

Lossy Integrator

$$1) \quad V_{in} = V_{in} \left(\frac{R_2}{R_1 + R_2} \right) \quad R_{TH} = \frac{R_1 R_2}{R_1 + R_2}$$

$$V_o(t) = V_{TH} e^{-t/R_C} = V_{in} \left(\frac{R_2}{R_1 + R_2} \right) e^{-t/R_1 R_2 C}$$

$$V_o(t) = V_{in} \left(\frac{R_2}{R_1 + R_2} \right) e^{-\frac{t(R_1 + R_2)}{R_1 R_2 C}}$$

$$2) \quad \frac{V_o}{V_i} = \frac{-R_2/R_1}{1 + s R_2 C} \quad s=0 \quad \frac{V_o}{V_i} = \frac{-R_2}{R_1} = -22$$

$$\frac{R_1 + R_2}{R_1 R_2 C} = \frac{23k}{(22k)(220n)}$$

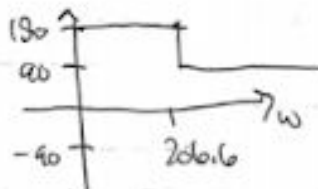
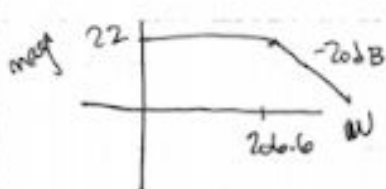
$$4.75206 kHz$$

$$R_1 = 1k\Omega$$

$$R_2 = 22k\Omega$$

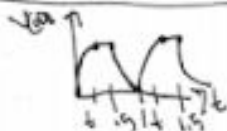
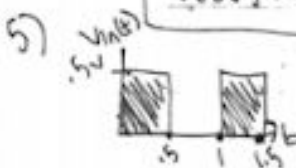
$$C = 220 nF$$

$$3) \quad 22 \left(\frac{1}{s + \frac{1}{0.00434}} \right) = 22 \left(\frac{1}{s + 206.6} \right)$$



$$4) \quad -22 \left(\frac{1}{1 + j\omega/206.6} \right) \quad V_o(t) = -22 \times 0.5 \times \left(\frac{1}{\sqrt{1 + \frac{\omega^2}{206.6^2}}} \right) \sin(2\pi 1000t - \tan^{-1} \frac{\omega}{206.6})$$

$$V_o(t) = 0.765 \sin(2\pi 1000t - 89.16^\circ)$$



⊗ Pseudo Differentiator

$$V_{TH} = V_{in}(t) \left(\frac{R_2}{R_1 + R_2} \right) \quad \tau = (R_1 + R_2)C$$

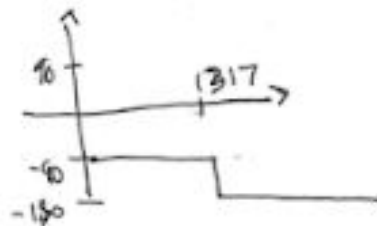
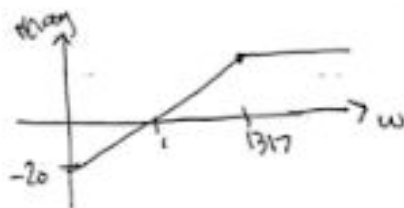
$$V_o(t) = V_{TH} e^{-t/\tau} = V_{in}(t) \left(\frac{R_2}{R_1 + R_2} \right) e^{-t/(R_1 + R_2)C}$$

$$\frac{V_o}{V_i} = -\frac{R_2}{R_1} = -22$$

$$R_1 = 1k\Omega \quad R_2 = 22k\Omega \quad C = 33nF$$

$$22 \frac{s}{s + 1/R_1C}$$

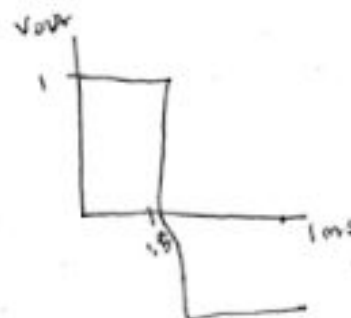
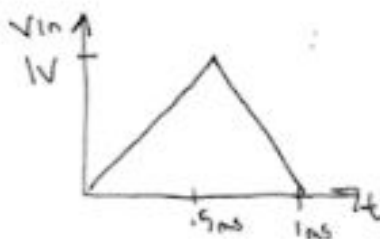
$$1317.5 \text{ Hz}$$



$$V_i(t) = 0.1 \sin(2\pi 1000t)$$

$$\frac{V_o}{V_i} = -22(1) \sqrt{\frac{2000^2}{1 + (2000)^2}} \sin\left(2000\pi + 90 - \tan^{-1}\left(\frac{1}{1317}\right)\right)$$

$$= .09 \sin(2\pi 1000 + 11.84^\circ)$$



Finite GBW Limitations

$$R_1 = 1k\Omega$$

$$23 = 1 + \frac{R_2}{R_1}$$

$$R_2 = 22k\Omega$$

$$g_{m1} = 1 + \frac{R_2}{R_1}$$

$$57 = 1 + \frac{R_2}{R_1}$$

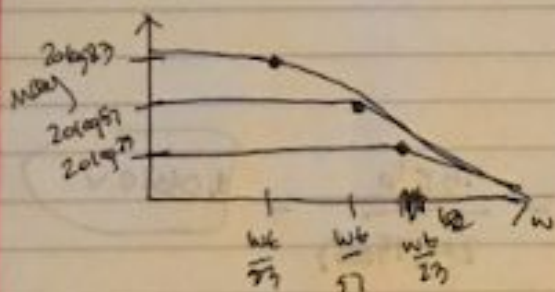
$$R_2 = 56k\Omega$$

$$82 = 1 + \frac{R_2}{R_1}$$

$$R_2 = 82k\Omega$$

$$\frac{V_o}{V_i} = G \left(\frac{1}{1 + \frac{s}{\omega_0}} \right) = \frac{G}{1 + \frac{s}{\omega_0}}$$

$$\frac{23}{1 + \frac{s}{\omega_0}} = \frac{23}{1 + \frac{23s}{\omega_0}} = \frac{23\omega_0}{\omega_0 + 23s} = \frac{23\omega_0}{s + \frac{\omega_0}{23}}$$



$$\frac{57\omega_0}{s + \frac{\omega_0}{57}}$$

$$\frac{82\omega_0}{s + \frac{\omega_0}{82}}$$

Slow Rate Limitations

$$\frac{V_o}{V_i} = 1$$



$$.5 \text{ V}/\mu\text{s} = .5 \times 10^{-6} \text{ V/s}$$

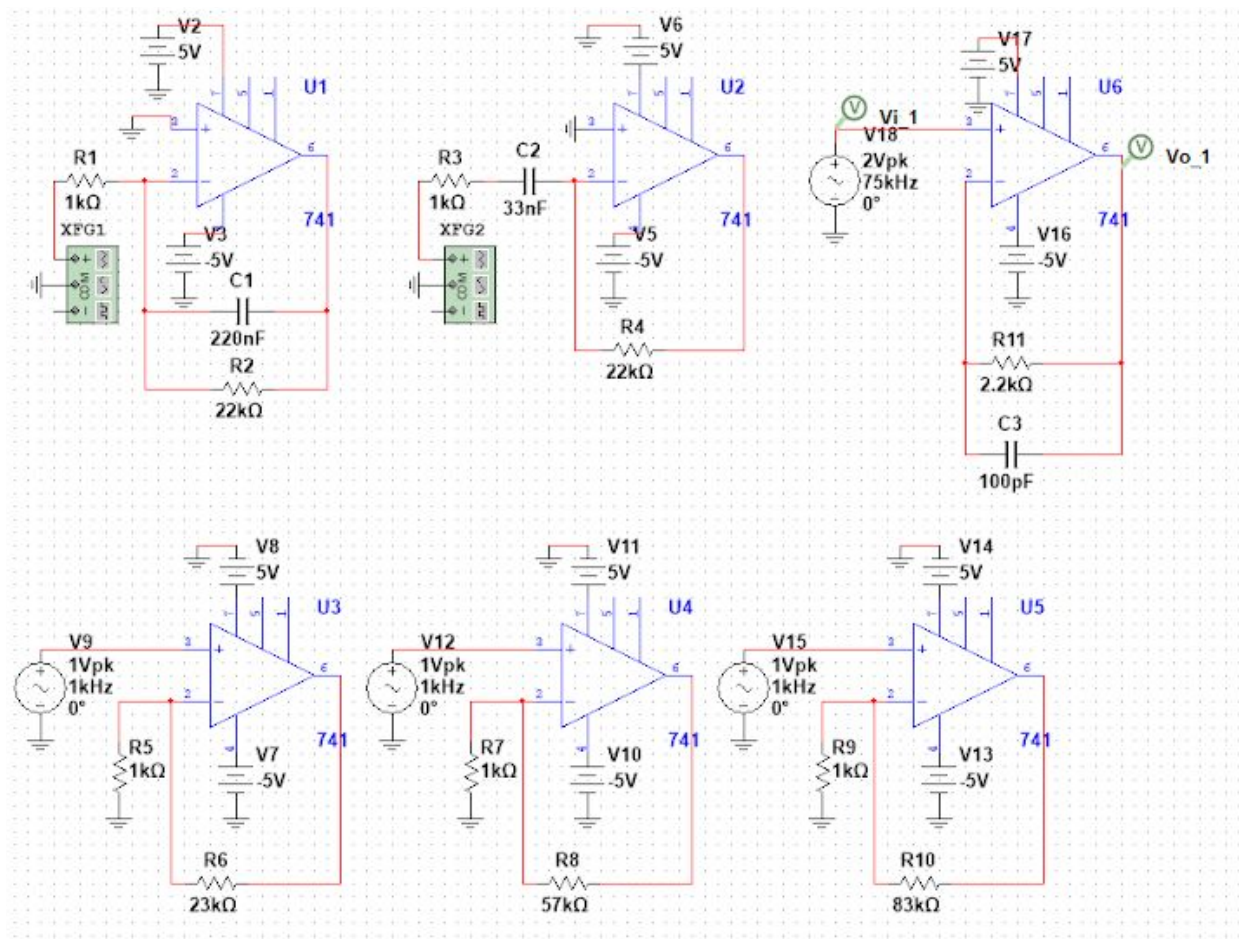
$$V_{out\max} = \sqrt{V_o^2 + V_i^2} = \sqrt{2} \text{ V}$$

$$f_{\max} = \frac{S_{\text{rate}}}{2\pi V_{out\max}} = \frac{.5 \times 10^{-6}}{2\pi \sqrt{2}} = 56269.76 \text{ Hz}$$

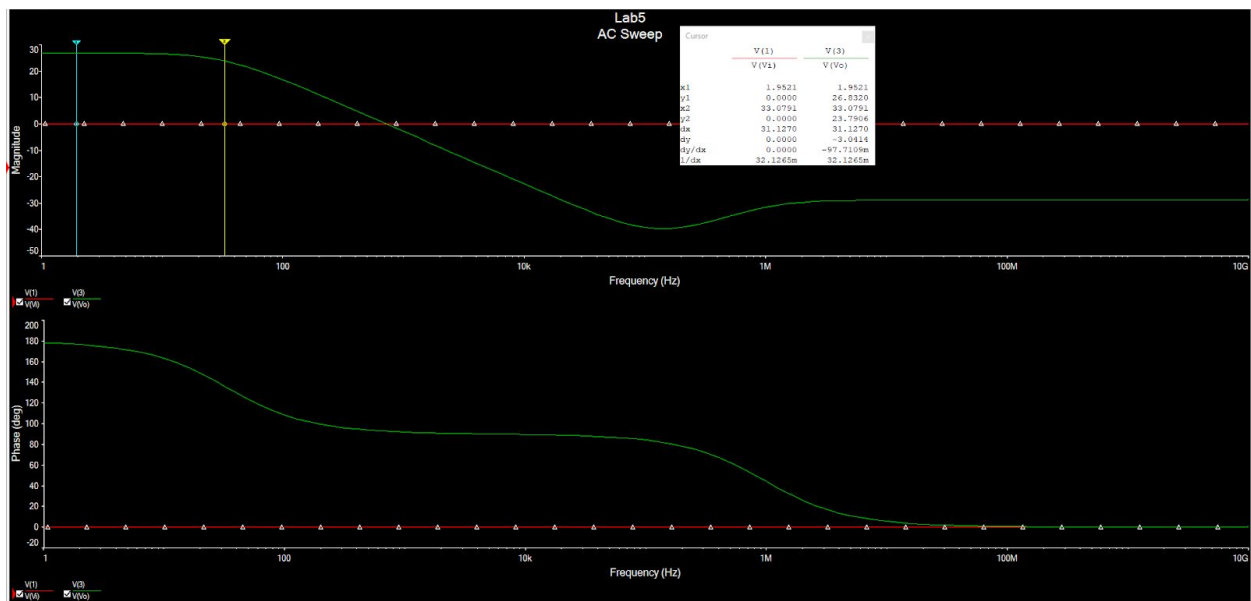
$$f_{\max} = 75000 \text{ Hz}$$

$$V_{out\max} = \frac{S_{\text{rate}}}{2\pi f_{\max}} = \frac{.5 \times 10^{-6}}{2\pi (75000)} = 1.0610 \text{ V}$$

Simulations



Lossy Integrator Bode Simulation



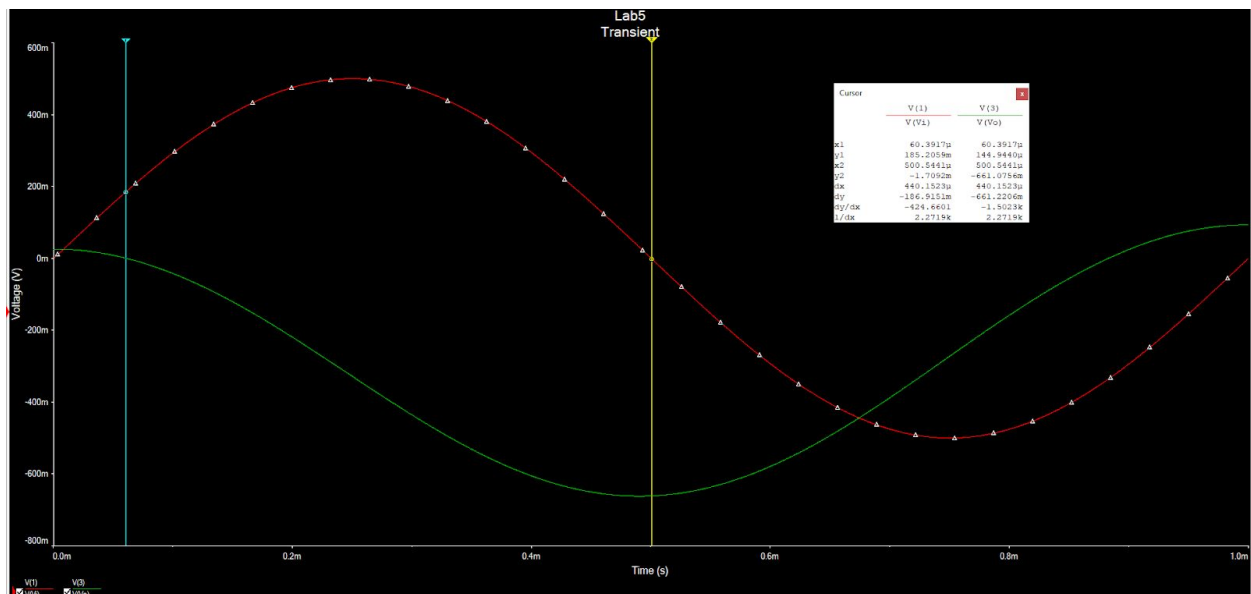
Low frequency gain = 26.8320 dB

3 dB frequency = 33.0791 Hz

1 kHz magnitude = 26.8320 dB

1 kHz phase = 178.25 °

Lossy Integrator Time-Domain Simulation

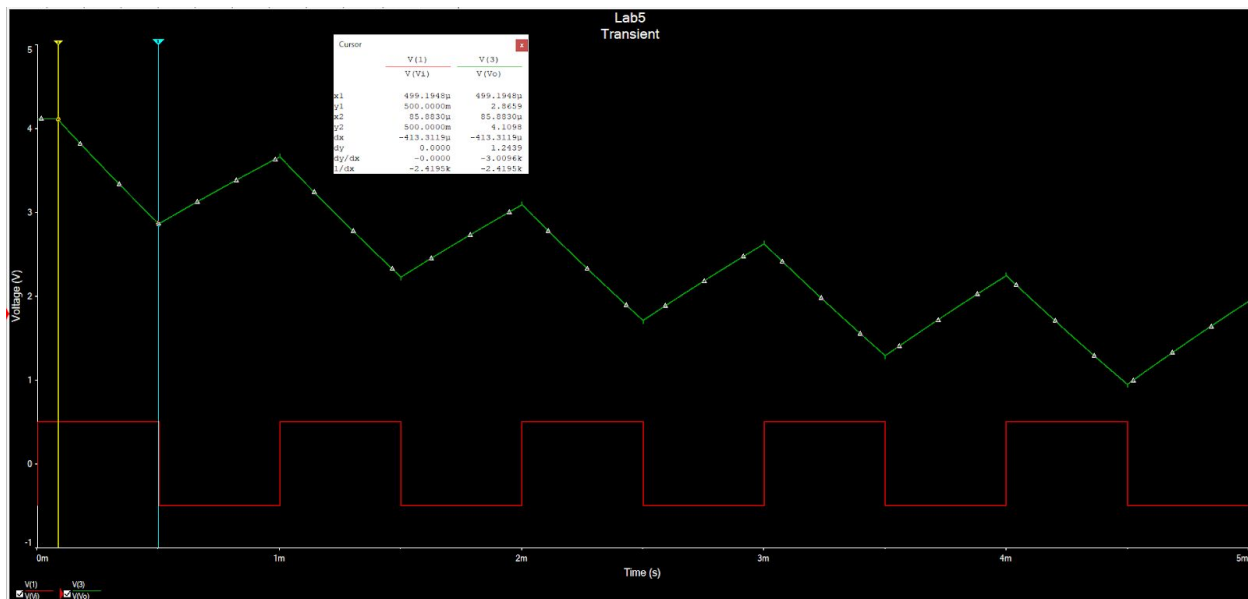


Vi Amplitude = 25.5433 mV

Vo Amplitude = 499.99 mV

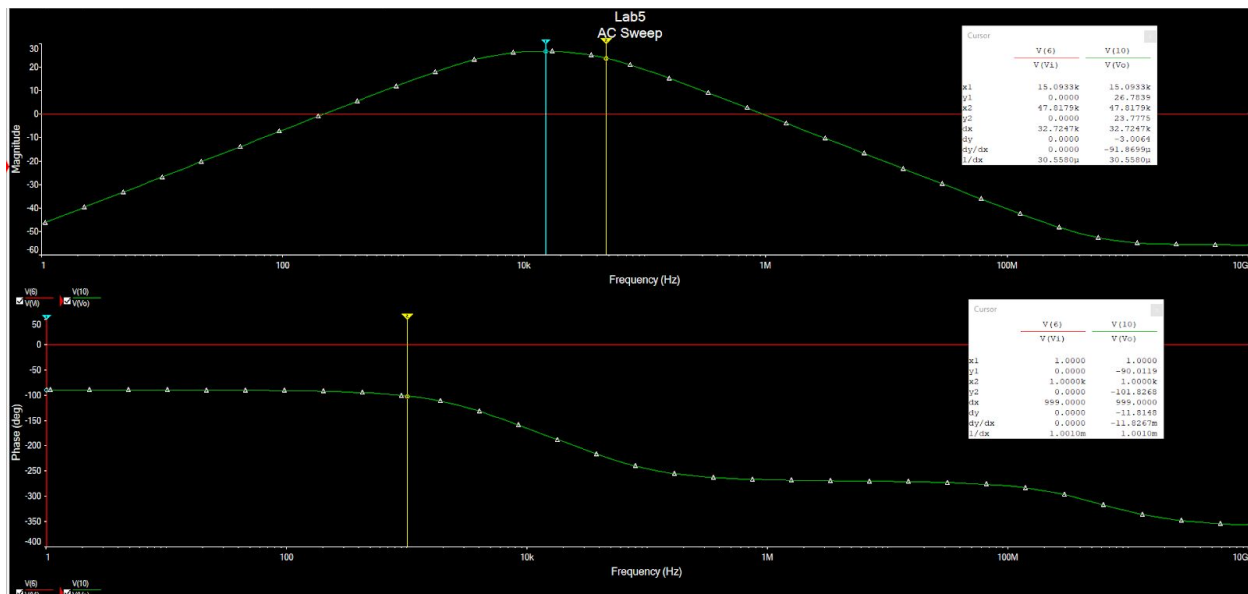
Phase Difference = 158.063 °

Lossy Integrator Time-Domain Simulation (Square Wave)



$V_{p2p} = 1.2439 \text{ V}$

Pseudo Differential Bode Simulation



Low frequency gain = -63.0482 dB

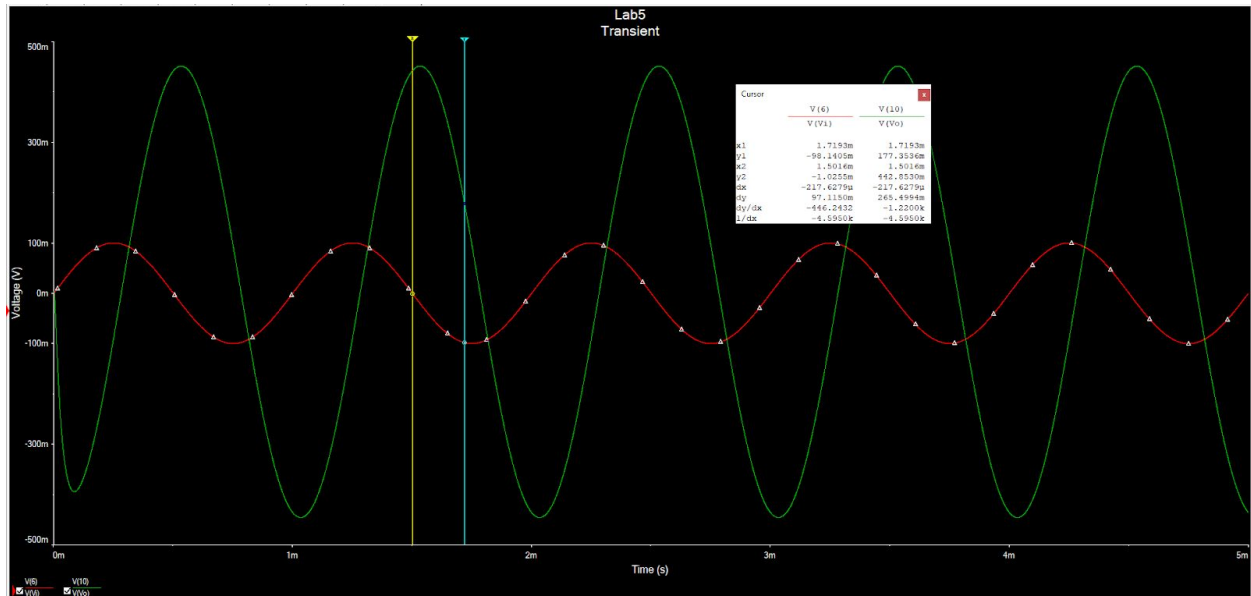
3 dB frequency low = 4368 Hz

3 dB frequency high = 47817 Hz

1 kHz magnitude = 13.2338 dB

1 khz phase = -101.8268 °

Pseudo Differential Time-Domain Simulation

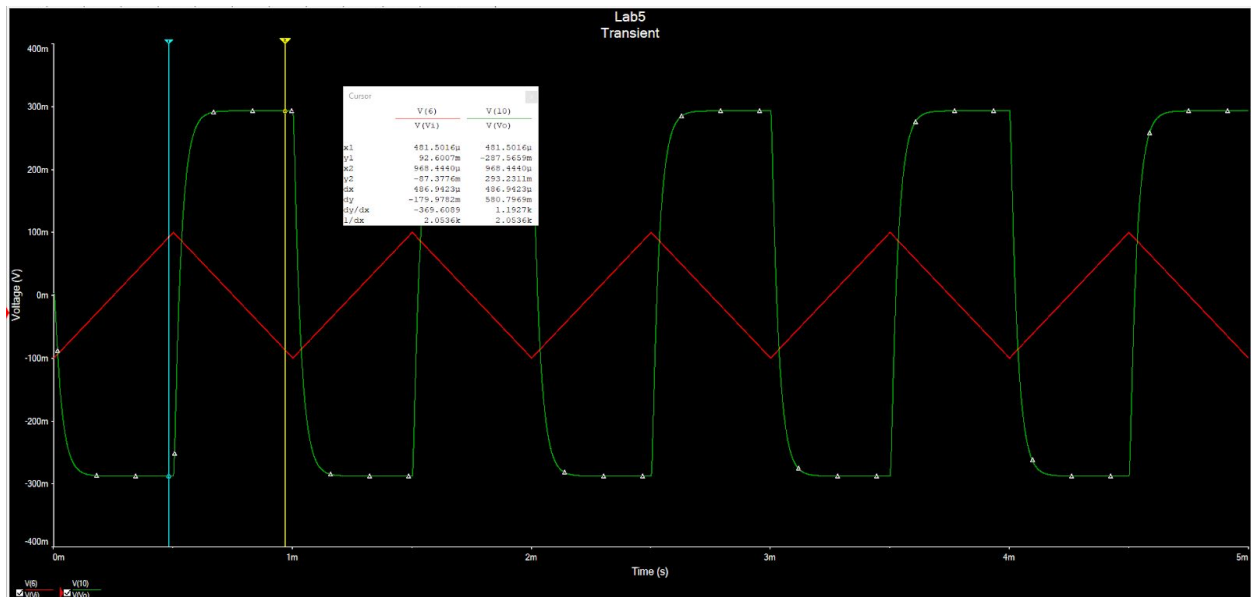


V_i Amplitude = 99.967 mV

V_o Amplitude = 451.4386 mV

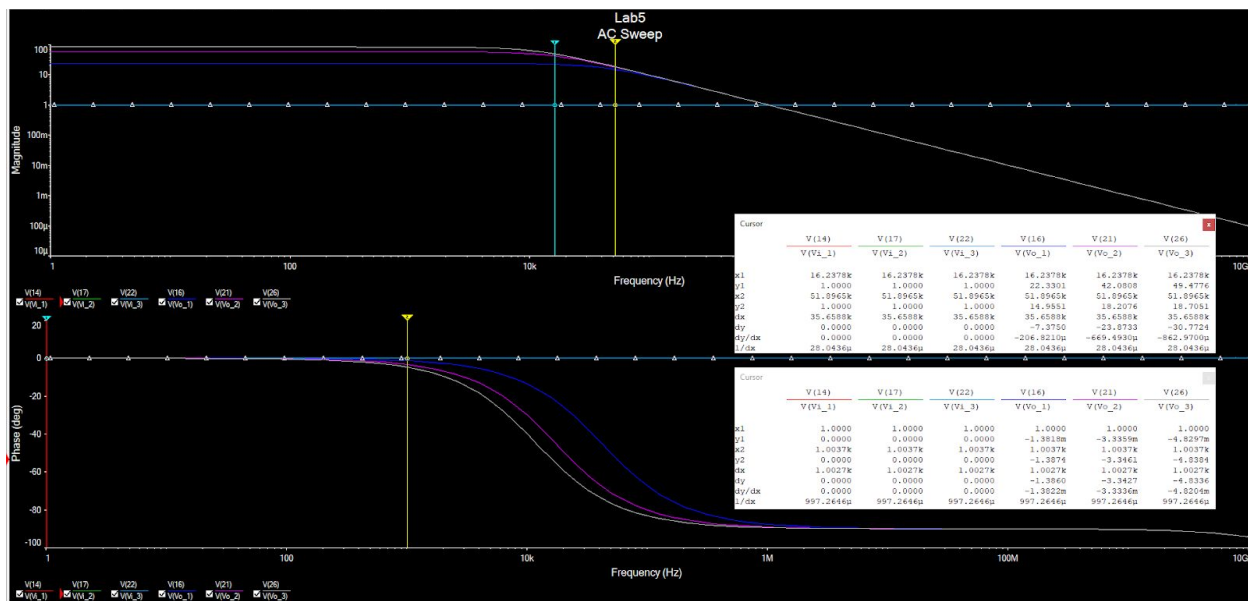
Phase Difference = -79.308°

Pseudo Differential Time-Domain Simulation (Triangular Wave)



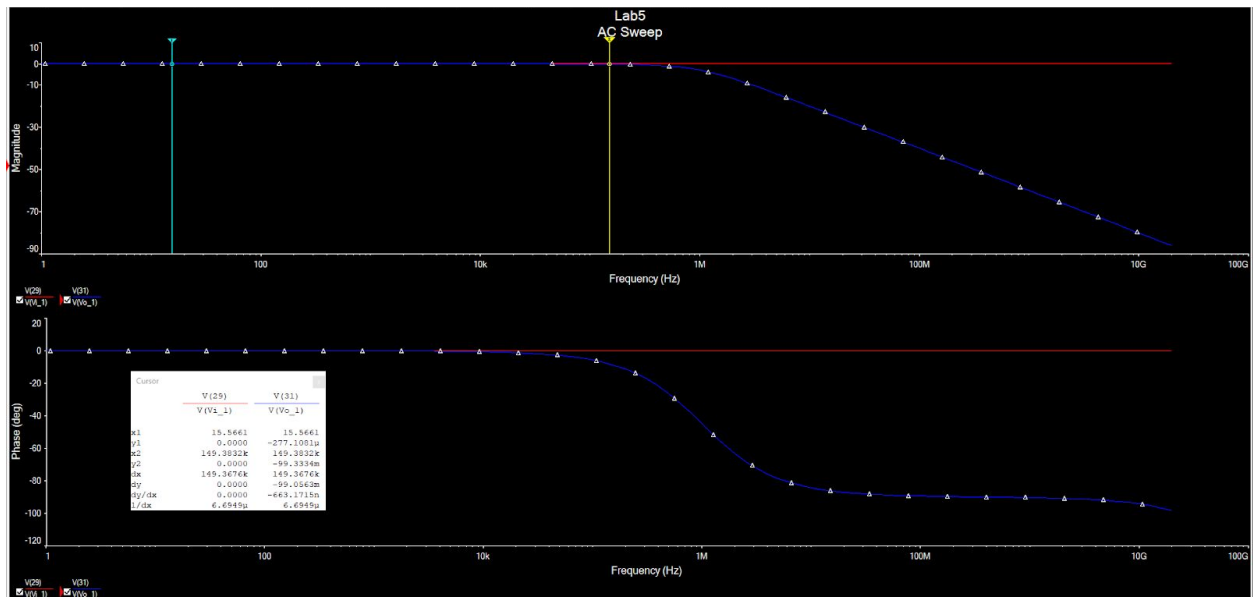
$V_{p2p} = 580.7969$ mV

Finite GBW Limitations Bode Simulation



Low Frequency Gain @ 23 = 27.6029 dB
 Low Frequency Gain @ 57 = 35.2658 dB
 Low Frequency Gain @ 83 = 38.4817 dB
 3 dB Frequency @ 23 = 41.325 kHz
 3 dB Frequency @ 57 = 17.2917 kHz
 3 dB Frequency @ 83 = 12.052 kHz

Slew Rate Limitations Bode Simulation



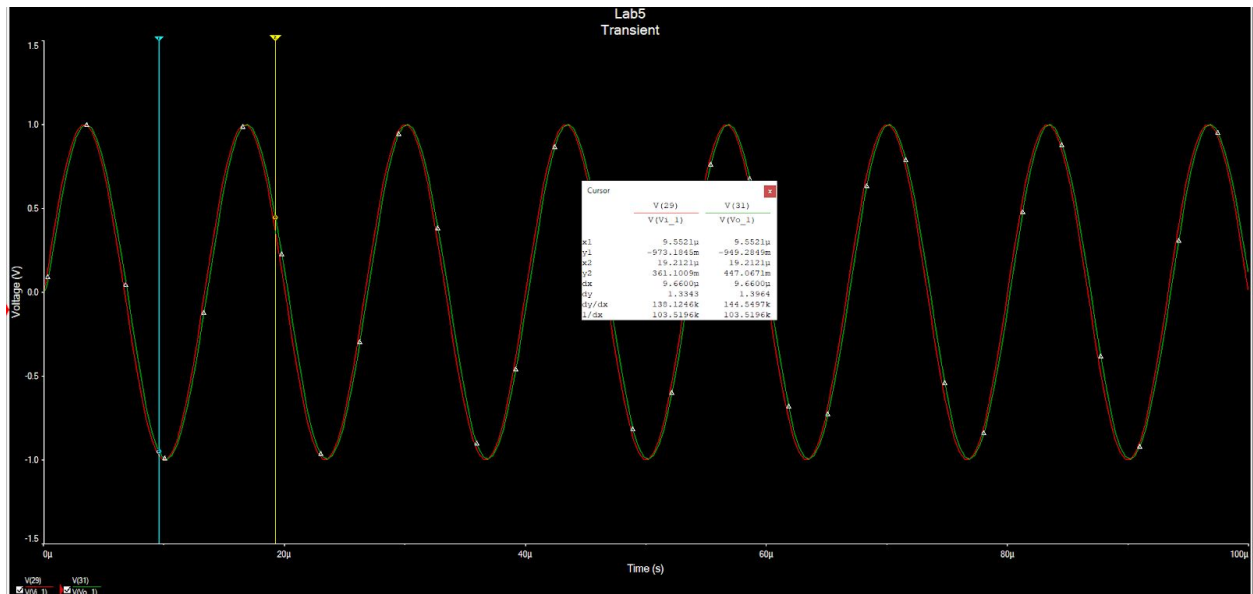
Low Frequency Gain = -277.1081 μ dB

3 dB Frequency = 994.8678 kHz

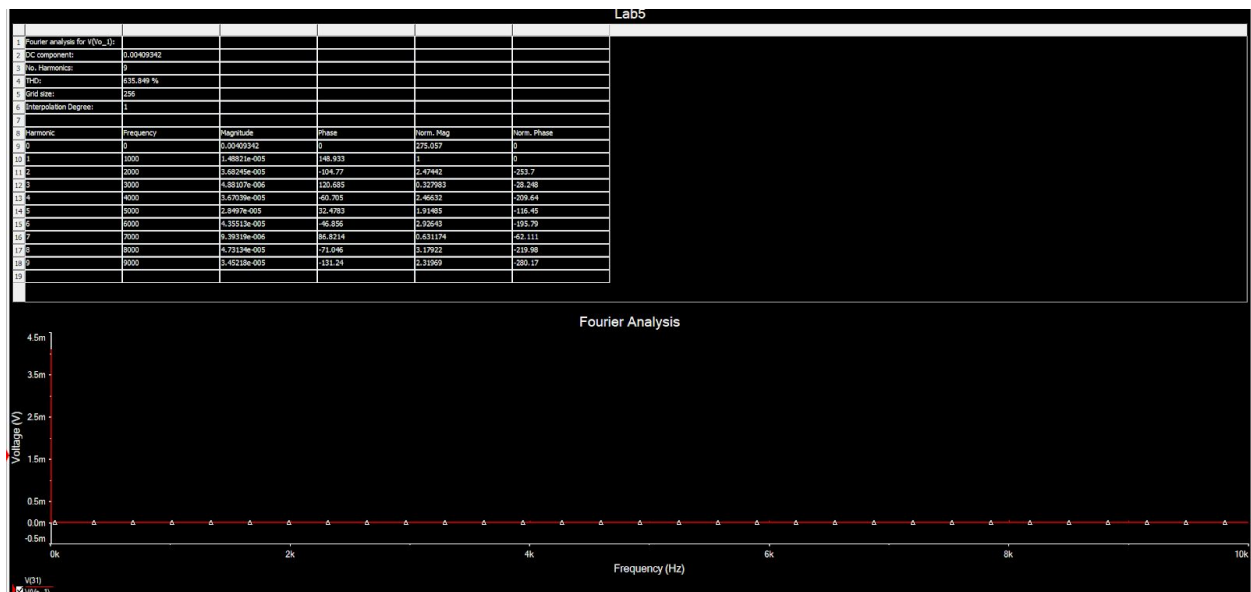
75 kHz Magnitude = -25.9007 mdB

150 kHz Magnitude = -99.3334 mdB

Slew Rate Limitations Time-Domain Simulation (75 kHz 1V)

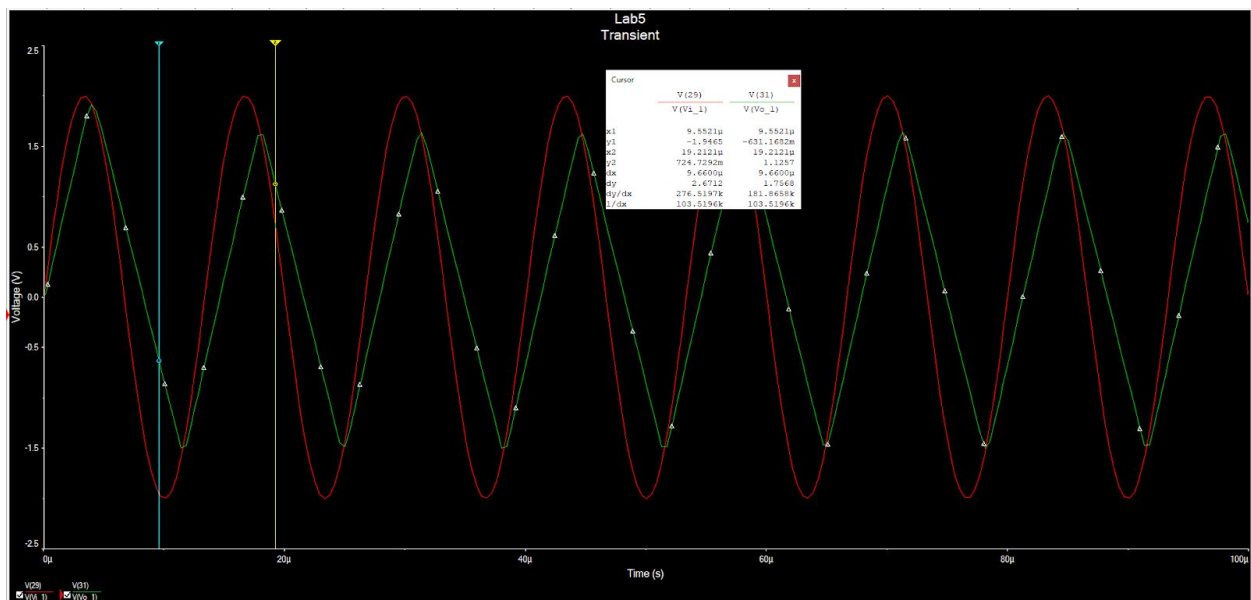


Slew Rate Limitations Fourier Simulation (75 kHz 1V)

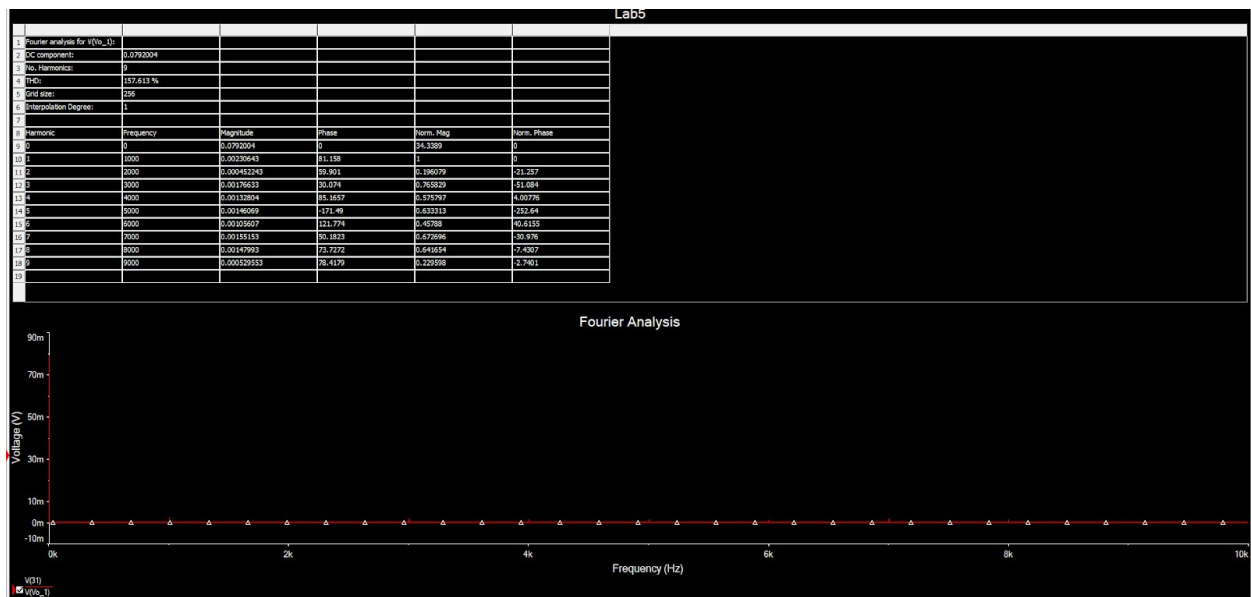


THD = 635.849 %

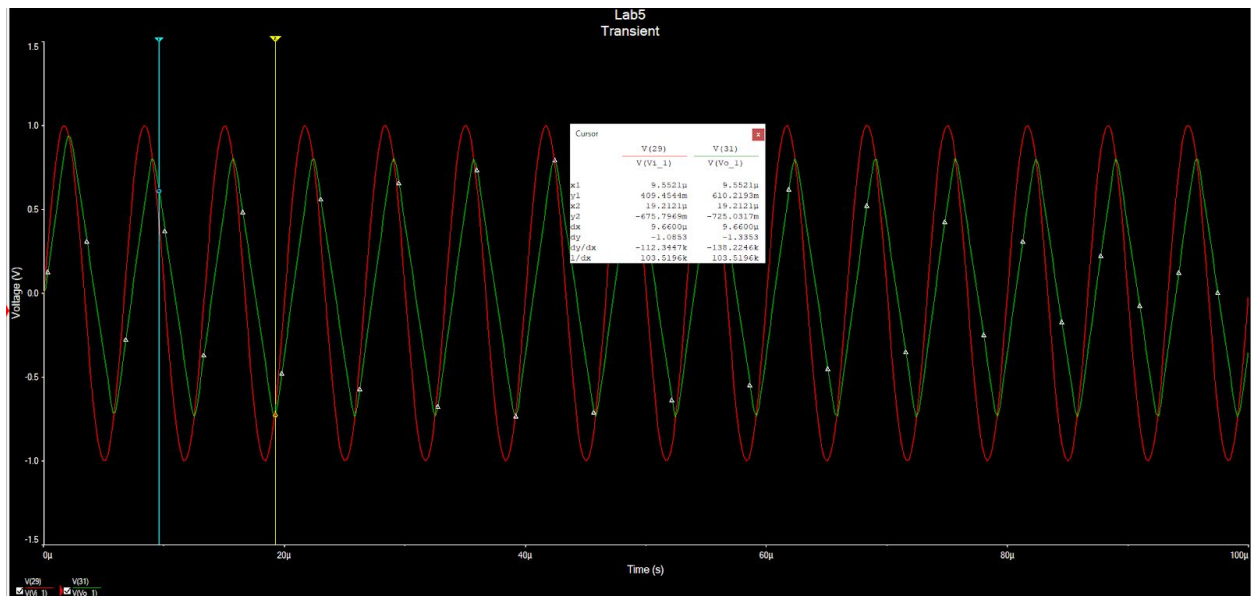
Slew Rate Limitations Time-Domain Simulation (75 kHz 2V)



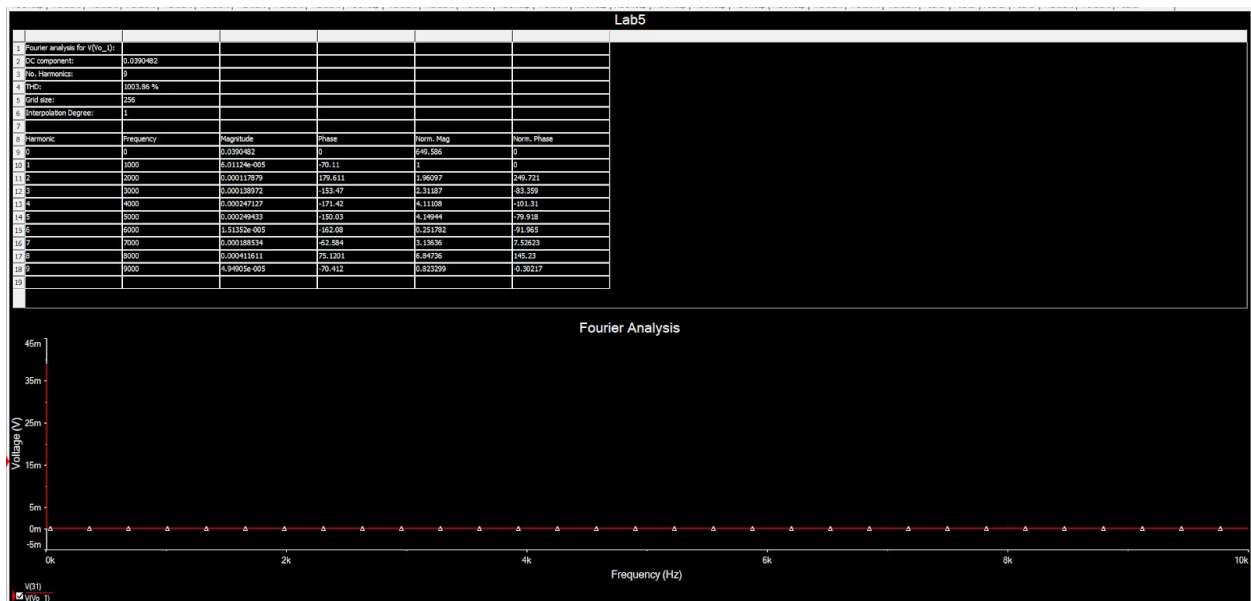
Slew Rate Limitations Fourier Simulation (75 kHz 2V)



Slew Rate Limitations Time-Domain Simulation (150 kHz 1V)



Slew Rate Limitations Fourier Simulation (150 kHz 1V)



THD = 1003.86 %