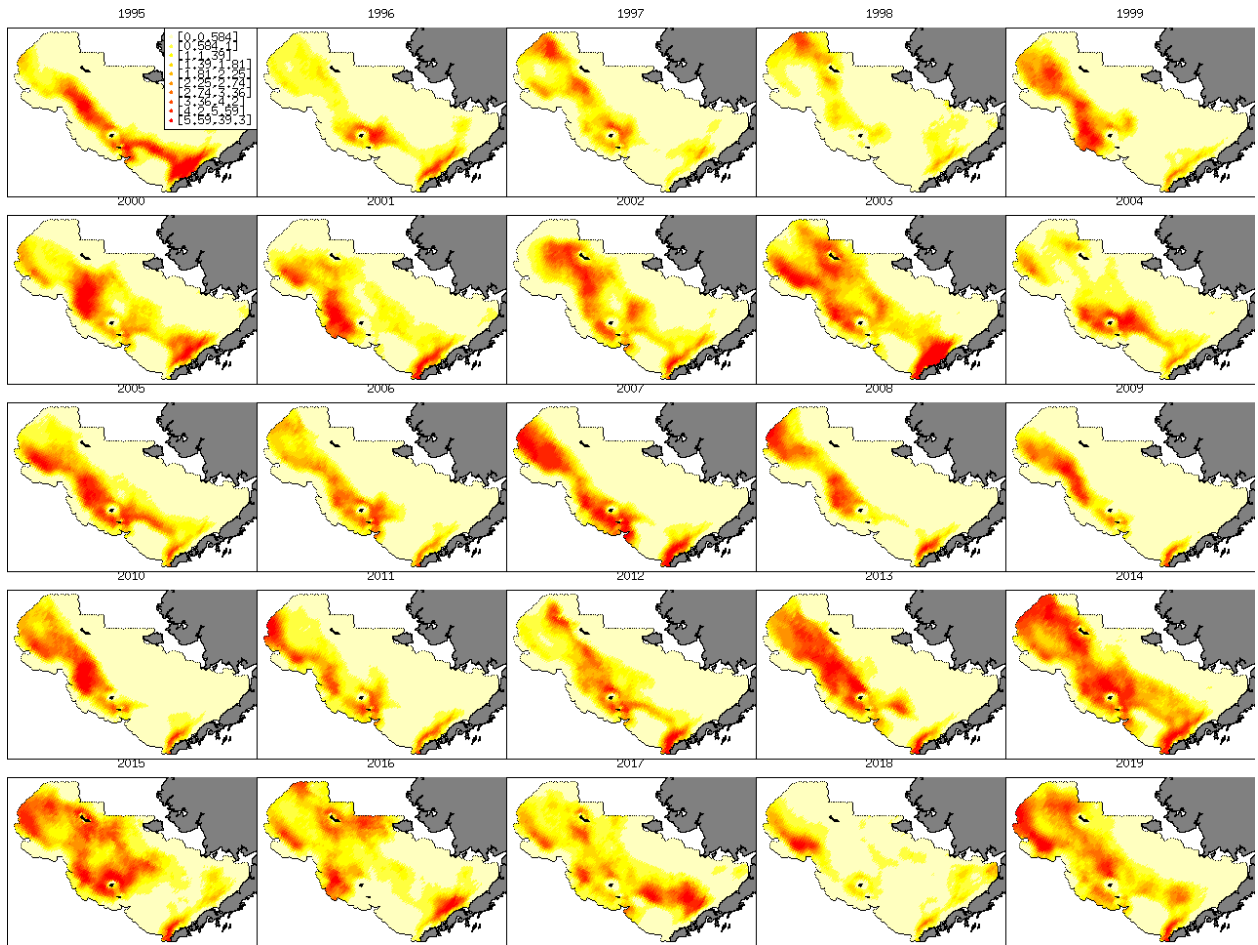


Figure 13

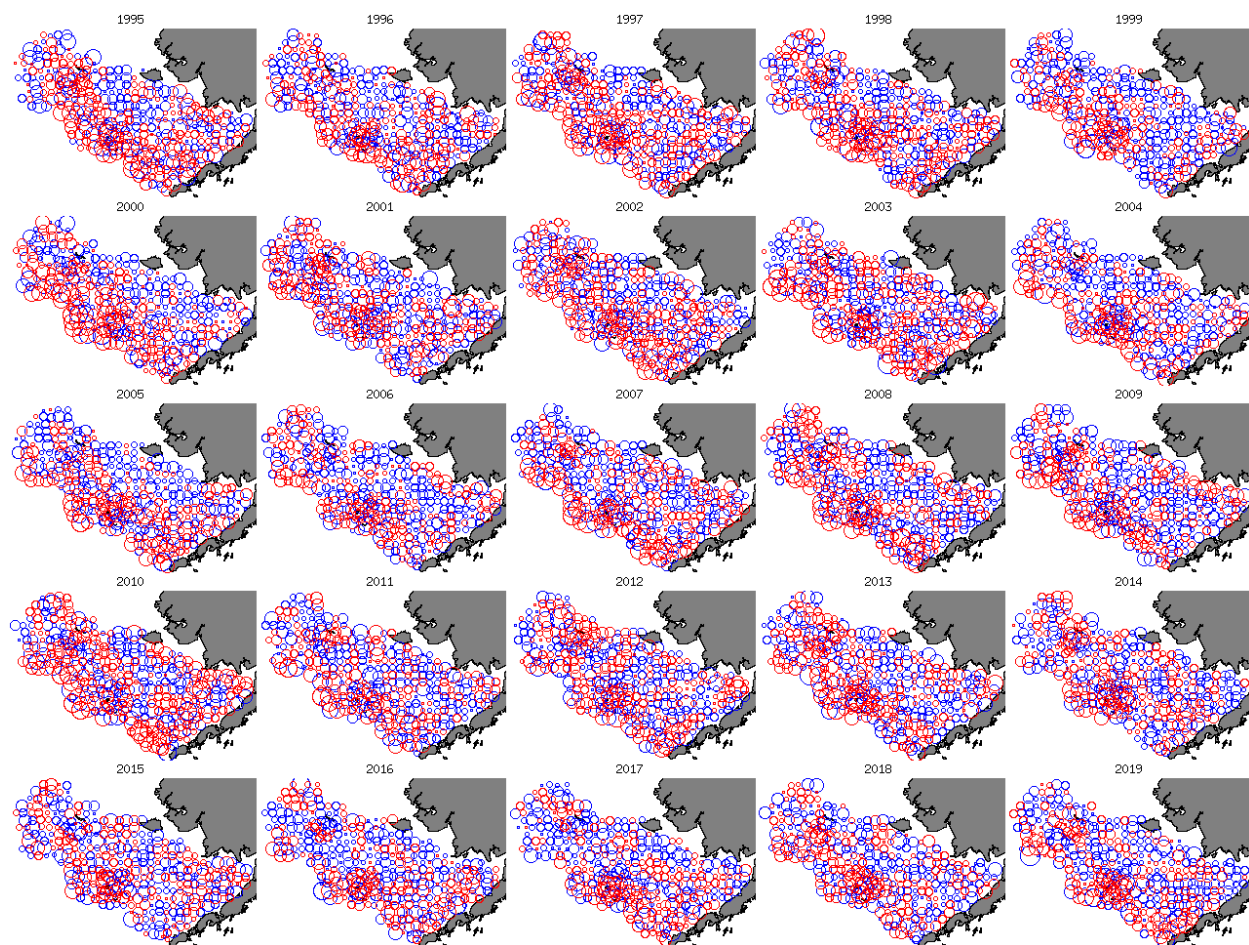


Figure 14

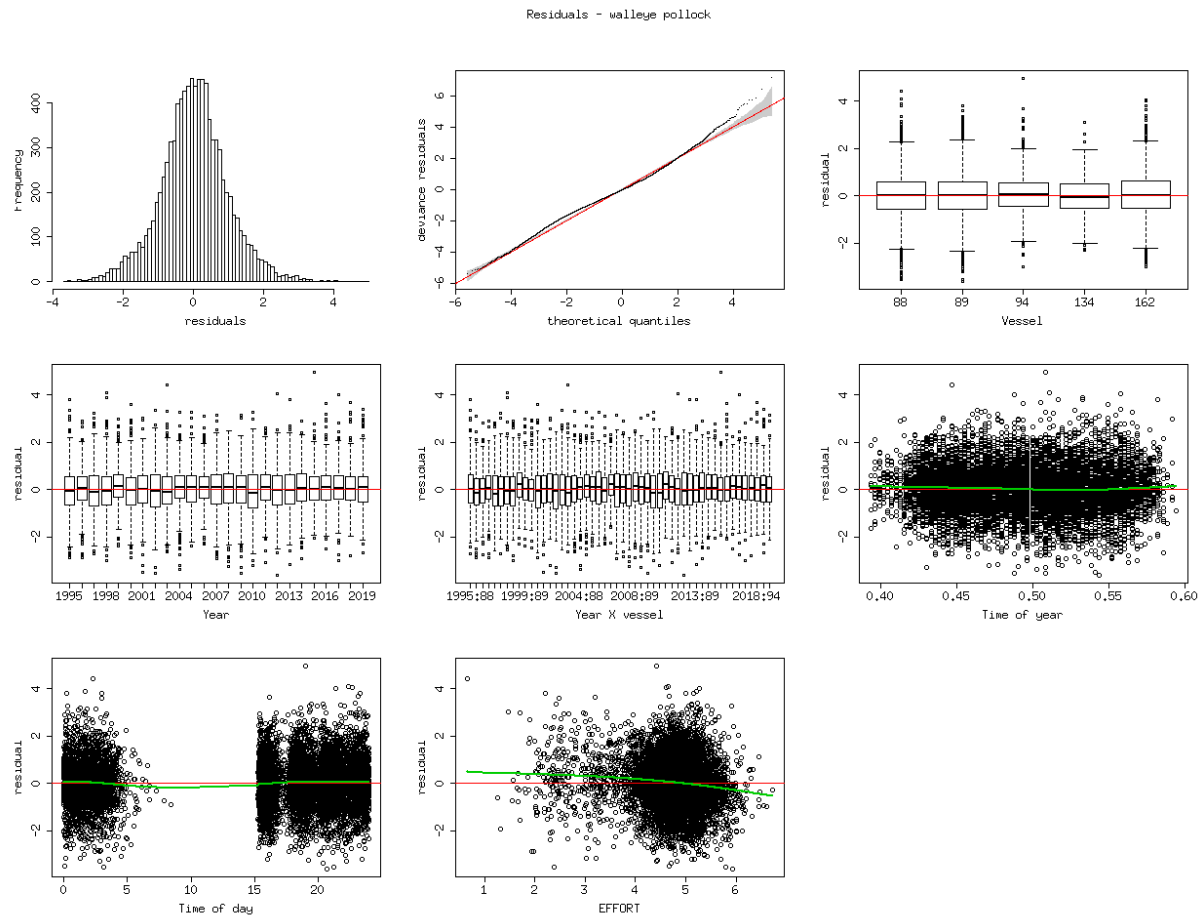


Figure 15

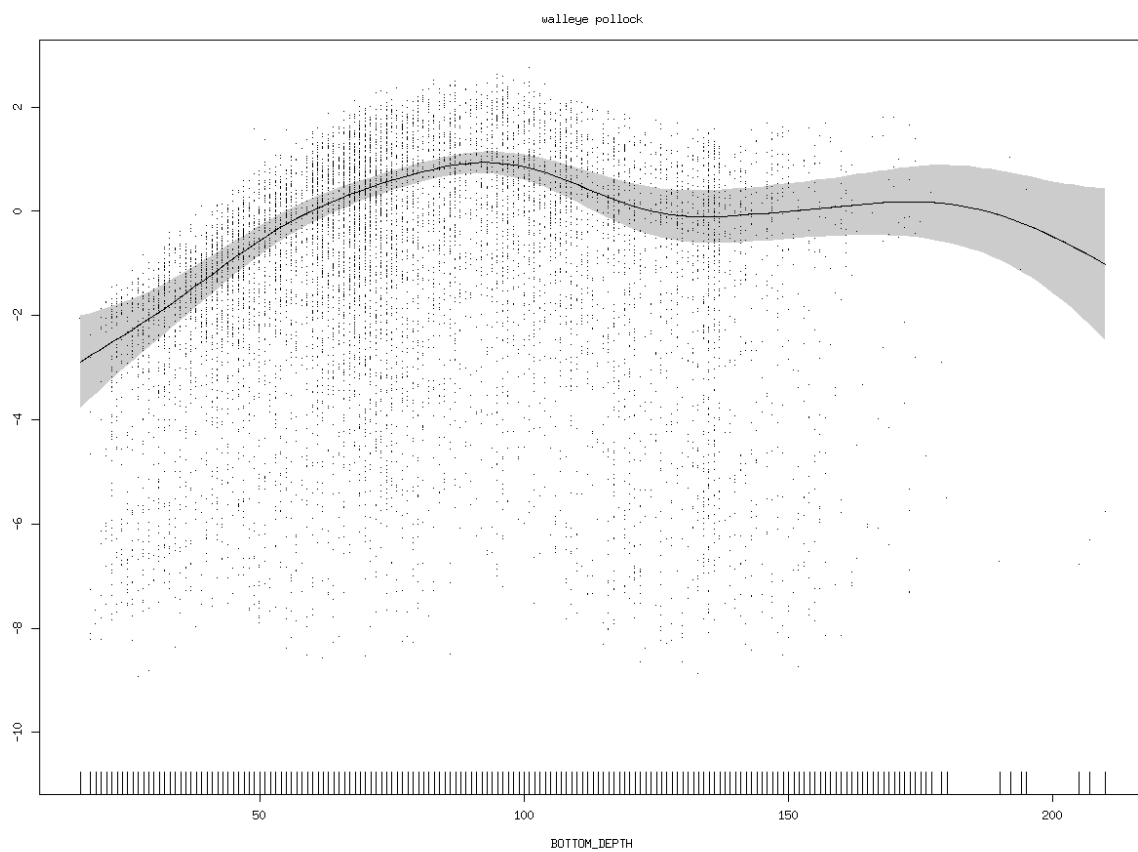


Figure 16

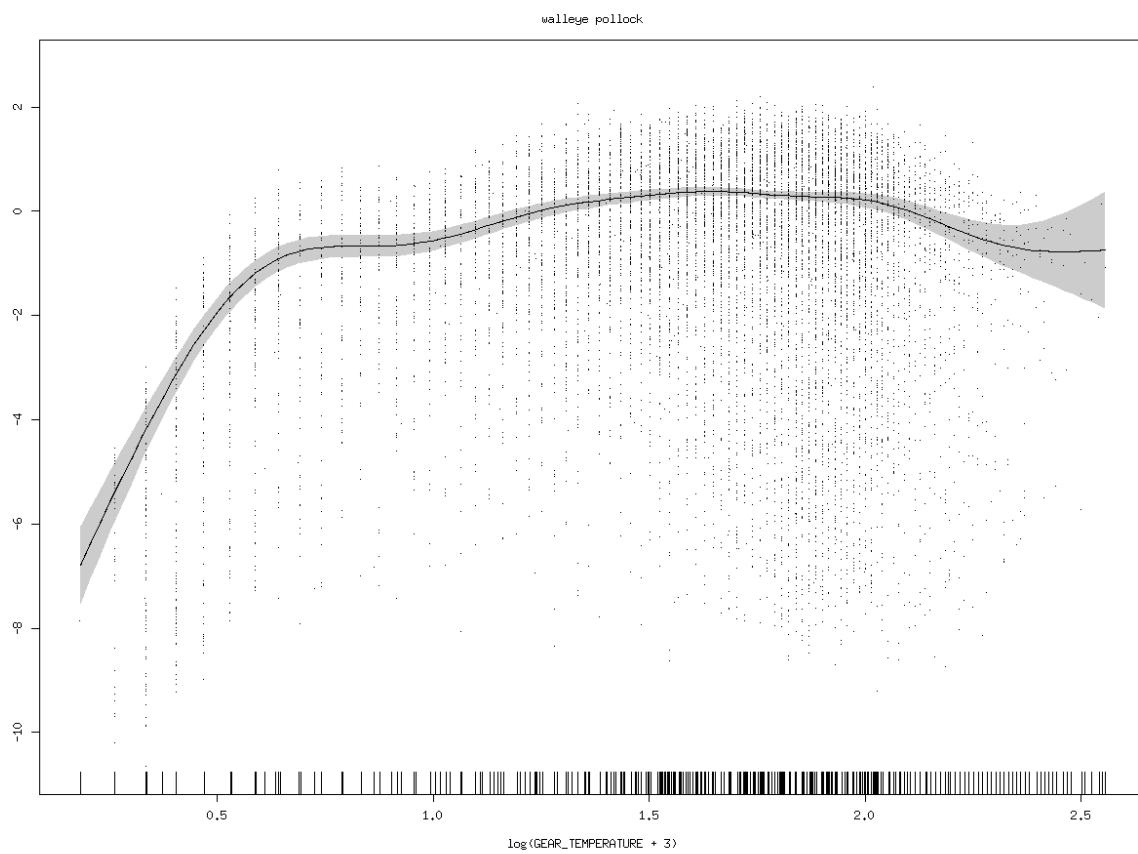


Figure 17

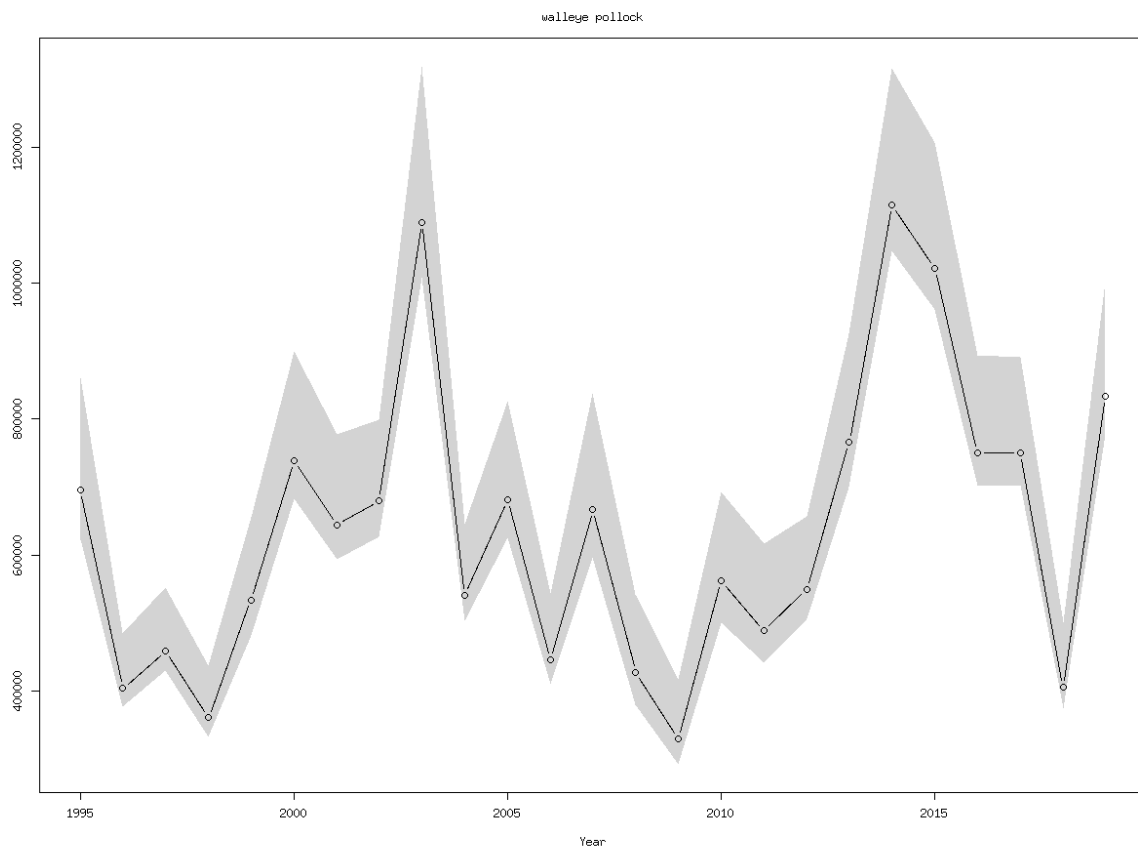


Figure 18

2.4 Yellowfin Sole

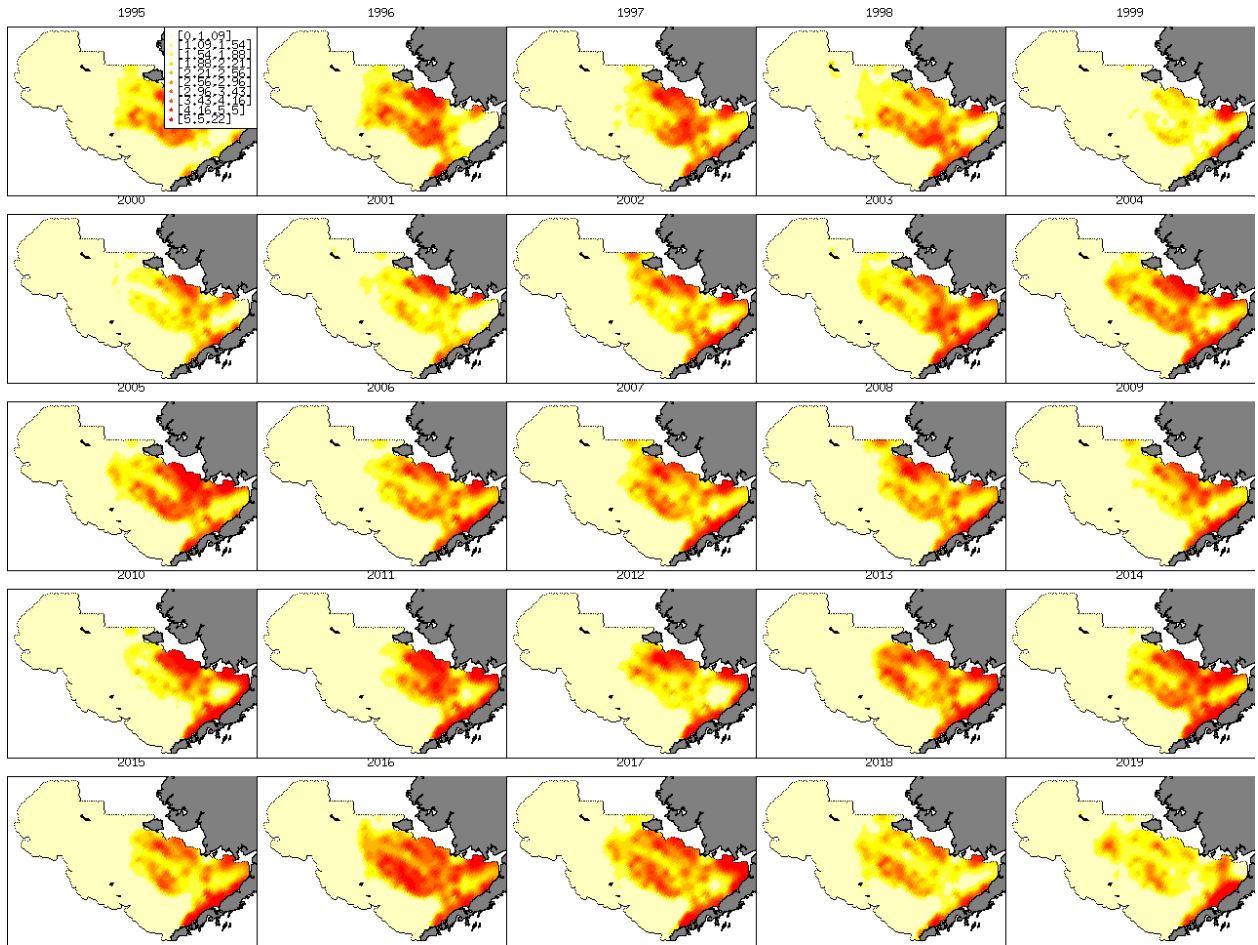


Figure 19

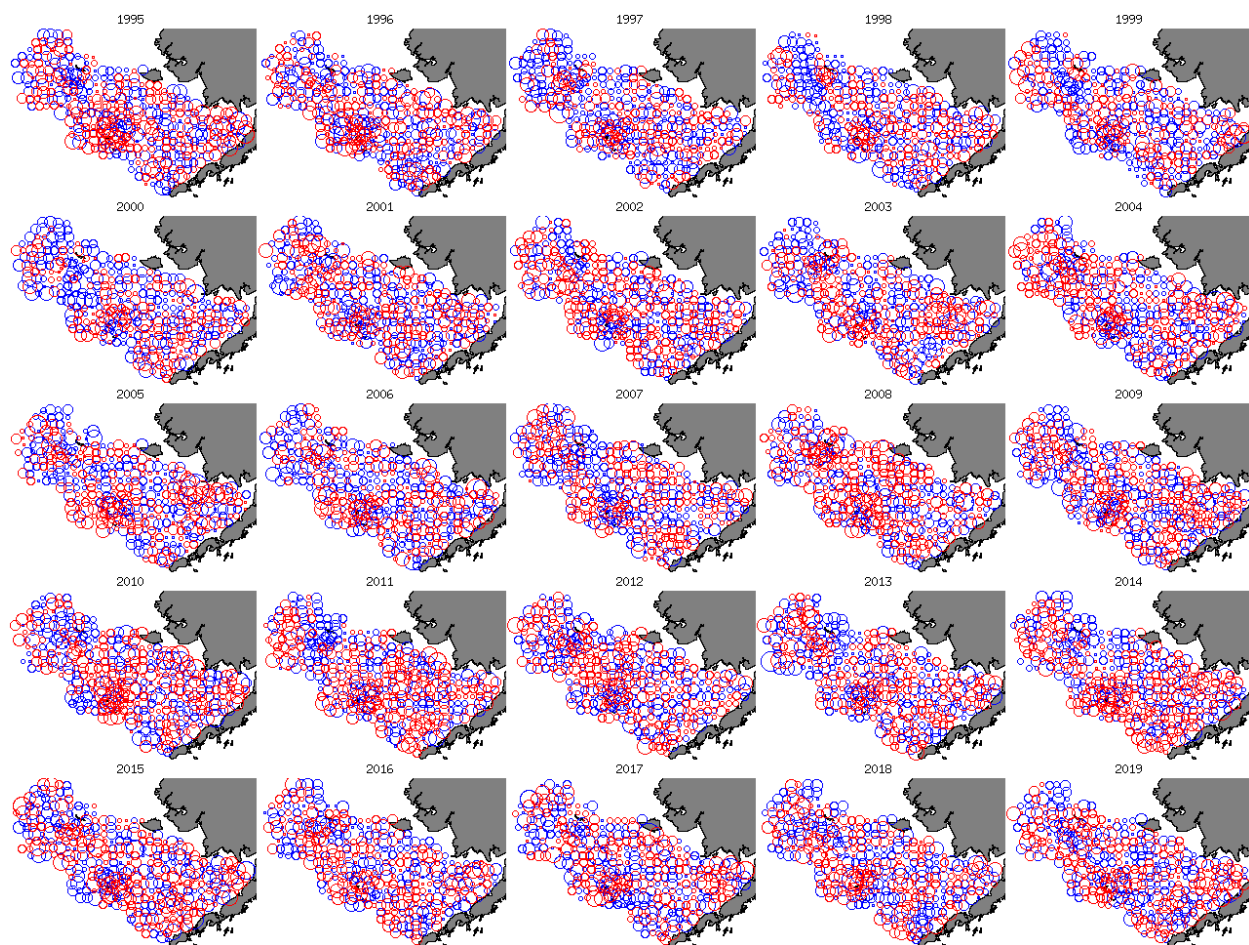


Figure 20

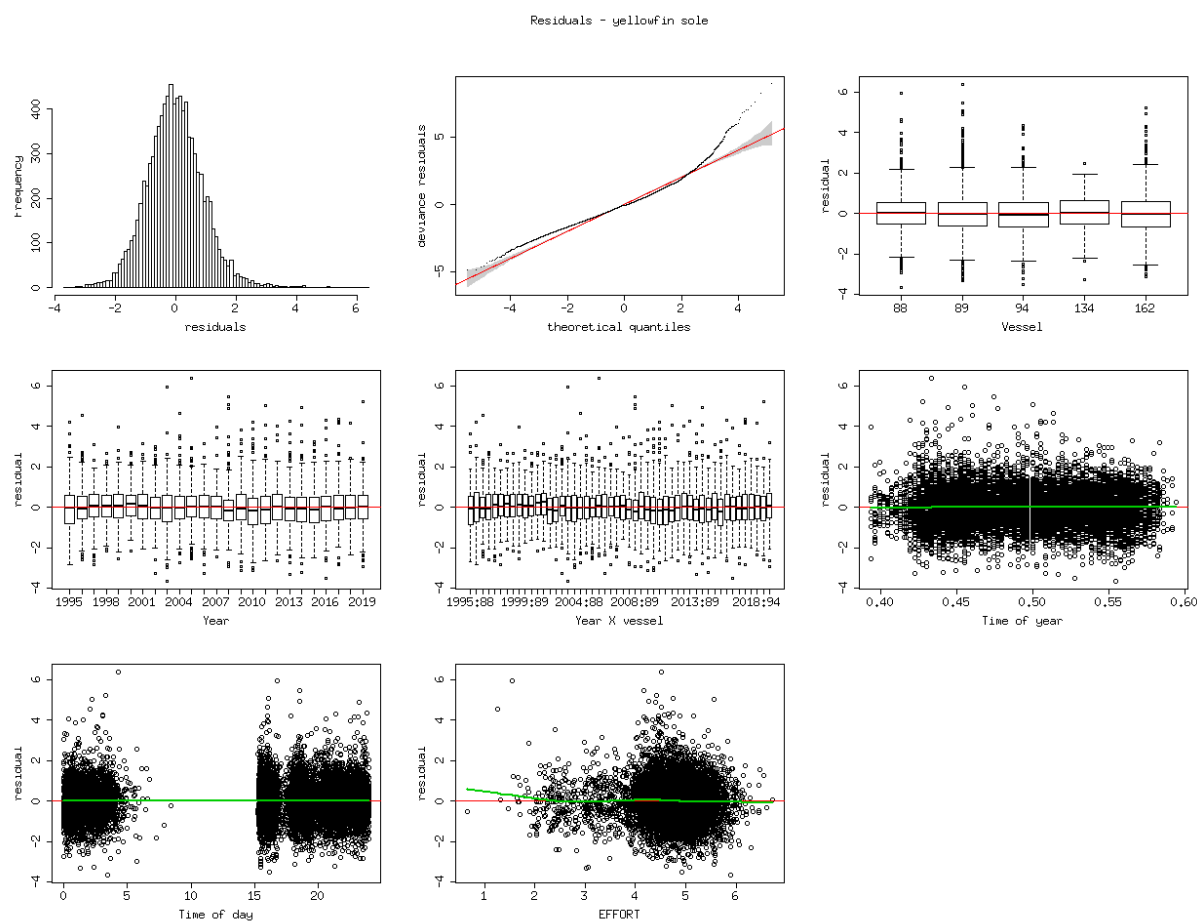


Figure 21

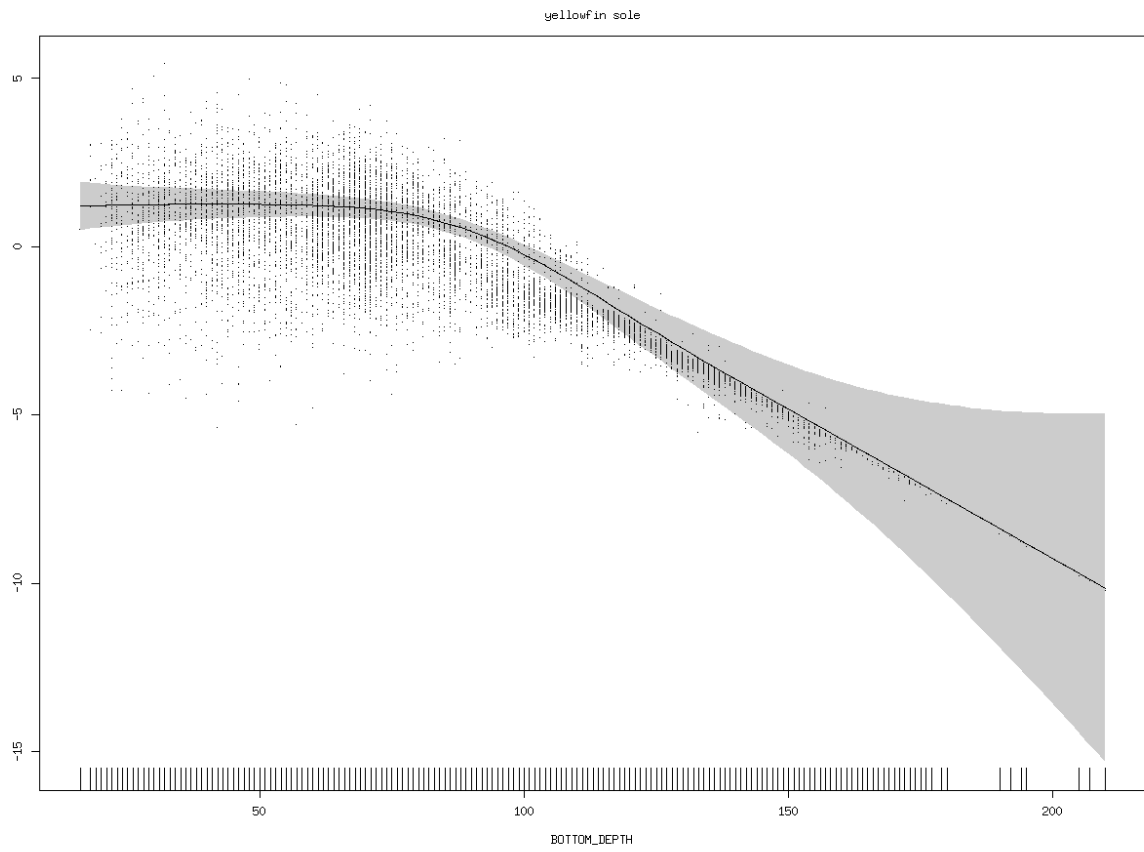


Figure 22

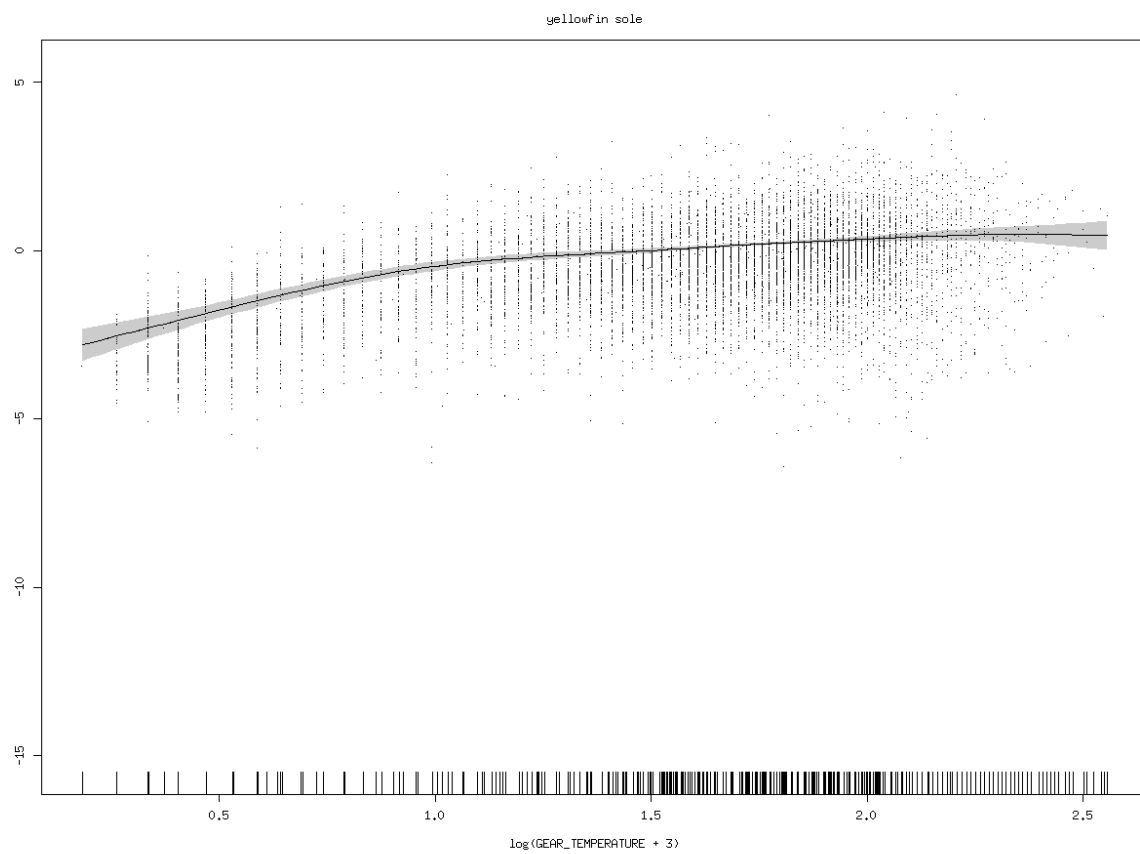


Figure 23

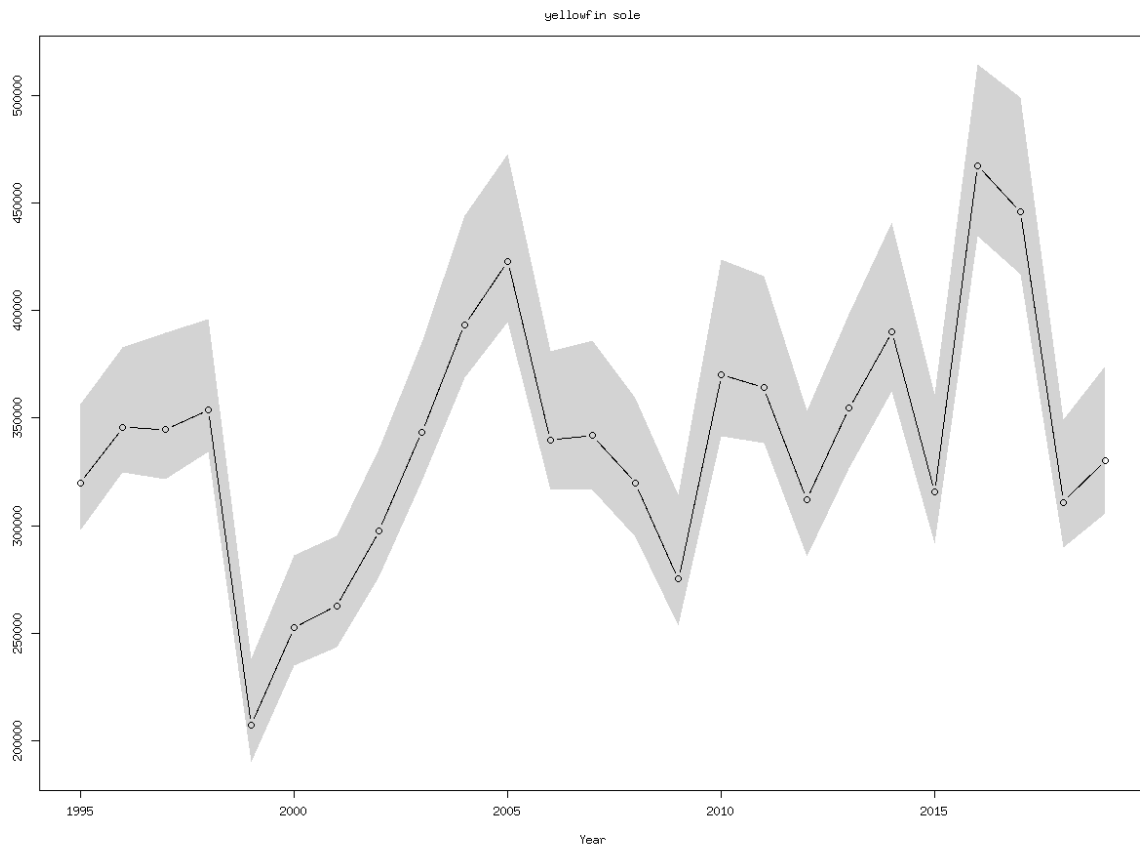


Figure 24

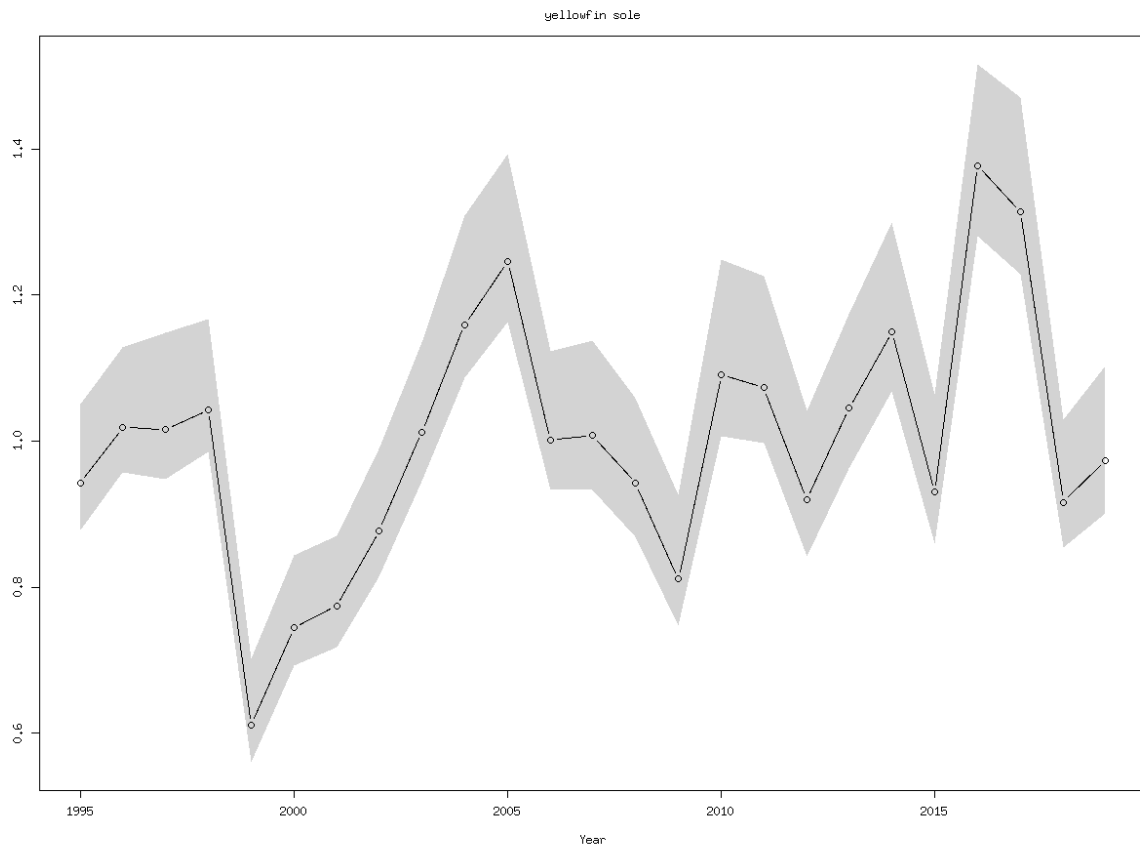


Figure 25

3 Appendix

3.1 Retrospective analyses

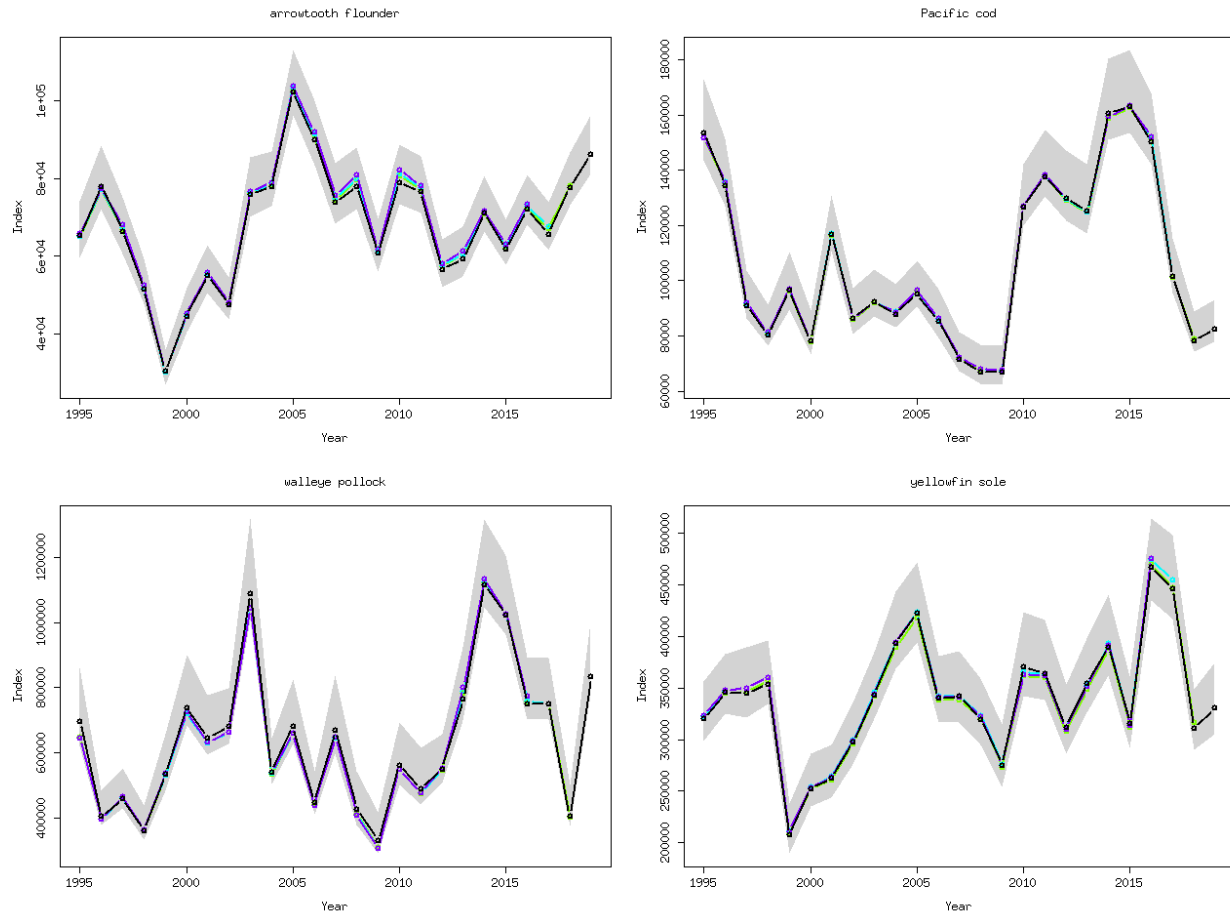


Figure 26

3.2 Simulation and re-estimation

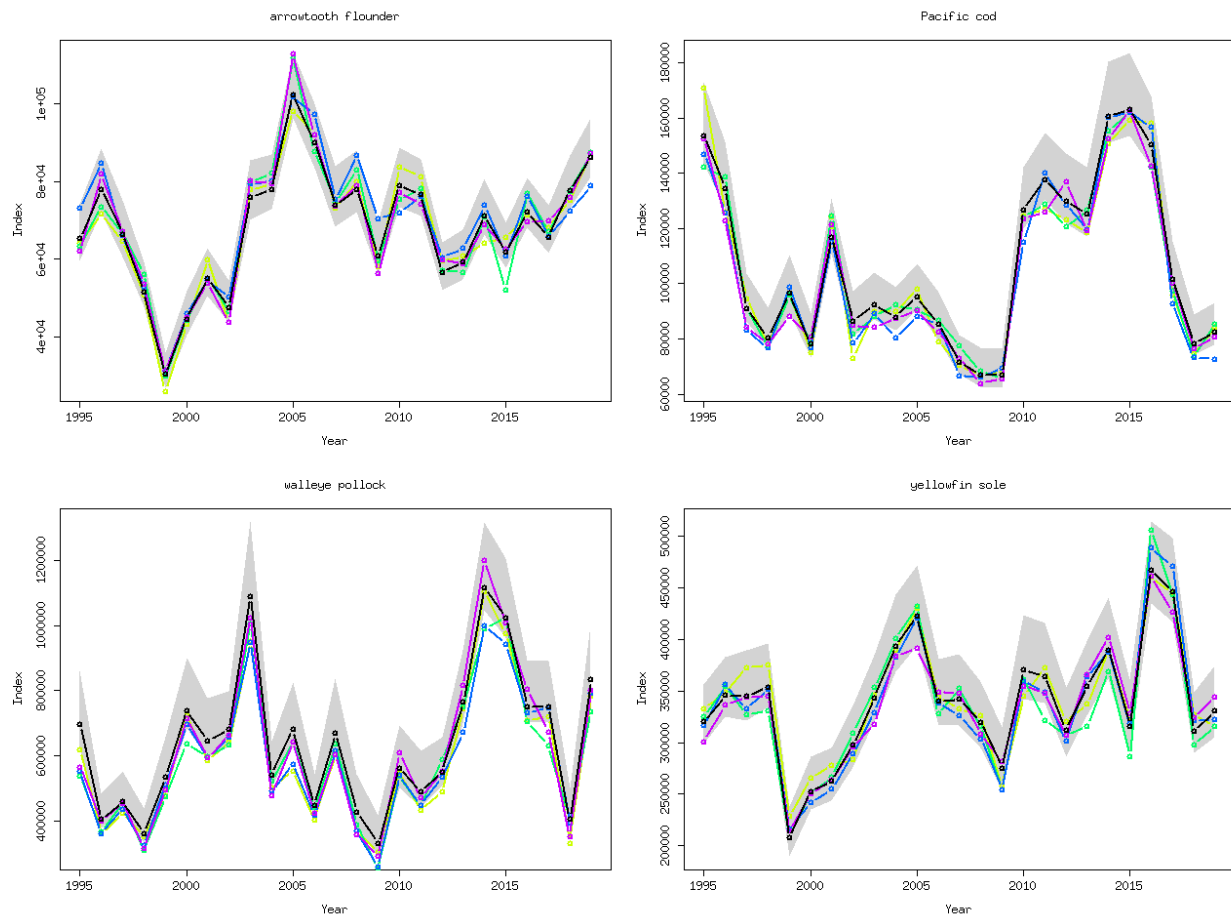


Figure 27

3.3 Model summaries

```
> lapply(models,function(x) summary(x$pModels[[1]]))
$`arrowtooth flounder`

Family: Tweedie(p=1.474)
Link function: log

Formula:
A1 ~ Year + s(sx, sy, bs = c("ts"), k = 376) + s(sx, sy, bs = c("ts"),
  k = 50, by = Year, id = 1) + s(BOTTOM_DEPTH, bs = "ts", k = 10) +
  s(log(GEAR_TEMPERATURE + 3), bs = "ts", k = 10)

Parametric coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  -4.0146     0.3386 -11.855 < 2e-16 ***
Year1996      0.2471     0.3880   0.637 0.524256
Year1997     -1.5989     0.4691  -3.409 0.000656 ***
Year1998     -0.7966     0.4161  -1.915 0.055580 .
Year1999     -2.0330     0.5815  -3.496 0.000474 ***
Year2000     -0.2848     0.4265  -0.668 0.504244
Year2001     -0.2261     0.4054  -0.558 0.576996
Year2002     -0.5920     0.4110  -1.440 0.149831
Year2003      1.3209     0.3659   3.611 0.000307 ***
Year2004      1.5948     0.3655   4.364 1.29e-05 ***
Year2005      2.6777     0.3538   7.569 4.13e-14 ***
Year2006      1.5239     0.4055   3.758 0.000172 ***
Year2007      1.5530     0.4033   3.851 0.000119 ***
Year2008      2.5197     0.4013   6.279 3.58e-10 ***
Year2009      1.0640     0.4341   2.451 0.014273 *
Year2010      1.8781     0.3967   4.734 2.23e-06 ***
Year2011      1.7768     0.3712   4.787 1.72e-06 ***
Year2012      2.3444     0.4127   5.681 1.39e-08 ***
Year2013      1.8036     0.3931   4.589 4.52e-06 ***
Year2014      1.5352     0.3701   4.148 3.38e-05 ***
Year2015      1.4205     0.3765   3.773 0.000162 ***
Year2016      3.0735     0.3508   8.762 < 2e-16 ***
Year2017      2.5873     0.3556   7.276 3.74e-13 ***
Year2018      3.0920     0.3487   8.866 < 2e-16 ***
Year2019      2.7424     0.3534   7.761 9.39e-15 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Approximate significance of smooth terms:
              edf Ref.df      F p-value
s(sx,sy)      194.795   375  4.206 < 2e-16 ***
s(sx,sy):Year1995  15.573    49  1.449 < 2e-16 ***
s(sx,sy):Year1996  19.342    49  1.239 1.88e-13 ***
s(sx,sy):Year1997  15.962    49  1.501 < 2e-16 ***
s(sx,sy):Year1998  17.535    49  0.979 3.96e-10 ***
s(sx,sy):Year1999  12.658    49  1.785 < 2e-16 ***
s(sx,sy):Year2000  16.365    49  0.902 2.21e-09 ***
s(sx,sy):Year2001  17.836    49  0.709 5.14e-06 ***
s(sx,sy):Year2002  17.522    49  0.511 0.00176 **
s(sx,sy):Year2003  21.909    49  0.786 8.79e-06 ***
s(sx,sy):Year2004  21.552    49  0.957 3.09e-08 ***
s(sx,sy):Year2005  23.744    49  1.950 < 2e-16 ***
s(sx,sy):Year2006  18.840    49  1.041 1.50e-10 ***
s(sx,sy):Year2007  18.090    49  0.799 2.92e-07 ***
s(sx,sy):Year2008  18.411    49  0.902 1.24e-08 ***
s(sx,sy):Year2009  16.236    49  1.145 1.57e-13 ***
s(sx,sy):Year2010  18.434    49  1.153 1.37e-12 ***
s(sx,sy):Year2011  20.460    49  0.554 0.00252 **
s(sx,sy):Year2012  16.836    49  0.875 6.88e-09 ***
```

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s(sx,sy):Year2013      17.966      49    0.847 5.33e-08 ***
s(sx,sy):Year2014      20.851      49    1.399 2.82e-15 ***
s(sx,sy):Year2015      20.053      49    0.754 6.58e-06 ***
s(sx,sy):Year2016      24.497      49    3.210 < 2e-16 ***
s(sx,sy):Year2017      21.559      49    2.367 < 2e-16 ***
s(sx,sy):Year2018      25.314      49    4.519 < 2e-16 ***
s(sx,sy):Year2019      24.513      49    4.236 < 2e-16 ***
s(BOTTOM_DEPTH)        6.100        9    10.575 < 2e-16 ***
s(log(GEAR_TEMPERATURE + 3)) 6.034      9   131.639 < 2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

R-sq.(adj) = 0.667   Deviance explained = 90.1%
-ML = 17536   Scale est. = 1.5924    n = 9384

$'Pacific cod'

Family: Tweedie(p=1.679)
Link function: log

Formula:
A1 ~ Year + s(sx, sy, bs = c("ts"), k = 376) + s(sx, sy, bs = c("ts"),
  k = 50, by = Year, id = 1) + s(BOTTOM_DEPTH, bs = "ts", k = 10) +
  s(log(GEAR_TEMPERATURE + 3), bs = "ts", k = 10)

Parametric coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  2.64496    0.05085  52.019 < 2e-16 ***
Year1996     -0.45197    0.07271  -6.216 5.33e-10 ***
Year1997     -0.64965    0.06821  -9.524 < 2e-16 ***
Year1998     -0.92022    0.07296 -12.613 < 2e-16 ***
Year1999     -0.21910    0.07109  -3.082 0.00206 **
Year2000     -0.74665    0.06761 -11.044 < 2e-16 ***
Year2001     -0.41667    0.06684  -6.234 4.78e-10 ***
Year2002     -0.92248    0.07273 -12.684 < 2e-16 ***
Year2003     -0.97593    0.07925 -12.315 < 2e-16 ***
Year2004     -0.84616    0.07388 -11.453 < 2e-16 ***
Year2005     -0.74524    0.07479  -9.965 < 2e-16 ***
Year2006     -0.49470    0.06749  -7.330 2.51e-13 ***
Year2007     -0.55840    0.06654  -8.392 < 2e-16 ***
Year2008     -0.41801    0.06782  -6.164 7.43e-10 ***
Year2009     -0.56906    0.06913  -8.232 < 2e-16 ***
Year2010     -0.06746    0.06561  -1.028 0.30387
Year2011     -0.23320    0.06534  -3.569 0.00036 ***
Year2012      0.18523    0.06686   2.770 0.00561 **
Year2013     -0.03940    0.06530  -0.603 0.54622
Year2014     -0.21130    0.06957  -3.037 0.00239 **
Year2015     -0.33181    0.07283  -4.556 5.29e-06 ***
Year2016     -0.24466    0.08434  -2.901 0.00373 **
Year2017     -0.49622    0.06820  -7.276 3.76e-13 ***
Year2018     -1.09104    0.08513 -12.816 < 2e-16 ***
Year2019     -0.93164    0.08677 -10.737 < 2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Approximate significance of smooth terms:
              edf Ref.df      F p-value
s(sx,sy)      260.1556   375   4.403 < 2e-16 ***
s(sx,sy):Year1995  26.3557    49   2.908 < 2e-16 ***
s(sx,sy):Year1996  27.0969    49   1.040 2.85e-07 ***
s(sx,sy):Year1997  26.0467    49   0.976 9.08e-07 ***
s(sx,sy):Year1998  26.0935    49   1.404 7.87e-13 ***
s(sx,sy):Year1999  24.4457    49   4.373 < 2e-16 ***
s(sx,sy):Year2000  25.3893    49   1.983 < 2e-16 ***
s(sx,sy):Year2001  26.6074    49   1.617 7.65e-16 ***

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s(sx,sy):Year2002      25.8847      49      1.377 1.67e-12 ***
s(sx,sy):Year2003      26.0720      49      1.465 9.40e-14 ***
s(sx,sy):Year2004      25.9032      49      0.873 1.71e-05 ***
s(sx,sy):Year2005      26.1291      49      0.784 0.000233 ***
s(sx,sy):Year2006      24.9854      49      1.328 3.56e-12 ***
s(sx,sy):Year2007      25.0859      49      1.255 4.83e-11 ***
s(sx,sy):Year2008      24.7428      49      1.882 < 2e-16 ***
s(sx,sy):Year2009      24.3875      49      2.472 < 2e-16 ***
s(sx,sy):Year2010      25.8600      49      3.870 < 2e-16 ***
s(sx,sy):Year2011      27.0687      49      1.756 < 2e-16 ***
s(sx,sy):Year2012      26.0366      49      2.462 < 2e-16 ***
s(sx,sy):Year2013      26.3077      49      2.119 < 2e-16 ***
s(sx,sy):Year2014      27.4053      49      3.369 < 2e-16 ***
s(sx,sy):Year2015      26.9707      49      3.292 < 2e-16 ***
s(sx,sy):Year2016      27.3574      49      1.262 3.06e-10 ***
s(sx,sy):Year2017      26.3894      49      1.251 1.90e-10 ***
s(sx,sy):Year2018      26.0931      49      2.039 < 2e-16 ***
s(sx,sy):Year2019      26.0659      49      0.952 1.88e-06 ***
s(BOTTOM_DEPTH)        0.2803        9      0.042 0.093818 .
s(log(GEAR_TEMPERATURE + 3)) 8.7453      9 148.403 < 2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

R-sq.(adj) =  0.299   Deviance explained = 59.2%
-ML = 32074   Scale est. = 1.4565      n = 9384

$'walleye pollock'

Family: Tweedie(p=1.802)
Link function: log

Formula:
A1 ~ Year + s(sx, sy, bs = c("ts"), k = 376) + s(sx, sy, bs = c("ts"),
  k = 50, by = Year, id = 1) + s(BOTTOM_DEPTH, bs = "ts", k = 10) +
  s(log(GEAR_TEMPERATURE + 3), bs = "ts", k = 10)

Parametric coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  3.47867    0.06542  53.175 < 2e-16 ***
Year1996     -0.28839    0.09711  -2.970 0.00299 **
Year1997     -0.19221    0.08711  -2.207 0.02737 *
Year1998     -0.45103    0.09534  -4.731 2.28e-06 ***
Year1999     -0.09562    0.08636  -1.107 0.26825
Year2000      0.18236    0.08234   2.215 0.02680 *
Year2001      0.08372    0.08553   0.979 0.32770
Year2002      0.05806    0.09257   0.627 0.53052
Year2003      0.43904    0.10272   4.274 1.94e-05 ***
Year2004      0.02975    0.09488   0.314 0.75390
Year2005     -0.02600    0.09807  -0.265 0.79095
Year2006     -0.46343    0.08408 -5.512 3.66e-08 ***
Year2007     -0.78046    0.08553 -9.125 < 2e-16 ***
Year2008     -1.09437    0.08804 -12.431 < 2e-16 ***
Year2009     -1.61948    0.09042 -17.910 < 2e-16 ***
Year2010     -0.75648    0.08544 -8.854 < 2e-16 ***
Year2011     -0.59394    0.08698 -6.829 9.17e-12 ***
Year2012      0.05184    0.08387   0.618 0.53655
Year2013     -0.02041    0.08230  -0.248 0.80413
Year2014      0.70548    0.09001   7.838 5.14e-15 ***
Year2015      0.98858    0.09277  10.656 < 2e-16 ***
Year2016      0.63022    0.11423   5.517 3.55e-08 ***
Year2017      0.62097    0.08502   7.304 3.06e-13 ***
Year2018     -0.11777    0.11305  -1.042 0.29757
Year2019      0.35637    0.11572   3.080 0.00208 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Approximate significance of smooth terms:

	edf	Ref.df	F	p-value
s(sx,sy)	251.260	375	4.358	< 2e-16 ***
s(sx,sy):Year1995	32.517	49	3.905	< 2e-16 ***
s(sx,sy):Year1996	32.674	49	1.812	6.65e-16 ***
s(sx,sy):Year1997	32.776	49	1.516	9.70e-12 ***
s(sx,sy):Year1998	32.655	49	2.227	< 2e-16 ***
s(sx,sy):Year1999	32.037	49	2.176	< 2e-16 ***
s(sx,sy):Year2000	33.250	49	2.001	< 2e-16 ***
s(sx,sy):Year2001	33.296	49	2.611	< 2e-16 ***
s(sx,sy):Year2002	33.181	49	2.665	< 2e-16 ***
s(sx,sy):Year2003	33.807	49	2.657	< 2e-16 ***
s(sx,sy):Year2004	33.123	49	1.859	2.23e-16 ***
s(sx,sy):Year2005	32.933	49	1.377	7.83e-10 ***
s(sx,sy):Year2006	31.841	49	1.725	5.27e-15 ***
s(sx,sy):Year2007	31.532	49	2.021	< 2e-16 ***
s(sx,sy):Year2008	30.801	49	2.609	< 2e-16 ***
s(sx,sy):Year2009	30.090	49	2.946	< 2e-16 ***
s(sx,sy):Year2010	31.436	49	2.123	< 2e-16 ***
s(sx,sy):Year2011	32.249	49	1.404	2.04e-10 ***
s(sx,sy):Year2012	32.333	49	3.010	< 2e-16 ***
s(sx,sy):Year2013	32.479	49	2.733	< 2e-16 ***
s(sx,sy):Year2014	33.948	49	1.632	6.60e-13 ***
s(sx,sy):Year2015	34.295	49	3.020	< 2e-16 ***
s(sx,sy):Year2016	33.828	49	3.296	< 2e-16 ***
s(sx,sy):Year2017	33.956	49	3.638	< 2e-16 ***
s(sx,sy):Year2018	33.119	49	3.755	< 2e-16 ***
s(sx,sy):Year2019	33.487	49	2.933	< 2e-16 ***
s(BOTTOM_DEPTH)	7.031	9	12.969	< 2e-16 ***
s(log(GEAR_TEMPERATURE + 3))	8.570	9	53.074	< 2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

R-sq.(adj) = 0.218 Deviance explained = 64.9%

-ML = 43891 Scale est. = 2.2291 n = 9384

\$'yellowfin sole'

Family: Tweedie(p=1.596)

Link function: log

Formula:

A1 ~ Year + s(sx, sy, bs = c("ts"), k = 376) + s(sx, sy, bs = c("ts"),
k = 50, by = Year, id = 1) + s(BOTTOM_DEPTH, bs = "ts", k = 10) +
s(log(GEAR_TEMPERATURE + 3), bs = "ts", k = 10)

Parametric coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-0.3295	0.1575	-2.092	0.036461 *
Year1996	-0.2647	0.2135	-1.239	0.215220
Year1997	0.1852	0.1953	0.948	0.342987
Year1998	1.6461	0.1696	9.704	< 2e-16 ***
Year1999	0.7492	0.1787	4.191	2.80e-05 ***
Year2000	-0.2490	0.2021	-1.232	0.218000
Year2001	-0.3313	0.2056	-1.611	0.107114
Year2002	-0.7905	0.2128	-3.715	0.000205 ***
Year2003	-1.0058	0.2221	-4.528	6.03e-06 ***
Year2004	-0.2179	0.2044	-1.066	0.286448
Year2005	-0.1188	0.2046	-0.580	0.561720
Year2006	-0.1089	0.2065	-0.527	0.598098
Year2007	-0.3555	0.2141	-1.660	0.096910 .
Year2008	0.1417	0.1981	0.715	0.474494
Year2009	-0.6346	0.2163	-2.934	0.003359 **
Year2010	-0.9092	0.2334	-3.895	9.89e-05 ***

Year2011	-1.3411	0.2345	-5.718	1.11e-08	***
Year2012	-0.0310	0.2047	-0.151	0.879661	
Year2013	-0.3022	0.2067	-1.461	0.143918	
Year2014	-1.4150	0.2524	-5.607	2.12e-08	***
Year2015	-0.9652	0.2296	-4.203	2.66e-05	***
Year2016	-0.6363	0.2329	-2.732	0.006303	**
Year2017	0.5584	0.1921	2.906	0.003665	**
Year2018	0.1317	0.2029	0.649	0.516281	
Year2019	0.5525	0.1908	2.896	0.003790	**

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Approximate significance of smooth terms:

	edf	Ref.df	F	p-value	
s(sx,sy)	256.348	375	7.077	< 2e-16	***
s(sx,sy):Year1995	21.225	49	1.211	6.94e-12	***
s(sx,sy):Year1996	21.516	49	1.566	< 2e-16	***
s(sx,sy):Year1997	22.008	49	0.675	0.000344	***
s(sx,sy):Year1998	24.360	49	4.959	< 2e-16	***
s(sx,sy):Year1999	21.511	49	1.742	< 2e-16	***
s(sx,sy):Year2000	20.918	49	0.554	0.004681	**
s(sx,sy):Year2001	21.240	49	0.751	2.57e-05	***
s(sx,sy):Year2002	20.993	49	0.871	5.31e-07	***
s(sx,sy):Year2003	21.193	49	1.448	1.47e-15	***
s(sx,sy):Year2004	22.031	49	1.047	3.97e-09	***
s(sx,sy):Year2005	22.148	49	1.066	2.30e-09	***
s(sx,sy):Year2006	21.395	49	0.441	0.065885	.
s(sx,sy):Year2007	20.980	49	0.687	0.000135	***
s(sx,sy):Year2008	21.349	49	0.904	2.42e-07	***
s(sx,sy):Year2009	20.090	49	0.995	4.11e-09	***
s(sx,sy):Year2010	20.050	49	1.783	< 2e-16	***
s(sx,sy):Year2011	20.047	49	1.306	6.95e-14	***
s(sx,sy):Year2012	20.814	49	1.317	1.02e-13	***
s(sx,sy):Year2013	20.547	49	1.280	3.03e-13	***
s(sx,sy):Year2014	20.232	49	1.157	1.89e-11	***
s(sx,sy):Year2015	20.389	49	0.983	8.21e-09	***
s(sx,sy):Year2016	21.738	49	1.038	4.24e-09	***
s(sx,sy):Year2017	22.833	49	2.001	< 2e-16	***
s(sx,sy):Year2018	22.552	49	1.241	8.72e-12	***
s(sx,sy):Year2019	22.971	49	3.786	< 2e-16	***
s(BOTTOM_DEPTH)	4.536	9	7.134	< 2e-16	***
s(log(GEAR_TEMPERATURE + 3))	5.849	9	28.026	< 2e-16	***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

R-sq.(adj) = 0.517 Deviance explained = 89.5%

-ML = 28609 Scale est. = 1.9959 n = 9384

> sink()

3.4 gam.check output

```
> lapply(models,function(x) gam.check(x$pModels[[1]]))

Method: ML   Optimizer: outer newton
full convergence after 5 iterations.
Gradient range [-0.002136276,0.00194813]
(score 17535.69 & scale 1.592435).
Hessian positive definite, eigenvalue range [1.342862,3891.959].
Model rank = 1643 / 1643

Basis dimension (k) checking results. Low p-value (k-index<1) may
indicate that k is too low, especially if edf is close to k'.

      k'    edf k-index p-value
s(sx,sy)      375.00 194.80    0.91 0.325
s(sx,sy):Year1995    49.00 15.57    0.91 0.350
s(sx,sy):Year1996    49.00 19.34    0.91 0.320
s(sx,sy):Year1997    49.00 15.96    0.91 0.350
s(sx,sy):Year1998    49.00 17.54    0.91 0.365
s(sx,sy):Year1999    49.00 12.66    0.91 0.245
s(sx,sy):Year2000    49.00 16.36    0.91 0.330
s(sx,sy):Year2001    49.00 17.84    0.91 0.325
s(sx,sy):Year2002    49.00 17.52    0.91 0.360
s(sx,sy):Year2003    49.00 21.91    0.91 0.345
s(sx,sy):Year2004    49.00 21.55    0.91 0.315
s(sx,sy):Year2005    49.00 23.74    0.91 0.335
s(sx,sy):Year2006    49.00 18.84    0.91 0.325
s(sx,sy):Year2007    49.00 18.09    0.91 0.295
s(sx,sy):Year2008    49.00 18.41    0.91 0.360
s(sx,sy):Year2009    49.00 16.24    0.91 0.390
s(sx,sy):Year2010    49.00 18.43    0.91 0.315
s(sx,sy):Year2011    49.00 20.46    0.91 0.395
s(sx,sy):Year2012    49.00 16.84    0.91 0.330
s(sx,sy):Year2013    49.00 17.97    0.91 0.355
s(sx,sy):Year2014    49.00 20.85    0.91 0.320
s(sx,sy):Year2015    49.00 20.05    0.91 0.345
s(sx,sy):Year2016    49.00 24.50    0.91 0.260
s(sx,sy):Year2017    49.00 21.56    0.91 0.380
s(sx,sy):Year2018    49.00 25.31    0.91 0.290
s(sx,sy):Year2019    49.00 24.51    0.91 0.330
s(BOTTOM_DEPTH)      9.00 6.10    0.90 0.075 .
s(log(GEAR_TEMPERATURE + 3)) 9.00 6.03    0.87 <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Method: ML   Optimizer: outer newton
full convergence after 6 iterations.
Gradient range [-0.004418967,0.002864712]
(score 32074.49 & scale 1.456504).
Hessian positive definite, eigenvalue range [0.03936054,6935.119].
Model rank = 1643 / 1643

Basis dimension (k) checking results. Low p-value (k-index<1) may
indicate that k is too low, especially if edf is close to k'.

      k'    edf k-index p-value
s(sx,sy)      375.00 260.16    0.93 0.40
s(sx,sy):Year1995    49.00 26.36    0.93 0.41
s(sx,sy):Year1996    49.00 27.10    0.93 0.43
s(sx,sy):Year1997    49.00 26.05    0.93 0.38
s(sx,sy):Year1998    49.00 26.09    0.93 0.30
s(sx,sy):Year1999    49.00 24.45    0.93 0.40
s(sx,sy):Year2000    49.00 25.39    0.93 0.38
```

s(sx,sy):Year2001	49.00	26.61	0.93	0.42
s(sx,sy):Year2002	49.00	25.89	0.93	0.47
s(sx,sy):Year2003	49.00	26.07	0.93	0.44
s(sx,sy):Year2004	49.00	25.90	0.93	0.46
s(sx,sy):Year2005	49.00	26.13	0.93	0.46
s(sx,sy):Year2006	49.00	24.98	0.93	0.41
s(sx,sy):Year2007	49.00	25.09	0.93	0.44
s(sx,sy):Year2008	49.00	24.74	0.93	0.42
s(sx,sy):Year2009	49.00	24.39	0.93	0.34
s(sx,sy):Year2010	49.00	25.86	0.93	0.42
s(sx,sy):Year2011	49.00	27.07	0.93	0.39
s(sx,sy):Year2012	49.00	26.04	0.93	0.45
s(sx,sy):Year2013	49.00	26.31	0.93	0.42
s(sx,sy):Year2014	49.00	27.41	0.93	0.42
s(sx,sy):Year2015	49.00	26.97	0.93	0.43
s(sx,sy):Year2016	49.00	27.36	0.93	0.41
s(sx,sy):Year2017	49.00	26.39	0.93	0.38
s(sx,sy):Year2018	49.00	26.09	0.93	0.43
s(sx,sy):Year2019	49.00	26.07	0.93	0.42
s(BOTTOM_DEPTH)	9.00	0.28	0.97	0.98
s(log(GEAR_TEMPERATURE + 3))	9.00	8.74	0.93	0.19

Method: ML Optimizer: outer newton
full convergence after 7 iterations.
Gradient range [-0.01721491,2.286906e-05]
(score 43890.63 & scale 2.229106).
Hessian positive definite, eigenvalue range [1.887655,7560.673].
Model rank = 1643 / 1643

Basis dimension (k) checking results. Low p-value (k-index<1) may indicate that k is too low, especially if edf is close to k'.

	k'	edf	k-index	p-value
s(sx,sy)	375.00	251.26	0.88	0.020 *
s(sx,sy):Year1995	49.00	32.52	0.88	0.025 *
s(sx,sy):Year1996	49.00	32.67	0.88	0.050 *
s(sx,sy):Year1997	49.00	32.78	0.88	0.025 *
s(sx,sy):Year1998	49.00	32.66	0.88	0.030 *
s(sx,sy):Year1999	49.00	32.04	0.88	0.020 *
s(sx,sy):Year2000	49.00	33.25	0.88	0.025 *
s(sx,sy):Year2001	49.00	33.30	0.88	0.010 **
s(sx,sy):Year2002	49.00	33.18	0.88	0.025 *
s(sx,sy):Year2003	49.00	33.81	0.88	0.010 **
s(sx,sy):Year2004	49.00	33.12	0.88	0.020 *
s(sx,sy):Year2005	49.00	32.93	0.88	0.010 **
s(sx,sy):Year2006	49.00	31.84	0.88	0.025 *
s(sx,sy):Year2007	49.00	31.53	0.88	0.020 *
s(sx,sy):Year2008	49.00	30.80	0.88	0.030 *
s(sx,sy):Year2009	49.00	30.09	0.88	0.010 **
s(sx,sy):Year2010	49.00	31.44	0.88	0.030 *
s(sx,sy):Year2011	49.00	32.25	0.88	0.035 *
s(sx,sy):Year2012	49.00	32.33	0.88	0.025 *
s(sx,sy):Year2013	49.00	32.48	0.88	0.025 *
s(sx,sy):Year2014	49.00	33.95	0.88	<2e-16 ***
s(sx,sy):Year2015	49.00	34.30	0.88	0.010 **
s(sx,sy):Year2016	49.00	33.83	0.88	0.005 **
s(sx,sy):Year2017	49.00	33.96	0.88	0.020 *
s(sx,sy):Year2018	49.00	33.12	0.88	0.025 *
s(sx,sy):Year2019	49.00	33.49	0.88	0.010 **
s(BOTTOM_DEPTH)	9.00	7.03	0.91	0.645
s(log(GEAR_TEMPERATURE + 3))	9.00	8.57	0.91	0.745

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Method: ML Optimizer: outer newton

```

full convergence after 8 iterations.
Gradient range [-0.0002554647,0.0001669659]
(score 28608.91 & scale 1.995875).
Hessian positive definite, eigenvalue range [1.817765,5950.313].
Model rank = 1643 / 1643

```

Basis dimension (k) checking results. Low p-value (k-index<1) may indicate that k is too low, especially if edf is close to k'.

	k'	edf	k-index	p-value
s(sx,sy)	375.00	256.35	0.91	0.115
s(sx,sy):Year1995	49.00	21.22	0.91	0.145
s(sx,sy):Year1996	49.00	21.52	0.91	0.130
s(sx,sy):Year1997	49.00	22.01	0.91	0.160
s(sx,sy):Year1998	49.00	24.36	0.91	0.135
s(sx,sy):Year1999	49.00	21.51	0.91	0.115
s(sx,sy):Year2000	49.00	20.92	0.91	0.115
s(sx,sy):Year2001	49.00	21.24	0.91	0.155
s(sx,sy):Year2002	49.00	20.99	0.91	0.105
s(sx,sy):Year2003	49.00	21.19	0.91	0.160
s(sx,sy):Year2004	49.00	22.03	0.91	0.135
s(sx,sy):Year2005	49.00	22.15	0.91	0.140
s(sx,sy):Year2006	49.00	21.40	0.91	0.170
s(sx,sy):Year2007	49.00	20.98	0.91	0.175
s(sx,sy):Year2008	49.00	21.35	0.91	0.130
s(sx,sy):Year2009	49.00	20.09	0.91	0.130
s(sx,sy):Year2010	49.00	20.05	0.91	0.120
s(sx,sy):Year2011	49.00	20.05	0.91	0.135
s(sx,sy):Year2012	49.00	20.81	0.91	0.145
s(sx,sy):Year2013	49.00	20.55	0.91	0.100 .
s(sx,sy):Year2014	49.00	20.23	0.91	0.160
s(sx,sy):Year2015	49.00	20.39	0.91	0.165
s(sx,sy):Year2016	49.00	21.74	0.91	0.095 .
s(sx,sy):Year2017	49.00	22.83	0.91	0.165
s(sx,sy):Year2018	49.00	22.55	0.91	0.145
s(sx,sy):Year2019	49.00	22.97	0.91	0.150
s(BOTTOM_DEPTH)	9.00	4.54	0.92	0.325
s(log(GEAR_TEMPERATURE + 3))	9.00	5.85	0.93	0.695

```

---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

$'arrowtooth flounder'
$'arrowtooth flounder'$mfrow
[1] 2 2

```

```

$'Pacific cod'
$'Pacific cod'$mfrow
[1] 2 2

```

```

$'walleye pollock'
$'walleye pollock'$mfrow
[1] 2 2

```

```

$'yellowfin sole'
$'yellowfin sole'$mfrow
[1] 2 2

```

```

> sink()

```

References

- [1] Casper W. Berg. `surveyIndex`: R package for calculating survey indices by age from DATRAS exchange data. <https://github.com/casperwberg/surveyIndex>, 2014.
- [2] Casper W Berg, Anders Nielsen, and Kasper Kristensen. Evaluation of alternative age-based methods for estimating relative abundance from survey data in relation to assessment models. *Fisheries Research*, 151:91–99, 2014.