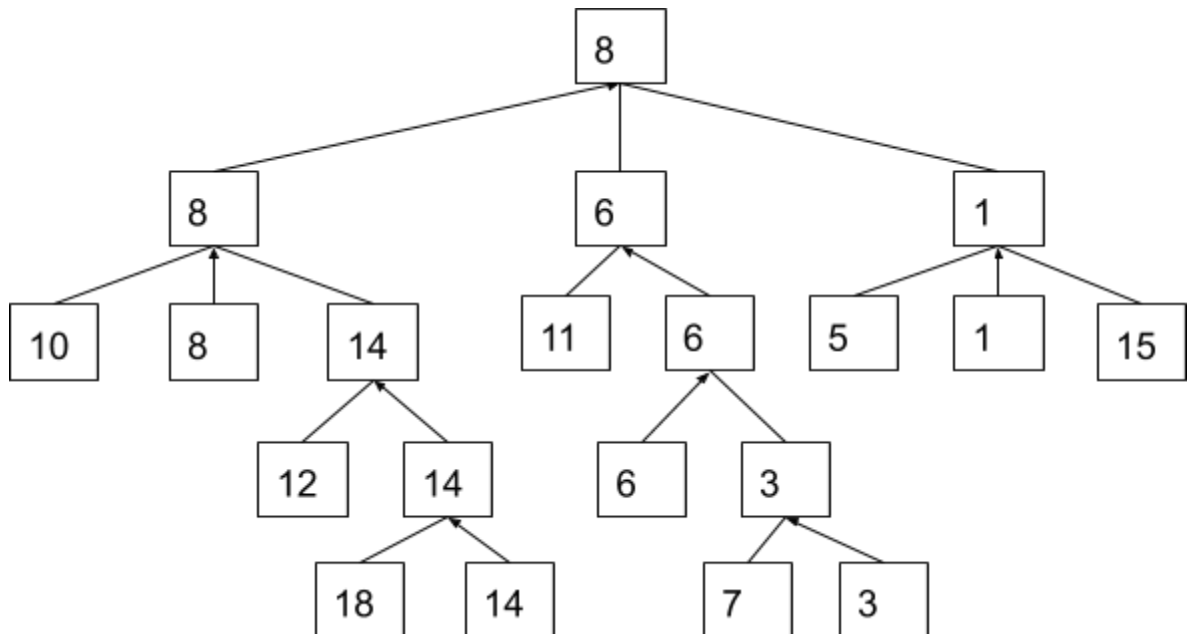


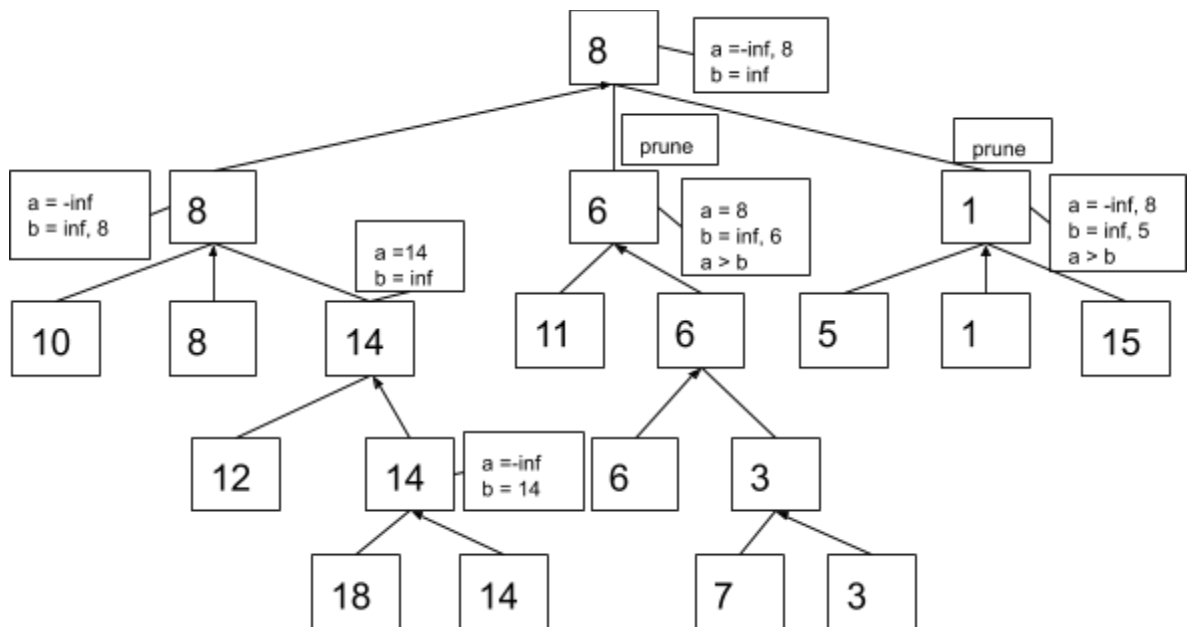
### Homework 3

1.



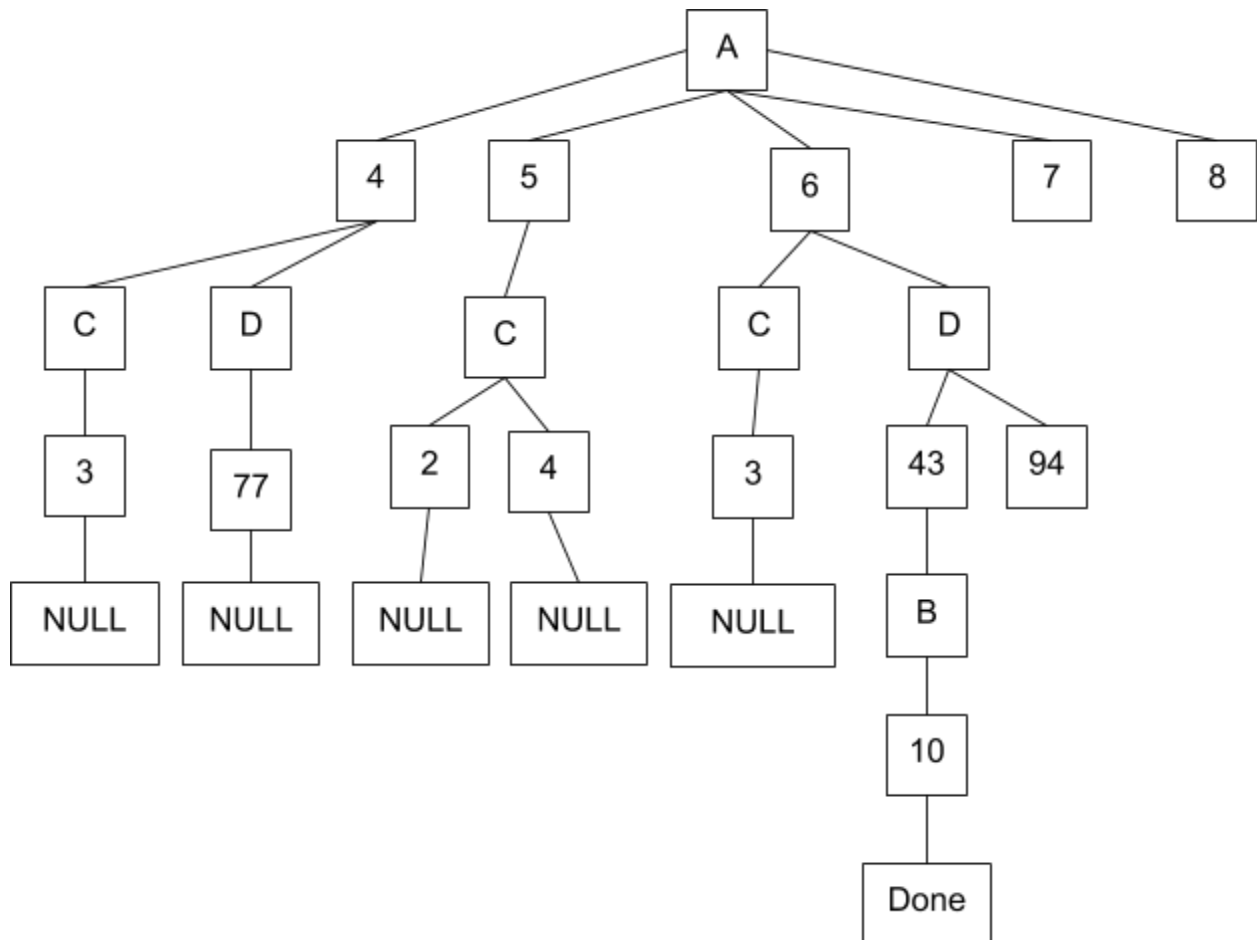
The maximum utility is that max can achieve is 8 with min playing optimally.

2.



3.

|                               | A = 4 | C = 3 | D = 77 | A = 5  | C = 2 | C = 4 | A = 6    | C = 3    | D = 43 | B = 10 |
|-------------------------------|-------|-------|--------|--------|-------|-------|----------|----------|--------|--------|
| A = [4, 5, 6, 7, 8]           | 4     | 4     | 4      | 5      | 5     | 5     | 6        | 6        | 6      | 6      |
| B = [10, 20, 30, 40]          |       |       | NULL   |        |       |       | 10       |          | 10     | 10     |
| C = [2, 3, 4]                 | 3     | 3     | 3      | [2, 4] | 2     | 4     | 3        | 3        | 3      | 3      |
| D = [28, 43, 56, 77, 94, 114] | 77    | 77    | 77     | NULL   |       |       | [43, 94] | [43, 94] | 43     | 43     |



We backtrack whenever we hit a NULL value. We arrive at a solution when A = 6, B = 10, C = 3, and D = 43. Those assignments satisfy the 3 constraints.

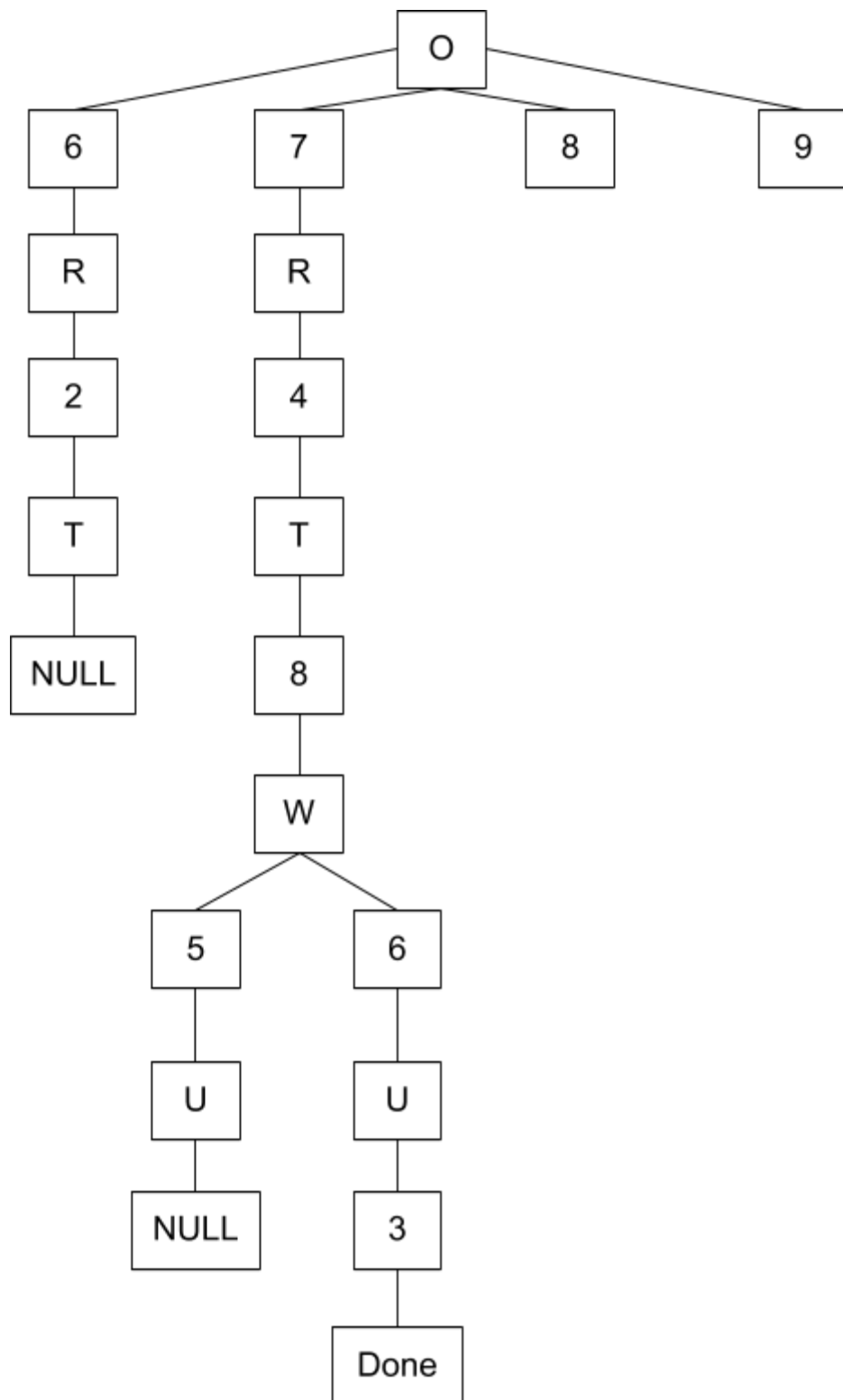
$$A + C = \text{Odd. } 6 + 3 = 9$$

$$A + D = \text{a square of an Integer. } 6 + 43 = 49$$

$$B + D < 60. \quad 10 + 43 = 53 < 60$$

4.

|  | O = 6                    | O = 7                 | T = 7                 | R = 4                 | W = 5 | W = 6 | U = 3 |
|--|--------------------------|-----------------------|-----------------------|-----------------------|-------|-------|-------|
| T =<br>[5,<br>6, 7,<br>8, 9]                   | NULL                     | 8                     | 8                     | 8                     | 8     | 8     | 8     |
| W =<br>[5,<br>6, 7,<br>8, 9]                   | [5, 7, 8, 9]             | [5, 6, 9]             | [5, 6, 9]             | [5, 6, 9]             | 5     | 6     | 6     |
| O =<br>[6,<br>7, 8,<br>9]                      | 6                        | 7                     | 7                     | 7                     | 7     | 7     | 7     |
| U =<br>[0,<br>2, 3,<br>4, 5,<br>6, 7,<br>8, 9] | [0, 3, 4, 5,<br>7, 8, 9] | [0, 2, 3, 5, 6,<br>9] | [0, 2, 3, 5, 6,<br>9] | [0, 2, 3, 5,<br>6, 9] | NULL  | 3     | 3     |
| R =<br>[0,<br>2, 3,<br>4, 5,<br>6, 7,<br>8, 9] | 2                        | 4                     | 4                     | 4                     | 4     | 4     | 4     |



When  $O = 7$ ,  $R = 4$ ,  $T = 8$ ,  $W = 6$ , and  $U = 3$  all conditions are satisfied and each letter is distinct.

$$O + O = 10 + R. \quad 7 + 7 = 10 + 4 = 14$$

$$W + W = 10 + U. \quad 6 + 6 + 1 = 10 + 3 = 13$$

$$T + T + 1 = 10 + O. \quad 8 + 8 + 1 = 10 + 7 = 17$$

As well as:

$$TWO + TWO = FOUR \quad = \quad 867 + 867 = 1734$$

is True.