

Merton Model for pricing options:

$$\frac{\partial u}{\partial \tau} = \frac{1}{2} \sigma_s^2 s^2 \frac{\partial^2 u}{\partial s^2} + (r - \mu \xi) s \frac{\partial u}{\partial s} - (r + \mu) u + \mu \int_0^\infty u(sy, \tau) p(y) dy$$

Black-Scholes Model for pricing options:

$$\frac{\partial w}{\partial t} = rw - rx \frac{\partial w}{\partial x} - \frac{1}{2} v^2 x^2 \frac{\partial^2 w}{\partial x^2}$$

Linear Convection Diffusion Equation:

$$\frac{\partial u}{\partial t} + c \frac{\partial u}{\partial x} = \frac{1}{\text{Re}} \frac{\partial^2 u}{\partial x^2}$$

$$\vec{u}^{n+1} = f(\vec{u}^n) = \mathcal{L}(\vec{u}^n) = \text{B}\vec{u}^n$$

Viscous Burger's Equation:

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} = \nu \frac{\partial^2 u}{\partial x^2}$$

Finite Difference Scheme:

$$\frac{\partial u}{\partial x} = \frac{u_{i+1} - u_{i-1}}{2\Delta x} + \mathcal{O}(\Delta x^2)$$

$$\frac{\partial^2 u}{\partial x^2} = \frac{u_{i+1} - 2u_i + u_{i-1}}{\Delta x^2} + \mathcal{O}(\Delta x^2)$$

$$\vdots$$

$$\frac{\partial \vec{u}_i}{\partial t} = \left( \frac{1}{\text{Re}\Delta x^2} - \frac{c}{2\Delta x} \right) u_{i+1} - \frac{2}{\Delta x^2} u_i + \left( \frac{1}{\text{Re}\Delta x^2} + \frac{c}{2\Delta x} \right) u_{i-1}$$

Singular Value Decomposition:

$$\min\{\|\mathbf{X} - u \cdot v\|_F\}$$

$$A = U \Sigma V^T$$