

1.  $F = \{C \rightarrow A, E \rightarrow F, G \rightarrow D, EG \rightarrow B, EG \rightarrow C, FG \rightarrow E\}$ 
  - a.  $(FG)^+ = \{F, G, E, D, C, B, A\}$
  - b. FG is a super key because it identifies all of the tuples in the relation, although it is minimal.
  - c. No,  $F^+ = \{F\}$  where  $R = \{A, B, C, D, E, F, G\}$
  - d. No,  $G^+ = \{G, D\}$  where  $R = \{A, B, C, D, E, F, G\}$
  - e. FG can be a primary key, because it contains minimal attributes to access all tuples in the relation.
2. Since both relations have a defined primary key and have a relationship, they must agree on the values of some attribute within each of their relations. For example, relation R and relation S have some attribute that have the same values, and the primary keys of each relation can be used to identify those values. Thus  $\alpha \rightarrow \beta$  and  $\beta \rightarrow \alpha$ , implying a one-to-one relationship.