

MASSACHUSETTS INSTITUTE OF TECHNOLOGY
Experimental Study Group

Physics 8.012

Problem Set 6

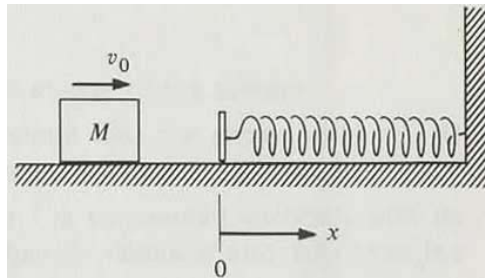
Readings: (KK) Kleppner, Daniel and Kolenkow, Robert, An Introduction to Mechanics, McGraw Hill, Inc., New York, 1973, Chapter 4.

Problems:

Chapter 4: 2, 5, 7, 9, 10, 12, 13

Problem 2:

A block of mass m slides along a horizontal table with speed v_0 . At $x = 0$ it hits a spring with spring constant k and begins to experience a friction force. The coefficient of friction is variable and is given by $u_k = bx$, where b is a constant. What is the change in mechanical energy when the block has first come momentarily to rest?

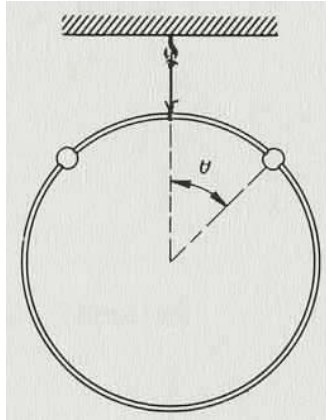


Problem 5:

A body of mass m whirls around on a string which passes through a fixed ring located at the center of the circular motion. The string is held by a person who pulls the string downward with a constant velocity of magnitude V so that the radial distance to the body decreases from an initial distance r_0 to a final distance r_f from the center. The body has an initial angular velocity ω_0 . You may neglect the effect of gravity. Show that the work done in pulling the string equals the increase in kinetic energy of the body.

Problem 7:

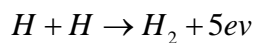
A ring of mass m_r hangs from a thread, and two identical beads of mass m_b slide on it without friction. The beads are released simultaneously from the top of the ring and slide down opposite sides.



- Draw free body force diagrams for the ring and the beads. What direction is the force of the bead on the ring pointing? Does it change as the bead moves. Can you still proceed with an analysis using Newton's second Law if you are not sure which way this force points? Try to find a physical explanation for the direction of this force.
- Show that the ring will start to rise if $m_b > (3/2)m_r$, and find the angle θ with respect to the vertical direction that this occurs.

Problem 9:

Consider the exothermic reaction (final kinetic energy is greater than the initial kinetic energy).



Two hydrogen atoms collide and produce a diatomic hydrogen molecule. However, when hydrogen atoms collide in free space they simply bounce apart. The reason is that it is impossible to satisfy the laws of conservation of energy and momentum in a simple two body collision which releases energy.

- Can you prove this? Try to analyse this collision in a reference frame moving with the velocity of the center of mass of the system.
- Can this two body reaction take place if the temperature is dramatically lowered to near zero degrees Kelvin? Try to give a physical explanation for your answer.

Problem 10:

A block of mass m_b on a horizontal table is connected to one end of a spring with spring constant k . The other end of the spring is attached to a wall. The block is set in motion so that it oscillates about its equilibrium point with amplitude A_0 .

- a) What is the period of the motion?

A lump of sticky putty of mass m_p is dropped onto the block. The putty sticks without bouncing. The putty hits the block at the instant when the velocity of the block is zero.

- b) Find the new period, the new amplitude, and the change in mechanical energy of the system.

The putty is removed and the block is set in motion. This time the putty is dropped and hits the block at the instant the block has its maximum velocity.

- c) Find the new period, the new amplitude, and the change in mechanical energy of the system.

Problem 12:

During the Second World War the Russians, lacking sufficient parachutes for airborne operations, occasionally dropped soldiers inside bales of hay onto snow. The human body can survive an average pressure of 30 lbs/in^2 . Suppose that the lead plane drops a dummy bale equal in weight to a loaded one from an altitude of 150 ft , and that the pilot observes that it sinks about 2 ft into the snow. If the weight of an average soldier is 144 lbs and his effective area is 5 ft^2 , is it safe to drop the men?

Problem 13:

A commonly used potential energy function to describe the interaction between two atoms is the Lennard-Jones 6,12 potential

$$U(r) = \varepsilon \left[(r_0/r)^{12} - 2(r_0/r)^6 \right].$$

- a) Show that the radius at the potential minimum is r_0 , and that the depth of the potential well is ε .
- b) Find the angular frequency of small oscillations about the stable equilibrium position for two identical atoms of mass m bound to each other by the Lennard-Jones interaction.