CSC 440 Assignment 5: Dynamic Programming - Seam Carving

Out: Tuesday, April 5th

Due: Monday, Apr 11th, by 11:59PM

Introduction

In a 2007 paper, Avidan and Shamir describe a new method for resizing images with minimal visual disruption. The breakthrough is an algorithm for removing the lowest *energy* vertical or horizontal seam in the image.

Both the demonstration video and original paper will be posted to EdStem. Please watch the video so that the terminology used here is clear.

You are given an image, and your task is to calculate the best vertical seam to remove. A vertical seam is a connected path of pixels, with one pixel per row of the image. Two pixels are *connected* if they are vertically or diagonally adjacent. The best vertical seam is the one that minimizes the total *energy* of pixels in the seam.

Remember, it is a convention in most computer graphics systems that (0,0) is the upper-left pixel.

Naive algorithm

How might we compute the lowest-energy seam? Simply compute all seams and choose the minimum.

You will need to implement a naive algorithm for benchmarking purposes, so think about this: for every pixel in the top row, how would you enumerate all seams starting from it? If you then built up a collection of (seam, energy) tuples, you could easily choose the one with the smallest energy.

Please think about this approach before moving on

Dynamic Programming algorithm

Here is the algorithm from the paper:

Subproblems

For each pixel (i, j), what is the lower-energy seam that starts at the top row of the image, but ends at (i, j)? image, but ends at (i, j)?

Relation

```
Let dp[i,j] be the solution to subproblem (i,j). Then dp[i,j] = min(dp[i,j-1], dp[i-1,j-1], dp[i+1,j-1]) + energy(i,j)
```

Assignment components

Implementation

Download a5.zip from EdStem and unzip it (please do not use your decompressor from assignment 4!)

You will need to install the Python Pillow library. You should be able to install it with:

```
pip install Pillow
or
  pip3 install Pillow
or
  easy_install Pillow
```

or download https://pypi.python.org/pypi/Pillow and from inside the archive run:

```
python setup.py install
```

In resizable_image.py, implement a function best_seam(self, dp=True) that returns a list of coordinates corresponding to the lowest-energy vertical seam to remove, e.g. [(5, 0), (5, 1), (4, 2), (5, 3), (6, 4)].

The class ResizeableImage inherits from ImageMatrix. You should use the following components of ImageMatrix in your program:

- self.energy(i,j) returns the energy of a pixel. This takes O(1) time, but the constant factor is large. If you call energy more than once on the same pixel, you should cache the result. This memoization is separate from the dynamic programming memoization (there are no subproblems involved) and so you should still cache the energy for a pixel even if dp == False.
- self.width and self.height are the width and height of the image.

Your implementation may be either bottom-up or top-down. But either way, it must respect the argument dp, which indicates whether or not dynamic programming should be used. If dp == True, then you should either use memoization or store the subproblem values in a table for re-use. If dp == False, then you should use a completely naive solution, probably recursive, that computes all possible seams independently.

- test your code using test_resizable_image.py, and submit resizable_image.py via Gradescope.
- you can also view your code working by running gui.py
- you should try out your code on other images of your choosing, once it's working

Since the default behavior of best_seam() is to perform dynamic programming, the test suite provided will only test that variant.

However, for small inputs, turning off dynamic programming should be possible.

You do not need to document any invariants for this assignment. However, you will still be graded on the design and representation of your code.

Benchmarking

On a variety of image files, time your code (just like with Assignment 1) both with and without dynamic programming. The sizes of inputs for the naive algorithm will by necessity be much smaller than for dynamic programming. Anything that runs without DP will be too fast to meaningfully time with DP. Conversely, anything worth timing with DP will be intractable without DP. Instead, you should aim for a range of inputs whose times range from a few seconds to a few minutes. You should test on enough inputs to be able to make convincing plots of running time. Clearly, there will be inputs on which only the dynamic programming solution is tractable, so I expect your naive plot will cover fewer data points. Think about what it means to vary the image size.

One easy tool for generating images of specific sizes is pixilart.com

Plot the running times. You should upload to gradescope a PDF including your plots and the analysis below.

Analysis

Come up with an analysis of the asymptotic complexity of the algorithm, both with and without dynamic programming. Write out the recurrence relations. Pay attention to **how many** subproblems there are, and how much smaller they are. Solve the recurrence relations (you do not need to show your work for this) and provide the solutions in the comments. Finally, answer the question: do these solutions make sense given the results of the benchmarking?

For this assignment, your solution must be in Python.

We will evaluate your solutions in Python 3.6.

This is a SOLO assignment!

This is a solo assignment. You may not work with a partner! You may not show your code to any other classmate, or anyone who is not a member of the course staff (instructor or TAs). You also may not allow your code to be seen by anyone who is not a member of the course staff. Please see the syllabus section on Academic Integrity, or ask the instructor if you have any questions.

You MAY discuss conceptual issues, your understanding of the algorithm, and even choices of data structures and representations with your classmates. But you may not share code.

This is a solo assignment

Lateness

Submissions will not be accepted after the due date, except with the intervention of the Dean's Office in the case of serious medical, family, or other personal crises.

Grading Rubric

Your grade will be based on four components:

- Functional Correctness (25%)
- Benchmarking comparison (25%)
- Design and Representation (25%)
- Analysis of the algorithm (25%)

For this assignment, you do not need to specifically state any invariants. However, we still expect your code to be well-documented and well-structured.

Helpful tips

- Write the naive implementation first! Once you get the dynamic programming solution into your brain, it can be hard to "un-see" it.
- The naive solution can (probably should) be recursive.
 - It will only work for very, very small inputs. You'll see why once you solve the recurrence relations.

- Your DP solution should probably not be recursive (because Cpython does not support efficient or deep recursion).
- You will not be able to benchmark the two solutions meaningfully on the same size inputs, but you should be able to plot both with different axes.
- Be sure to benchmark over a meaningful range of input sizes, and be careful to make sure random noise isn't affecting your results.
- The benchmarking an analysis is a significant part of your grade; allow yourself time for it!
- Don't overthink the naive algorithm. My solution for the dynamic programming approach is 28 lines of code. My solution for the naive implementation is 10, and it could be shorter.