LING 185A: Section 2

Thursday, October 9

Reminders

- Homework #1 is due at 11:59 PM on Friday, October 10.
 - Submit as a PDF on BruinLearn.
- Keep posting questions on Campuswire!

Wisdom

Writing a function? Start with a lambda: \x -> ...
 Don't know how to use x? Pattern match: case x of { ... }
 Got an f :: a -> b? And an x :: a? Apply the function: ... f x ...

These will take you far.

$\mathbf{Practice} \ \mathbf{Recursion}^{$

```
numbToInt :: Numb -> Int
numbToInt n evaluates to the nonnegative integer represented by n:
numbToInt Z ⇒* 0
numbToInt (S (S (S Z))) ⇒* 3
```

numbToInt :: Numb -> Int

```
lessThanOrEq :: Numb -> (Numb -> Bool)
```

 $lessThanOrEq \ m \ n \ evaluates \ to \ True \ if \ and \ only \ if \ numbToInt \ m \ is \ less \ than \ or \ equal \ to \ numbToInt \ n.$

lessThanOrEq (S (S Z)) (S (S (S Z))) \Longrightarrow^* True

lessThanOrEq :: Numb -> (Numb -> Bool)

```
greaterThan :: Numb -> (Numb -> Bool)
```

 $\mbox{\tt greaterThan } \mbox{\tt m } \mbox{\tt n} \mbox{\tt evaluates to } \mbox{\tt True if and only if } \mbox{\tt lessThanOrEq } \mbox{\tt m } \mbox{\tt n} \mbox{\tt evaluates to } \mbox{\tt False}.$

 $\texttt{greaterThan} \ \texttt{Eq} \ (\texttt{S} \ (\texttt{S} \ \texttt{Z})) \ (\texttt{S} \ (\texttt{S} \ \texttt{Z}))) \implies^* \texttt{False}$

greaterThan :: Numb -> (Numb -> Bool)

```
bigger :: Numb -> (Numb -> Numb)
```

bigger m n evaluates to the larger of m and n.

bigger (S (S Z)) (S Z) \Longrightarrow^* S (S Z)

bigger :: Numb -> (Numb -> Numb)

```
isSorted :: (a -> (a -> Bool)) -> ([a] -> Bool)
```

isSorted cmp 1 evaluates to True if and only if the list 1 is sorted according to the ordering cmp.

isSorted lessThanOrEq [Z, Z, S (S Z), S (S (S Z))] \Longrightarrow^* True

isSorted :: (a -> (a -> Bool)) -> ([a] -> Bool)

remove :: (a -> Bool) -> ([a] -> [a])

remove pred removes every x from its list argument such that pred $x \implies^*$ True.

remove (lessThanOrEq (S Z)) [Z, Z, S (S Z), S (S (S Z))] \Longrightarrow^* [Z, Z]

remove :: (a -> Bool) -> ([a] -> [a])

map :: (a -> b) -> ([a] -> [b])

map f applies f to every element of its list argument.

map numbToInt [Z, Z, S (S Z), S (S (S Z))] \Longrightarrow^* [0, 0, 2, 3]

(++) :: [a] -> ([a] -> [a])

 $\mathtt{x} \ +\! + \ \mathtt{y}$ evaluates to the concatenation of the lists \mathtt{x} and $\mathtt{y}.$

 $[Z, Z, S (S Z)] ++ [S Z, Z] \implies^* [Z, Z, S (S Z), S Z, Z]$